

Bayesian Aggregation of Categorical Distributions with Applications in Crowdsourcing

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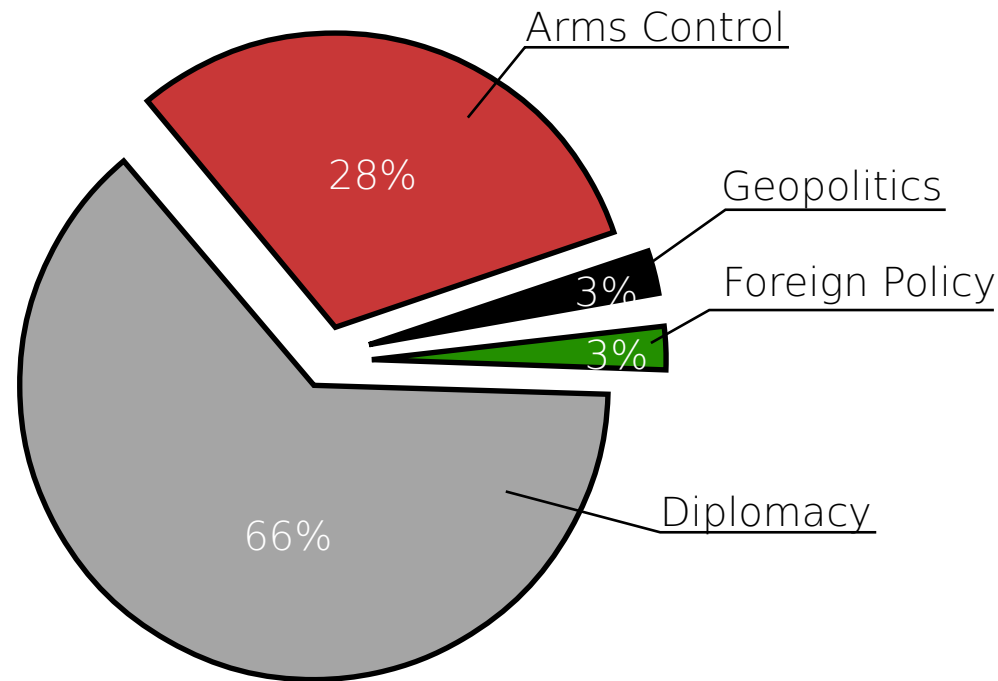
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Motivating Examples

Possible application domain include information retrieval and recommendation:



Source: BBC, 2017



Example judgment of proportions

Challenges

- Malicious participants (i.e. **spammers**) constitute up to 45% of all workers [Vuurens et al., 2011].
- Spammers increase the cost of judgment acquisition and degrade accuracy of the aggregation.

Previous Approaches

- Linear opinion pool (arithmetic mean)
 - ✓ Fast
 - ✗ Does not account for spammers
- Label distribution learning (LDL) framework [Geng, 2016]
 - ✓ Comprehensive
 - ✗ Does not account for spammers
- Independent Bayesian classifier combination (IBCC) [Kim et al, 2012]
 - ✓ Accounts for spammers
 - ✗ Does not aggregate distributions

Our Solution (MBCC)

