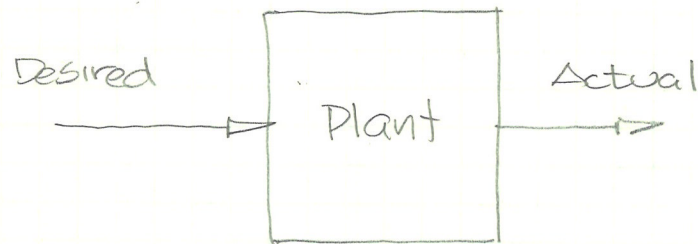


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Why We Add Feedback

The model for the ideal system would be one in which my desired output is always my actual output.



(the perfect teenager!)

As previously stated this is not possible for three primary reasons

(1) Plant dynamics (plant cannot track rapid input changes)

(2) Changes in or unmodeled plant dynamics

(3) External disturbances

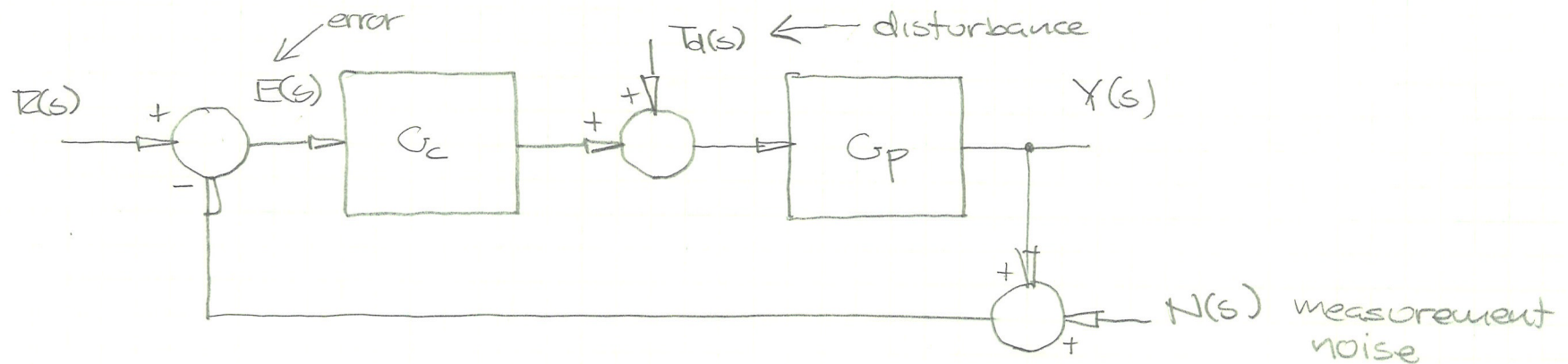
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Feedback allows us to 'get closer' to the ideal in many instances.

Given the following feedback system



Let's look at the effect of feedback on

$$\frac{Y(s)}{R(s)} = \frac{G_c G_p}{1 + G_c G_p}$$



we want this to close to 1

$$\frac{Y(s)}{T_d(s)} = \frac{G_p}{1 + G_c G_p}$$



want this to be small

$$\frac{Y(s)}{N(s)} = \frac{-G_c G_p}{1 + G_c G_p}$$



want this to be small

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It appears that if G_c is big in comparison to G_p and 1

$$\frac{Y(s)}{R(s)} \approx 1$$

$$\frac{Y(s)}{T_d(s)} \text{ is small}$$

$$\frac{Y(s)}{N(s)} \approx 1$$

(what happened?!)

(logical inferences?)

$$Y(s) = \frac{G_c G_p}{1 + G_c G_p} R(s) + \frac{G_p}{1 + G_c G_p} T_d(s) - \frac{G_c G_p}{1 + G_c G_p} N(s)$$

$$\begin{aligned} E(s) = R(s) - Y(s) &= \frac{1 + G_c G_p}{1 + G_c G_p} R(s) - \frac{G_c G_p}{1 + G_c G_p} R(s) - \frac{G_p}{1 + G_c G_p} T_d(s) + \frac{G_c G_p}{1 + G_c G_p} N(s) \\ &= \frac{1}{1 + G_c G_p} R(s) - \frac{G_p}{1 + G_c G_p} T_d(s) + \frac{G_c G_p}{1 + G_c G_p} N(s) \end{aligned}$$

↑
true error

Define the sensitivity as $S(s) = \frac{1}{1 + G_c G_p}$ $L(s) = G_c G_p$
↑
loop transmission