mcs_q_learning_sarsa

March 3, 2023

1 Monte Carlo Simulation

1.1 Dependencies

```
[26]: import random
from typing import List
from collections import defaultdict
import numpy as np
import matplotlib.pyplot as plt
```

1.2 Simulation function

Whenever we check the efficiency of a particular batch_size: - We decide if a subject is infected or by a probability samplied from (0.001, 0.1) range. - We split all the subjects in batches. - If there is any infected subject in the batch then we will consider to test them all. - If there is no infected subject in a batch then we consider we have done only one test.

1.3 Monte carlo sampling

We consider N subjects and number_of_trials trials for sampling a batch_size from the interval of [1, N/2]. - I decided to make the upper end for the batch_size to be equal to N/2 just to exclude those batch sizes that would definitely not be a viable choice.

```
[28]: N = 10_000
number_of_trials = 10_000

def get_random_batch_size(N) -> int:
    return int(random.uniform(1, N))

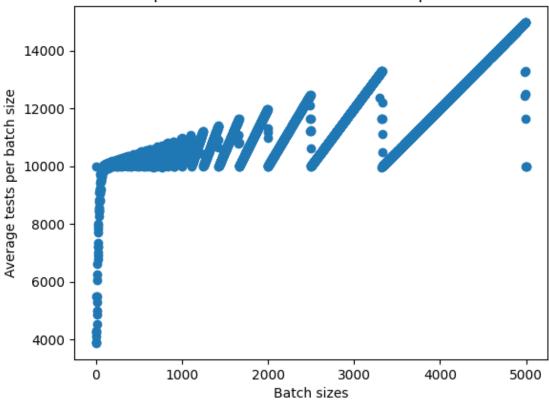
necessary_tests_per_batch_size = defaultdict(list)
for trial in range(number_of_trials):
    chosen_batch_size = get_random_batch_size(N / 2)
    result = simulate(N, chosen_batch_size)
    necessary_tests_per_batch_size[chosen_batch_size].append(result)
```

1.4 Results

1.4.1 Number of tests per batch size

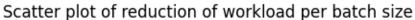
- The threshold for number of tests to be conducted is number_of_tests = \mathbb{N} for batch_size = 1
- We are searching for the value that minimizes the number of tests.
- We observe that for relatively big batch_sizes the number of tests is bigger than the threshold

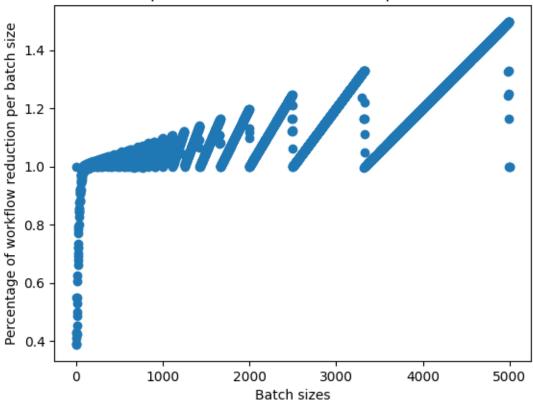




1.4.2 Expected reduction in workload

- The heuristic we use for this case is the average_tests_per_batch_size / N, where N is the threshold number of tests we would need to do if we test each subject individually.
- The heuristic result should be interpreted as: What is the percentage of number of tests with respect to N that we need to do under a particular batch_size





1.4.3 Best batch size under the particular experimental setup

```
[31]: min_pair = min(expected_reduction_in_workload_per_batch_size_dictionary.

→items(), key=lambda x: x[1])

print(f"Best batch_size={min_pair[0]} => implies that we should be conducting_

→only {min_pair[1] * 100}% number_of_tests with respect to N")
```

Best batch_size=5 => implies that we should be conducting only 38.72% number_of_tests with respect to N

2 Q learning versus SARSA

2.1 Dependencies

```
[32]: import random import numpy as np import matplotlib.pyplot as plt
```

2.2 Helpers

```
[33]: ROWS=4
      COLUMNS=21
      START = "S"
      GOAL = "G"
      CLIFF = "C"
      SNAKE PIT = "P"
      UP = "" "
      DOWN = "v"
      RIGHT = ">"
      LEFT = "<"
      ACTIONS = [UP, DOWN, RIGHT, LEFT]
      ACTION_POSITION_MAPPER = {
          UP: (-1, 0),
          RIGHT: (0, 1),
          DOWN: (1, 0),
          LEFT: (0, -1)
      }
      START_POSITION = (3, 0)
      GOAL_POSITION = (3, 20)
      SNAKE_PIT_POSITION = (0, 11)
      CLIFF_POSITIONS = [(3, cliff_column_index) for cliff_column_index in range(1, __
       →COLUMNS - 1)]
      def get_world(with_snake_pit):
          world = [[random.choice(ACTIONS) for _ in range(COLUMNS)] for _ in_
       →range(ROWS)]
          world[START_POSITION[0]][START_POSITION[1]] = START
          world[GOAL_POSITION[0]][GOAL_POSITION[1]] = GOAL
          if with_snake_pit:
              world[SNAKE_PIT_POSITION[0]][SNAKE_PIT_POSITION[1]] = SNAKE_PIT
          for cliff_position in CLIFF_POSITIONS:
             world[cliff_position[0]][cliff_position[1]] = CLIFF
          return world
      def print_world(world):
          for row in world:
              print(" ".join(row))
```

```
def choose_action(Q, new_state, epsilon):
    if np.random.uniform(0, 1) < epsilon:</pre>
        return random.choice(ACTIONS)
        actions_utilities = Q[new_state]
        return ACTIONS[np.argmax(actions_utilities)]
def get_start_state():
    return START_POSITION
def get new state(current state, action):
 position_updater = ACTION_POSITION_MAPPER[action]
 new_state = (current_state[0] + position_updater[0], current_state[1] +__
 →position_updater[1])
  # row invalidation
  if new_state[0] < 0 or new_state[0] > ROWS - 1:
     return current_state
  # column invalidation
  if new state[1] < 0 or new state[1] > COLUMNS - 1:
    return current state
 return new_state
def final_state(state):
    return state == GOAL_POSITION or state in CLIFF_POSITIONS
def get_reward(position, with_snake_pit):
    if position == GOAL_POSITION:
        return 20
    if position in CLIFF_POSITIONS:
        return -100
    if with_snake_pit and position in SNAKE_PIT_POSITION:
        return -100
    return -1
```