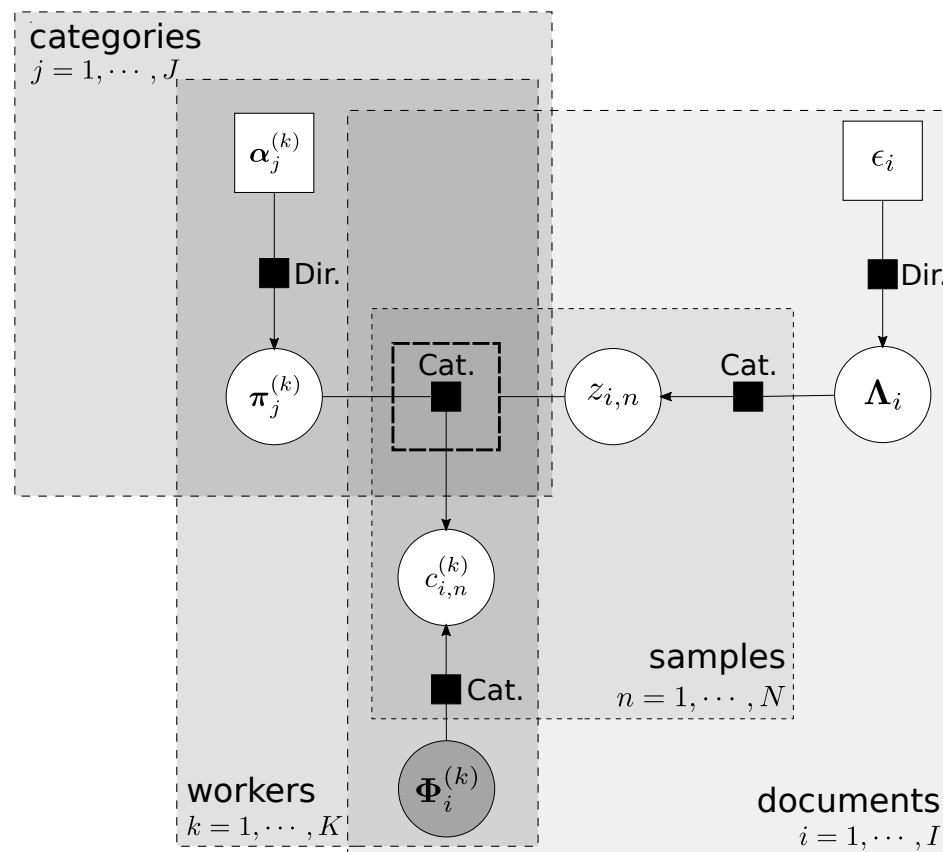
$\pi_j^{(k)} \sim \text{Dir}(\alpha_j^{(k)})$ j -th row of the confusion matrix of worker k

$\Lambda_i \sim \text{Dir}(\epsilon_i)$ Aggregated distribution of document i

$z_{i,n} \sim \text{Cat}(\Lambda_i)$ Sampled category n from aggregated distribution of document i

$c_{i,n}^{(k)} \sim \text{Cat}(\pi_{z_{i,n}}^{(k)})$ Sampled category n from worker k 's judgment of document i

$\Phi_i^{(k)}$ Judgment of document i by worker k (categorical dist.)



Factor graph of MBCC used for inference

Datasets

1. **SemEval**: 6 sentiments in 100 news headlines (1,000 judgments)
2. **IAPR-TC12**: 6 regions in 16 urban and rural scenes (441 judgments)
3. **Colours**: 10 colours in 20 countries' flag (460 judgments)

Task 55: Making peace from victory over poverty.

Joy [70] Sadness [0] Disgust [35]
Anger [0] Surprise [0] Fear [0]

SemEval



IAPR-TC12



Colours

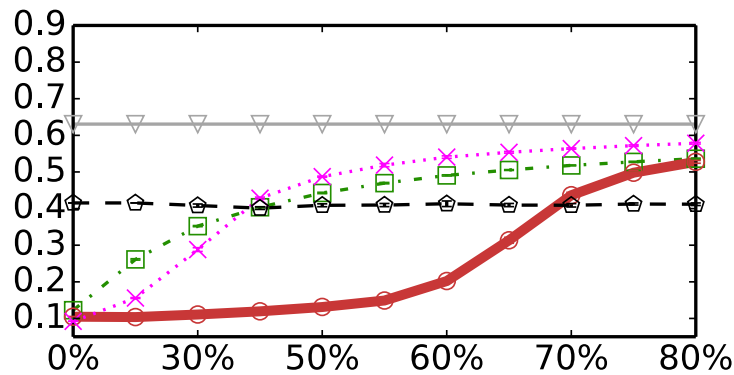
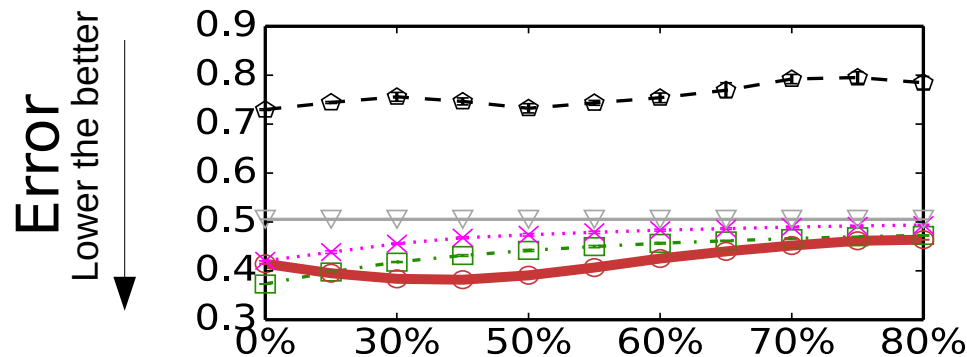
- Each dataset is augmented with additional synthetic spammers to explore the loss of accuracy as they increase in number.
- The distribution of each spammer k for each document i shares a prior Dirichlet distribution such that

