```
(5)
(a)
   1 library(ISLR)
   2 attach(Default)
   3 set.seed(1)
   4 fit <- glm(default ~ income + balance, data = Default, family = "binomial")
   5
      summary(fit)
   6
   6:1 (Top Level) $
  Console ~/ 🔅
     balance, default, income, student
 > set.seed(1)
 > fit <- glm(default ~ income + balance, data = Default, family = "binomial")
 > summary(fit)
 call:
 glm(formula = default ~ income + balance, family = "binomial",
      data = Default)
 Deviance Residuals:
 Min 1Q Median 3Q
-2.4725 -0.1444 -0.0574 -0.0211
                                           Max
 Coefficients:
                Estimate Std. Error z value Pr(>|z|)
  (Intercept) -1.154e+01 4.348e-01 -26.545 < 2e-16 *** income 2.081e-05 4.985e-06 4.174 2.99e-05 ***
               5.647e-03 2.274e-04 24.836 < 2e-16 ***
 balance
 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
  (Dispersion parameter for binomial family taken to be 1)
      Null deviance: 2920.6 on 9999 degrees of freedom
 Residual deviance: 1579.0 on 9997 degrees of freedom
 AIC: 1585
 Number of Fisher Scoring iterations: 8
(b)
B1
         train <- sample(dim(Default)[1], dim(Default)[1] / 2)</pre>
    12
    13
         (Top Level) $
    13:1
```

```
B2
    12 train <- sample(dim(Default)[1], dim(Default)[1] / 2)
    13 fit <- glm(default ~ income + balance, data = Default, family = "binomial", subset = train)
    14 summary(fit)
   15
   16
   26:1 (Top Level) $
                                                                                                                    R Scr
  Console ~/ <
  > train <- sample(dim(Default)[1], dim(Default)[1] / 2)
> fit <- glm(default ~ income + balance, data = Default, family = "binomial", subset = train)</pre>
  > summary(fit)
  glm(formula = default ~ income + balance, family = "binomial",
      data = Default, subset = train)
  Deviance Residuals:
  Min 1Q Median 3Q Max
-2.1891 -0.1573 -0.0605 -0.0226 3.6623
  Coefficients:
  Estimate Std. Error z value Pr(>|z|)
(Intercept) -1.136e+01 5.982e-01 -18.987 < 2e-16 ***
income 2.265e-05 6.947e-06 3.259 0.00112 **
balance 5.530e-03 3.142e-04 17.600 < 2e-16 ***
  Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
  (Dispersion parameter for binomial family taken to be 1)
      Null deviance: 1483.83 on 4999 degrees of freedom
  Residual deviance: 829.05 on 4997 degrees of freedom
  AIC: 835.05
  Number of Fisher Scoring iterations: 8
B3
           prob <- predict(fit, new= Default[-train, ], type = "response")</pre>
     19
           pred <- rep("No", length(prob))
pred[prob > 0.5] <- "Yes"</pre>
     20
     21
     22
     23
           (Top Level) $
     22:1
   Console ~/ 🔅
   > prob <- predict(fit, new= Default[-train, ], type = "response")
  > pred <- rep("No", length(prob))
> pred[prob > 0.5] <- "Yes"</pre>
```

```
B4
         prob <- predict(fit, new= Default[-train, ], type = "response")</pre>
    19
         pred <- rep("No", length(prob))
pred[prob > 0.5] <- "Yes"</pre>
    20
    21
    22
    23
         mean(pred != Default[-train, ]$default)
    24
    25
    26
    27
    24:1
         (Top Level) $
  Console ~/ 🙈
  > prob <- predict(fit, new= Default[-train, ], type = "response")</pre>
  > pred <- rep("No", length(prob))
> pred[prob > 0.5] <- "Yes"</pre>
  > mean(pred != Default[-train, ]$default)
  [1] 0.028
  >
```

(c)

