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# Modeling of Lithium-Ion Battery Degradation for Cell Life Assessment

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**Abstract**—Rechargeable lithium-ion batteries are promising candidates for building grid-level storage systems because of their high energy and power density, low discharge rate, and decreasing cost. A vital aspect in energy storage planning and operations is to accurately model the aging cost of battery cells, especially in irregular cycling operations. This paper proposes a semi-empirical lithium-ion battery degradation model that assesses battery cell life loss from operating profiles. We formulate the model by combining fundamental theories of battery degradation and our observations in battery aging test results. The model is adaptable to different types of lithium-ion batteries, and methods for tuning the model coefficients based on manufacturer's data are presented. A cycle-counting method is incorporated to identify stress cycles from irregular operations, allowing the degradation model to be applied to any battery energy storage (BES) applications. The usefulness of this model is demonstrated through an assessment of the degradation that a BES would incur by providing frequency control in the PJM regulation market.

**Index Terms**—Batteries, Energy storage, Life estimation, Power system economics

## NOMENCLATURE

$f_c, f_t$	Linearized degradation model for cycle aging and for calendar aging.
$f_d, f_d^{\text{cyc}}$	Linearized degradation model the general form, and the per-cycle form.
$f_d^t, f_{d,1}$	Linearized degradation rate per unit time and per cycle.
$f_L^{\text{cyc}}$	Actual degradation rate per cycle.
$i$	Index of cycles.
$L, L_{\text{cal}}, L_{\text{cyc}}$	The overall, calendar, and cycle life of batteries.
$N$	Number of cycles.
$n$	Indicator for full or half cycles.
$S_\delta, S_\sigma, S_T, S_t$	Stress factor model for cycle depth of discharge, cycle average state of charge, cell temperature, and time.
$T_c, T_{\text{ref}}$	Cell temperature and its reference point.
$t, t_c$	Time, and time per cycle.
$\alpha_{\text{sei}}, \beta_{\text{sei}}$	Coefficients for the SEI model.
$\delta$	Cycle depth of discharge.
$\sigma, \sigma_{\text{ref}}$	Cycle average state of charge and its reference point.
$k_{[\dots]}$	Coefficients in stress factor models.

B. Xu and D. Kirschen are with University of Washington, USA; a majority of the work in this paper was carried out during B. Xu's master thesis at ABB Switzerland Ltd, in collaboration with the Power System Lab of ETH Zurich.

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## I. INTRODUCTION

Lithium-ion batteries are prime candidates for electric vehicle (EV) and grid storage applications [1], because of their high power density and higher cycle life compared to other battery types [2], [3]. In addition, the manufacturing cost of lithium-ion batteries is expected to continue to decrease. Because of the increasing interest in applications of battery energy storage (BES) for energy arbitrage [4], frequency control [5], [6], voltage support [7], peak shaving [8], and as a demand response resource in data centers and smart buildings [9], [10], accurate methods for value assessment are needed. A key factor in the operational planning of BES is the operating cost, a majority of which stems from the degradation of battery cells. A model that formulates the degradation process as a function of battery operations is therefore critical to account for the battery operating cost.

Battery degradation models can be classified into theoretical models and empirical models. Theoretical degradation studies [11]–[16] usually focus on the loss of lithium ions and other active materials. These models provide detailed explanations of the various degradation mechanisms and how they are affected by the use and condition of the battery. However, at the planning stage one can only predict the operating pattern of BES, and no information is available on the detailed cell conditions. Theoretical studies linking operation-level observations to the molecular-level degradation processes are still insufficient [17], [18]. It is therefore difficult to directly correlate the charging and discharging patterns with the molecular-level processes occurring inside the battery cells.

Empirical models are more convenient to incorporate with storage planning and operations studies [19]–[23]. Each of these empirical degradation model is tailored for a specific BES application, where the BES operating region is narrow and a model based on some degradation experiments can achieve a satisfactory accuracy. Empirical models are limited by the underlying experimental data. A model developed for a particular application scenario may therefore not be applicable to another. For example, empirical battery degradation models for EV often assume a regular daily charging pattern. Such a model is unlikely to be applicable to predict the performance of a battery used for frequency regulation, where the BES follows a stochastic charging and discharging signal. Obtaining an accurate empirical model of battery degradation therefore requires that operation-specific battery aging experiments be performed for each new application. Such tests take months or even years and would have to be performed in advance using

expensive test facilities.

To get around these difficulties, this paper proposes a semi-empirical battery capacity degradation model intended for off-line battery life assessments. The model combines theoretical analyses with experimental observations, and provides a model that is accurate not only within the operating region covered by the experimental data, but is also applicable to other operating conditions.

Capacity fading in battery cells due to charging and discharging is similar to the fatigue process of materials subjected to cyclic loading [11], [18], [24]. Each cycle causes an independent stress, and the loss of battery life is the result of the accumulation of all cycles. Millner [25] developed an analytical cycle-based model based on Zhurkov's crack propagation theory [26] and the Arrhenius relationship [12]. Building on this basis, we incorporate the theory of solid electrolyte interphase (SEI) film formation with our experimental observations and decouple the degradation process into a non-linear model and a linearized model. In addition, we implement the rainflow cycle-counting algorithm [27][28] to quantify cycles in the battery's state of charge (SoC) profile. This algorithm is widely used for fatigue analysis and has been applied to battery cycle analysis in [29]–[31].

Along with the proposed degradation model, this paper describes a method for tuning the model coefficients based on battery calendar and cycle life test data typically provided by most battery cell manufacturers. Using this tuning procedure, BES owners can adapt the proposed degradation model to the specific lithium-ion battery cells that they have purchased, and perform life assessments for any type of BES application.

