
A TRANSFORMER MODEL FOR RETROSYNTHESIS

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ABSTRACT

We describe a Transformer model for a retrosynthetic reaction prediction task. The model is trained end-to-end on 45 033 experimental reaction examples extracted from USA patents. Our final model can successfully predict the reactants set for 42.7% of cases on the external test set. During the training procedure, we applied different learning rate schedules and snapshot learning. These techniques can prevent overfitting and thus can be a reason to get rid of internal validation dataset that is advantageous for deep models with millions of parameters. We thoroughly investigated different approaches to train Transformer models and found snapshot learning with averaging weights on learning rates minima works best. While decoding the model output probabilities there is a strong influence of the temperature that improves at $T=1.3$ the accuracy of models up to 1-2%.

Keywords Retrosynthesis prediction · Computer Aided synthesis Planning · Character-based models · Transformer

1 Introduction

New chemical compounds drive technological advances in material, agricultural, environmental, and medical sciences, thus, embracing all fields of scientific activities which have been bringing social and economic benefits throughout human history. Design of chemicals with predefined properties is an arena of QSAR/QSPR (Quantitative Structure Activity/Property Relationships) approaches aimed at finding correlations between molecular structures and their desired outcomes and then applying these models to optimise activity/property of compounds.

The advent of deep learning [1] gave a new impulse for virtual modeling and also opened a venue for a promising set of generative methods based on Recurrent Neural Networks [2], Variational Autoencoders [3], and Generative Adversarial Networks trained with reinforcement learning [4, 5]. These techniques are changing the course of QSAR studies from the observation to the invention: from a virtual screening of available compounds to direct synthesis of new candidates. Generative models can produce big sets of promising molecules and impaired with SMILES-based QSAR methods [6] provide a strong foundation for creating highly optimized focussed libraries, but estimation of synthetic availability of these compounds is an open question though several scores based on fragmentation [7] and machine learning [8] approaches have been developed. To synthesize a molecule, one should have a plan of a multi-step synthesis and also a set of available reactants. Finding an optimal combination of reactants, reactions, and conditions to obtain the compound with good yield, sufficient quality, and quantity is not a trivial task even for experts in organic chemistry. Recent advances in the computer-aided synthesis planning are reviewed in [9, 10, 11].

The retrosynthetic analysis worked out by E. J. Corey [12] tries to account for all factors while deriving the synthetic route. It iteratively decomposes the molecule on simpler blocks till all of them become available either by purchase or by synthesis described in the literature. At each step, fig. 1, all possible disconnections (rules) with known reactions

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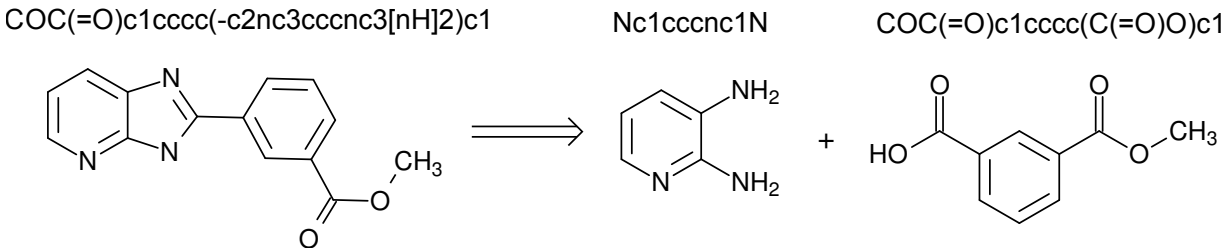


Figure 1: An example of a retrosynthetic reaction: on the left side of the arrow the target molecule is depicted, and on the right side the one possible set of reactants that can lead to the target is shown in common chemistry-like scheme and using SMILES notation. Here two successive amidation reactions result in cyclisation and aromatization.

simplify the target molecule bringing to the scene less complex compounds. Some of them may be already available, while the others undergo the next step of retrosynthesis decomposition. Due to the recursive nature of the procedure, it can deal with thousands of putative compounds so computational retrosynthetic approaches can greatly help chemists in finding the best routes. Managing of the database of such rules is complicated and more critical the models based on it are not ready to accommodate new reactions and will always be outdated. Almost more than 60 years of developing rule-based systems ended with no remarkable success in synthesis planning programs. Another approach to tackle the problem is to use so-called template-free methods inspired by the success of machine-translation. They don't require the database of templates and rules due to an inherent possibility to derive this information during training directly from a database of organic reactions with clearly designated roles of reactants, products, reagents, and conditions.

The analogy between machine translation and retrosynthesis is evident: each target molecule has its predecessors from which it can be synthesized as every meaningful sentence one can translate from source language to target one. If all parts of a reaction are written in SMILES notation, then our source and target sentence are composed of valid SMILES tokens as words. The main goal of the work is to build a model which could for a given target molecule for our example³ COC(=O)c1cccc(-c2nc3ccnc3[nH]2)c1 in fig. 1 correctly predict the set of reactants. Namely, it should predict Nc1ccnc1N.COC(=O)c1cccc(C(=O)O)c1 in this case.

Neural sequence-to-sequence (seq2seq) approach has been recently applied for a direct reaction prediction task [13, 14] with outstanding statistical parameters of final models – 90.4% of accuracy on test set. Seq2seq modeling has been also tested on retrosynthesis task [15], but due to the complex nature of retrosynthesis itself and difficulty in estimating the correct predictions of reactants⁴, accuracy on the test set was moderate 37.4% but still comparable to rule-based systems 35.4%. We questioned about the possibility of improvement models for one-step retrosynthesis utilizing modern neural network architectures and training techniques. Applying the Transformer Model [16], together with cyclical learning rate schedule [17], resulted in a single model with accuracy 42.7%, that is more than 5% higher compare to the baseline model [15].

Our main contributions are:

- We show that for this particular task there is no need to use a validation dataset for early-stopping or other parameters optimization. We trained all the parameters directly from the training dataset.
- Applying weights averaging and snapshot learning helped to train the most precise model for one-step retrosynthesis prediction. We averaged weights on 5 successive cycles of learning rate schedule.
- Increasing the temperature while performing a beam-search procedure improves the accuracy up to 2%.

2 Approach

2.1 Dataset

In this study we used the same dataset of reactions as in [15]. This dataset was filtered from the USPTO database [19] originally derived from the USA patents and contains 50 000 reactions classified into 10 reaction types [20]. The authors

³ This reaction is in the test set and it was correctly predicted by our model.

⁴ A target molecule usually can be synthesized with different reactions starting from different sets of reactants. The predictions of the model may be correct from organic chemist point of view but differ from the reactant set in ground truth. This may lead to underestimation of effectiveness of models.

