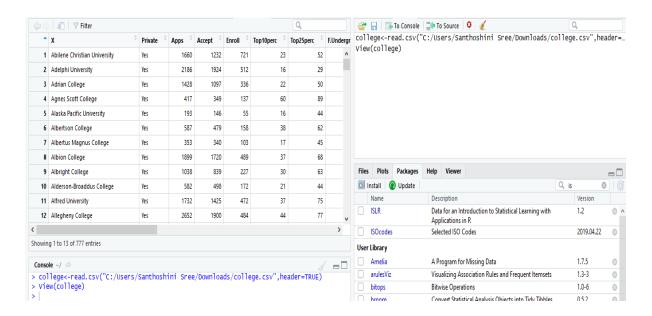
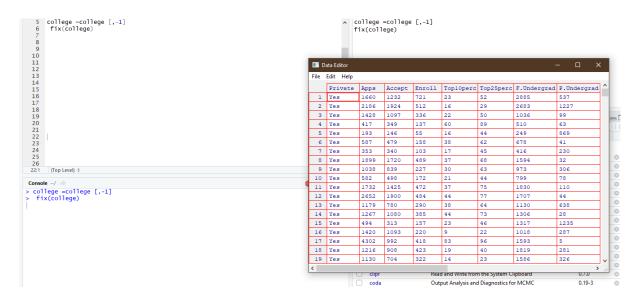
LAB#1

CHAPTER 2

8. (a) college<-read.csv("C:/Users/SanthoshiniSree/Downloads/college.csv",header= TRUE) View(college)



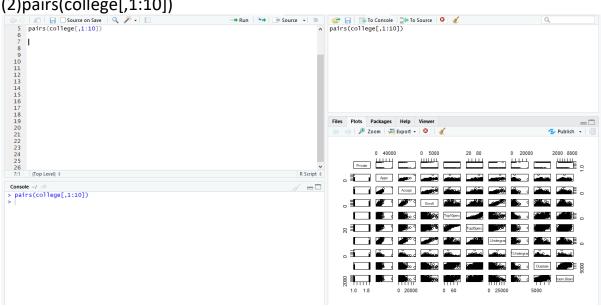
(b) Rownames(college)=college[,1] Fix(college)



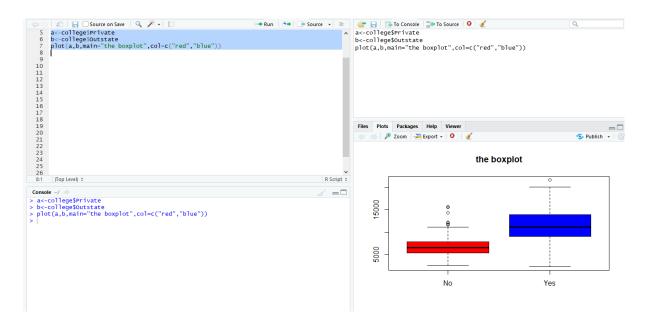
(c) (1)

```
Run Source - =
     summary(college)
  7
  8
  9
 10
 11
 12
 13
 14
 15
 16
 17
 18
 19
 20
 21
 22
 23
 24
 25
 26
 5:17
     (Top Level) $
                                                                             R Script $
Console ~/ 🧀
                                                                                > summary(college)
Private
                                            Enroll
                                                        Top10perc
              Apps
                             Accept
                              : 72
                         Min.
                                                            : 1.00
         Min. : 81
1st Qu.: 776
          Min.
                    81
                                      Min. : 35
No :212
                                                      Min.
Yes:565
                         1st Qu.:
                                  604
                                        1st Qu.: 242
                                                      1st Qu.:15.00
          Median : 1558
                         Median: 1110
                                        Median: 434
                                                      Median:23.00
                : 3002
          Mean
                         Mean : 2019
                                        Mean : 780
                                                      Mean :27.56
          3rd Qu.: 3624
                         3rd Qu.: 2424
                                        3rd Qu.: 902
                                                      3rd Qu.:35.00
          Max. :48094
                         Max. :26330
                                        Max. :6392
                                                      Max. :96.00
                F.Undergrad
                                                                 Room.Board
  Top25perc
                               P. Undergrad
                                                  Outstate
Min.
      : 9.0
               Min.
                         139
                              Min.
                                         1.0
                                               Min.
                                                     : 2340
                                                               Min.
                                                                    :1780
1st Qu.: 41.0
               1st Qu.:
                         992
                              1st Qu.:
                                         95.0
                                               1st Qu.: 7320
                                                               1st Qu.:3597
                              Median :
                                               Median: 9990
Median: 54.0
               Median: 1707
                                        353.0
                                                               Median :4200
Mean : 55.8
               Mean : 3700
                                        855.3
                                               Mean :10441
                              Mean :
                                                               Mean :4358
3rd Qu.: 69.0
                3rd Qu.: 4005
                               3rd Qu.: 967.0
                                                3rd Qu.:12925
                                                               3rd Qu.:5050
Max. :100.0
               Max. :31643
                              Max.
                                     :21836.0
                                               Max. :21700
                                                               Max.
                                                                    :8124
                  Personal Personal
   Books
                                   PhD
                                                 Terminal
                                                               S.F.Ratio
     : 96.0
                               Min.
                                        8.00
                                               Min.
                Min. : 250
                                    :
                                                    : 24.0
                                                              Min.
                                                                   : 2.50
                         050
       . 470 0
                               1.0+ 000
                                       62 00
                                               10+ 00
```

