Anomaly Detection

Lecture Notes for Chapter 9

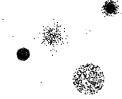
Introduction to Data Mining, 2nd Edition by Tan, Steinbach, Karpatne, Kumar

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Anomaly/Outlier Detection

- What are anomalies/outliers?
 - The set of data points that are considerably different than the remainder of the data



- Natural implication is that anomalies are relatively rare
 - One in a thousand occurs often if you have lots of data
 - Context is important, e.g., freezing temps in July
- Can be important or a nuisance
 - 10 foot tall 2 year old
 - Unusually high blood pressure

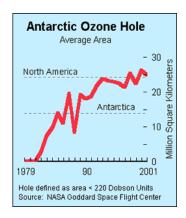
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Importance of Anomaly Detection

Ozone Depletion History

- In 1985 three researchers (Farman, Gardinar and Shanklin) were puzzled by data gathered by the British Antarctic Survey showing that ozone levels for Antarctica had dropped 10% below normal levels
- Why did the Nimbus 7 satellite, which had instruments aboard for recording ozone levels, not record similarly low ozone concentrations?
- The ozone concentrations recorded by the satellite were so low they were being treated as outliers by a computer program and discarded!



Sources:

http://exploringdata.cqu.edu.au/ozone.html http://www.epa.gov/ozone/science/hole/size.html

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Causes of Anomalies

- Data from different classes
 - Measuring the weights of oranges, but a few grapefruit are mixed in
- Natural variation
 - Unusually tall people
- Data errors
 - 200 pound 2 year old

Distinction Between Noise and Anomalies

- Noise is erroneous, perhaps random, values or contaminating objects
 - Weight recorded incorrectly
 - Grapefruit mixed in with the oranges
- Noise doesn't necessarily produce unusual values or objects
- Noise is not interesting
- Anomalies may be interesting if they are not a result of noise
- Noise and anomalies are related but distinct concepts

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General Issues: Number of Attributes

- Many anomalies are defined in terms of a single attribute
 - Height
 - Shape
 - Color
- Can be hard to find an anomaly using all attributes
 - Noisy or irrelevant attributes
 - Object is only anomalous with respect to some attributes
- However, an object may not be anomalous in any one attribute

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General Issues: Anomaly Scoring

- Many anomaly detection techniques provide only a binary categorization
 - An object is an anomaly or it isn't
 - This is especially true of classification-based approaches
- Other approaches assign a score to all points
 - This score measures the degree to which an object is an anomaly
 - This allows objects to be ranked
- In the end, you often need a binary decision
 - Should this credit card transaction be flagged?
 - Still useful to have a score
- How many anomalies are there?

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Other Issues for Anomaly Detection

- Find all anomalies at once or one at a time
 - Swamping
 - Masking
- Evaluation
 - How do you measure performance?
 - Supervised vs. unsupervised situations
- Efficiency
- Context
 - Professional basketball team

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Variants of Anomaly Detection Problems

- Given a data set D, find all data points x ∈ D with anomaly scores greater than some threshold t
- Given a data set D, find all data points x ∈ D having the top-n largest anomaly scores
- Given a data set D, containing mostly normal (but unlabeled) data points, and a test point x, compute the anomaly score of x with respect to D

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Model-Based Anomaly Detection

- Build a model for the data and see
 - Unsupervised
 - Anomalies are those points that don't fit well
 - Anomalies are those points that distort the model
 - Examples:
 - Statistical distribution
 - Clusters
 - Regression
 - Geometric
 - Graph
 - Supervised
 - Anomalies are regarded as a rare class
 - Need to have training data

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Additional Anomaly Detection Techniques

- Proximity-based
 - Anomalies are points far away from other points
 - Can detect this graphically in some cases
- Density-based
 - Low density points are outliers
- Pattern matching
 - Create profiles or templates of atypical but important events or objects
 - Algorithms to detect these patterns are usually simple and efficient