2.2 Model input

```
token_regex = "([[\^]]+)|Br?|Cl?|N|O|S|P|F|I|b|c|n|o|s|p|\\(|\\)|\\.|=|#|-|\\+|\\\\\\\\\\\\\\\\|\\\\/|:|~|@|\\?|>|\\*|\\$|\\%|[0-9]{2}|[0-9])".
```

Our final vocabulary has length of 66 symbols⁶:

```
chars = " ^#%()+- .0123456789=@ABCDEFGHIJKLMNPRSTVXYZ[\ ]abcdefghijklmnopqrstuvwxyz$"
```

2.3 Transformer model

The Transformer has wholly got rid of any recurrences or convolutional operations. To tackle distances between elements of a string a positional encoding matrix was proposed with elements equal to the values of trigonometric functions depending on the position in a string and also the position in the embedding direction. Summed with learned embeddings positional encodings do their job linking far located parts of the input together. The output of self-attention layers is then mixed with original data, layer-wise normalized, and passed position-wise through a couple of ordinary dense layers to go further either in next level of self-attention layers or to a decoder as an information-rich vector representing the input. The decoder part of Transformer resembles the encoder but has an additional self-attention layer which corresponds to encoder's output.

⁷The encoder and the decoder share embeddings in this study.

Transformer model shows the state-of-the-art results in machine translation and reaction prediction outcomes [14]. The latter work showed that training the Transformer on large and noisy datasets results in a model that can outperform not only other machine models but also well qualified and experienced organic chemists.

2.4 Model inference

The model tries to estimate the probability of the next symbol over the model’s vocabulary given all previous symbols in the string. Technically, the Transformer model first calculates logits, z_i , and then transforms them to probabilities.

$$z_i = \text{Transformer}(\{x_1, x_2, x_3, \dots, x_L\}, \{y_1, y_2, y_3, \dots, y_{i-1}\}) \quad (1)$$

Here x_i is the input of the models at i position; L – the length of the input string; y_i is the decoded output of the model up to position $(i - 1)$; and z_i – logits that are to be converted to probabilities:

$$q_i = \frac{\exp(z_i/T)}{\sum_{j=0}^V \exp(z_j/T)} \quad (2)$$

where V is the size of the vocabulary (66 in this work) and T stands for the temperature⁸ usually assigned to 1.0 in standard softmax layers. With higher T the landscape of the probability distribution becomes more smooth. During the training the model adapts its weights to better predict q_i , so $y_i = q_i$.

During the inference however we have several possibilities how to convert q_i into y_i , namely greedy and beam search. The first one picks up a symbol with maximum probability whereas the second one at each step holds *top* – K (K = beam’s size) suggestions of the model and summarises the overall likelihood for each of K final decodings. The beam search allows better inference and the probability landscape exploration compared to the greedy search because at a particular step of decoding it may choose a symbol with less than maximum probability, but the total likelihood of the result can be higher due to more significant probabilities on the next steps.

2.5 Training heuristics

Training a Transformer model is a challenge, and several heuristics have been proposed [17], some of them were used in this study:

Using as bigger batch size as possible. However, due to our hardware limitations we could not set the batch size more than 64⁹;

Increasing the learning rate at the beginning of training up to warmup steps¹⁰. The authors of the original Transformer paper [16] used 4 000 steps for warming. The Transformer model for reaction prediction task from [14] used 8 000 steps. We have also tried different values for warmup and eventually found that 16 000 works well with our model.

Applying cyclic learning rate schedules. This tips can generally improve any model [21] through better loss landscape exploration with bigger learning rates after the optimiser felt down to some local minima. For this study we used the following scheme for learning rate calculation depending on the step:

$$u(\text{step}) = \begin{cases} \text{warmup} + (\text{step} \bmod \text{cycle}), & \text{if } \text{step} \geq \text{cycle} \\ \text{step}, & \text{otherwise} \end{cases}$$

where *cycle* stands for the number of steps while the learning rate is decreasing before raising to the maximum again.

$$\lambda(\text{step}) = \text{factor} * \frac{\min(1.0, u(\text{step})/\text{warmup})}{\max(u(\text{step}), \text{warmup})} \quad (3)$$

where *factor* is just a constant. Big values of *factor* introduce numerical instability during training, so after several trials we set *factor* = 20.0. The curve for learning rate in this study is shown in fig. 3, plot (4, f).

⁸Similar to formula of Boltzmann (Gibbs) distribution used in statistical mechanics.

⁹Our first implementation of the model required a lot of memory to deal with masks of reactants and products. Though later we improved the code we still remained this size for consistency of the results.

¹⁰In our implementation 1 step is equivalent to 1 batch. The number of reactions for training is 40 029 + 5 004, so one epoch is equal to 704 batches.

Averaging weights during last steps (usually 10- 20) of training or at minima of learning rates in case of snapshot learning [22]. Also with cyclic learning rate schedules it is possible to average weights of those models that have minimum in losses just before increasing of the rate. Such approach leads to more stable and plain region in loss landscapes [21].

3 Results

3.1 Learning details and evaluation of models for retrosynthesis prediction

For this study, we implemented The Transformer model in Tensorflow [23] library to support its integration in our in-house programs set (<https://github.com/bigchem/retrosynthesis>). All values reported are averages for three repetitive runs, see p. 10 for details. Preliminary modeling showed that the architecture with 3 layers and 8 attention heads works well for the datasets, though we tried combinations of 2, 3, 4, 5 layers with 6, 8, 10, 12 heads. So all calculations were performed with these values fixed. The number of learnable parameters of the model is 1 882 176, embedding layer common for product and reactants has size 64.

Following the standard machine learning protocol, we trained our first models (T1) using three datasets for training, validation, and external testing (8:1:1) as was done in [15]. Learning curves for T1 are depicted in fig. 3, (c) and (d) for training and validation loss, respectively, (a) shows the original learning rate schedule developed by the authors of the Transformer but with 16 000 warmup steps. On reaching cross-entropy loss about 0.1 on the validation dataset, it stagnates without noticeable fluctuations as training loss steadily decreases. After warming up phase the learning rate begins fading and eventually after 1 000 epochs its value reaches 2.8×10^{-5} inevitable causing to stop training because of too small updates.

During the decoding procedure, we explored the influence of the temperature parameter on the final quality of prediction and found that inferring at higher temperatures gives better result then at $T=1$. This observation similarly repeated for all our models. Fig. 2 shows the influence of this parameter on the reactants prediction of the part of the training set. Clearly, at $T=1.3$ the model reaches the maximum of chemically-based accuracy. This fact one can explain that at higher temperatures the landscape of output probabilities of the model is softer letting the beam-search procedure to find more suitable ways during decoding. Of course, the temperature influences only relative distances between peaks, so it does not affect the greedy search method.