Depending on different predictors included in the training and validation set, the validation test error rate is varying.

```
25 train <- sample(dim(Default)[1], dim(Default)[1] / 2)</pre>
   fit <- glm(default ~ income + balance, data = Default, family = "binomial", subset = train)
prob <- predict(fit, new= Default[-train, ], type = "response")
        pred<- rep("No", length(prob))
pred[prob > 0.5] <- "Yes"</pre>
           mean(pred != Default[-train, ]$default)
   30
   31
          (Top Level) $
  31:1
                                                                                                                                                                                    R
 Console ~/ 🥖
> train <- sample(dim(Default)[1], dim(Default)[1] / 2)
> fit <- glm(default ~ income + balance, data = Default, family = "binomial", subset = train)
> prob <- predict(fit, new= Default[-train, ], type = "response")
> pred<- rep("No", length(prob))
> pred[prob > 0.5] <- "Yes"</pre>
> mean(pred != Default[-train, ]$default)
[1] 0.0252
> train <- sample(dim(Default)[1], dim(Default)[1] / 2)</pre>
> fit <- glm(default ~ income + balance, data = Default, family = "binomial", subset = train)
> prob <- predict(fit, new= Default[-train, ], type = "response")</pre>
> pred<- rep("No", length(prob))
> pred[prob > 0.5] <- "Yes"
  mean(pred != Default[-train, ]$default)
[1] 0.0246
[1] 0.0246
> train <- sample(dim(Default)[1], dim(Default)[1] / 2)
> fit <- glm(default ~ income + balance, data = Default, family = "binomial", subset = train)
> prob <- predict(fit, new= Default[-train, ], type = "response")
> pred<- rep("No", length(prob))
> pred[prob > 0.5] <- "Yes"
> mean(pred != Default[-train, ]$default)
[1] 0.0266
> |
```

(d) Including student dummy variable is not showing any decreasing difference in the test error

(6)

(a)

The standard error rates of the coefficients beta0, beta1 and beta2 are 0.4348, 0.000004985, 0.0002274

```
1 library(ISLR)
      attach(Default)
     set.seed(1)
     fit <- glm(default ~ income + balance, data = Default, family = "binomial")
      summary(fit)
   6
  7:1
     (Top Level) $
 Console ~/ <
> fit <- glm(default ~ income + balance, data = Default, family = "binomial")
> summary(fit)
glm(formula = default ~ income + balance, family = "binomial",
    data = Default)
Deviance Residuals:
Min 1Q Median 3Q
-2.4725 -0.1444 -0.0574 -0.0211
                                         мах
              Estimate Std. Error z value Pr(>|z|)
(Intercept) -1.154e+01 4.348e-01 -26.545 < 2e-16 ***
             2.081e-05 4.985e-06
                                   4.174 2.99e-05 ***
income
balance
             5.647e-03 2.274e-04 24.836 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 2920.6 on 9999 degrees of freedom
Residual deviance: 1579.0 on 9997 degrees of freedom
AIC: 1585
Number of Fisher Scoring iterations: 8
>
```

(c)

The bootstrap standard error rates of beta0, beta1 and beta2 are 4.285621e-01, 4.950151e-06 and 2.236899e-04

(d)

The two methods are giving approximately same error rates.

```
(9)
(a)
    58 library(MASS)
    59 attach(Boston)
    60 mue<-mean(medv)
    61 mue
    62
    63
    64
    65
    66
    67
    68
    69
    70
    71
   62:1
        (Top Level) $
  Console ~/ 🔗
  K IS a corraporactive project with many contributors.

Type 'contributors()' for more information and
  'citation()' on how to cite R or R packages in publications.
  Type 'demo()' for some demos, 'help()' for on-line help, or
  'help.start()' for an HTML browser interface to help.
  Type 'q()' to quit R.
  [Workspace loaded from ~/.RData]
  > library(MASS)
  > attach(Boston)
  The following object is masked _by_ .GlobalEnv:
      age
 > mue<-mean(medv)
  > mue
  [1] 22.53281
```

```
(b)
    64 se <- sd(medv) / sqrt(dim(Boston)[1])
    65
       se
    66
       П
    67
    68
    69
    70
   71
   66:1
       (Top Level) $
  Console ~/ A
  > se <- sd(medv) / sqrt(dim(Boston)[1])</pre>
  [1] 0.4088611
```

