

# ch03\_dynamics

January 24, 2022

## 0.1 Problem 0: Implementation

Implement the `derivatives` function in `chap3/mav_dynamics.py` using the quaternion form of the dynamics described in equations (B.1) through (B.4) of *Appendix B* in the book. Note that the dynamics utilized are from the Aerosonde UAV from Table E.2. The first column of these parameters should provide / aid your intuition about what is occurring.

Below are some useful code snippets and hints: \* `st = DynamicState(state)`: Extract the numpy matrix into a struct for easy access of states. Note that the `DynamicsState` struct is defined on line 46. \* `fm = ForceMoments(forces_moments)`: Extract forces and moments into a struct for easy access. Note that the `ForceMoments` struct is defined on line 124. \* The momentum terms are defined in `mav_sim.parameters.aerosonde_parameters.py` and are imported as `MAV` (i.e., to get  $\Gamma_1$ , call `MAV.gamma1`) \* Equation (3.14) can be used instead of (B.1) by converting the quaternion to a rotation matrix using `Quaternion2Rotation(state[IND.QUAT])` \* The velocity values can be extracted as a vector as `state[IND.VEL]`

## 0.2 Problem 1: No Inputs, Zero Initial Conditions

For this problem, you will test the dynamics function with no input forces and torques, and all initial velocities set to zero. Set the initial conditions such that the vehicle starts at zero north and east position, and an altitude of 5 meters. Set the initial attitude (yaw) to  $\frac{\pi}{4}$  and zero roll and pitch. Set all velocities to zero.

### 0.2.1 Question: What behavior do you expect (try to be explicit in terms of what different states will do)?

**Answer:** rotate about the z axis and lift vehicle

### 0.2.2 Question: Was the behavior as expected. If not, what did you observe differently from what you thought you would? Why did this difference occur?

**Answer:** rotate about the z axis and lift vehicle

```
[1]: # Note that this cell can be run separately to initialize for other cell blocks
from mav_sim.chap3.mav_dynamics import DynamicState, ForceMoments
from mav_sim.chap3.run_sim import run_sim
from mav_sim.message_types.msg_sim_params import MsgSimParams
from mav_sim.tools.display_figures import display_data_view, display_mav_view
from mav_sim.chap2.mav_viewer import MavViewer
from mav_sim.chap3.data_viewer import DataViewer
```

```

import math
import numpy as np

# The viewers need to be initialized once due to restart issues with qtgraph
if 'mav_view' not in globals():
    print("Initializing mav_view")
    global mav_view
    mav_view = MavViewer() # initialize the mav viewer
if 'data_view' not in globals():
    print("Initializing data_view")
    global data_view
    data_view = DataViewer() # initialize view of data plots

def run_sim_and_display(sim_params, state, fm):
    global mav_view
    global data_view
    data_view.reset(sim_params.start_time)
    (mav_view, data_view) = run_sim(sim_params, state, fm, mav_view, data_view)
    display_data_view(data_view)
    display_mav_view(mav_view)