Section III describes the structure of the model, including the linear and nonlinear aging property of lithium-ion batteries. Section III introduces the linearized degradation model and the stress models. Section IV illustrates the cycle identification method. Section V presents a set of model parameters derived from LMO battery degradation test data, and Section VI demonstrates an example of using the model to assess the operational value of a battery energy storage system in a grid-level application. Section VII discusses these results and concludes.

## II. MODEL STRUCTURE

The degradation rate of battery cells depends not only on external stress factors such as charging, discharging, time, and temperature, but also on its current state of life. Battery degradation is therefore a nonlinear process with respect to time and stress cycles, which complicates the analysis of test results and the predictive modeling of the aging process. We therefore propose a degradation model which combines a nonlinear component and a linear component. The nonlinear component models the SEI film formation and thus the effect of battery life on the degradation. Separating this effect allows the development of a linear model of the different stress factors

### A. Calendar and cycle aging

Battery aging consists of calendar aging and cycle aging [11], [18], [24], [25], [32]. Calendar aging reflects the

battery's inherent degradation over time, the rate of which is affected by the temperature and the SoC of the battery. Calendar aging  $L_{\text{cal}}$  over a period of time  $t$  can therefore be expressed as a function of the average SoC ( $\bar{\sigma}$ ) and the cell temperature ( $\bar{T}_c$ ):

$$L_{\text{cal}} = f_t(t, \bar{\sigma}, \bar{T}_c). \quad (1)$$

Cycle aging is the life lost each time the battery cycles between charging and discharging. We describe the  $i$ th cycle by its depth of discharge ( $\delta_i$ ), the average SoC of that cycle ( $\sigma_i$ ), and the average cell temperature  $T_{c,i}$ . Since we model each cycle as a single stress event independent of the others, the accumulated degradation is the sum of the capacity reduction caused by each cycle [33]. The cycle aging  $L_{\text{cyc}}$  is then expressed as follows:

$$L_{\text{cyc}} = \sum_i^N n_i f_c(\sigma_i, \delta_i, T_{c,i}), \quad (2)$$

where  $N$  is the number of cycles identified in the operation, and  $n_i$  indicates whether cycle  $i$  is a full or half cycle, and is used to incorporate the rainflow cycle-counting algorithm. Section IV describes the method we adopted to identify cycles from irregular operations. Calendar aging and cycle aging are linear degradation processes with respect to the number of cycles and can be expressed as a function  $f_d$  of  $t$ ,  $\delta$ ,  $\sigma$ , and  $T_c$ :

$$f_d(t, \delta, \sigma, T_c) = f_t(t, \bar{\sigma}, \bar{T}_c) + \sum_i^N n_i f_c(\delta_i, \sigma_i, T_{c,i}). \quad (3)$$

When the battery has not been operated,  $N = 0$  and the degradation consists only of calendar aging. We can write the  $f_d$  as a function with respect to the degradation occurred in one unit time:

$$f_d = t f_t(1, \bar{\sigma}, \bar{T}_c). \quad (4)$$

For simplicity, we denote  $f_t(1, \bar{\sigma}, \bar{T}_c)$  as  $f_d^t$  to represent the life lost in one unit time.

When battery operation consists of repeated cycles with the same DoD and average SoC, we combine the calendar and cycle aging models and recast Eq. (3) into a function ( $f_d^{\text{cyc}}$ ) that is linear with respect to number of cycles

$$f_d^{\text{cyc}}(t, \delta, \sigma, T_c, N) = N(f_t(t_c, \sigma, T_c) + f_c(\delta, \sigma, T_c)), \quad (5)$$

where  $t_c$  is the duration of one cycle. Note that when all cycles are the same, the average temperature and SoC of a single cycle are the same as those of the entire operation, therefore  $\bar{T}_c = T_c$  and  $\bar{\sigma} = \sigma$ , and the temperature and SoC inputs of  $f_t$  and  $f_c$  are the same. Eq. (5) can be rewritten to simplify the cycling aging as accumulated cycling life damage

$$f_d^{\text{cyc}}(t, \delta, \sigma, T_c, N) = N f_d^{\text{cyc}}(t, \delta, \sigma, T_c, 1). \quad (6)$$

For simplicity, we denote  $f_d^{\text{cyc}}(t, \delta, \sigma, T_c, 1)$  as  $f_{d,1}$  to represent the life lost in one cycle.

### B. Modeling of SEI film formation

The proposed calendar and cycle aging models suggest that the degradation rate is the same as long as the cycles are the same. However this is not what we observed in lithium-ion battery degradation experiments. The degradation rate of lithium-ion battery is not a linear process with respect to number of cycles, battery aging tests (Fig. 1) have shown that in cycling tests the degradation rate is significantly higher during the early cycles than during the later cycles, and then increases rapidly when reaching the end of life (EoL). This observation indicates the degradation rate of lithium-ion batteries depends on its current life state. We incorporate the battery life ( $L$ ) into the model and express the actual per-cycle degradation rate ( $dL/d(Cycle)$ ) as a function ( $f_L^{cyc}$ ) of  $L$  and the linear degradation rate over one cycle  $f_d^{cyc}$

$$\frac{dL}{d(Cycle)} = f_L^{cyc}(L, f_d^{cyc}), \quad (7)$$

where  $L$  is normalized between zero and one, with  $L = 0$  indicating a new battery. Battery end of life is typically defined as the point at which the battery only provides 80% of its rated maximum capacity, i.e.,  $L = 0.2$ .