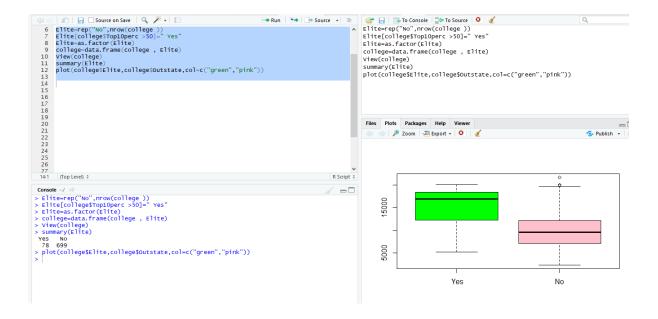
(2)pairs(college[,1:10])



(3)a<-college\$Private b<-college\$Outstate plot(a,b,col=c("red","yellow"))



```
(4)
Elite=rep("No",nrow(college ))
Elite[college$Top10perc >50]=" Yes"
Elite=as.factor(Elite)
college=data.frame(college , Elite)
View(college)
summary(Elite)
plot(college$Elite,college$Outstate,col=c("green","pink"))
```



(5)

par(mfrow=c(2,2))

a<-college\$Enroll

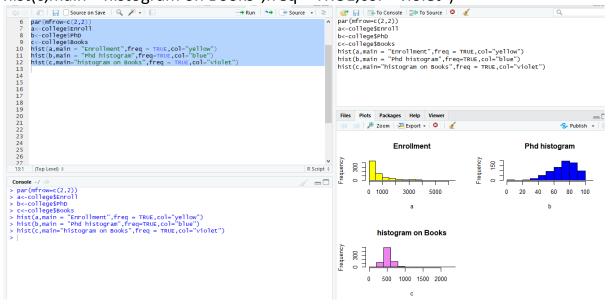
b<-college\$PhD

c<-college\$Books

hist(a,main = "Enrollment",freq = TRUE,col="yellow")

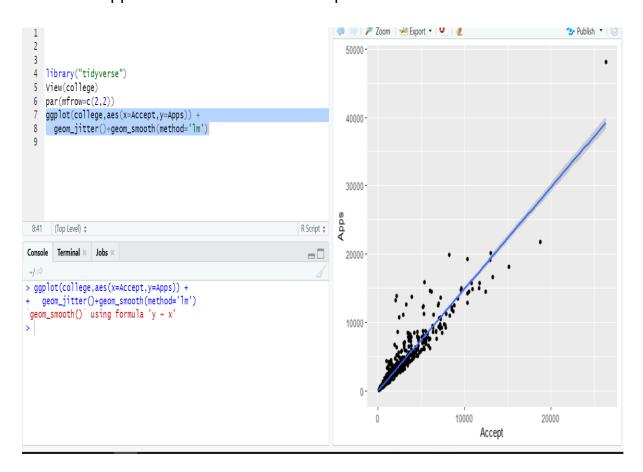
hist(b,main = "Phd histogram",freq=TRUE,col="blue")

hist(c,main="histogram on Books",freq = TRUE,col="violet")

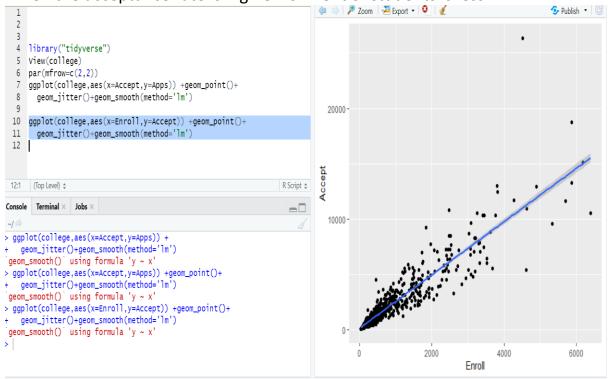


(6)

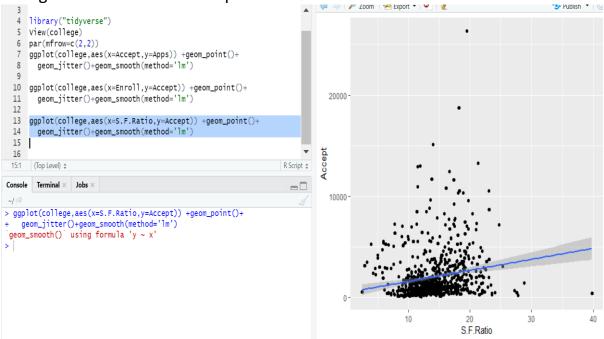
When the applications are more the acceptance rate is less



When the acceptance rate is high enrollment of students is less



Colleges which have less acceptance have less student to teacher ratio.