2.3 Sarsa implementation

```
[34]: def run_sarsa(epochs = 2000, epsilon=0, with_snake_pit=False, alpha = 0.1, usegamma = 0.9):
Q = {(i,j):[0, 0, 0, 0] for i in range(ROWS) for j in range(COLUMNS)}
```

```
rewards_history = []
for _ in range(epochs):
  current_state = get_start_state()
  current_action = choose_action(Q, current_state, epsilon=epsilon)
  reward_per_epoch = 0
  while not final_state(current_state):
    new_state = get_new_state(current_state, current_action)
    new_action = choose_action(Q, new_state, epsilon=epsilon)
    reward = get_reward(new_state, with_snake_pit)
    reward_per_epoch += reward
    current_action_index_in_Q = ACTIONS.index(current_action)
    Q_current = Q[current_state][current_action_index_in_Q]
    new_action_index_in_Q = ACTIONS.index(current_action)
    Q_next = Q[new_state][new_action_index_in_Q]
    Q[current_state][current_action_index_in_Q] = Q_current + (alpha *_
current_state = new_state
    current_action = new_action
  rewards_history.append(reward_per_epoch)
return Q, rewards_history
```

2.4 Q Learning + replay buffer implementation

```
new_state = get_new_state(current_state, current_action)
    reward = get_reward(new_state, with_snake_pit)
    replay_buffer.append((current_state, current_action, reward, new_state))
    if len(replay_buffer) > REPLAY_BUFFER_SIZE:
      replay_buffer.pop(0)
    if replay buffer enabled:
      if len(replay_buffer) > REPLAY_BUFFER_BATCH_SIZE:
        buffer memory = random.sample(replay buffer, REPLAY BUFFER BATCH SIZE)
        for experience in buffer_memory:
         current_state_history, current_action_history, reward_history,__

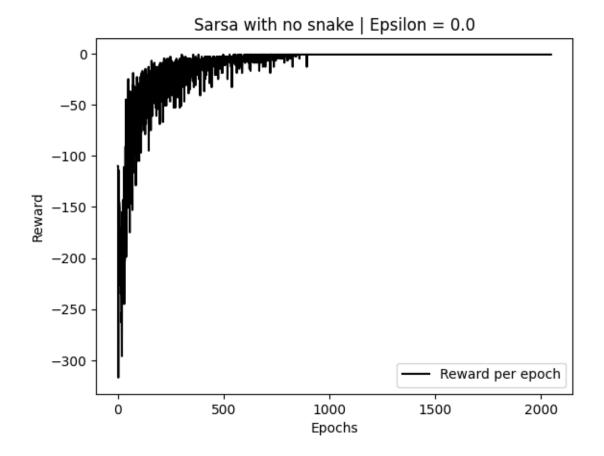
¬new_state_history = experience
         current_action_index_in_Q = ACTIONS.index(current_action_history)
         Q_current = Q[current_state_history][current_action_index_in_Q]
         max_Q_next = max(Q[new_state_history])
         Q[current_state_history][current_action_index_in_Q] = Q_current +
else:
      current_action_index_in_Q = ACTIONS.index(current_action)
      Q_current = Q[current_state][current_action_index_in_Q]
     max_Q_next = max(Q[new_state])
      Q[current state][current action index in Q] = Q current + (alpha *,,
current_state = new_state
    reward_per_epoch += reward
  rewards_history.append(reward_per_epoch)
return Q, rewards_history
```