The first factor contributing to the non-linearity of the degradation rate is that this rate is proportional to the number of active lithium ions left in the battery [25]. This can be expressed as follows:

$$f_L^{cyc}(L, f_d^{cyc}) = (1 - L)f_d^{cyc}(t, \delta, \sigma, T_c, 1), \quad (8)$$

and the battery life is obtained by integrating the equation with respect to  $L$ ,

$$L = 1 - e^{-\sum_n f_d^{cyc}(t, \delta, \sigma, T_c, 1)} = 1 - e^{-f_d}. \quad (9)$$

However this relationship does not model the fast-aging stage at the early cycles. While this fast rate of early degradation might be caused by various mechanisms, a major cause is the formation of the Solid Electrolyte Interphase (SEI) film. When a new battery starts to operate, a certain amount of active lithium ions are consumed to form this film [11], [18], [34]. The rate at which this film is formed decreases when a stable film has been formed [35], [36]. To model this theory, we assume that a certain portion of the battery's active material is consumed in the transient stage to form the SEI film. The

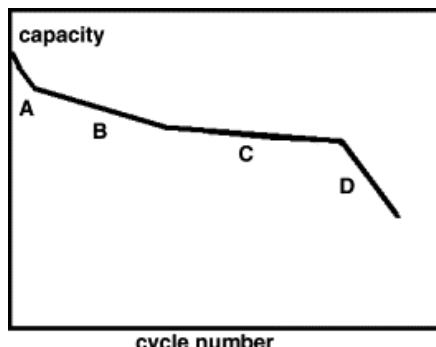


Fig. 1: General capacity degradation behavior of lithium-ion batteries [15].

formation rate is inversely proportional to the SEI film already formed, and stops when a stable SEI has been formed (steady-state stage).

Let  $\alpha_{sei}$  be the portion of the charge capacity irreversibly consumed during the SEI film formation. The total normalized battery capacity is then divided into two portions: the SEI portion  $\alpha_{sei}$ , and the rest that fades at a rate proportional to the battery life  $(1 - \alpha_{sei})$ . We model the SEI formation process similarly to Eq. (9) but at a different linearized rate  $f_{sei}$ , and model the battery life as a two-exponential function:

$$L = 1 - \alpha_{sei}e^{-f_{sei}} - (1 - \alpha_{sei})e^{-f_d}, \quad (10)$$

The parameter  $\alpha_{sei}$  appears to be highly dependent on the design of the battery. The authors of [37]–[39] concluded that  $\alpha_{sei}$  depends on the specific surface area of the graphite as well as on the layer formation conditions and that the value of  $\alpha_{sei}$  varies from 3% to 8%. Other studies [16], [40] concluded that  $\alpha_{sei}$  can reach values up to around 16%. The aging rate of SEI is dependent on the composition of the electrolyte used [41], [42], as well as on the cell temperature [43], [44] and battery operation reactions such as the interactions between the positive and negative electrodes [11]. Since usage and temperature also contributes to SEI formation, we will assume that  $f_{sei}$  is proportional to  $f_d$ :

$$f_{sei} = \beta_{sei}f_d, \quad (11)$$

Eq. (10) therefore becomes

$$L = 1 - \alpha_{sei}e^{-\beta_{sei}f_d} - (1 - \alpha_{sei})e^{-f_d}. \quad (12)$$

Eq. (12) only applies to a fresh battery with  $L = 0$ , it is suitable in planning studies where the entire battery life is assessed. To apply the model to a used battery, the current battery life must be obtained. Because lithium-ion batteries have a very fast initial degradation rate, for most used batteries, the SEI film formation period is finished and the battery life is near or below 0.9. In such cases Eq. (12) can be simplified by assuming the current battery life  $L'$  and neglecting the SEI film formation stage.

$$L = 1 - (1 - L')e^{-f_d}. \quad (13)$$

Eq. (13) can be used when on-site battery life diagnostic is possible. In such cases the battery life can be constantly updated and Eq. (13) used as a tool to predict the battery's degradation for upcoming operations.

### C. Evaluating SEI Parameters

Most battery degradation test results record the faded capacity versus cycle number (cycling aging tests) or time (calendar aging tests) at specified ambient condition and operation pattern. Rewriting Eq. (12) to apply the SEI model to cycling test data:

$$L = 1 - \alpha_{sei}e^{-N\beta_{sei}f_{d,1}} - (1 - \alpha_{sei})e^{-Nf_{d,1}}, \quad (14)$$

A fitting algorithm can then be used to fit the values of  $\alpha_{sei}$ ,  $\beta_{sei}$ , and  $f_{d,1}$  in Eq. (14) to the experimental degradation data.

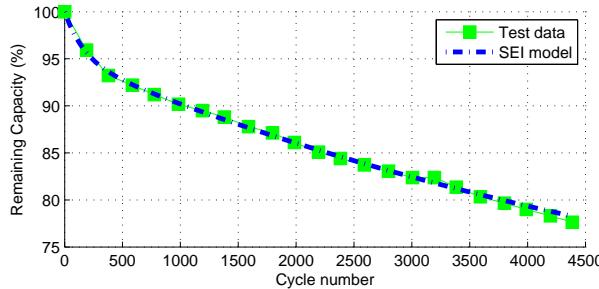


Fig. 2: An example of degradation curve and the fitting of the SEI model.

Similarly, calendar test data can be fitted to the following equation to obtain  $f_d^t$

$$L = 1 - \alpha_{sei} e^{-t\beta_{sei} f_d^t} - (1 - \alpha_{sei}) e^{-tf_d^t}, \quad (15)$$

Fig 2 illustrates this data and this parameter fitting procedure.

### III. STRESS FACTOR MODELS

The linearized degradation rate,  $f_d$ , obtained by fitting Eq. 12 to any battery life test curve (Fig. 2 for example), is the degradation rate after the dependence on battery life has been removed. This linearized degradation rate therefore depends only on the operation of the battery, as described by the number of cycles, the State of Charge (SoC), the Depth of Discharge (DoD), the cell temperature, and the elapsed time.