$$\Phi_i^{(k)} \sim \text{Dir}(\mathbf{1}).$$

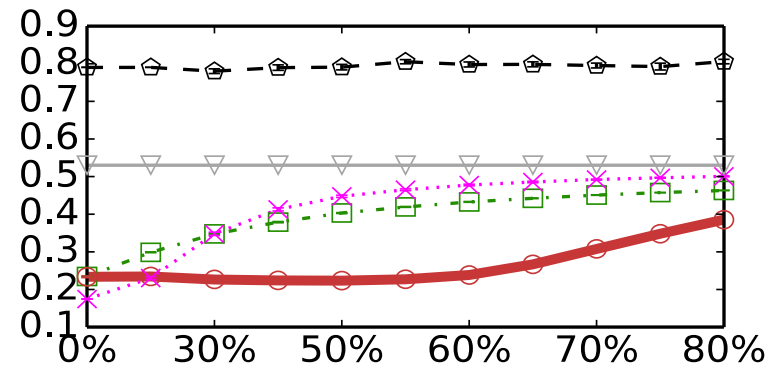
Results 1: Aggregation Error

Aggregation error is robust to an increasing ratio of spammers:

SemEval dataset



IAPR-TC12 dataset



Colours dataset

Results 2: Classification of Workers

Accuracy of classifying diligent workers from spammers is improved:

Confusion matrices

		Judgment			
		1	2	3	4
True Category	1	0.25	0.25	0.25	0.25
	2	0.00	0.50	0.00	0.50
	3	0.00	0.00	1.00	0.00
	4	0.00	0.50	0.00	0.50

Worker 1

		Judgment			
		1	2	3	4
True Category	1	1	0	0	0
	2	0	1	0	0
	3	0	0	1	0
	4	0	0	0	1

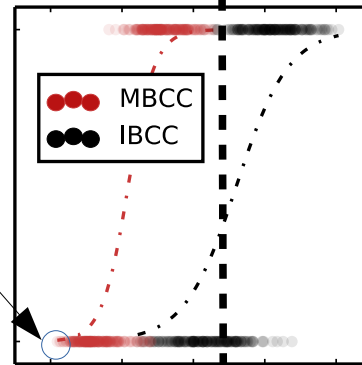
Perfect worker

Threshold of error

Spammers

Euclidean distance

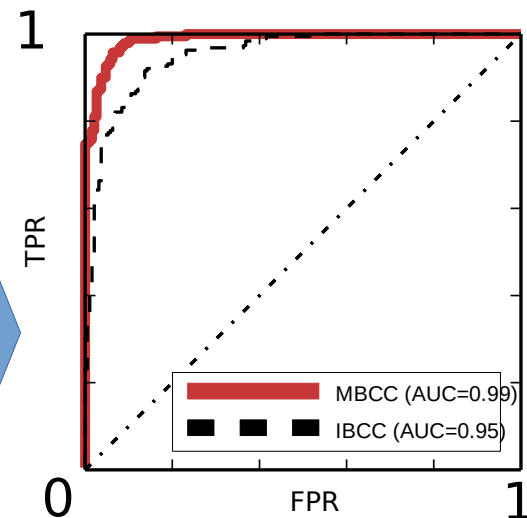
Diligent workers



Error

Scatter plot (SemEval)

Varying threshold



ROC curve (SemEval)

References

- [1] Vuurens et al., "How Much Spam Can You Take? An Analysis of Crowd sourcing Results to Increase Accuracy", CIR, 2011.
- [2] X. Geng, "Label distribution learning". IEEE Transactions on Knowledge and Data Engineering, 2016.
- [3] Kim et al., "Bayesian Classifier Combination", AISTATS, 2012.
- [4] M. Bacharach, "Normal Bayesian Dialogues", Journal of the American Statistical Association, 1979.