If we apply the early stopping technique, we should select the model around 200 epoch. Effectiveness of such a model marked $T1_1$ in table 1 resulted in TOP-1 37.9% on the test set. If we choose the last one model obtained at 1 000 epoch, then the model $T1_2$ gives us better value – 39.8%. In this case, we did not see any need of the validation dataset and

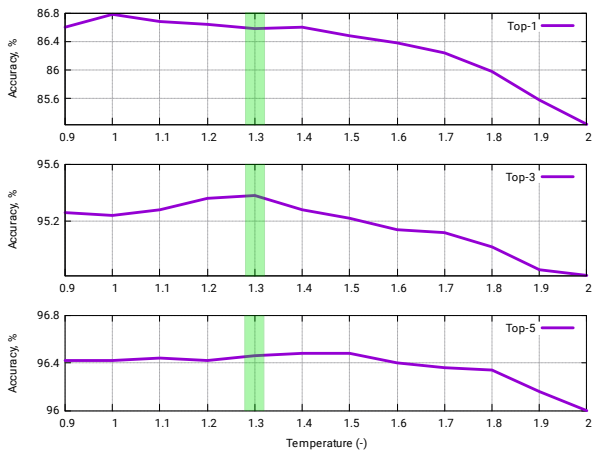


Figure 2: Dependence of the beam search on temperature. For better exploration, higher temperatures are more useful. In this study we explored $T=1.3$. Bigger values significantly worse for Top-3, and approximately the same for Top-1 and Top-5. This curve was derived from the training dataset.

Table 1: Accuracy (%) of the models on test set when all reactants were correctly predicted.

Model	Greedy	Top-1	Top-3	Top-5	Description
Seq2Seq		37.4	52.4	57.0	Literature result from [15] based on Seq2Seq architecture.
T1	34.4	37.9	57.3	62.7	Transformer Model trained with validation control set (early stopping, ~200 epochs).
$T1_1$	37.3	39.8	59.1	63.9	The same as T1, but without early stopping (1000 epochs).
T2	39.3	41.8	61.3	67.2	Transformer Model trained on both training and validation sets for 1000 epochs.
T3	40.6	42.7	63.9	69.8	Transformer Model trained with cyclic learning rate schedule for 1000 epochs. Averaging cycles 6,7,8,9, and 10.

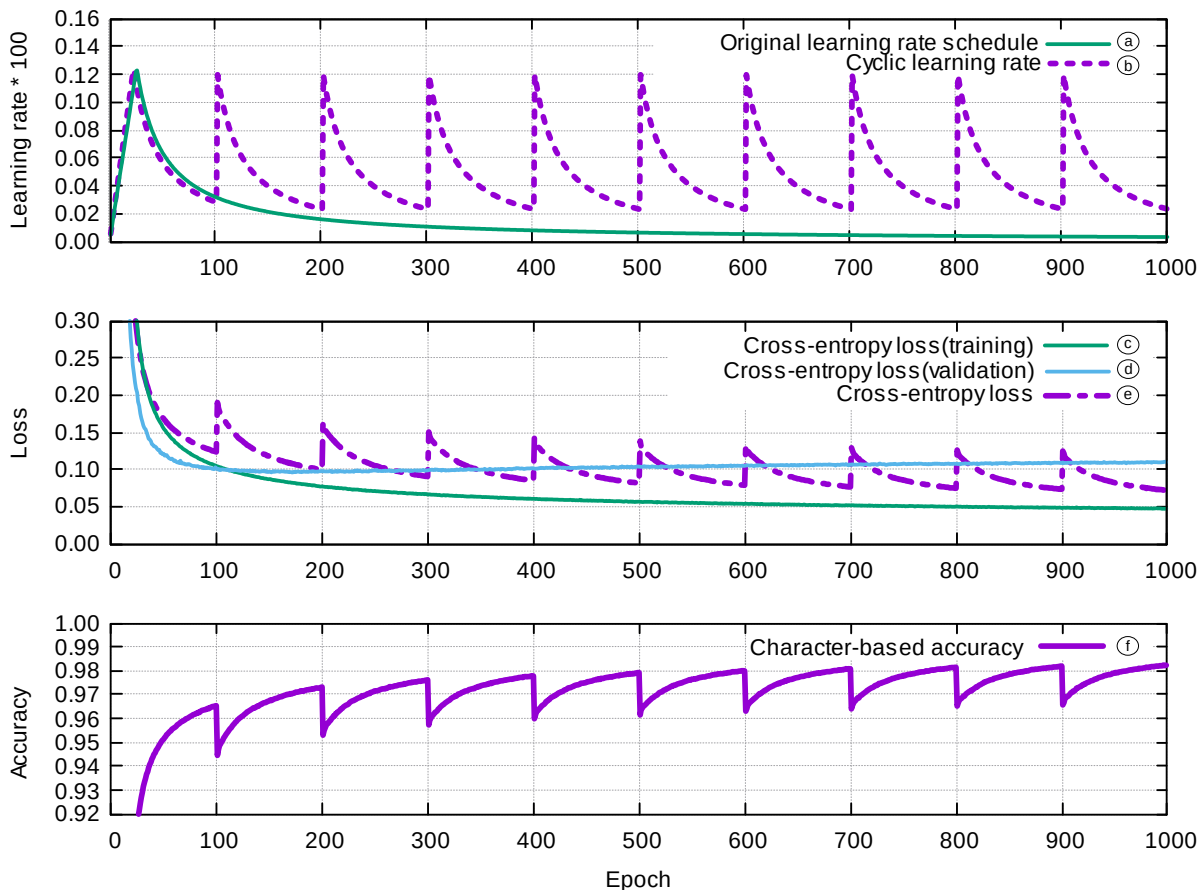


Figure 3: Summary of learning curves for the Transformer model: a) original learning rate schedule with warmup; b) cyclic learning rate with warmup; c) cross-entropy loss for training and d) validation; e) cross-entropy loss and f) character-based accuracy for training a model with cyclic learning schedule.

keeping in mind that our model has almost 2 millions of parameters we decided to combine training and validation sets and train our next models on both data, e.g., without validation. The model T2 was trained on all data and with the same learning rate schedule as T1. The results obtained when applying T2 to the test set are better than for T1 set namely 41.8% vs. 39.8%.

Then we trained our model with cyclic learning rate schedule, eq. 3, fig. 3 (b) for better exploration of loss landscape. During training, we also saved the character-based accuracy of the model, fig. 3, (f). This snapshot training regime [22] produces a set of different weights at each minimum of learning rate. Averaging them is to some extent equivalent to a consensus of models but within one model [21]. We tried different averaging regimes for T3 and found that averaging on 6-7-8-9-10 cycles gives better results.

Our final T3 model outperforms [15] by 5.3% with beam search and more critical it is also effective with greedy search 40.6%. The latter one is much faster and consequently more suitable for virtual screening campaigns.

It worth to notice that TOP-5 accuracy reaches almost 70%. That means the model can correctly predict reactants but sometimes scoring is wrong and TOP-1 is much less. We tried to improve TOP-1 scoring with internal confidence estimation.