The temperature effect on degradation has been well studied [12], [25], [45] and is modeled as a stress factor that accelerates the ongoing degradation process. We formulate both the calendar aging and the cycle aging as processes that are accelerated by the temperature stress model  $S_T$

$$f_c(\delta, \sigma, T_c) = S_{\delta, \sigma}(\delta, \sigma) S_T(T_c), \quad (16)$$

$$f_t(t, \sigma, T_c) = S_{t, \sigma}(t, \sigma) S_T(T_c), \quad (17)$$

where  $S_{\delta, \sigma}$  and  $S_{t, \sigma}$  are mixed stress factor models. The influence of stress factors such as current (C-rate), DoD and average SoC on the degradation has not yet been explained satisfactorily [18]. In our approach, we neglect the C-rate effect because the battery current is linked to the cell temperature and DoD. The SoC level affects the calendar aging rate, while the average cycle SoC affects the cycle aging rate [11], [25]. Therefore we model the SoC as an accelerating factor similar to temperature:

$$f_c(\delta, \sigma, T_c) = S_{\delta}(\delta) S_{\sigma}(\sigma) S_T(T_c), \quad (18)$$

$$f_t(t, \sigma, T_c) = S_t(t) S_{\sigma}(\sigma) S_T(T_c). \quad (19)$$

In this formulation, cycles and time are modeled as actual factors that reduce the life of the battery, while SoC and temperature influence the rate of degradation. The model uses a reference point of SoC and temperature, at which the stress model has a value of one, indicating that the degradation rate are unaffected at the reference condition. The SoC and temperature stress model in the cycling aging and the calendar aging are the same, while the inputs are different. The cycling aging model uses the average SoC and temperature of each

identified cycle, while the calendar aging model uses the average SoC and temperature over the entire operation period.

For cycling aging tests, we represent the degradation over one cycle  $f_{d,1}$  as

$$f_{d,1} = [S_{\delta}(\delta) + S_t(t_c)] S_{\sigma}(\sigma) S_T(T_c). \quad (20)$$

For calendar aging tests, if we set  $\delta$  to zero,  $f_{d,t}$  in Eq. (15) becomes

$$f_{d,t} = S_t(t) S_{\sigma}(\sigma) S_T(T_c). \quad (21)$$

The following sections propose stress models and illustrates the procedure used to calculate the model parameters.

#### A. Temperature Stress Model

The stress model for temperature is derived from Arrhenius' equation, which models the temperature dependence of the rate of a chemical reaction [12], [45]:

$$S_T(T) = e^{k_T(T - T_{ref}) \frac{T_{ref}}{T}}, \quad (22)$$

where  $k_T$  is the temperature stress coefficient, and  $T_{ref}$  is the reference temperature in degree Kelvin. A reasonable value for the reference temperature is 293K or 25°C, which is the temperature at which most calendar aging experiments are performed.

To determine the value of  $k_T$ , calendar aging test data at different temperatures but the same SoC can be used. Given two data sets  $(t_A, H_A)$  and  $(t_B, H_B)$  measured at different cell temperatures  $T_A$  and  $T_B$ , Eq. (15) can be used to obtain the linearized degradation rate of the test data curve. We denote the degradation rate of the test data curve measured at the temperature  $T = T_A$  as  $f_{d,t[T=T_A]}$ , then it follows that

$$\frac{S_T(T_A)}{S_T(T_B)} = \frac{f_{d,t[T=T_A]}}{f_{d,t[T=T_B]}}. \quad (23)$$

If we select a temperature as reference, we can write:

$$S_T(T_A) = \frac{f_{d,t[T=T_A]}}{f_{d,t[T=T_{ref}]}}. \quad (24)$$

The value of  $k_T$  is obtained by applying an exponential fit to the temperature series and corresponding  $S_T$  values.

While Arrhenius' equation indicates that the degradation rate decreases with temperature, this relationship does not hold for low temperatures. The metallic lithium reacts with the electrolyte and may contribute to accelerated aging [11]. Low temperatures also increase the battery's impedance and decrease its performance [46]–[48]. The authors of [49] show that 20°C is a dividing line between high and low temperature behaviors, because the battery's impedance drops with temperature as long as the temperature remains above 20°C, but increases if the temperature drops below 20°C. The calendar aging test data used in this research indicates that the degradation rate at 15°C is smaller than at 20°C. However, since no data was available for temperatures lower than 15°C, it is recommended to use the proposed temperature stress model only for batteries operating above 15°C.

### B. SoC Stress Model

We adopt the SoC stress model from [25]:

$$S_\sigma = e^{k_\sigma(\sigma - \sigma_{\text{ref}})}, \quad (25)$$

where  $k_\sigma$  is the SoC stress coefficient,  $\sigma_{\text{ref}}$  is the reference SoC level, which is usually selected around 0.4 to 0.5. To determine the value of  $k_\sigma$ , calendar aging test data for different SoC levels and a similar method for determining  $k_T$  can be used. The value of  $S_\sigma(\sigma_A)$  can then be obtained from test data as follows:

$$S_\sigma(\sigma_A) = \frac{f_{d,t[\sigma=\sigma_A]}}{f_{d,t[\sigma=\sigma_{\text{ref}}]}}. \quad (26)$$

This stress model indicates a higher degradation rate at high SoC level and a lower rate at lower SoC levels, matching the Tafel relationship. This is in line with the experimental data obtained in this work and results from other researchers [11], [50]. However, although a low SoC does not increase capacity fading rate directly, it increases the impedance and power fading [11], [51], therefore low SoC levels will accelerate cycle aging rates. This effect is not modeled in this work, but should be incorporated in operation optimizations.