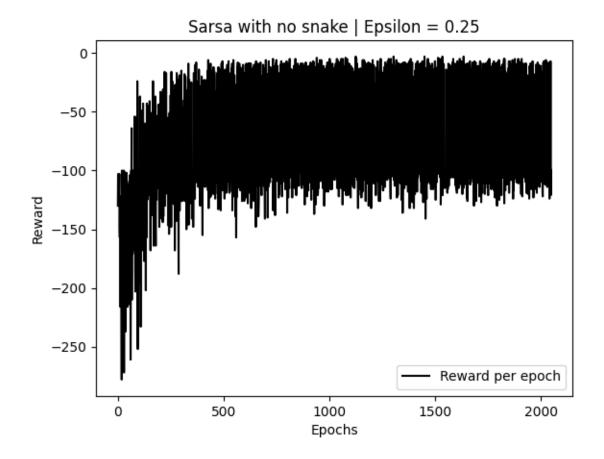
2.5 Results

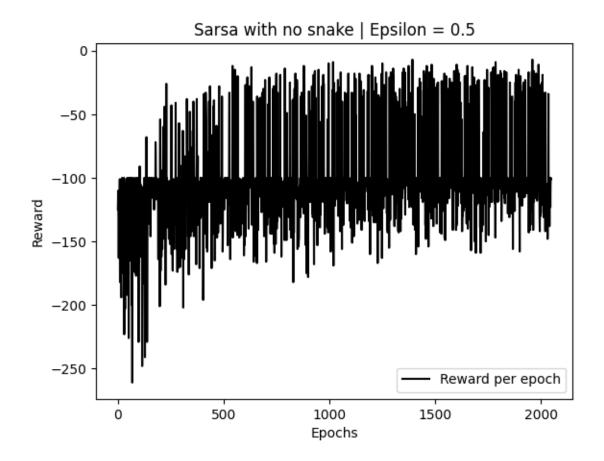
2.5.1 Sarsa with no snake

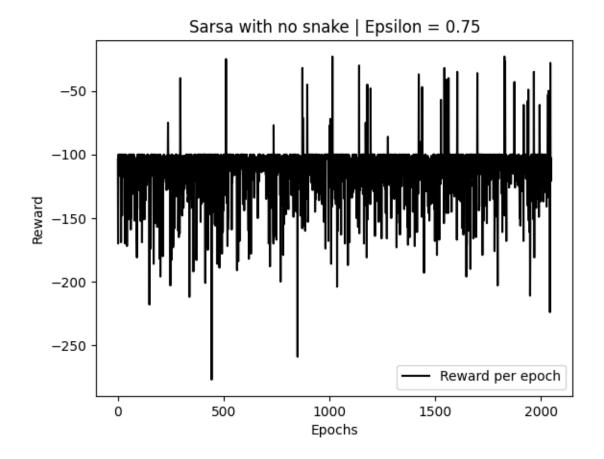
- We notice that in this case for smaller epsilon values, the agent manages to find the path to the goal, walking safe path.
- It manages to construct better global policy for smaller epsilon values.
- As epsilon increases, his exploration increases, and arguably, by change, he just falls down the cliff and ends the episode. That's the reason for some experiments, he didn't manage to construct a good policy to the goal position.

```
[36]: epochs = 2048
      x = np.linspace(1, epochs, epochs)
      for epsilon in [0.0, 0.25, 0.5, 0.75, 1.0]:
          Q, rewards_history = run_sarsa(epochs=epochs, epsilon=epsilon)
          # Plot rewards
          plt.plot(x, rewards_history, color='black', label=f"Reward per epoch")
          plt.xlabel('Epochs')
          plt.ylabel('Reward')
          plt.legend()
          plt.title(f"Sarsa with no snake | Epsilon = {epsilon}")
          plt.show()
          world = get_world(with_snake_pit=False)
          for position in Q:
              actions_utilities = Q[position]
              if world[position[0]][position[1]] not in [GOAL, START, CLIFF]:
                  world[position[0]][position[1]] = ACTIONS[np.
       →argmax(actions_utilities)]
          # Printing world
          print_world(world)
          print("-" * 80)
```

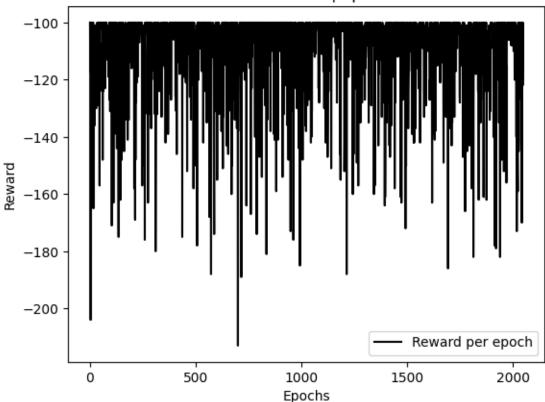












2.5.2 Q learning with no replay buffer and no snake

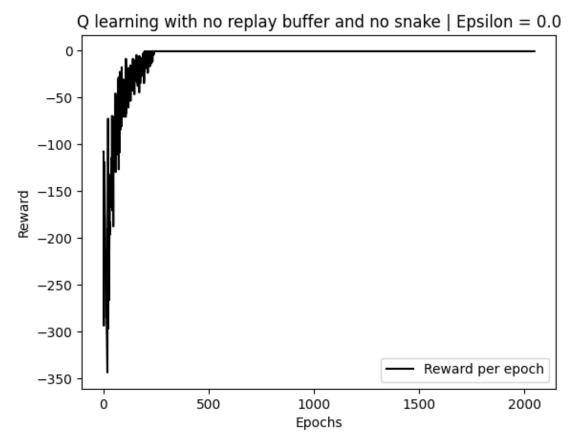
- We notice that in this case for smaller epsilon values, the agent manages to find the optimal path to the goal.
- We observe that for any values of epsilon, the agent is always trying to construct the most optimal path.
- For higher values of epsilon, the agent fails to construct a viable policy because is falling down the cliff most of the times. That thing will change when we add replay buffer.