3.2 Internal scoring

The beam search calculates the sum of negative logarithms of probabilities of selecting a token at a particular step, and thus, this value can be a measure of internal confidence. To check this hypothesis, we selected T3-2 model and estimated its internal performance to distinguish between correct and invalid predictions. The

parameters of the classifier were: AUC = 0.77, optimal threshold = 0.00678. Then we validated the model with an additional condition: if the score is less than optimal threshold we selected the answer, otherwise we went to the next candidate in the possible reactant sets returned by the beam search. The results were even worse than without thresholds, 28.45 vs. 42.42. A possible explanation is that the estimation does not deal with organic chemistry. The model tries to derive some character-based scoring relying only on tokens in a string and increasing this value does not influence the quality of prognosis. The same effect we saw during training when the character accuracy is 98% whereas chemistry-based metric is much lower.

Estimation of optimal thresholds on training sets almost always a bad idea due to the biasing of a model to its source data. The correct way is to use validation dataset instead. We built the classifier for the T1-2 with characteristics: AUC = 0.65, optimal threshold 0.00396, and applied it for testing the model. The results were again worse, 14.1% vs. 40.85%. There are no significant differences of accuracies when using unnormalized or normalized on the length of the reactants string scores. Fig. 4 shows ROC curves for T1-2 and T3-2 models derived at T=1.3. Evidently one cannot use this estimation to improve TOP-1 scoring.

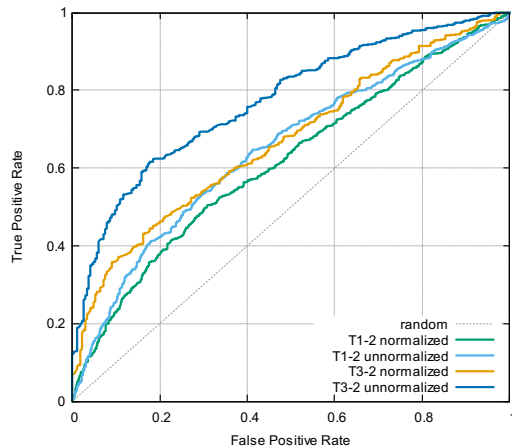


Figure 4: Internal classification performance.

4 Discussion

Much attention paid in the scientific literature for rule-based approaches [24, 25]. Since the authors of [26] have described the algorithm of automatic rule extraction from mapped reaction database several implementations of the procedure appeared, and then widely accepted by researchers. However, it should be noticed that, first, there is no algorithm to make atom-mapping [11] if it is absent (the typical situation with laboratory notebooks (ELN) for example). Second, all available information on synthesis usually contains only positive reactions, so all binary classification accuracies are inevitable overestimated because of artificial negative sets exploited in studies. Finally, the absence of commonly accepted dataset for testing makes the results of different groups practically disparate and biased to those problems the authors tried to solve. The authors of [25] selected 40 molecules from DrugBank database to test their multiscale models, whereas [15] used database specially prepared for classification [20].

Our model can correctly predict reactant set in TOP-5 with accuracy 69.8%. Internal confidence estimation cannot guarantee a correct solution, so different scoring methods should be developed. One of the promising ways is to use a forward reaction prediction model to estimate whether it is possible to assemble a target molecule from reactants proposed. The scoring model should have excellent characteristics and probably it is possible to apply the same cycling learning rate and snapshot averaging to build it.

First work on applying reinforcement learning for the whole retrosynthetic path [24] showed superior performance compared to the rule-based methods developed before. More important if can deal with several steps of synthesis. But the policy learned during the training again used extracted rules limiting the method. Thus, the development of models for direct estimation of reactants is still of prime importance. Embedding such systems in policy networks within reinforcement learning paradigm can bring forward an entirely data-driven approach to solve challenging organic synthesis problems.

5 Conclusions

We have described a Transformer model for retrosynthesis one-step prediction task. Our final model trained with cyclic learning rate schedule and its weights were averaged during last five loss minimum. The model outperforms the previous published retrosynthetic character-based model by 5.3%. It also does not require the extraction of specific rules, atom mappings, and reaction types in reaction dataset. We believe it is possible to improve the model further applying knowledge distillation method [18] for example. The current model can be used as a building block for reinforcement learning aimed at solving complex organic problems.

All source code and also models built are available online via github

<https://github.com/bigchem/retrosynthesis>

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6 Appendix

In this section we report all characteristics of repetitive runs of all models built in this study. Average values based on this data are summed in table 1. For every run we report learning curves with loss functions and learning rate, then model relevant information are collected in a table including greedy search decoding accuracies, beam search accuracies for Top-1, Top-3, and Top-5.

6.1 Model 1

6.1.1 Model 1 (run-1)

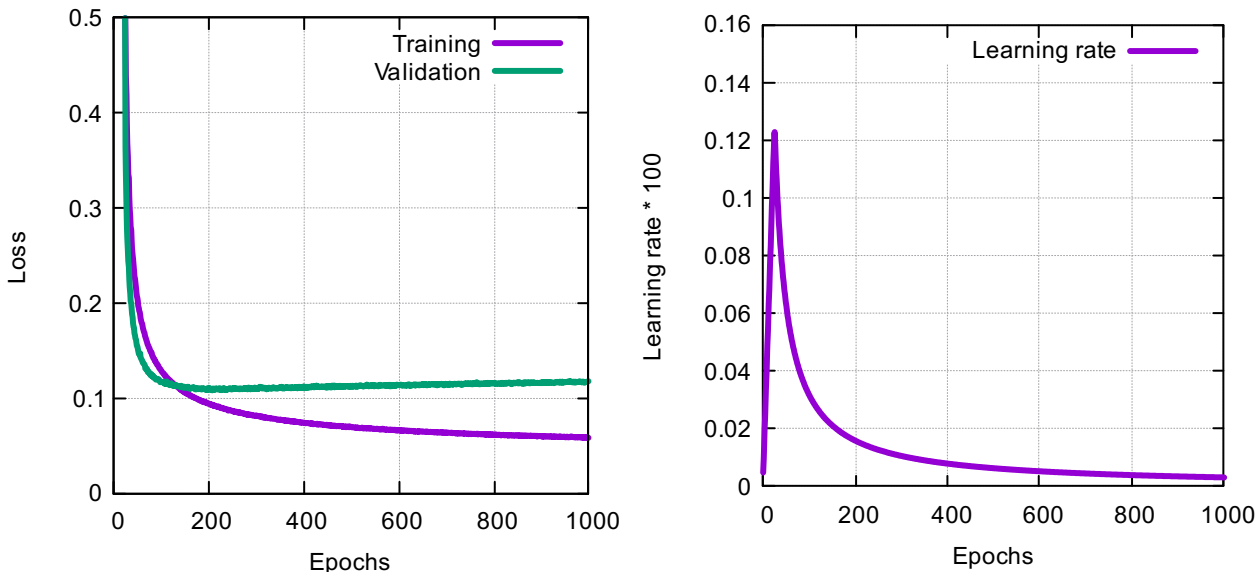


Figure 5: Learning curves and rate schedule for T1 model. Losses for training and validation datasets on the left, usual learning rate schedule on the right.

Table 2: Parameters of T11 run.

