

## Copilot

The previous code snippet can be adapted to solve the second-order differential equation as follows:

```
import numpy as np

def f(v, k, m, g):
    magv = np.linalg.norm(v)
    return np.array([k * magv * v[0], k * magv * v[1] - g])

def runge_kutta(f, x0, y0, v0, h, n, k, m, g):
    x = np.array([x0, y0])
    v = v0
    for i in range(n):
        k1 = h * f(v, k, m, g)
        k2 = h * f(v + 0.5*k1, k, m, g)
        k3 = h * f(v + 0.5*k2, k, m, g)
        k4 = h * f(v + k3, k, m, g)
        v = v + (1/6)*(k1 + 2*k2 + 2*k3 + k4)
        x = x + h * v
    return x, v
```

In this Python function,  $f$  is the function that you want to solve,  $x_0$  and  $y_0$  are the initial conditions for the position,  $v_0$  is the initial velocity,  $h$  is the step size,  $n$  is the number of steps,  $k$  is the drag coefficient,  $m$  is the mass of the projectile, and  $g$  is the acceleration due to gravity. The function returns the approximate position at  $x_0 + n \cdot h$ ,  $y_0 + n \cdot h$  and the final velocity.

Please note that this is a simplified model and actual projectile motion can be more complex due to factors like wind, spin, and variable air density. Also, the step size  $h$  may need to be adjusted based on the specifics of the problem to ensure the accuracy of the solution.