(9)

(a) The quantitative predictors are:

Mpg, cylinders, displacement, horsepower, weight, acceleration, year and origin

The qualitative predictor is: name

(b)Range of each predictor can be shown using sapply()

```
sapply(Auto[1:8],function(x) range(x))
   2
 1:1
      (Top Level) $
Console ~/ 🔅
> sapply(Auto[1:8],function(x) range(x))
      mpg cylinders displacement horsepower weight acceleration year origin
[1,]
                  3
                                                                     70
      9.0
                               68
                                          46
                                                1613
                                                              8.0
                  8
                              455
                                                5140
                                                                              3
[2,] 46.6
                                          230
                                                              24.8
                                                                     82
>
```

(c)mean() and sd() function gives mean and standard deviation of the values

```
sapply(Auto[1:8],function(x) mean(x) )
sapply(Auto[1:8],function(x) sd(x) )
  3:1
        (Top Level) $
Console ~/ 🙈
> sapply(Auto[1:8],function(x) mean(x) )
                                                                                                                      year
            mpg
                     cylinders displacement
                                                        horsepower
                                                                                weight acceleration
                                                                                                                                      origin
 23.445918 5.471939 194.411990
sapply(Auto[1:8],function(x) sd(x))
mpg cylinders displacement
7.8050075 1.7057832 104.6440039
                                                        104.469388 2977.584184
                                                                                             15.541327
                                                                                                               75.979592
                                                                                                                                  1.576531
                                                                                weight acceleration
                                                        horsepower
                                                                                                                                     origin
                                                                                                                      vear
                                                        38.4911599 849.4025600
                                                                                                               3.6837365
                                                                                                                                 0.8055182
                                                                                             2.7588641
```

(d) To remove observations anti_join is used. anti_join is from the library dplyr. This function returns all rows of x where there is no matching values of y.

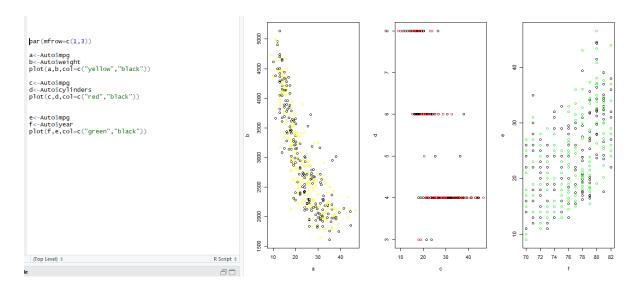
```
library(dplyr)
a<-anti_join(Auto,Auto[10:85,])</pre>
       view(a)
sapply(a[1:8],function(x) mean(x) )|
sapply(a[1:8],function(x) sd(x) )
sapply(a[1:8], function(x) max(x)-min(x))
sapply(a[1:8],function(x) range(x) )
 4:36 (Top Level) $
                                                                                                                                                         R Script $
 Console ~/
                                                                                                                                                       a --
> a<-anti_join(Auto,Auto[10:85,])
Joining, by = c("mpg", "cylinders", "displacement", "horsepower", "weight", "acceleration", "year", "origin", "nam</pre>
> sapply(a[1:8],function(x) mean(x) )
mpg cylinders displacement
24.404430 5.373418 187.240506
> sapply(a[1.8],function(x) sd(x) )
                                                          horsepower
                                                                                  weight acceleration
                                                                                                                                          origin
                                                          100.721519 2935.971519
                                                                                                                   77.145570
                                                                                                                                       1.601266
            mpg cylinders displacement
                                                                                  weight acceleration
                                                          horsepower
     7 867283
                        1.654179
                                         99.678367
                                                           35.708853
                                                                            811.300208
                                                                                                 2.693721
                                                                                                                    3.106217
                                                                                                                                       0.819910
> sapply(a[1:8], function(x) max(x)-min(x))
mpg cylinders displacement
35.6 5.0 387.0
> sapply(a[1:8],function(x) range(x))
                                                                                                                                         origin
2.0
                                                                                  weight acceleration
                                                                                                                          year
12.0
                                                                 184.0
                                                                                  3348.0
                                                                                                       16.3
mpg cylinders displacement horsepower weight acceleration year origin [1,]\ 11.0 3 68 46 1649 8.5 70 1
[2,] 46.6
                                         455
                                                        230
                                                                 4997
                                                                                   24.8
                                                                                             82
                                                                                                         3
```

(e)

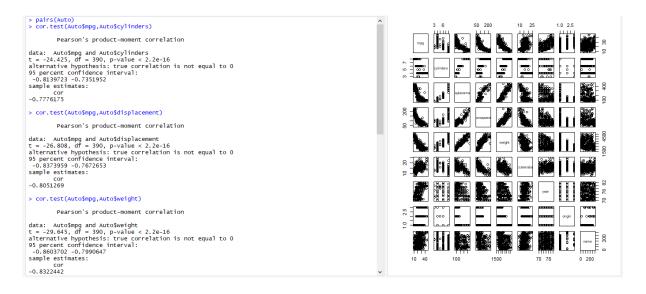
plot 1: Less mpg cylinders have high weight.