Parameter	Value	Top-1	Top-3	Top-5
Early stopping loss (training / validation)	0.09345 / 0.10864			
Last training loss (training / validation)	0.05867 / 0.11819			
Epoch (early stopping)	208			
Greedy search (early stopping, epoch 208)		32.83		
Greedy search (last, epoch 999)		34.75		
Greedy (last 10 average, epoch, 990 - 999)		35.57		
Beam, T = 1.0 (early)		35.57	54.14	59.13
Beam, T = 1.3 (early)		35.93	54.59	59.51
Beam, T = 1.0 (last)		37.15	55.22	60.49
Beam, T = 1.3 (last)		37.67	55.97	61.01
Beam, T = 1.0 (last 10 average)		37.83	56.08	60.63
Beam, T = 1.3 (last 10 average)		38.15	56.71	61.31

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t1-1-early.h5>

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t1-1-last.h5>

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t1-1-avg.h5>

6.1.2 Model 1 (run-2)

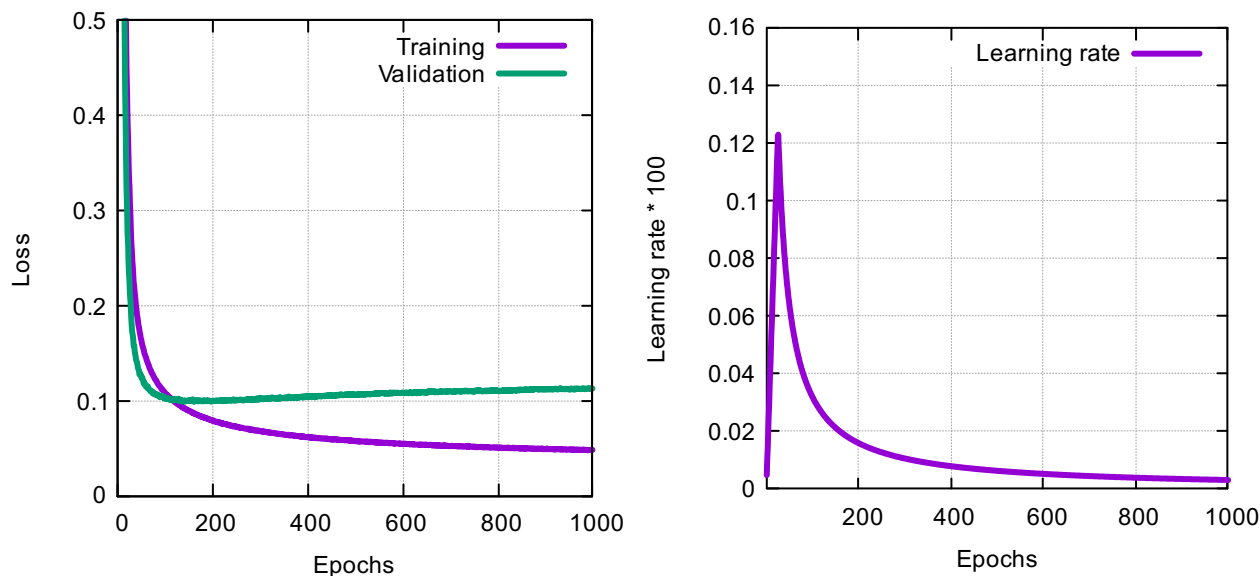


Figure 6: Learning curves and rate schedule for T1 model. Losses for training and validation datasets on the left, usual learning rate schedule on the right.

Table 3: Parameters of T12 run.

Parameter	Value	Top-1	Top-3	Top-5
Early stopping loss (training / validation)	0.08681 / 0.09926			
Last training loss (training / validation)	0.04863 / 0.11316			
Epoch (early stopping)	162			
Greedy search (early stopping, epoch 162)		34.63		
Greedy search (last, epoch 990)		38.07		
Greedy (last 10 average, epoch, 990 - 999)		38.19		
Beam, T = 1.0 (early)		37.45	56.71	62.43
Beam, T = 1.3 (early)		38.31	57.93	63.35
Beam, T = 1.0 (last)		39.83	58.63	64.45
Beam, T = 1.3 (last)		40.67	59.53	64.97
Beam, T = 1.0 (last 10 average)		40.22	59.05	64.91
Beam, T = 1.3 (last 10 average)		40.85	59.85	65.45

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t1-2-early.h5>

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t1-2-last.h5>

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t1-2-avg.h5>

6.1.3 Model 1 (run-3)

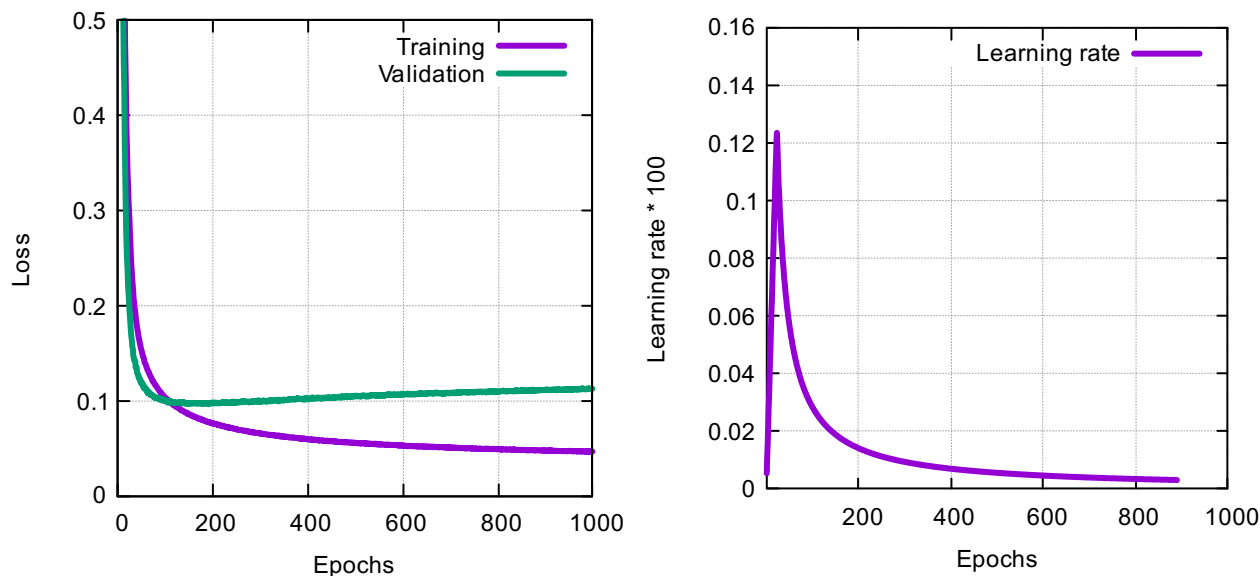


Figure 7: Learning curves and rate schedule for T1 model. Losses for training and validation datasets on the left, usual learning rate schedule on the right.

Table 4: Parameters of T13 run.