```

Initializing mav\_view  
 Initializing data\_view

```

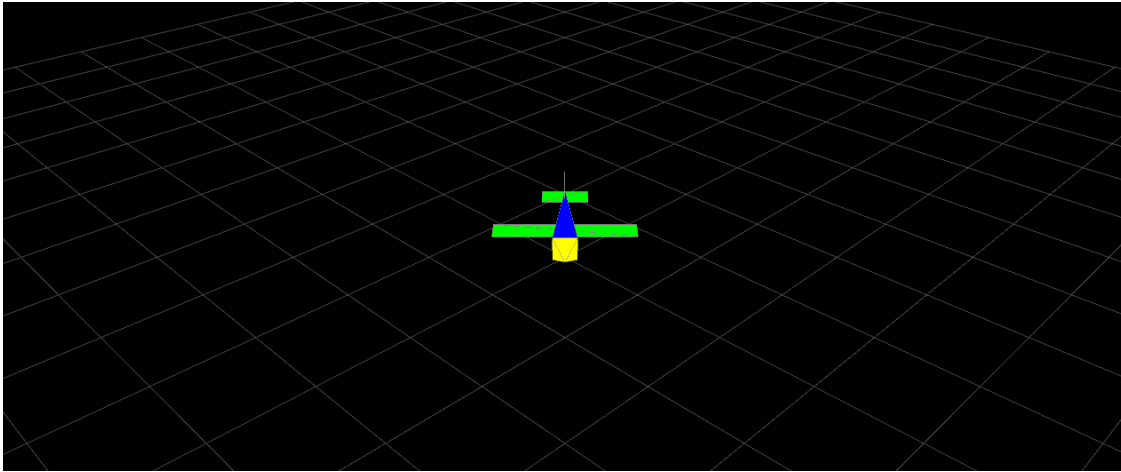
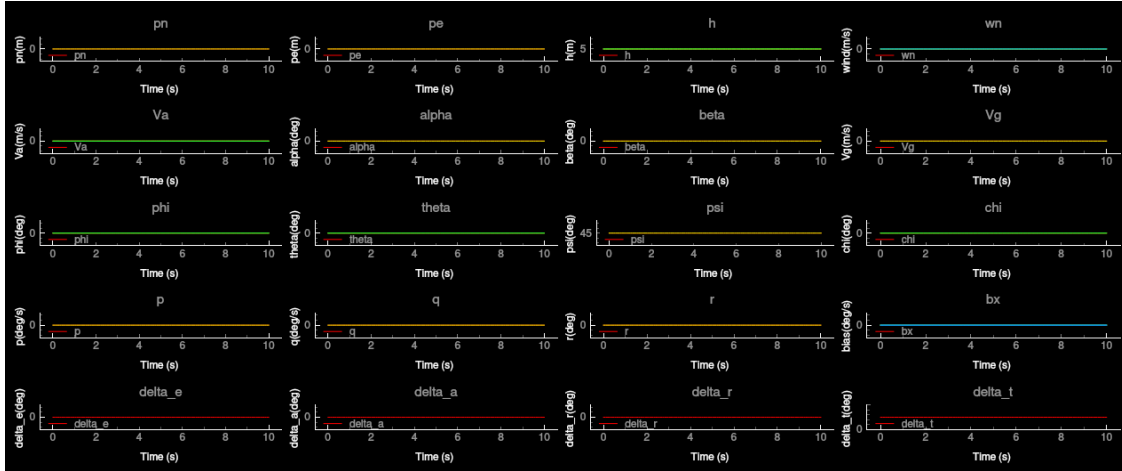
[2]: # Initialize the simulation parameters
sim_params = MsgSimParams(end_time=20.) # Sim ending in 10 seconds
state = DynamicState(state=np.zeros([13,1])) # State initialized to zeros
state.set_attitude_euler(0., 0., math.pi/4)
fm = ForceMoments(force_moment=np.zeros([6,1])) # Set all forces equal to zero

state.down = -5

# Run the simulation and display the data
run_sim_and_display(sim_params, state, fm)

```

Press Command-Q to exit...



### 0.3 Problem 2: No Inputs, Non-Zero Initial Conditions

For this problem, you will test the dynamics function with no input forces and torques. Set the initial velocities such that the UAV is flying straight at  $1 \frac{m}{s}$ . Set the initial conditions such that the vehicle starts at zero north, zero east, and an altitude of 5 meters. Set the initial attitude (yaw) to  $\frac{\pi}{4}$  with zero roll and pitch.

**0.3.1 Question:** What behavior do you expect (try to be explicit in terms of what different states will do)?

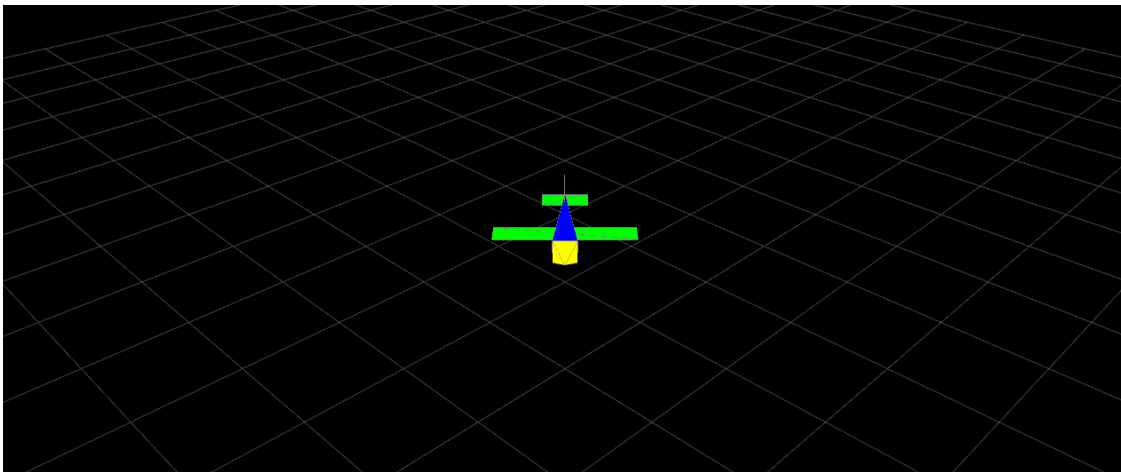
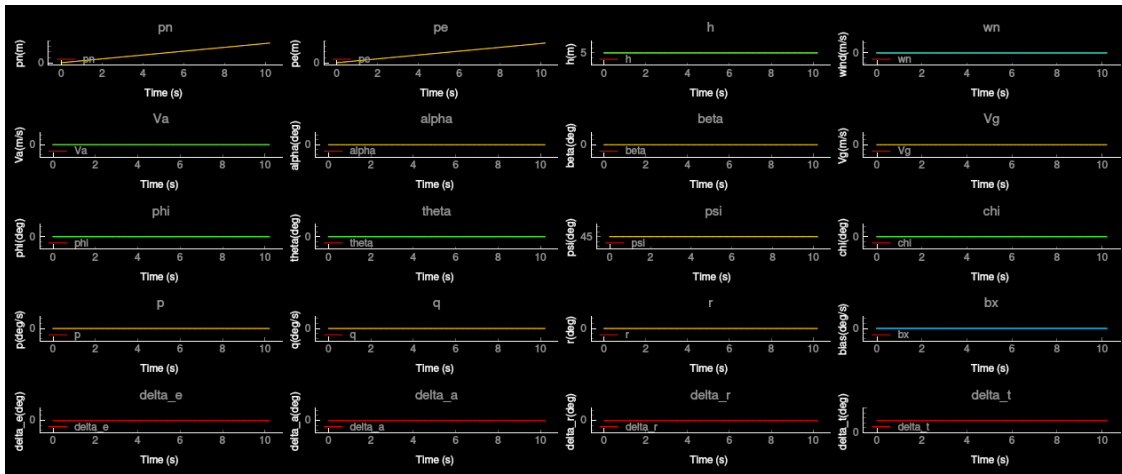
**Answer:** Plane starts moving slowly forward in the rotated z axis direction