Plot2: Most of the cylinders have less mpg.

Plot 3: Over time cars are becoming systematic.



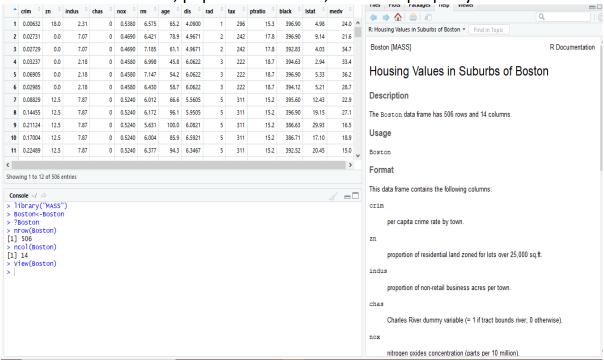
(f) Every predictor correlates with mpg. This can be shown using pair() function, which return plot matrix.



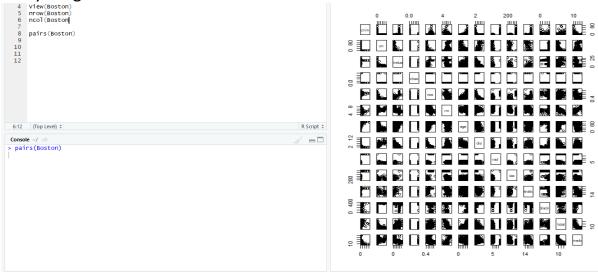
```
> cor.test(Auto$mpg,Auto$acceleration)
        Pearson's product-moment correlation
data: Auto$mpg and Auto$acceleration
t = 9.2277, df = 390, p-value < 2.2e-16
alternative hypothesis: true correlation is not equal to 0
95 percent confidence interval:
0.3384724 0.5013550
sample estimates:
     cor
0.4233285
> cor.test(Auto$mpg,Auto$year)
        Pearson's product-moment correlation
data: Auto$mpg and Auto$year
t = 14.08, df = 390, p-value < 2.2e-16
alternative hypothesis: true correlation is not equal to 0
95 percent confidence interval:
0.5108684 0.6426366
sample estimates:
    cor
0.580541
> cor.test(Auto$mpg,Auto$origin)
        Pearson's product-moment correlation
data: Auto$mpg and Auto$origin
t = 13.531, df = 390, p-value < 2.2e-16
alternative hypothesis: true correlation is not equal to 0
95 percent confidence interval:
0.4938051 0.6290414
sample estimates:
     cor
0.5652088
```

(10)

(a)There are 506 rows and 14 columns. The rows represent the locality of Boston. The crime rate, pupil-teacher ratio, full value property tax and more.



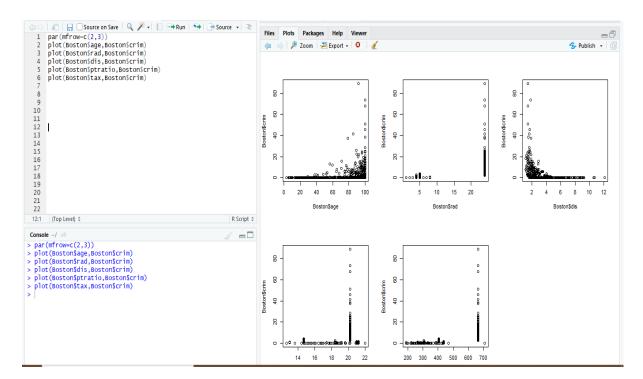
(b) As shown, there are many scatter plots and is difficult to read and clean everything.



(c)

Plot(Boston\$age,Boston\$crim)-units build in 1940 have more crime rates Plot(Boston\$rad,Boston\$crim)-radial highways have more crime rates Plot(Boston\$dis,Boston\$crim)-closer to work area have more rates Plot(Boston\$ptratio,Boston\$crim)-when pupil-teacher is high it has more crime rates

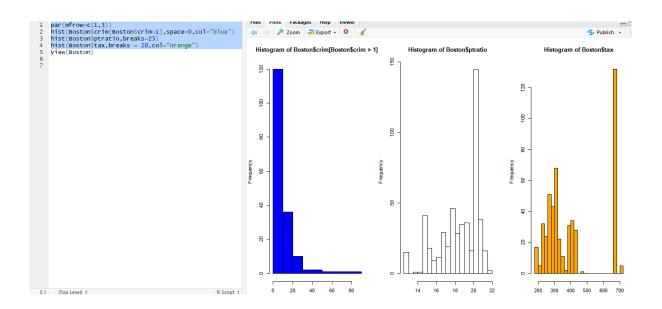
Plot(Boston\$tax,Boston\$crim)-property tax rate has more crime.