Parameter	Value	Top-1	Top-3	Top-5
Early stopping loss (training / validation)	0.07795 / 0.09662			
Last training loss (training / validation)	0.04654 / 0.11285			
Epoch (early stopping)	193			
Greedy search (early stopping, epoch 193)		35.63		
Greedy search (last, epoch 998)		38.13		
Greedy (last 10 average, epoch, 990 - 999)		38.03		
Beam, T = 1.0 (early)		38.75	58.55	64.47
Beam, T = 1.3 (early)		39.53	59.25	65.23
Beam, T = 1.0 (last)		40.05	59.35	64.27
Beam, T = 1.3 (last)		40.41	60.49	64.85
Beam, T = 1.0 (last 10 average)		39.96	59.83	64.46
Beam, T = 1.3 (last 10 average)		40.41	60.81	65.18

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t1-3-early.h5>

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t1-3-last.h5>

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t1-3-avg.h5>

6.2 Model 2

6.2.1 Model 2 (run-1)

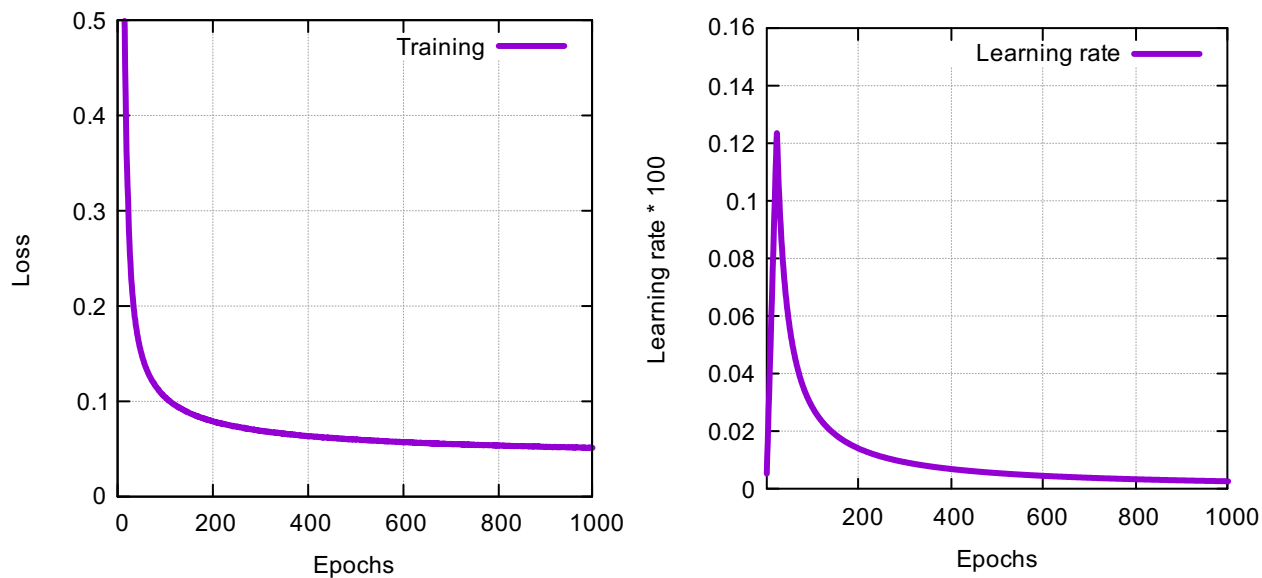


Figure 8: Learning curves and rate schedule for T2 model. Loss for training on the left, usual learning rate schedule on the right.

Table 5: Parameters of T21 run.

Parameter	Value	Top-1	Top-3	Top-5
Last training loss	0.05108			
Greedy search (last, epoch 981)		38.85		
Greedy (last 10 average, epoch, 990 - 999)		39.25		
Beam, T = 1.0 (last)		40.57	60.19	66.77
Beam, T = 1.3 (last)		41.17	60.65	67.28
Beam, T = 1.0 (last 10 average)		40.98	60.29	67.00
Beam, T = 1.3 (last 10 average)		41.61	60.85	67.37

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t2-1-last.h5>

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t2-1-avg.h5>

6.2.2 Model 2 (run-2)

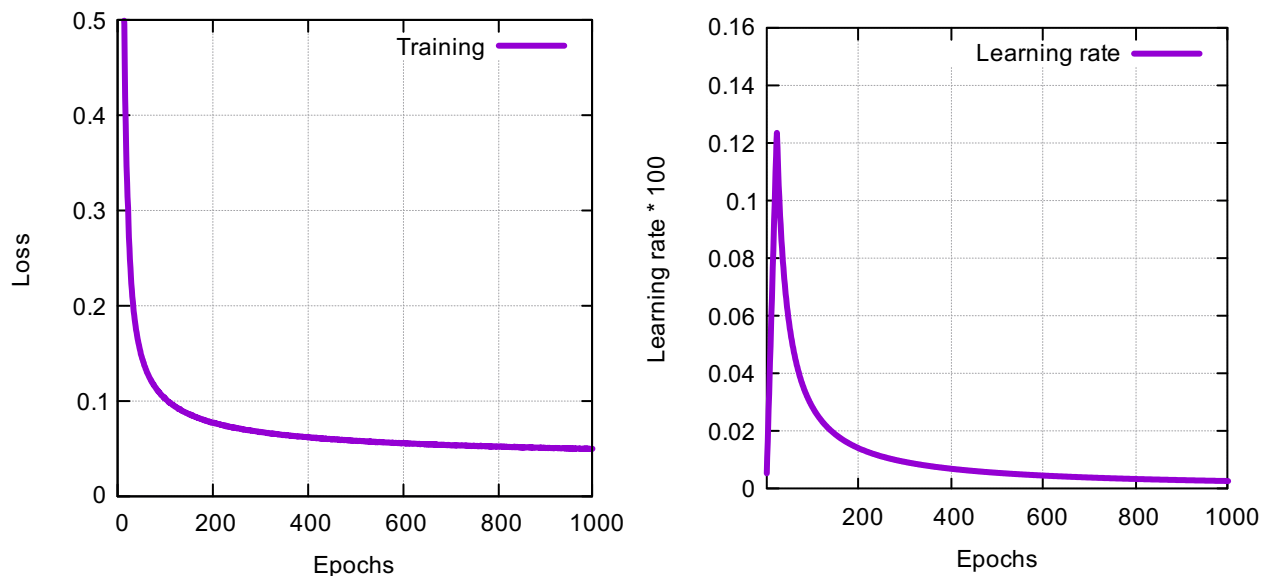


Figure 9: Learning curves and rate schedule for T2 model. Loss for training on the left, usual learning rate schedule on the right.

Table 6: Parameters of T22 run.