**0.3.2 Question:** Was the behavior as expected. If not, what did you observe differently from what you thought you would? Why did this difference occur?

**Answer:** Plane starts moving slowly forward in the rotated z axis direction

```
[3]: # Initialize the simulation parameters
sim_params = MsgSimParams(end_time=20.) # Sim ending in 10 seconds
state = DynamicState(state=np.zeros([13,1])) # State initialized to zeros
state.set_attitude_euler(0., 0., math.pi/4)
fm = ForceMoments(force_moment=np.zeros([6,1])) # Set all forces equal to zero
state.u = 1
state.down = -5
# Run the simulation and display the data
run_sim_and_display(sim_params, state, fm)
```

Press Command-Q to exit...



## 0.4 Problem 3: No Inputs, Non-Zero Initial Rotational Velocities

For this problem, you will test the dynamics function with no input forces and torques, but with initial rotational velocities. Set the initial velocities such that the UAV is at rest. Set the initial conditions such that the vehicle starts at zero north, zero east, and an altitude of 5 meters. Set the initial attitude (yaw) to  $\frac{\pi}{4}$  with zero roll and pitch. Set the initial roll rate to 0.5 rad/s.

**0.4.1 Question:** What behavior do you expect (try to be explicit in terms of what different states will do)?

**Answer:** rotate in z direction and spin about the nose of the vehicle

**0.4.2 Question:** Was the behavior as expected. If not, what did you observe differently from what you thought you would? Why did this difference occur?