### C. Time Stress Model

After removing the life-dependence and other stress factors, the time stress model is a linear function of time:

$$S_t(t) = k_t t. \quad (27)$$

Once the temperature and SoC stress model coefficients ( $k_T$  and  $k_\sigma$ ) have been determined,  $k_t$  can be easily calculated using the results of calendar aging tests:

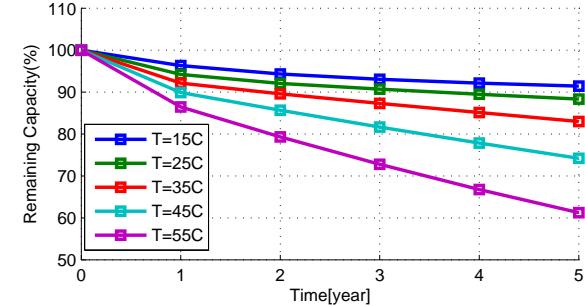
$$k_t = \frac{f_{d,t[T=T_A,\sigma=\sigma_A]}}{t S_T(T_A) S_\sigma(\sigma_A)}, \quad (28)$$

where  $f_{d,t[T=T_A,\sigma=\sigma_A]}$  denotes that the linearized degradation rate is obtained at the condition ( $T = T_A$ ,  $\sigma = \sigma_A$ ), and  $t$  is the duration of the calendar aging test.

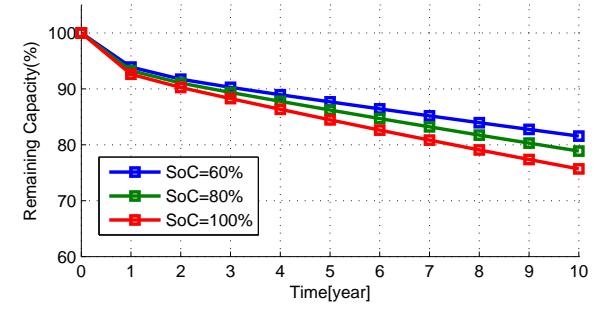
### D. DoD Stress Model

The DoD stress model is a critical part of the degradation model because it determines the degradation caused by one cycle under the reference conditions. The DoD stress model is very dependent on the lithium-ion battery type. Because the available theoretical studies quantifying the relationship between cycle DoD and the amount of capacity fade are insufficient, most DoD stress models nowadays are empirical. Although linear DoD stress models are commonly incorporated in optimization models [22], [52], it is widely accepted that the cycle DoD has a nonlinear impact on degradation. For the same amount of energy processed by a battery, a higher cycle DoD leads to a more severe damage. Nonlinear DoD stress models from the literature can be grouped into two classes: exponential models ( $S_{\delta,e}$ ) [25], [53]

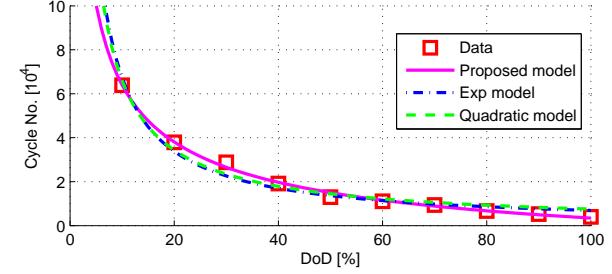
$$S_{\delta,e}(\delta) = k_{\delta,e1} \delta \exp(k_{\delta,e2} \delta), \quad (29)$$



(a) Calendar aging with varying temperature at 50% SoC.



(b) Calendar aging with varying SoC at 25°C.



(c) Cycle life before reaching 80% EoL at reference conditions.

Fig. 3: Battery degradation test data.

and quadratic models ( $S_{\delta,q}$ ) [18], [19]

$$S_{\delta,q}(\delta) = k_{\delta,q1} \delta^{k_{\delta,q2}}, \quad (30)$$

where all  $k$ 's are model parameters. These models are either purely empirical or derived based on theoretical assumptions. In either case, the coefficients are determined by fitting test data.

We can obtain DoD stress data by conducting experiments under the designed reference condition, or use the proposed temperature, SoC, and time stress model to eliminate all other stress factors from the degradation data. Given a set of cycling aging test data, the linearized degradation rate of one cycle under specified conditions, denoted as  $f_{d,1[\delta=\delta_A, \sigma=\sigma_A, T=T_A, t_p=t_{p,A}]}$ , can be obtained from Eq. (14). Given the other stress models developed in Section III-A to III-C, the DoD stress model  $S_\delta$  can be calculated using (20) as follows:

$$S_\delta(\delta_A) = \frac{f_{d,1[\delta=\delta_A, \sigma=\sigma_A, T=T_A, t_p=t_{p,A}]}}{S_T(T_A) S_\sigma(\sigma_A)} - S_t(t_{p,A}). \quad (31)$$

The DoD stress model can then be obtained by fitting a curve to the data set  $(\delta_A, S_\delta(\delta_A))$ .

DoD stress models from the literature do not provide a satisfactory fit to the LMO battery data. In particular, these models tend to over-estimate the LMO battery life at high cycle DoD. Considering that none of these model is designed specifically for LMO batteries, we propose a new empirical DoD stress model:

$$S_\delta(\delta) = (k_{\delta 1} \delta^{k_{\delta 2}} + k_{\delta 3})^{-1}, \quad (32)$$

where  $k_{\delta 1}$ ,  $k_{\delta 2}$ , and  $k_{\delta 3}$  are empirical coefficients. This model achieves a R-squared value of 0.993 in data fitting, while the R-squared value for the exponential model is 0.958, and 0.967 for the quadratic model. Fig. 3c shows the DoD test data and the curve fitting results.