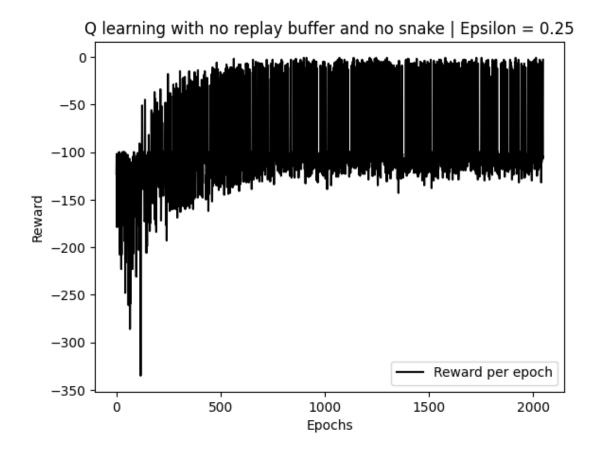
```
[37]: epochs = 2048

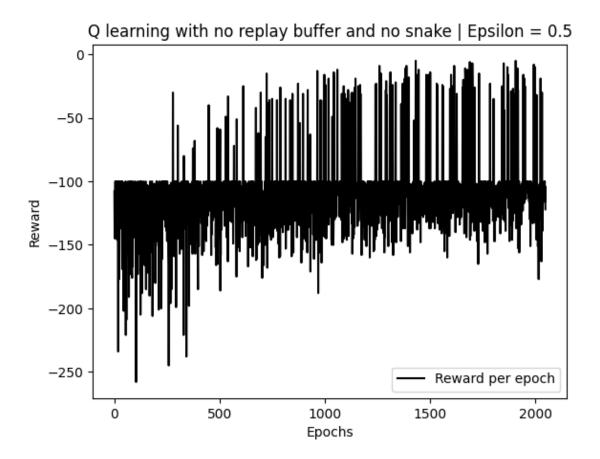
x = np.linspace(1, epochs, epochs)

for epsilon in [0.0, 0.25, 0.5, 0.75, 1.0]:
```

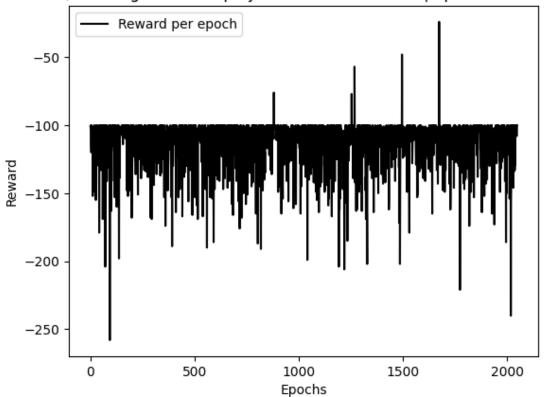
```
Q, rewards_history = run_q_learning(epochs=epochs, epsilon=epsilon,_u
oreplay_buffer_enabled=False, with_snake_pit=False)
  # Plot rewards
  plt.plot(x, rewards_history, color='black', label=f"Reward per epoch")
  plt.xlabel('Epochs')
  plt.ylabel('Reward')
  plt.legend()
  plt.title(f"Q learning with no replay buffer and no snake | Epsilon = 11
plt.show()
  world = get_world(with_snake_pit=False)
  for position in Q:
      actions_utilities = Q[position]
      if world[position[0]][position[1]] not in [GOAL, START, CLIFF]:
          world[position[0]][position[1]] = ACTIONS[np.
→argmax(actions_utilities)]
  # Printing world
  print_world(world)
  print("-" * 80)
```

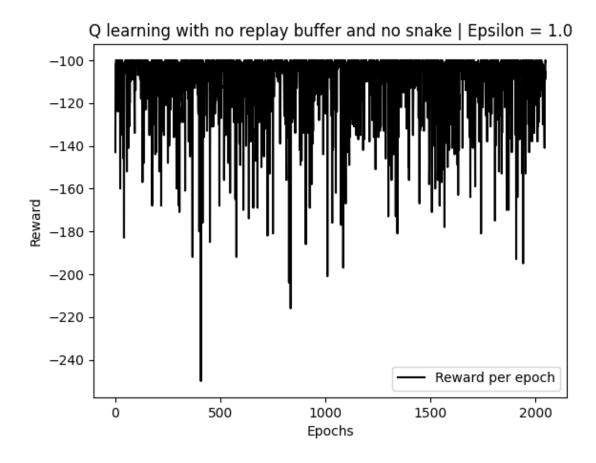






Q learning with no replay buffer and no snake | Epsilon = 0.75

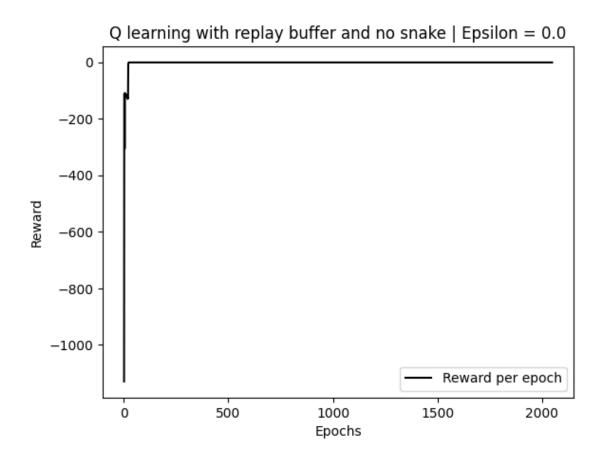


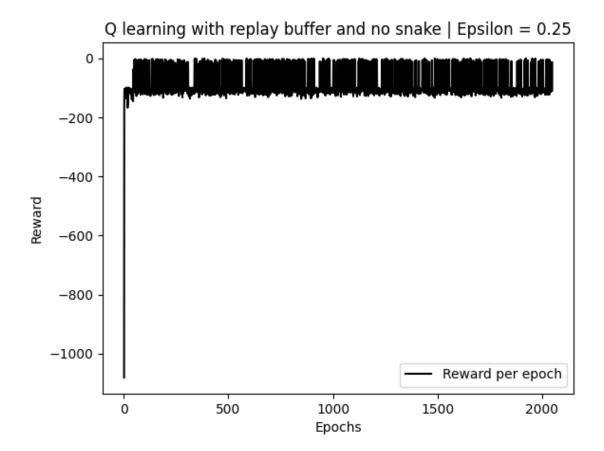


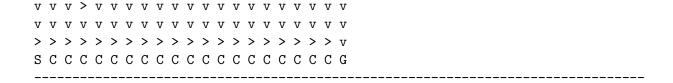
2.5.3 Q learning with replay buffer and no snake