(d) par(mfrow=c(1,3))

barplot(Boston\$crim[Boston\$crim>1],space=0,col="blue")- From 0-10 the the bar has significantly increased

hist(Boston\$ptratio,breaks=25)- The ratio is high between 20 to 22 hist(Boston\$tax,breaks = 20,col="orange")- In between 680-690 the property tax is high.



(e) 35 suburbs

(g)

the crime rate for the median value of owner occupied homes is 38.3518 this means crime rate is high in that area far from highways and Charles river area. So, it is not a better place to live

```
subset(Boston,medv==min(Boston$medv))
 3
    summary(Boston)
 4
 4:1
      (Top Level) $
Console ~/ 🔅
> subset(Boston,medv==min(Boston$medv))
       crim zn indus chas
                            nox
399 38.3518 0
               18.1
                       0 0.693 5.453
406 67.9208 0 18.1
                       0 0.693 5.683
    age
         dis rad tax ptratio black
399 100 1.4896 24 666
                          20.2 396.90
406 100 1.4254 24 666
                          20.2 384.97
    1stat medv
399 30.59
406 22.98
             5
> summary(Boston)
      crim
                          zn
Min.
      : 0.00632
                   Min.
                          :
                              0.00
1st Qu.: 0.08204
                   1st Qu.:
                              0.00
Median : 0.25651
                   Median :
                             0.00
Mean
       : 3.61352
                   Mean
                          : 11.36
 3rd Qu.: 3.67708
                    3rd Qu.: 12.50
Max.
       :88.97620
                   Max.
                           :100.00
     indus
                      chas
Min.
       : 0.46
                Min.
                       :0.00000
1st Qu.: 5.19
                1st Qu.:0.00000
Median : 9.69
                Median :0.00000
Mean
       :11.14
                Mean
                        :0.06917
 3rd Qu.:18.10
                 3rd Qu.:0.00000
       :27.74
                Max.
                        :1.00000
Max.
     nox
                        rm
Min.
       :0.3850
                Min.
                         :3.561
1st Qu.:0.4490
                 1st Qu.:5.886
Median :0.5380
                 Median :6.208
Mean
       :0.5547
                 Mean
                         :6.285
 3rd Qu.:0.6240
                  3rd Qu.:6.623
                        :8.780
Max.
       :0.8710
                  Max.
     age
                       dis
Min.
       : 2.90
                 Min. : 1.130
                  1st Qu.: 2.100
1st Qu.: 45.02
Median : 77.50
                  Median : 3.207
```

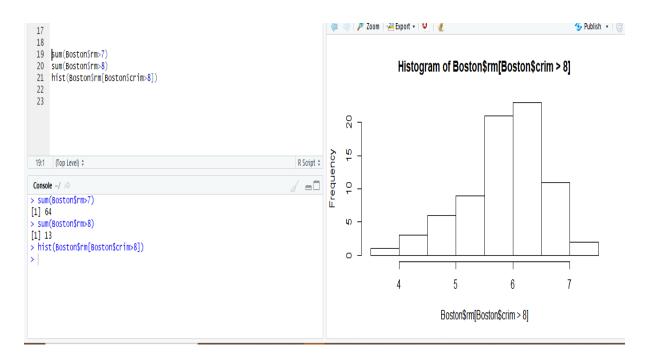
(h)

sum(Boston\$rm>7)
sum(Boston\$rm>8)

There are 64 suburbs that average more than 7 rooms per dwelling and 13 suburbs that average more than 8 rooms per dwelling.

hist(Boston\$rm[Boston\$crim>8])

In the histogram, the bar simultaneously increased in between the values 5.5 to 6.5



CHAPTER 3

Q8. This question involves the use of simple linear regression on the "Auto" data set.

- a. Use the lm() function to perform a simple linear regression with "mpg" as the response and "horsepower" as the predictor. Use the summary() function to print the results. Comment on the output. For example:
- i. Is there a relationship between the predictor and the response?

```
1  #install.packages('ISLR')
2  llibrary(ISLR)
3  data(Auto)
4  fit <- lm(mpg ~ horsepower, data = Auto)
5  summary(fit)</pre>
> data(Auto)
> fit <- lm(mpg ~ horsepower, data = Auto)</pre>
> summary(fit)
call:
lm(formula = mpg ~ horsepower, data = Auto)
Residuals:
      Min
                1Q
                      Median
                                      3Q
                                                Max
 -13.5710 -3.2592 -0.3435
                                  2.7630 16.9240
Coefficients:
               Estimate Std. Error t value Pr(>|t|)
 (Intercept) 39.935861 0.717499
                                       55.66 <2e-16 ***
                                                  <2e-16 ***
horsepower -0.157845
                            0.006446 -24.49
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 4.906 on 390 degrees of freedom
                                   Adjusted R-squared: 0.6049
Multiple R-squared: 0.6059,
F-statistic: 599.7 on 1 and 390 DF, p-value: < 2.2e-16
```

Answer: As per the hypothesis testing, The p-value from the above screenshot corresponding to the F-statistic is 7.03198910^{-81}, this indicates a clear evidence of a relationship between "mpg" and "horsepower".

ii. How strong is the relationship between the predictor and the response?