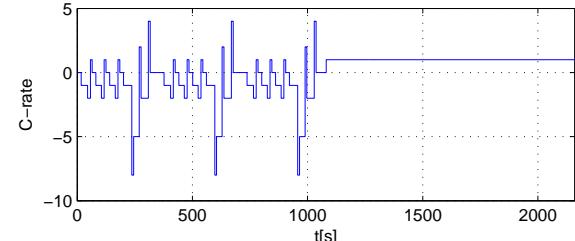
The proposed model is similar to the quadratic DoD model, but introduces a new constant  $k_{\delta 3}$ . In our fitting results,  $k_{\delta 1}$  has a positive value while  $k_{\delta 2}$  and  $k_{\delta 3}$  have negative values. Compared to exponential and quadratic models, the proposed model predicts lower cycle life at low DoD cycles. This modeling difference is a result of different lithium-ion battery types. Lithium-ion batteries with different electrode materials differ significantly in their aging mechanisms and cycle life. Compared to the Li(NiMnCo)O<sub>2</sub> battery studied in [54] and the LiFePO<sub>4</sub> battery studied in [25], LMO battery degradation not only leads to capacity fading but also greatly increases the cell resistance, causing LMO batteries to have shorter cycle lives [34]. The difference in aging mechanism is possibly the reason why the proposed model provides a better fit compared to the exponential and the quadratic models.

Note that the proposed DoD stress model only applies to LMO batteries. For other types of lithium-ion batteries, one should select an appropriate DoD stress model based on the battery type and the test data.

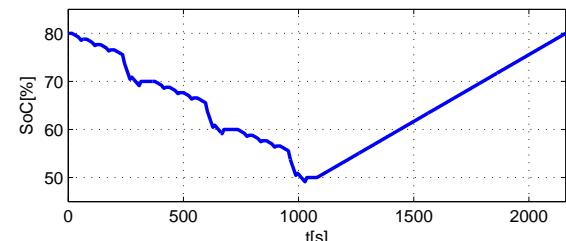
#### IV. MODEL APPLICATION TO IRREGULAR CYCLES

The linearized model described by Eq. (3) evaluates battery capacity loss from a series of cycles, each with different cycle parameters such as DoD, average SoC, temperature. Identifying directly the number of cycles, the DoD and the average SoC of each cycle is difficult from a SoC profile resulting from irregular battery operation. We therefore adopt the rainflow cycle-counting algorithm [27][28] that is widely used in fatigue studies and has been applied to battery cycle analysis in [29]–[31]. This algorithm make possible the application of Miner's rule [33] to assess the fatigue life, and is also applicable to damage accumulation processes such as battery degradation.

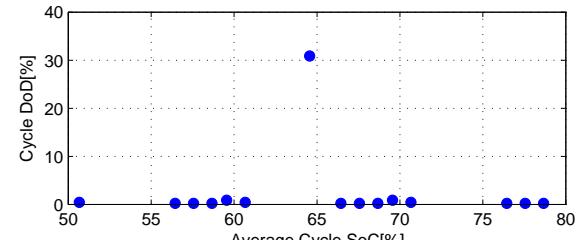
The input to this algorithm [55] is the SoC profile, and it outputs the following results: 1) cycle amplitude; 2) cycle mean value; 3) cycle number (0.5 for a half cycle, or 1 for a full cycle); 4) cycle begin time; 5) cycle end time. We convert the rainflow counting results into the stress factors described in Eq. (3): 1) the DoD of the  $i$ th cycle  $\delta_i$  which is twice the  $i$ th rainflow cycle amplitude; 2) the average SoC of the  $i$ th cycle  $\sigma_i$  which is the  $i$ th rainflow cycle mean value; 3) the average cycle temperature of the  $i$ th cycle  $T_{c,i}$  which is calculated as the mean temperature between the start and end times of the  $i$ th rainflow cycle; 4) the average profile SoC  $\bar{\sigma}$  is the mean



(a) Example DST C-rate profile.



(b) Example DST SoC profile.



(c) Distribution of counted cycles.

Fig. 4: The DST profile and rainflow cycle counting example.

value of the rainflow cycle mean values; 5) the average profile temperature  $\bar{T}_c$  is the mean value of the temperature profile. Fig. 4 shows an example of the counting results.

#### V. EXAMPLE MODEL PARAMETERS

##### A. Model Parameters

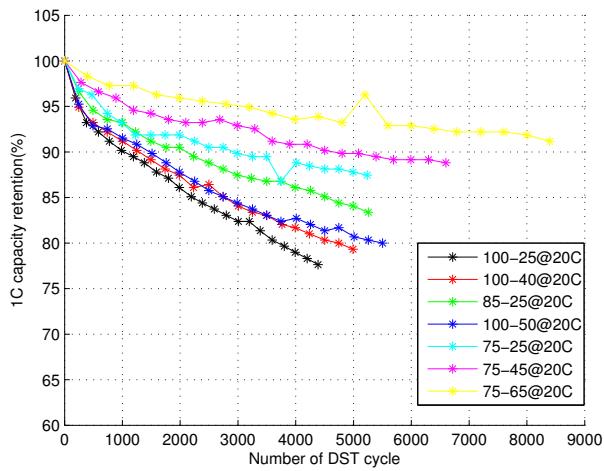
The proposed degradation model requires at least two sets of data to obtain the model parameters: the battery calendar aging test data with specified SoC and temperature, and the battery cycle life data with specified DoD and temperature. Examples of these data curves are shown in Fig. 3. The cycle life data are normalized to the reference condition. Table I shows a set of model coefficients tuned using LMO battery degradation test data from the same manufacturer.