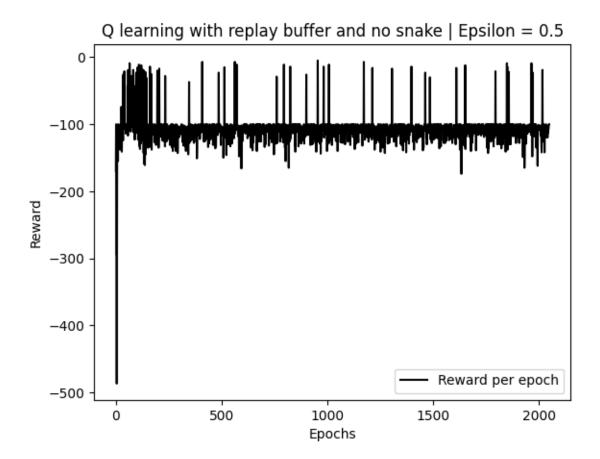
- Replay buffer is an element of stability to Q-learning execution.
- We observe that for a high value of epsilon = 0.75 the agent managed to find a viable (in particular, optimal) policy to the goal state.
- Clearly, replay buffer is an improvement to the normal version, but for epsilon = 1, it didn't manage to construct the proper policy. The reasons for that are:
 - Chance, because due to a completely random exploration, it might just happen (Given 2048 epochs) for the agent to never find the path to the goal state.
 - Replay buffer hyperparameters (REPLAY_BUFFER_SIZE = 2048, RE-PLAY_BUFFER_BATCH_SIZE = 1024). I argue that by fine tuning replay buffer's hyperparameters and by experimenting some epochs in which the agent manages to find a way to the goal under the complete randomness of epsilon=1, then a proper policy might be derived.

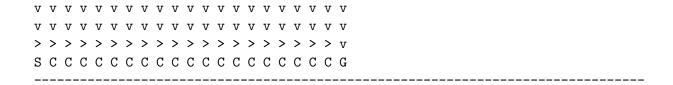
```
[38]: epochs = 2048
      x = np.linspace(1, epochs, epochs)
      for epsilon in [0.0, 0.25, 0.5, 0.75, 1.0]:
          Q, rewards_history = run_q_learning(epochs=epochs, epsilon=epsilon,__
       Greplay_buffer_enabled=True, with_snake_pit=False)
          # Plot rewards
          plt.plot(x, rewards_history, color='black', label=f"Reward per epoch")
          plt.xlabel('Epochs')
          plt.ylabel('Reward')
          plt.legend()
          plt.title(f"Q learning with replay buffer and no snake | Epsilon = L
       →{epsilon}")
          plt.show()
          world = get_world(with_snake_pit=False)
          for position in Q:
              actions_utilities = Q[position]
              if world[position[0]][position[1]] not in [GOAL, START, CLIFF]:
                  world[position[0]][position[1]] = ACTIONS[np.
       →argmax(actions_utilities)]
          # Printing world
          print_world(world)
          print("-" * 80)
```