Answer: We could see that there is a negative correlation between mpg and horsepower as the coefficient value is -0.16. The unit rise in horsepower decrease the 0.16 milage per gallon. Means there is a fair and considerable correlation between response and predictor variable. Also, we can see that RSE of the lm.fit was 4.906 which indicates a percentage error of 20.9237141%. We could see that the multiple R

square is 0.6059483, which means 60.5948258% of the variability in "mpg" will be explained using "horsepower".

iii. Is the relationship between the predictor and the response positive or negative?

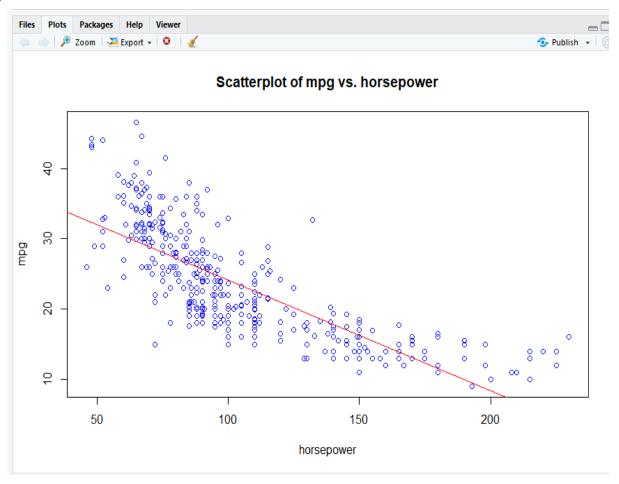
Answer: As the correlation coefficient is negative from the above screenshot, we can say that there is negative linear relationship between mpg and horsepower.

iv. What is the predicted mpgmpg associated with a "horsepower" of 98? What are the associated 95% confidence and prediction intervals?

Answer:

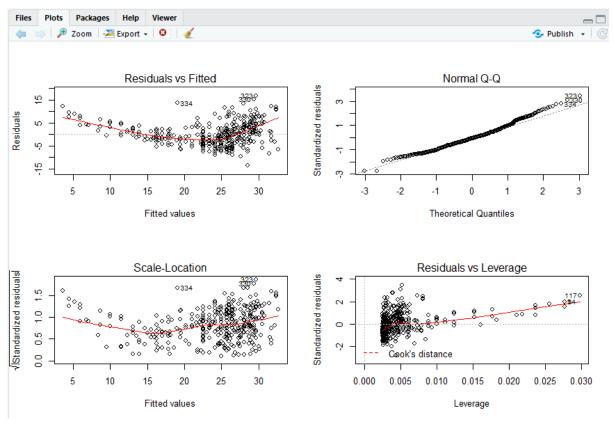
b. Plot the response and the predictor. Use the abline() function to display the least squares regression line.

```
> plot(Auto$horsepower, Auto$mpg, main = "Scatterplot of mpg vs. horsepower", xlab = "horsepower", ylab = "mpg", col = "blue
")
> abline(fit, col = "red")
> |
```



c. Use the plot() function to produce diagnostic plots of the least squares regression fit. Comment on any problems you see with the fit.

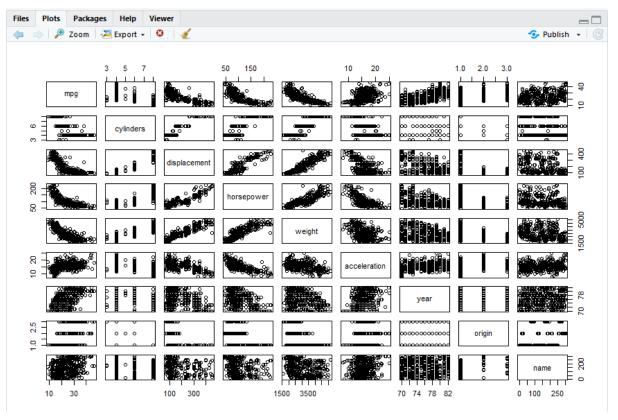
```
> par(mfrow = c(2, 2))
> plot(fit)
> |
```



The plot of residuals versus fitted values indicates the presence of non-linearity in the data. The plot of standardized residuals versus leverage indicates the presence of a few outliers (higher than 2 or lower than -2) and a few high leverage points.