##### B. Dynamic Stress Test Cycling

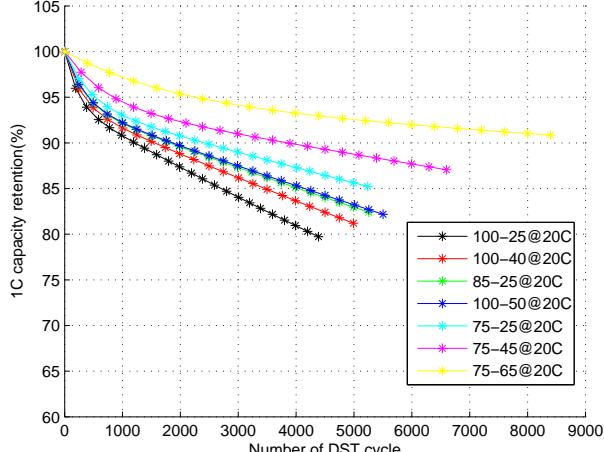
In addition to the calendar and cycle aging test data, the manufacturer provided a set of Dynamic Stress Test (DST) battery test results in order to illustrate the battery's performance in mixed-cycle operations. For each test, the cell first starts at a set SoC level and the DST profile is applied repetitively until the set stop level is reached. The cell is then recharged back to the starting level at a 1 C-rate to finish one test cycle. Fig. 4a shows a DST C-rate example consisting of three consecutive

TABLE I: Degradation Model Parameters

Nonlinear Degradation Model			
$\alpha_{sei}$	5.75E-2	$\beta_{sei}$	121
DoD Stress Model			
$k_{\delta 1}$	1.40E5	$k_{\delta 2}$	-5.01E-1
$k_{\delta 3}$	-1.23E5		
SoC Stress Model			
$k_{\sigma}$	1.04	$\sigma_{ref}$	0.50
Temperature Stress Model			
$k_T$	6.93E-2	$T_{ref}$	25°C
Calendar Aging Model			
$k_t$			4.14E-10/s



(a) Original DST Data.



(b) Reproduced DST Data.

Fig. 5: Comparison of actual data and model reproduction.

DST profiles. The resulting change in SoC is shown in Fig. 4b. Fig. 4c shows the identified cycles as a distribution of cycle DoDs with respect to the average cycle SoC.

We repeated the DST test in simulations to reproduce the SoC profile and the average cell temperature. For cell temperature, we use a simple thermal model derived from [56], the simulated average cell temperature was 21°C, 1 degree higher than the test room temperature. The aging curves are

calculated based on the reproduced profile and using the proposed degradation model and the rainflow cycle-counting algorithm. Fig. 5a shows the test data. Fig. 5b shows the reconstructed degradation curve for the DST test. The legend in both figures indicates the starting and ending SoC percentage for each test curve and the test room temperature. These results show that the reconstructed profile is very close to the experimental data. The percentage error between the data and the estimation is 14%, corresponding to a ±3% capacity estimation error at 80% end of life (20% of the capacity is lost, the actual remaining capacity is between 77% to 83%). Such error is reasonable due to the absence of the original SoC profile of the DST test and detailed test procedures.

The major difference between the test data and model estimations occurs in the first few hundreds cycles, where a strong nonlinearity is apparent. In particular, the three test cases starting at 100% SoC, represented by the black (100-25), red (100-40), and dark blue (100-50) curves in Fig. 5a, show a very fast degradation rate during the early cycles. This early degradation causes an obvious gap between the dark blue curve and the green curve (85-25) in the test data. This phenomenon is possibly due to cell over-voltages caused by high SoC during cycling. However, due to the lack of experimental data and lab testing records, we are unable to model and identify the excessive life damage induced by overvoltage. Nevertheless, utilizing the SEI model described in Eq. (14), we are able to remove the effect of early degradation and extract the linearized degradation rate. Our linearization shows that the dark blue case and the green case have the same linearized degradation rate. This result is also correctly reproduced by the proposed model, which show that the dark blue curve coincides with the green curve in Fig. 5b.

## VI. MODEL APPLICATION CASE STUDY

The purpose of the proposed degradation model is to estimate the capacity fading that would arise from actual battery operation, and therefore assess the BES degradation cost. In particular, we developed the proposed model to assess the value of BES in providing frequency regulation. In this study, we investigate the induced capacity losses of a BES participating in PJM's frequency regulation market.

The secondary frequency control signal in this market is split into a dynamic control signal (RegD) and a traditional control signal (RegA). The dynamic signal is the high-pass filtered part of the area control error, which has a larger signal ramp rate and a smaller energy deviation, and is designed for fast-responding units [57]. With the newly introduced two-part offer policy, regulation payments are determined based on the unit's reserve capacity as well as its performance in following the control signal. The performance of each regulation provider is evaluated based on the correlation, delay, and precision of its response to the regulation signal. Fast-responding units, such as BES, can be very competitive in this market.

Providing regulation services requires the commitment of a minimum amount of energy capacity, which is measured in MWh/MW, or hours [58]. We consider the cases of a BES

TABLE II: Comparison of the degradation of different lithium-ion battery types when providing frequency regulation in the PJM system.