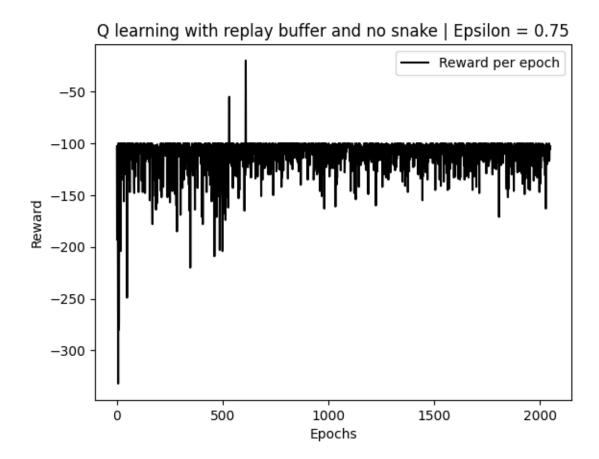


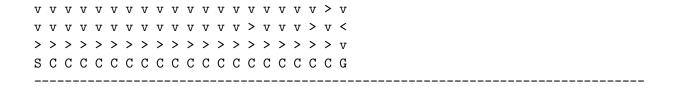


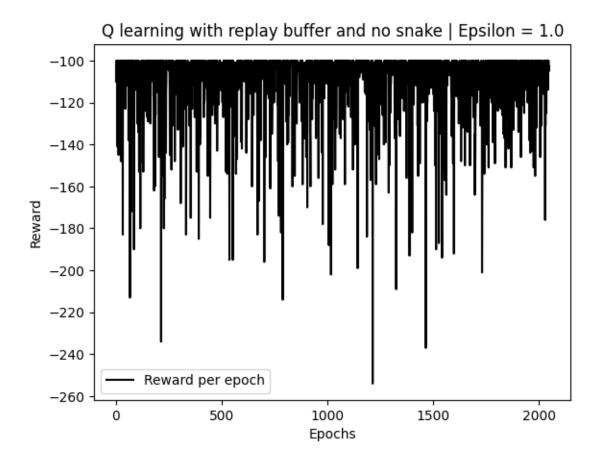












2.5.4 Sarsa with snake

- Adding the snake created some disturbances around its position, but the agent is still managing to derive the right safe policy for small values of epsilon.
- For high values of epsilon we experience the same situation as in with no snake situation.

```
[39]: epochs = 2048
x = np.linspace(1, epochs, epochs)

for epsilon in [0.0, 0.25, 0.5, 0.75, 1.0]:
    Q, rewards_history = run_sarsa(epochs=epochs, epsilon=epsilon, with_snake_pit=True)
    # Plot rewards
    plt.plot(x, rewards_history, color='black', label=f"Reward per epoch")
```

```
plt.xlabel('Epochs')
plt.ylabel('Reward')
plt.legend()
plt.title(f"Sarsa with snake | Epsilon = {epsilon}")
plt.show()

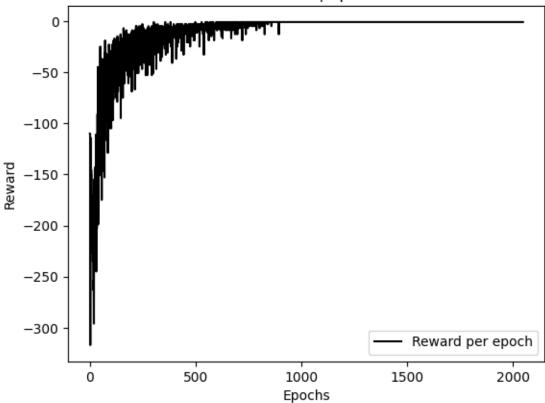
world = get_world(with_snake_pit=True)
for position in Q:
    actions_utilities = Q[position]
    if world[position[0]][position[1]] not in [GOAL, START, CLIFF, world[position[0]][position[1]] = ACTIONS[np.

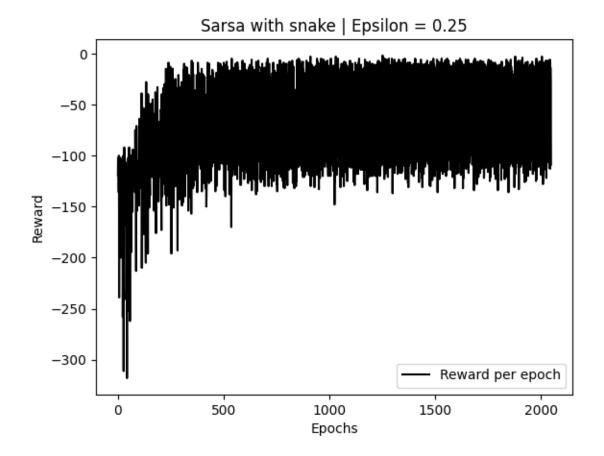
argmax(actions_utilities)]

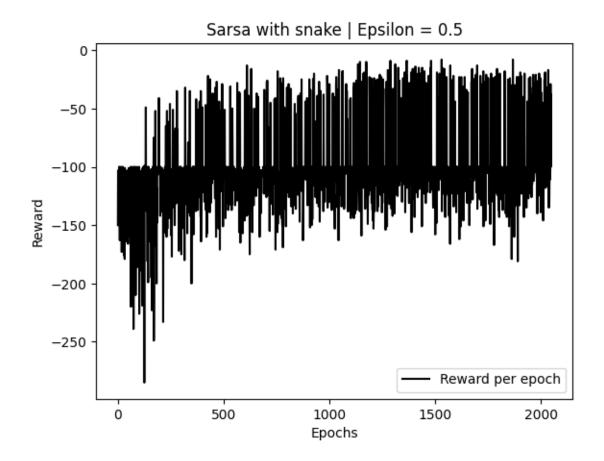
# Printing world
print_world(world)

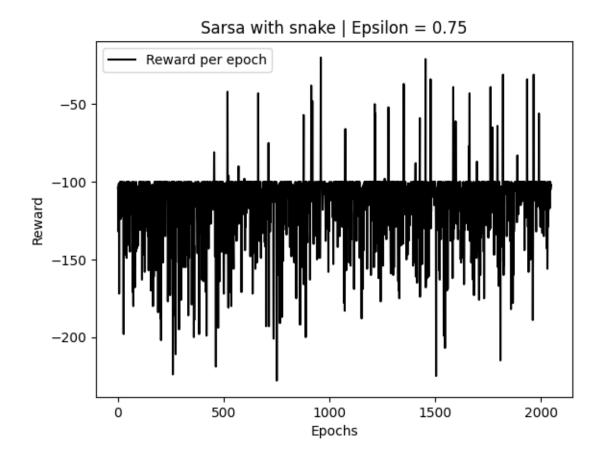
print("-" * 80)
```