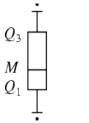
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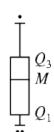
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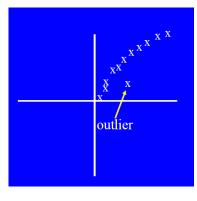
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Visual Approaches

- Boxplots or scatter plots
- Limitations
 - Not automatic
 - Subjective







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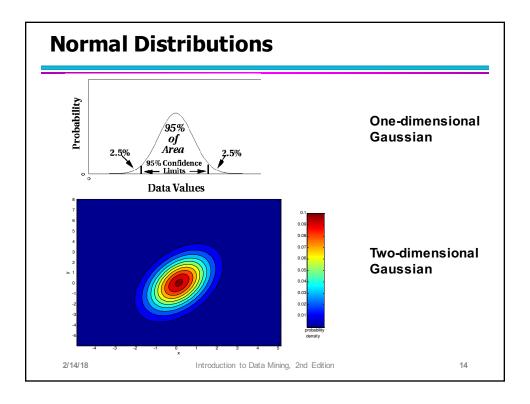
Statistical Approaches

Probabilistic definition of an outlier: An outlier is an object that has a low probability with respect to a probability distribution model of the data.

- Usually assume a parametric model describing the distribution of the data (e.g., normal distribution)
- Apply a statistical test that depends on
 - Data distribution
 - Parameters of distribution (e.g., mean, variance)
 - Number of expected outliers (confidence limit)
- Issues
 - Identifying the distribution of a data set
 - Heavy tailed distribution
 - Number of attributes
 - Is the data a mixture of distributions?

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Grubbs' Test

- Detect outliers in univariate data
- Assume data comes from normal distribution
- Detects one outlier at a time, remove the outlier, and repeat
 - H₀: There is no outlier in data
 - H_A: There is at least one outlier
- $G = \frac{\max \left| X \overline{X} \right|}{}$ • Grubbs' test statistic:
- Reject H₀ if:

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Statistical-based – Likelihood Approach

- Assume the data set D contains samples from a mixture of two probability distributions:
 - M (majority distribution)
 - A (anomalous distribution)
- General Approach:
 - Initially, assume all the data points belong to M
 - Let L_t(D) be the log likelihood of D at time t
 - For each point x_t that belongs to M, move it to A
 - ◆ Let L_{t+1} (D) be the new log likelihood.
 - Compute the difference, $\Delta = L_t(D) L_{t+1}(D)$
 - If $\Delta > c$ (some threshold), then x_t is declared as an anomaly and moved permanently from M to A

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Statistical-based – Likelihood Approach

- Data distribution, D = (1λ) M + λ A
- M is a probability distribution estimated from data
 - Can be based on any modeling method (naïve Bayes, maximum entropy, etc)
- A is initially assumed to be uniform distribution
- Likelihood at time t:

$$\begin{split} L_{t}(D) &= \prod_{i=1}^{N} P_{D}(x_{i}) = \left((1-\lambda)^{|M_{t}|} \prod_{x_{i} \in M_{t}} P_{M_{t}}(x_{i}) \right) \left(\lambda^{|A_{t}|} \prod_{x_{i} \in A_{t}} P_{A_{t}}(x_{i}) \right) \\ LL_{t}(D) &= \left| M_{t} \middle| \log(1-\lambda) + \sum_{x_{i} \in M_{t}} \log P_{M_{t}}(x_{i}) + \middle| A_{t} \middle| \log\lambda + \sum_{x_{i} \in A_{t}} \log P_{A_{t}}(x_{i}) \right. \end{split}$$

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Strengths/Weaknesses of Statistical Approaches

- Firm mathematical foundation
- Can be very efficient
- Good results if distribution is known
- In many cases, data distribution may not be known
- For high dimensional data, it may be difficult to estimate the true distribution
- Anomalies can distort the parameters of the distribution