- 9. This question involves the use of multiple linear regression on the "Auto" data set.
 - a. Produce a scatterplot matrix which include all the variables in the data set.

```
> pairs(Auto)
> |
```



b. Compute the matrix of correlations between the variables using the function cor(). You will need to exclude the "name" variable, which is qualitative.

```
> names(Auto)
 [1] "mpg
                     "cylinders"
                                     "displacement" "horsepower"
                                                                     "weight"
                                                                                     "acceleration" "year"
 [8] "origin"
                     "name"
> cor(Auto[1:8])
                     mpg cylinders displacement horsepower
                                                                 weight acceleration
                                                                                                     origin
                                                                                           vear
mpg
cylinders
               1.0000000 -0.7776175
                                       -0.8051269 -0.7784268 -0.8322442
                                                                           0.4233285
                                                                                      0.5805410 0.5652088
              -0.7776175
                          1.0000000
                                       0.9508233
                                                   0.8429834
                                                              0.8975273
                                                                          -0.5046834 -0.3456474 -0.5689316
displacement -0.8051269
                          0.9508233
                                       1.0000000
                                                                          -0.5438005 -0.3698552
                                                   0.8972570
                                                              0.9329944
                                                                                                -0.6145351
              -0.7784268
                          0.8429834
                                       0.8972570
                                                   1.0000000
                                                              0.8645377
                                                                          -0.6891955
                                                                                      -0.4163615
horsepower
weight
              -0.8322442
                          0.8975273
                                       0.9329944
                                                   0.8645377
                                                              1.0000000
                                                                          -0.4168392
                                                                                     -0.3091199 -0.5850054
                                      -0.5438005 -0.6891955 -0.4168392
acceleration
               0.4233285 -0.5046834
                                                                           1.0000000
                                                                                      0.2903161
                                                                                                  0.2127458
               0.5805410 -0.3456474
                                       -0.3698552 -0.4163615 -0.3091199
                                                                                      1.0000000
                                                                           0.2903161
                                                                                                  0.1815277
year
origin
               0.5652088 -0.5689316
                                      -0.6145351 -0.4551715 -0.5850054
                                                                           0.2127458
                                                                                      0.1815277
                                                                                                  1.0000000
```

c. Use the lm() function to perform a multiple linear regression with "mpg" as the response and all other variables except "name" as the predictors. Use the summary() function to print the results. Comment on the output. For instance:

i. Is there a relationship between the predictors and the response?

By considering the hypothesis testing, the p-value corresponding to the F-statistic is 2.037105910^ {-139}, this indicates a clear evidence of a relationship between "mpg" and the input predictors.

ii. Which predictors appear to have a statistically significant relationship to the response?

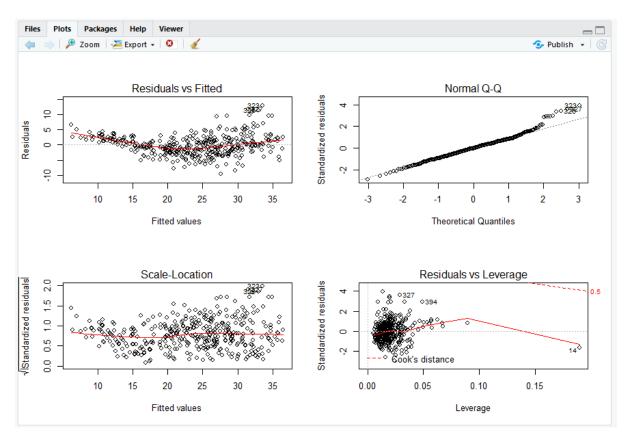
Answer: From the above screenshot reference, the p-value of all the predictors is below threshold that is 0.05 except cylinders, acceleration and horsepower.

iii. What does the coefficient for the "year" variable suggest?

Answer: The coefficient of variable "year" suggesting that a unit increase in year increases 0.75 times the miles per gallon(mpg). With we can say that, cars are becoming fuel efficient year by year.

d. Use the plot() function to produce diagnostic plots of the linear regression fit. Comment on any problems you see with the fit. Do the residual plots suggest any unusually large outliers? Does the leverage plots identify any observations with unusually high leverages?

```
> par(mfrow = c(2, 2))
> plot(fit2)
> |
```



From the above screenshots, we can see that there is some trend in the distribution of residuals which disobeys the assumption of homoscedasticity. Hence, it indicates the mild non-linearity. The standardized residuals versus leverage plot indicates the presence of a few outliers.

e. Use the * and : symbols to fit linear regression models with interaction effects. Do any interactions appear to be statistically significant?

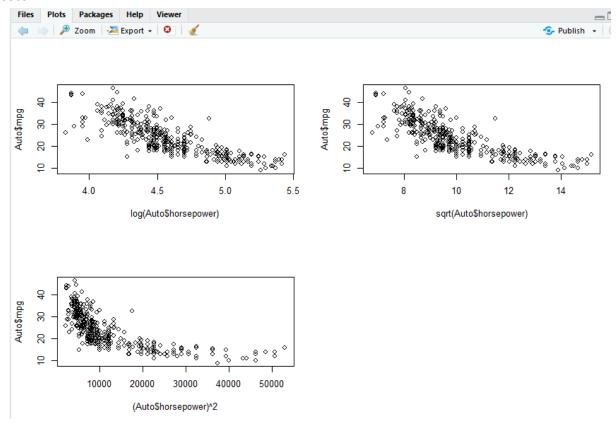
From the correlation matrix above, we have obtained the two highest correlated pairs like cylinders and displacement and weight and have used them for interaction effects.