Regulation type	PJM RegD				PJM RegA			
	Case 1	Case 2	Case 3	Case 4	Case 5	Case 6	Case 7	Case 8
BES energy capacity (MWh/MW)	0.25	0.50	0.75	1.00	1.00	2.00	3.00	4.00
Performance score	0.90	0.96	0.99	0.99	0.81	0.86	0.90	0.92
LMO battery capacity loss (%)	1.60	0.96	0.76	0.66	0.63	0.41	0.34	0.31
LFP battery capacity loss (%)	0.75	0.35	0.26	0.22	0.39	0.25	0.21	0.20
NMC battery capacity loss (%)	1.56	0.54	0.32	0.24	0.70	0.38	0.30	0.26

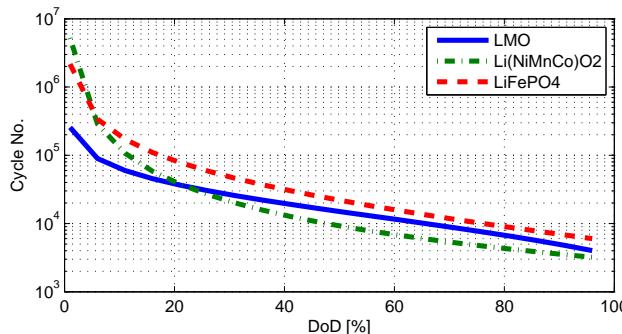


Fig. 6: Comparison of cycle life for different types of lithium-ion batteries adjusted to reference conditions.

providing RegD service with a committed capacity of less than one hour and of another BES providing RegA service with a committed capacity larger than one hour. In both cases, we evaluate the capacity that they will lose if they were to provide these services seamlessly for one month, assuming that an SoC control scheme [5], [59] maintains the SoC level in accordance with the storage energy capacity.

We assume that all battery cells are identical, that there are no losses from the battery management system (BMS) and the power electronics, and that the BMS has ideal control over all battery cells. We use a simplified resistive circuit model [49] to simulate a single battery cell with 1.1 Ah nominal capacity and a 3.3 V nominal voltage. The number of cells in the BES is calculated by dividing the MWh capacity by the nominal cell energy capacity (V·Ah). The power extracted from each cell is calculated by dividing the BES output power by the number of battery cells. The cell current is calculated by dividing the cell output power by the cell's terminal voltage, and the cell SoC is calculated by integrating the output current. Because the corresponding C-rates are mostly below one, we assume that the cooling system of the BES maintains a fixed cell temperature of 25°C.

We considered three DoD stress models to represent three types of lithium-ion batteries: the proposed LMO model, the exponential model for Lithium Iron Phosphate (LFP) batteries [25], and the quadratic model for Lithium Nickel Manganese Cobalt Oxide (NMC) batteries [18], [54]. A cycle life comparison of the three batteries is shown in Fig. 6, all models were adjusted to the reference condition (25°C cell temperature, 50% average SoC). In each simulation, cycles are identified by applying using the rainflow counting algorithm

to the SoC profile. The faded capacity is calculated using the linear aging model of Eq. (3). The capacity lost is assessed with the three battery models considering both calendar and cycle aging. In addition to the degradation, we calculate the average performance score of the regulation response.

This performance score increases with the BES energy capacity because more energy is available to be stored and injected into the grid. In battery degradation, we can identify a converging trend in the capacity loss when the BES energy capacity increases. This is because cycles have smaller DoD and the cycle aging becomes slower. In very large BES, the cycle aging approaches zero, leaving only the calendar aging. As the BES size decreases, the degradation is more severe, but does not necessarily lead to a higher cost because the numbers of battery cells involved are different. For example, when providing 1 MW RegD, the absolute amount of capacity lost in Case 1 with a LMO battery is 4 kWh, while in Case 4 the loss is 6.6 kWh. In the battery type comparison, LFP shows the longest cycle life. Other studies [34], [60] have also shown that LFP cells have longer cycle life compared to other types of lithium-ion batteries. Yet this result does not lead to the conclusion that LFP cells are the best choice for frequency regulation because battery types also differ in efficiency, energy density, and production cost. In this case study, we only provide an assessment of the capacity loss aspect. In actual operations, one must also consider the performance, the cooling, the efficiency, as well as the purchase and replacement cost of battery cells.

## VII. CONCLUSION

This paper proposes a battery degradation model that can estimate capacity fading in irregular battery operation. Several fundamental theories of battery degradation, including the Arrhenius relationship and the SEI film formation, are considered in the design of this model. While the parameters derived in this paper were obtained from experimental data with a specific battery type, the proposed model and the parameter tuning method can be applied to model degradation in other types of lithium-ion batteries. In particular, we propose a new empirical DoD stress model that best fits our LMO battery cycle test data. The case study demonstrates that by using different DoD stress models, the proposed degradation model can be applied to LFP and NMC batteries. The life loss of these three types of lithium-ion batteries are compared when under a scenario where they provide frequency regulation in the PJM market.

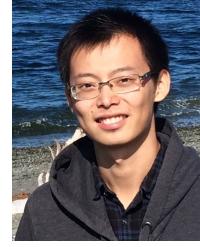
The SEI model includes the life-dependence characteristic of battery degradation, and serves as a tool for linearizing aging curves. Test data and studies from the literature have shown that the formation rate of SEI films varies greatly between cells, even cells of the same type. Because experimental errors cannot be eliminated due to the limited size of the data set, it is difficult to model the SEI film formation accurately. The SEI model is suitable for estimating battery life at the planning stage. In actual BES operations, battery life should be constantly updated using on-site diagnostics.

The model can be further improved in several aspects. One is to introduce other stress factors, such as current magnitude (C-rate), over-voltage, and low-SoC. These factors are highly coupled with the stress factors considered in the proposed model. Delicate experiments must be designed to decouple the effect of these inter-related factors for accurate modeling. The adopted rainflow algorithm is not causal and can only be applied off-line over a recorded SoC profile, making it unsuitable for real-time evaluations. Future work is thus required to develop a real-time degradation estimator for degradation-limiting controllers.

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