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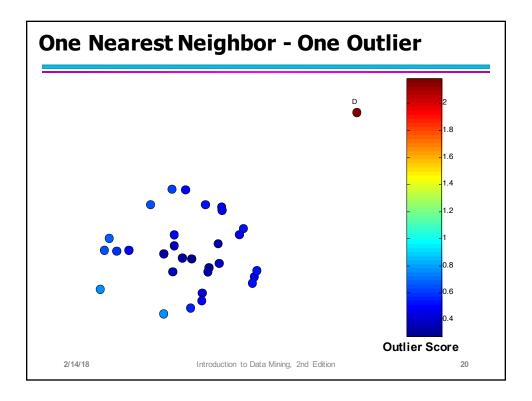
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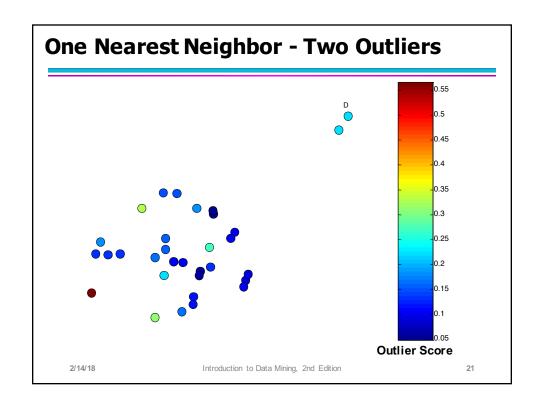
Distance-Based Approaches

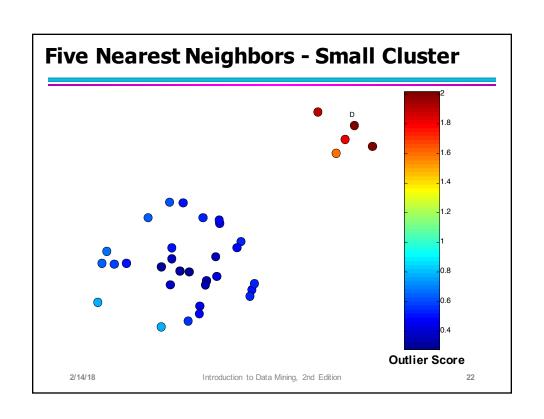
- Several different techniques
- An object is an outlier if a specified fraction of the objects is more than a specified distance away (Knorr, Ng 1998)
 - Some statistical definitions are special cases of this
- The outlier score of an object is the distance to its kth nearest neighbor

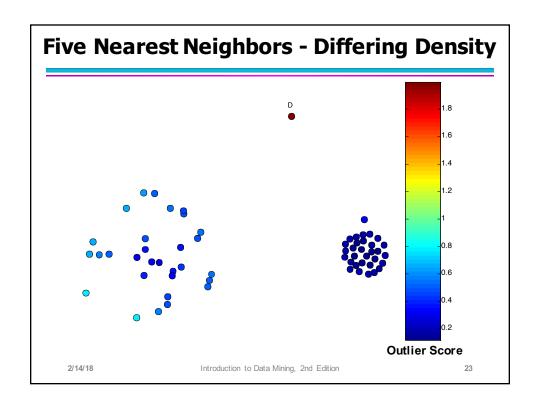
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Strengths/Weaknesses of Distance-Based Approaches

- Simple
- Expensive O(n²)
- Sensitive to parameters
- Sensitive to variations in density
- Distance becomes less meaningful in highdimensional space

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Density-Based Approaches

- Density-based Outlier: The outlier score of an object is the inverse of the density around the object.
 - Can be defined in terms of the k nearest neighbors
 - One definition: Inverse of distance to kth neighbor
 - Another definition: Inverse of the average distance to k neighbors
 - DBSCAN definition
- If there are regions of different density, this approach can have problems