From the above p-values, we could see that the interaction between displacement and weight is statistically significant, while the interaction between cylinders and displacement is not.

f. Try a few different transformations of the variables, such as logXlog X, X--VX, X2X2. Comment on your findings.

Answer:

```
> par(mfrow = c(2, 2))
> plot(log(Auto$horsepower), Auto$mpg)
> plot(sqrt(Auto$horsepower), Auto$mpg)
> plot((Auto$horsepower)^2, Auto$mpg)
> |
```



So far, we have used horsepower as is for model fitting. But the value as is doesn't fit linear as its log transformation fits in the first plot.

- Q10. This question should be answered using the "Carseats" data set.
- (a) Fit a multiple regression model to predict Sales using Price, Urban, and US.

```
View(Carseats)
  2
     ?Carseats
  3 model<-lm(Sales~Price+Urban+US,data=Carseats)</pre>
  4 summary(model)
  5
 6:1 (Top Level) $
Console ~/ A
> View(Carseats)
> ?Carseats
> model<-lm(Sales~Price+Urban+US,data=Carseats)
> summary(model)
lm(formula = Sales ~ Price + Urban + US, data = Carseats)
Residuals:
          1Q Median
                         3Q
   Min
-6.9206 -1.6220 -0.0564 1.5786 7.0581
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1
Residual standard error: 2.472 on 396 degrees of freedom
Multiple R-squared: 0.2393, Adjusted R-squared: 0.2335
F-statistic: 41.52 on 3 and 396 DF, p-value: < 2.2e-16
```

(b) Provide an interpretation of each coeffiffificient in the model. Be careful—some of the variables in the model are qualitative!

Answer:

The coefficient of the 'price' factors might be deciphered by saying that the normal impact of a cost of 1 dollar is a reduction of 54.4588492 units in the sales any remaining indicators staying fixed. The coefficient of the 'urban' factors might be deciphered by saying that the unit deals are 21.9161 units not exactly rural area, The coefficient of the 'US' factors might be deciphered by saying that the normal deals in the US store are 1200.572 units more than in a no US store any remaining predictors.

(c) Write out the model in equation form, being careful to handle the qualitative variables properly.

```
Sales = 13.0434 + (-0.0544) *price + (-0.02191)*urban + (1.2005727)*US + \epsilon
```

(d) For which of the predictors can you reject the null hypothesis H0: $\beta j = 0$? Answer:

'Price' and 'US' variables can be rejected.

(e) On the basis of your response to the previous question, fit a smaller model that only uses the predictors for which there is evidence of association with the outcome.

```
View(Carseats)
   2
       ?Carseats
model<-lm(Sales~Price+Urban+US,data=Carseats)
       summary(model)
       (Top Level) $
 Console ~/ 6
 > View(Carseats)
 > model<-lm(Sales~Price+Urban+US,data=Carseats)
 > summary(model)
 lm(formula = Sales ~ Price + Urban + US, data = Carseats)
 Residuals:
 Min 1Q Median 3Q Max
-6.9206 -1.6220 -0.0564 1.5786 7.0581
Coefficients:
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 2.472 on 396 degrees of freedom
Multiple R-squared: 0.2393, Adjusted R-squared: 0.2335
F-statistic: 41.52 on 3 and 396 DF, p-value: < 2.2e-16
  1 View(Carseats)
      ?Carseats
   3
      model<-lm(Sales~Price+US,data=Carseats)
   4 summary(model)
5
  5:1 (Top Level) $
Console ~/ <
> View(Carseats)
> ?Carseats
> model<-lm(Sales~Price+US,data=Carseats)
> summary(model)
lm(formula = Sales ~ Price + US, data = Carseats)
Residuals:
Min 1Q Median 3Q Max
-6.9269 -1.6286 -0.0574 1.5766 7.0515
Coefficients:
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 2.469 on 397 degrees of freedom
Multiple R-squared: 0.2393, Adjusted R-squared: 0.395
F-statistic: 62.43 on 2 and 397 DF, p-value: < 2.2e-16
```

(f) How well do the models in (a) and (e) fit the data?

The smaller model has better R square value compared to bigger model.

(g) Using the model from (e), obtain 95 % confidence intervals for the coefficient(s).

```
View(Carseats)
  1
  2
      ?Carseats
  3
      model<-lm(Sales~Price+US,data=Carseats)
  4
      summary(model)
   5
      confint(model)
  6
  7
       (Top Level) $
Console ~/ 🔅
> confint(model)
                   2.5 %
                               97.5 %
(Intercept) 11.79032020 14.27126531
             -0.06475984 -0.04419543
USYes
              0.69151957
                           1.70776632
```

(h) Is there evidence of outliers or high leverage observations in the model from (e)?