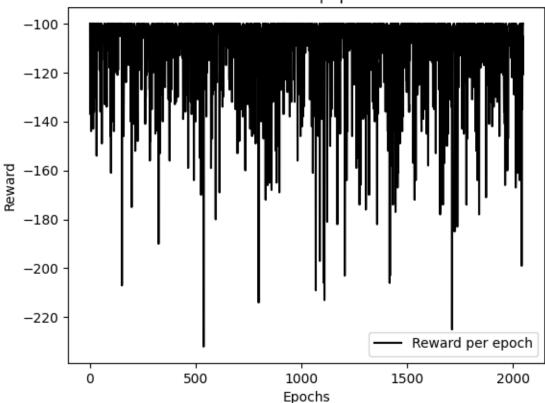








Sarsa with snake | Epsilon = 1.0



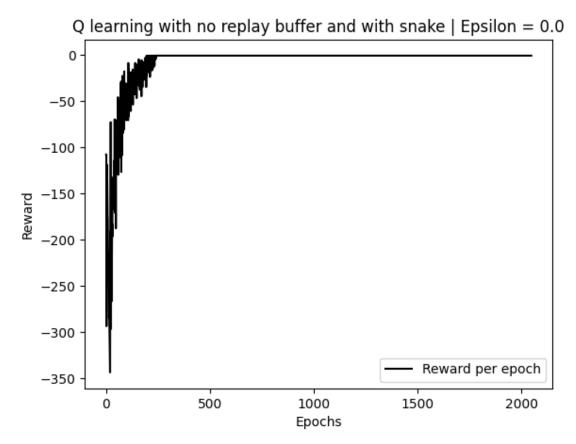
2.5.5 Q learning with no replay buffer and with snake

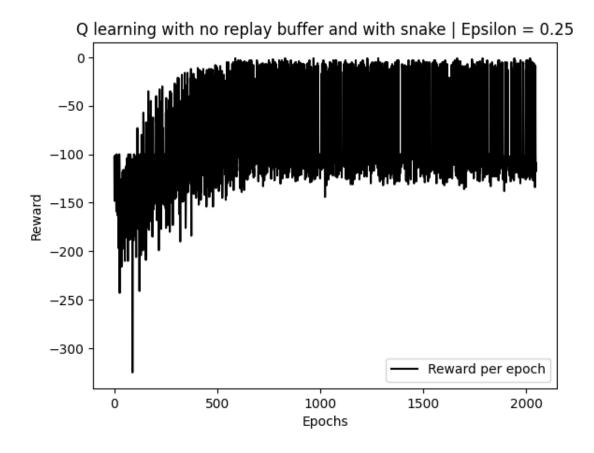
- We observe that the snake doesn't affect the agent's ability to derive the optimal policy to the goal state.
- For higher values of epsilon (same case as before), the agent (arguably, falls down the cliff) fails to construct an appropriate policy to the goal state.

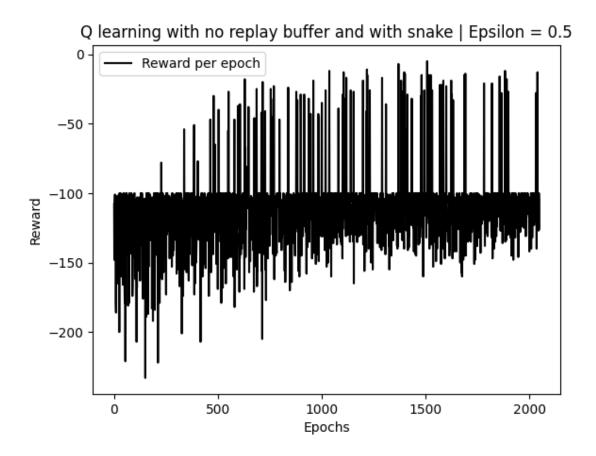
```
[40]: epochs = 2048
x = np.linspace(1, epochs, epochs)

for epsilon in [0.0, 0.25, 0.5, 0.75, 1.0]:
    Q, rewards_history = run_q_learning(epochs=epochs, epsilon=epsilon,useplay_buffer_enabled=False, with_snake_pit=True)
# Plot rewards
```

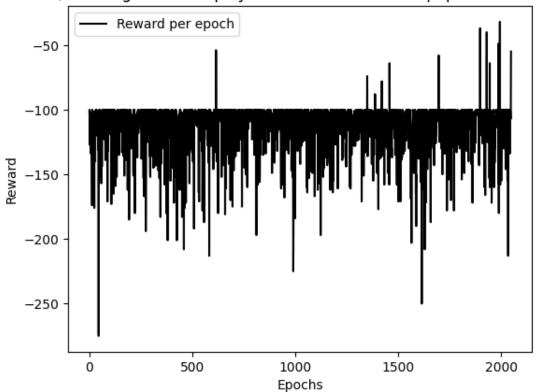
```
plt.plot(x, rewards_history, color='black', label=f"Reward per epoch")
  plt.xlabel('Epochs')
  plt.ylabel('Reward')
  plt.legend()
  plt.title(f"Q learning with no replay buffer and with snake | Epsilon = __
plt.show()
  world = get_world(with_snake_pit=True)
  for position in Q:
      actions_utilities = Q[position]
      if world[position[0]][position[1]] not in [GOAL, START, CLIFF, __
SNAKE_PIT]:
          world[position[0]][position[1]] = ACTIONS[np.
→argmax(actions_utilities)]
  # Printing world
  print_world(world)
  print("-" * 80)
```