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Relative Density

 Consider the density of a point relative to that of its k nearest neighbors

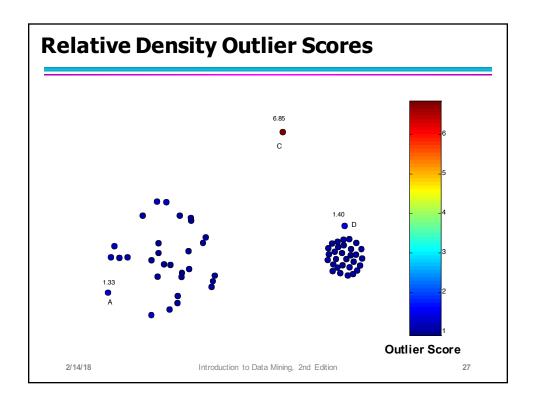
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average relative density(\mathbf{x}, k) = \frac{density(\mathbf{x}, k)}{\sum_{\mathbf{y} \in N(\mathbf{x}, k)} density(\mathbf{y}, k) / |N(\mathbf{x}, k)|}. (10.7)
```

Algorithm 10.2 Relative density outlier score algorithm.

- 1: $\{k \text{ is the number of nearest neighbors}\}$
- 2: for all objects x do
- 3: Determine $N(\mathbf{x}, k)$, the k-nearest neighbors of \mathbf{x} .
- 4: Determine $density(\mathbf{x}, k)$, the density of \mathbf{x} , using its nearest neighbors, i.e., the objects in $N(\mathbf{x}, k)$.
- 5: end for
- 6: for all objects \mathbf{x} do
- Set the outlier score(x, k) = average relative density(x, k) from Equation 10.7.
- 8: end for

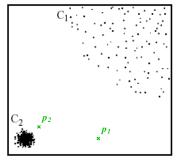
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Density-based: LOF approach

- For each point, compute the density of its local neighborhood
- Compute local outlier factor (LOF) of a sample p as the average of the ratios of the density of sample p and the density of its nearest neighbors
- Outliers are points with largest LOF value



In the NN approach, p_2 is not considered as outlier, while LOF approach find both p_1 and p_2 as outliers

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Strengths/Weaknesses of Density-Based Approaches

- Simple
- Expensive O(n²)
- Sensitive to parameters
- Density becomes less meaningful in highdimensional space

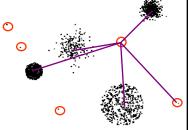
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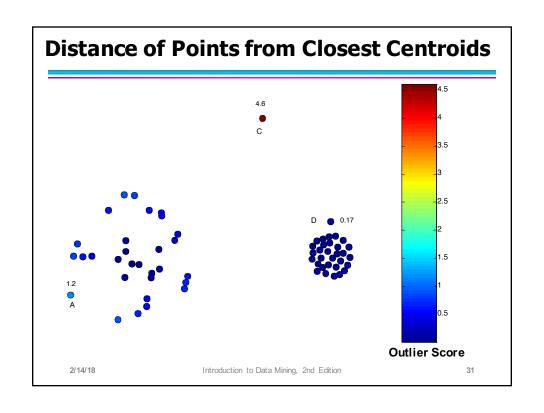
Clustering-Based Approaches

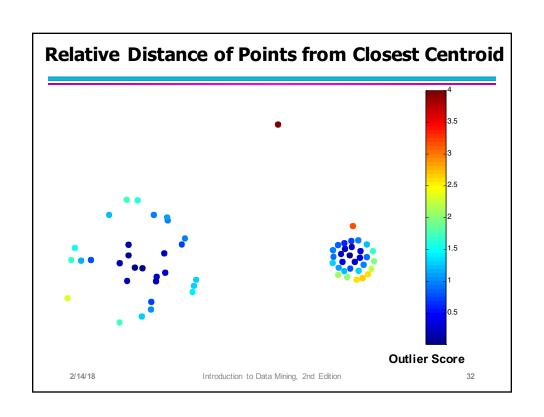
- Clustering-based Outlier: An object is a cluster-based outlier if it does not strongly belong to any cluster
 - For prototype-based clusters, an object is an outlier if it is not close enough to a cluster center
 - For density-based clusters, an objec is an outlier if its density is too low
 - For graph-based clusters, an object is an outlier if it is not well connected
- Other issues include the impact of outliers on the clusters and the number of clusters



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Strengths/Weaknesses of Distance-Based Approaches

- Simple
- Many clustering techniques can be used
- Can be difficult to decide on a clustering technique
- Can be difficult to decide on number of clusters
- Outliers can distort the clusters

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