Parameter	Value	Top-1	Top-3	Top-5
Last training loss	0.04943			
Greedy search (last, epoch 996)		38.79		
Greedy (last 10 average, epoch, 990 - 999)		39.11		
Beam, T = 1.0 (last)		40.98	60.39	66.38
Beam, T = 1.3 (last)		41.58	61.21	66.94
Beam, T = 1.0 (last 10 average)		41.14	60.59	66.41
Beam, T = 1.3 (last 10 average)		41.87	61.35	67.08

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t2-2-last.h5>

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t2-2-avg.h5>

6.2.3 Model 2 (run-3)

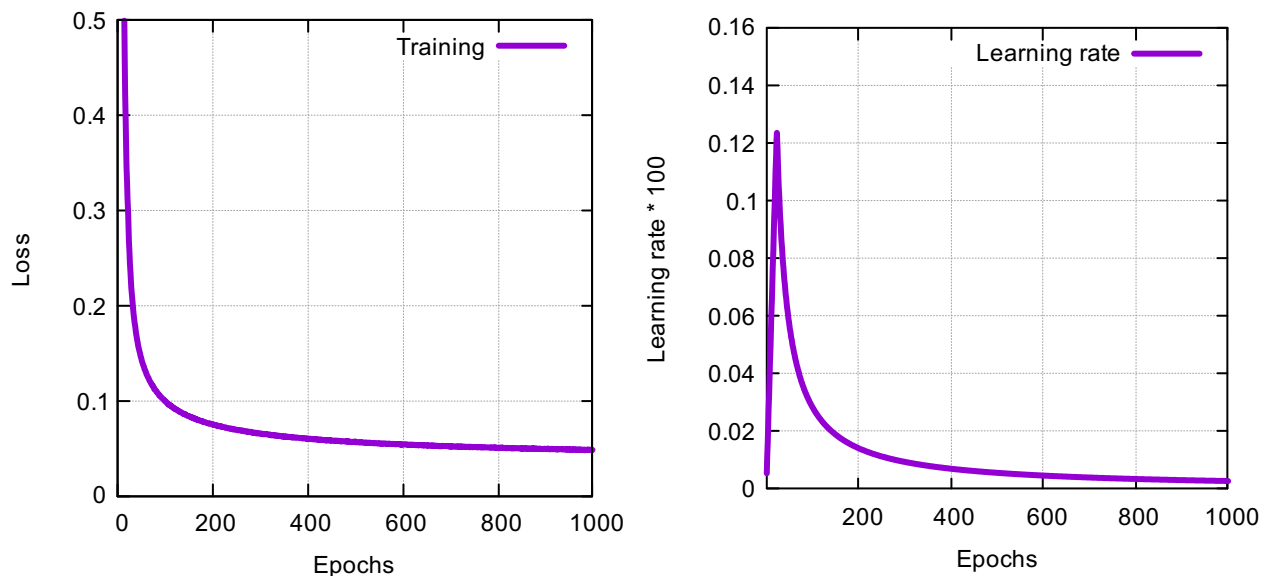


Figure 10: Learning curves and rate schedule for T2 model. Loss for training on the left, usual learning rate schedule on the right.

Table 7: Parameters of T23 run.

Parameter	Value	Top-1	Top-3	Top-5
Last training loss	0.04826			
Greedy search (last, epoch 984)		39.79		
Greedy (last 10 average, epoch, 990 - 999)		39.69		
Beam, T = 1.0 (last)		41.55	60.79	66.57
Beam, T = 1.3 (last)		41.85	61.63	67.32
Beam, T = 1.0 (last 10 average)		41.45	60.75	66.55
Beam, T = 1.3 (last 10 average)		42.02	61.73	67.19

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t2-3-last.h5>

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t2-3-avg.h5>

6.3 Model 3

6.3.1 Model 3 (run-1)

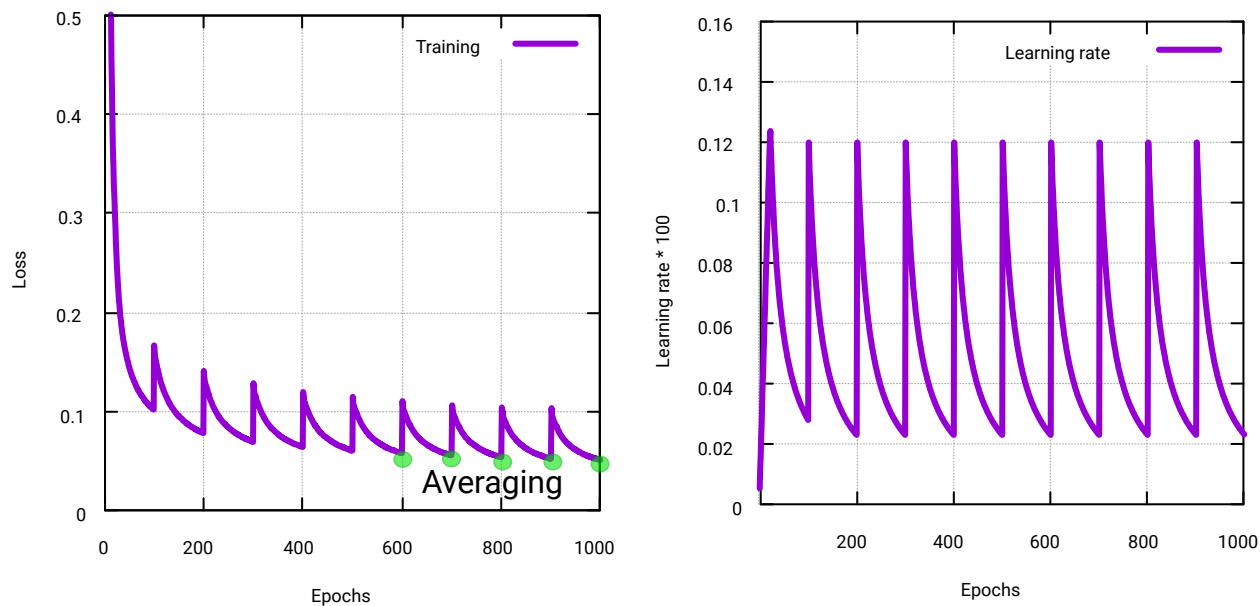


Figure 11: Learning curves and rate schedule for T3 model. Loss for training on the left, usual learning rate schedule on the right.

Table 8: Parameters of T31 run.