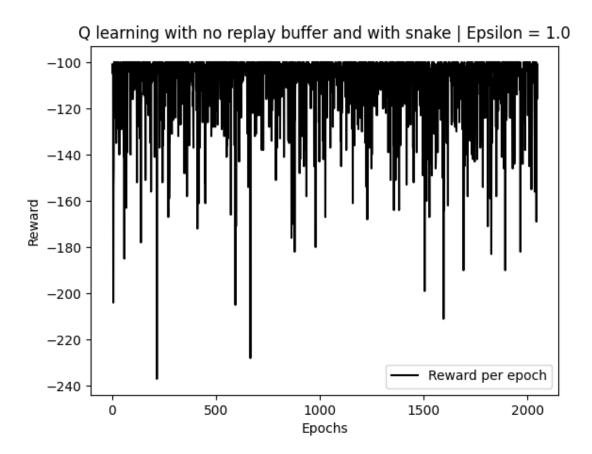












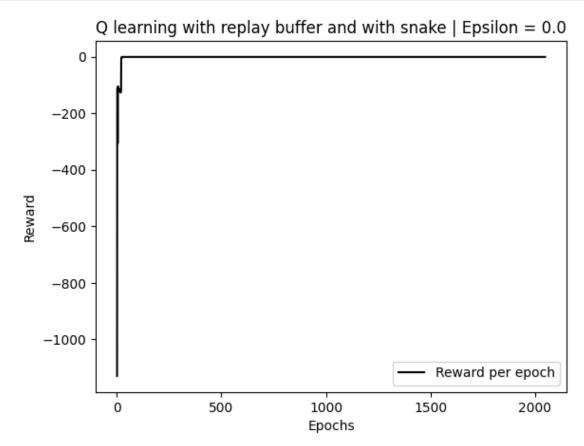
2.5.6 Q learning with replay buffer and with snake

- Same situation as before, the agent manages to construct the optimal policy under low values of epsilon.
- The snake pit seems to not have any quantifiable effect on the policy derivation process.
- Under bigger values of epsilon, the same problems(Chance and Hyperparameters) prevent the agent to derive a valid policy.

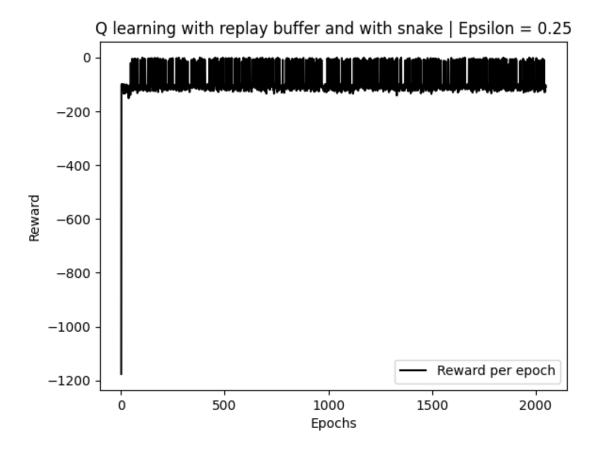
```
[41]: epochs = 2048
x = np.linspace(1, epochs, epochs)

for epsilon in [0.0, 0.25, 0.5, 0.75, 1.0]:
    Q, rewards_history = run_q_learning(epochs=epochs, epsilon=epsilon, epochs_eplay_buffer_enabled=True, with_snake_pit=True)
# Plot rewards
```

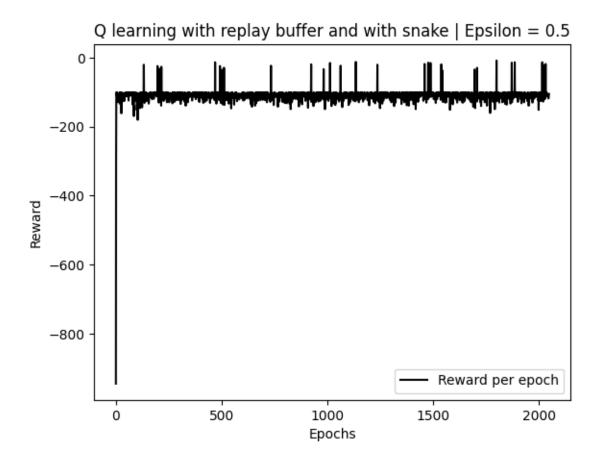
```
plt.plot(x, rewards_history, color='black', label=f"Reward per epoch")
  plt.xlabel('Epochs')
  plt.ylabel('Reward')
  plt.legend()
  plt.title(f"Q learning with replay buffer and with snake | Epsilon = ___
plt.show()
  world = get_world(with_snake_pit=True)
  for position in Q:
      actions_utilities = Q[position]
      if world[position[0]][position[1]] not in [GOAL, START, CLIFF, __
SNAKE_PIT]:
          world[position[0]][position[1]] = ACTIONS[np.
→argmax(actions_utilities)]
  # Printing world
  print_world(world)
  print("-" * 80)
```

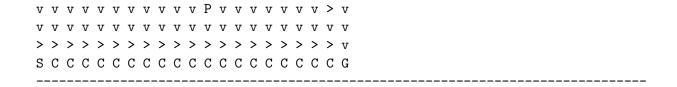


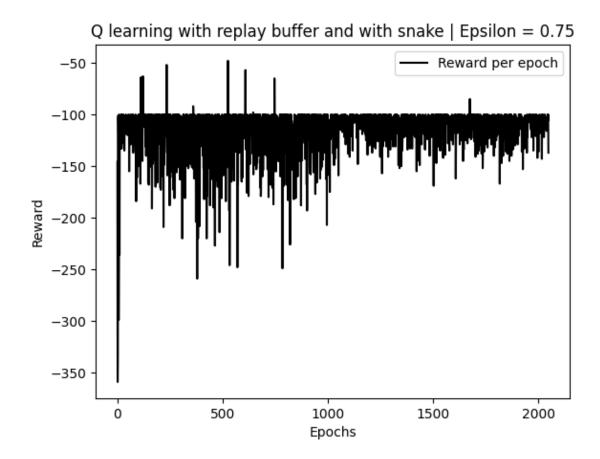




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