(c)

The bootstrap standard error rate is 0.41193 which is closer to 0.4088 that is the value obtained from b

```
85 set.seed(1)
 86 - boot.fn <- function(data, index) {
      mu <- mean(data[index])</pre>
       return (mu)
 89 }
 90 library(boot)
     boot(medv, boot.fn, 1000)
     (Top Level) $
 92:1
Console ~/ A
> set.seed(1)
> boot.fn <- function(data, index) {
   mu <- mean(data[index])</pre>
    return (mu)
> library(boot)
> boot(medv, boot.fn, 1000)
ORDINARY NONPARAMETRIC BOOTSTRAP
boot(data = medv, statistic = boot.fn, R = 1000)
Bootstrap Statistics :
   original bias
                          std. error
t1* 22.53281 0.008517589
                          0.4119374
```

(d)

The confidence interval of t.test() is closer to the confidence interval given by bootstrap

```
93
     t.test(medv)
     ci<- c(22.53 - 2 * 0.4119, 22.53 + 2 * 0.4119)
 95 ci
 96
     (Top Level) $
 96:1
Console ~/ 🔅
> t.test(medv)
        One Sample t-test
data: medv
t = 55.111, df = 505, p-value < 2.2e-16
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
 21.72953 23.33608
sample estimates:
mean of x
 22.53281
> ci<- c(22.53 - 2 * 0.4119, 22.53 + 2 * 0.4119)
> ci
[1] 21.7062 23.3538
```

(e)

```
97 med <- median(medv)
98 med
99 <
99:1 (Top Level) $

Console ~/  >> med <- median(medv)
> med
[1] 21.2
> |
```

(f)The median value is 21.2 which is equal to the value obtained in (e), with a standard error of 0.3745

```
101 - boot.fn <- function(data, index) {
          mu <- median(data[index])</pre>
   102
          return (mu)
   103
   104
        boot(medv, boot.fn, 1000)
   105
   106
         <
   106:1 (Top Level) $
  Console ~/ 🔅
  > boot.fn <- function(data, index) {
      mu <- median(data[index])</pre>
      return (mu)
 +
 > boot(medv, boot.fn, 1000)
 ORDINARY NONPARAMETRIC BOOTSTRAP
 call:
 boot(data = medv, statistic = boot.fn, R = 1000)
 Bootstrap Statistics :
     original bias std. error
          21.2 -0.0025
 t1*
                         0.374358
 > |
(g)
   107
        quantitymue <- quantile(medv, c(0.1))
   108 quantitymue
   109
         <
   109:1 (Top Level) $
  Console ~/ A
 > quantitymue <- quantile(medv, c(0.1))
 > quantitymue
   10%
 12.75
 > |
```

(h)

The tenth percentile is 12.75 which is again equal to the value obtained in (g), with a standard error of 0.49122

```
111 - boot.fn <- function(data, index) {
         mu <- quantile(data[index], c(0.1))</pre>
 113
         return (mu)
 114 }
 115 boot(medv, boot.fn, 1000)
 116
       <
 116:1 (Top Level) $
Console ~/ 🔅
> boot.fn <- function(data, index) {
   mu <- quantile(data[index], c(0.1))</pre>
   return (mu)
> boot(medv, boot.fn, 1000)
ORDINARY NONPARAMETRIC BOOTSTRAP
call:
boot(data = medv, statistic = boot.fn, R = 1000)
Bootstrap Statistics :
   original bias std. error
t1*
       12.75 0.0261 0.4912231
> |
```