Parameter	Value	Top-1	Top-3	Top-5
Last training loss	0.05173			
Averaging 6-7-8-9-10				
Greedy search		40.92		
Beam, T = 1.0		42.38	62.77	69.58
Beam, T = 1.3		42.80	63.82	70.28
Averaging 7-8-9-10				
Greedy search		40.50		
Beam, T = 1.0		42.38	62.91	69.76
Beam, T = 1.3		42.84	63.62	70.06
Averaging 8-9-10				
Greedy search		41.04		
Beam, T = 1.0		42.51	63.18	69.84
Beam, T = 1.3		43.19	63.93	70.50
Averaging 9-10				
Greedy search		41.06		
Beam, T = 1.0		42.66	63.09	69.20
Beam, T = 1.3		43.22	63.71	69.94

Model with weights averaging 6-7-8-9-10:

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t3-1.h5>

6.3.2 Model 3 (run-2)

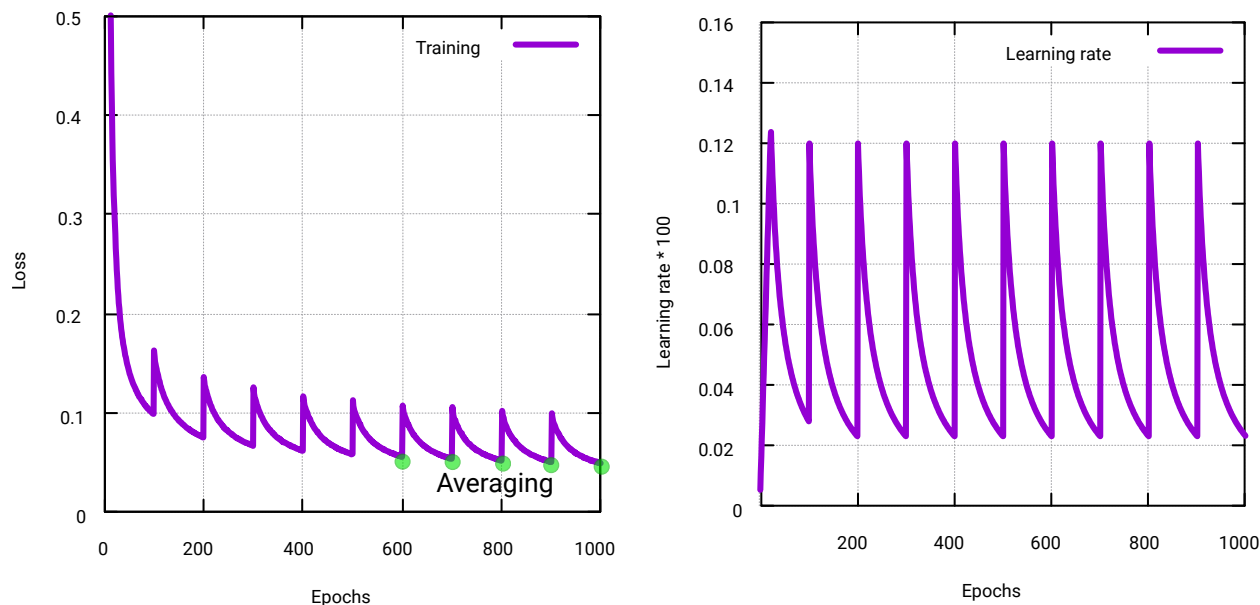


Figure 12: Learning curves and rate schedule for T3 model. Loss for training on the left, usual learning rate schedule on the right.

Table 9: Parameters of T32 run.

Parameter	Value	Top-1	Top-3	Top-5
Last training loss	0.04958			
Averaging 6-7-8-9-10				
Greedy search		40.32		
Beam, T = 1.0		41.90	62.70	68.80
Beam, T = 1.3		42.42	63.61	69.66
Averaging 7-8-9-10				
Greedy search		40.22		
Beam, T = 1.0		41.90	62.72	69.18
Beam, T = 1.3		42.42	63.59	69.92
Averaging 8-9-10				
Greedy search		40.56		
Beam, T = 1.0		41.96	62.53	69.18
Beam, T = 1.3		42.62	63.14	69.86
Averaging 9-10				
Greedy search		40.34		
Beam, T = 1.0		41.98	62.43	69.14
Beam, T = 1.3		42.34	63.03	69.70

Model with weights averaging 6-7-8-9-10:

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t3-2.h5>

6.3.3 Model 3 (run-3)

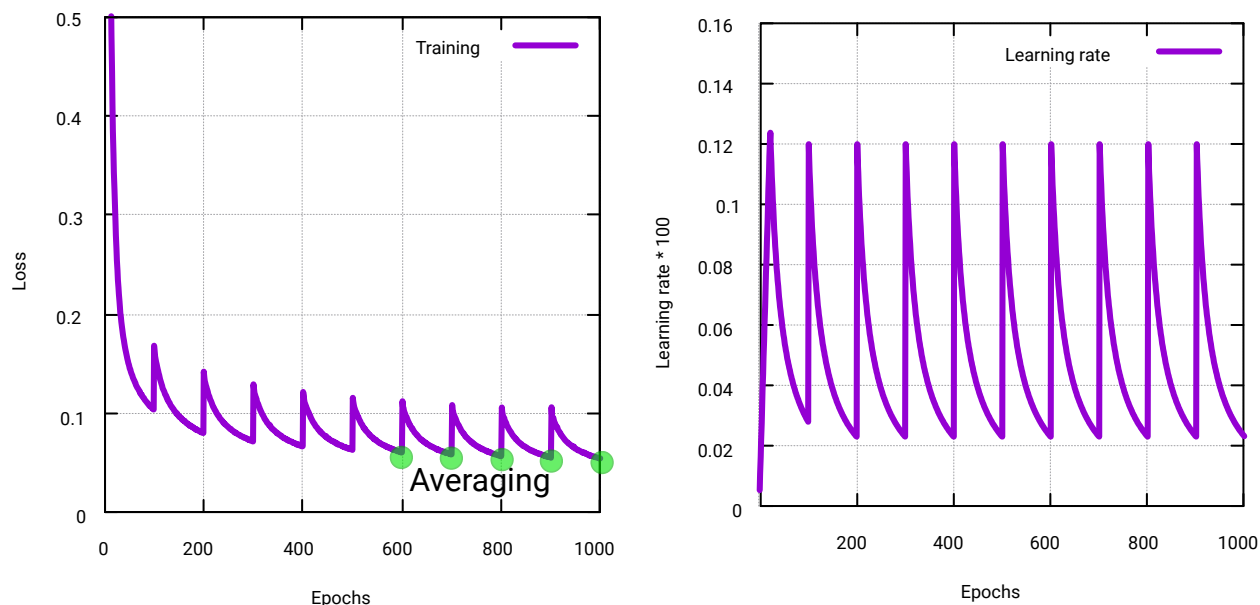


Figure 13: Learning curves and rate schedule for T3 model. Loss for training on the left, usual learning rate schedule on the right.

Table 10: Parameters of T33 run.

Parameter	Value	Top-1	Top-3	Top-5
Last training loss	0.05491			
Averaging 6-7-8-9-10				
Greedy search		40.62		
Beam, T = 1.0		42.24	63.25	69.38
Beam, T = 1.3		42.96	64.34	69.70
Averaging 7-8-9-10				
Greedy search		40.42		
Beam, T = 1.0		42.00	63.22	69.40
Beam, T = 1.3		42.76	64.20	69.80
Averaging 8-9-10				
Greedy search		40.38		
Beam, T = 1.0		41.84	62.96	69.08
Beam, T = 1.3		42.54	63.97	69.64
Averaging 9-10				
Greedy search		40.20		
Beam, T = 1.0		41.86	62.56	68.30
Beam, T = 1.3		42.62	63.39	69.12

Model with weights averaging 6-7-8-9-10:

<https://github.com/bigchem/retrosynthesis/papers/retrosynthesis/models/t3-3.h5>