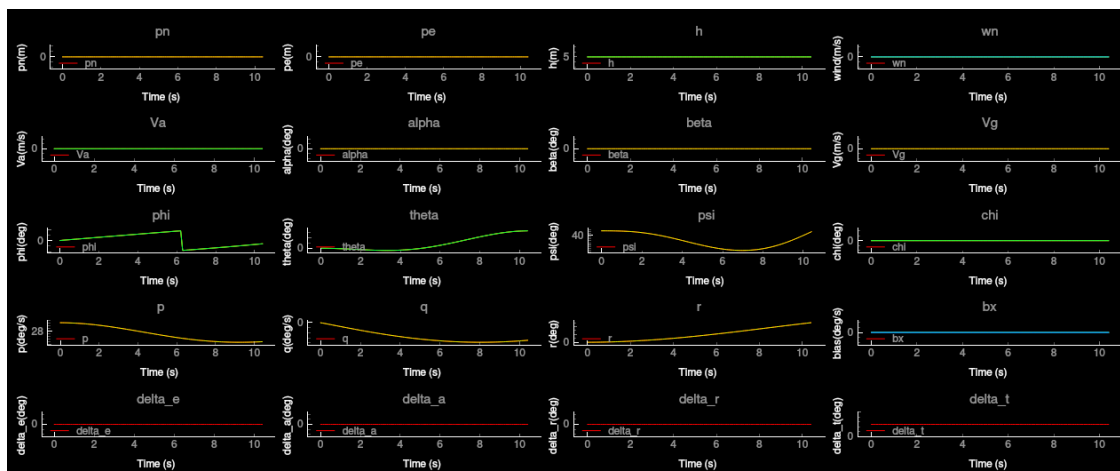
**Answer:** Vehicle began to wobble

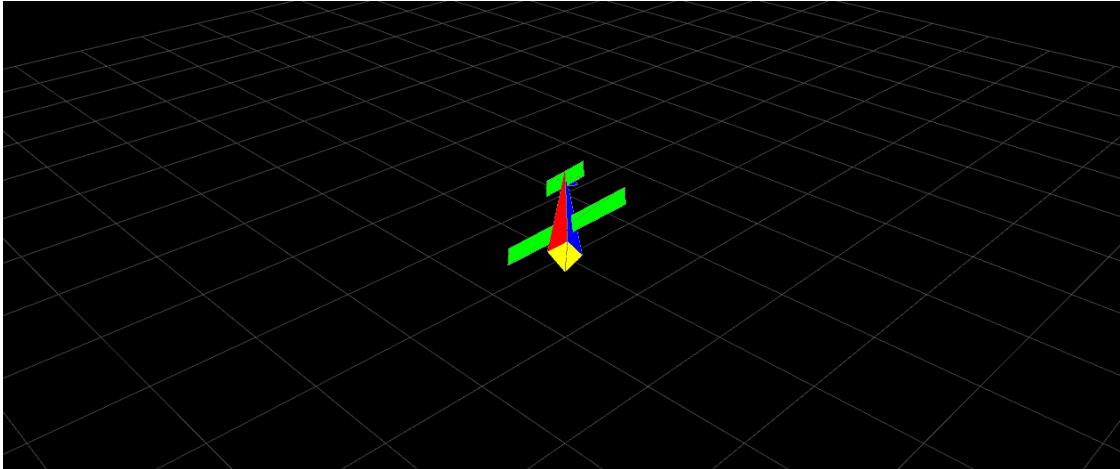
```
[4]: # Initialize the simulation parameters
sim_params = MsgSimParams(end_time=20.) # Sim ending in 10 seconds
state = DynamicState(state=np.zeros([13,1])) # State initialized to zeros
state.set_attitude_euler(0., 0., math.pi/4)
fm = ForceMoments(force_moment=np.zeros([6,1])) # Set all forces equal to zero
print('Need to choose parameters')

state.p = 0.5
state.down = -5
# Run the simulation and display the data
run_sim_and_display(sim_params, state, fm)
```

Need to choose parameters

Press Command-Q to exit...





## 0.5 Problem 4: Constant Force Inputs

For this problem, you will test the dynamics function with zero initial conditions and constant force inputs. Set the initial conditions such that the vehicle starts at zero north and east position, and an altitude of 5 meters. Set the initial attitude (yaw) to  $\frac{\pi}{4}$  and zero roll and pitch. Set all velocities to zero. Define the input forces to 0.1 \$ Newton in the direction of  $i^b$  and 0.5 Newton in an upwards direction.

**0.5.1 Question:** What behavior do you expect (try to be explicit in terms of what different states will do)?

**Answer:** plane will move forward and down

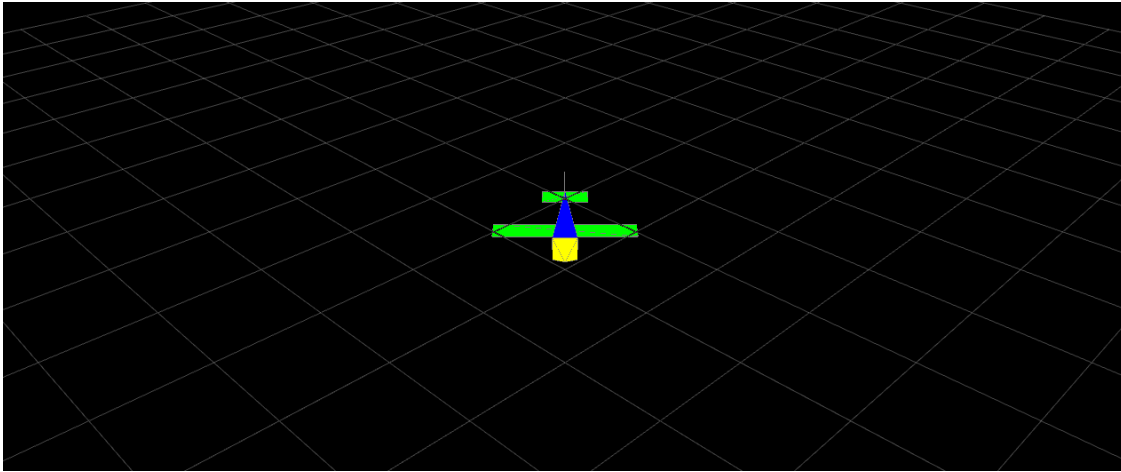
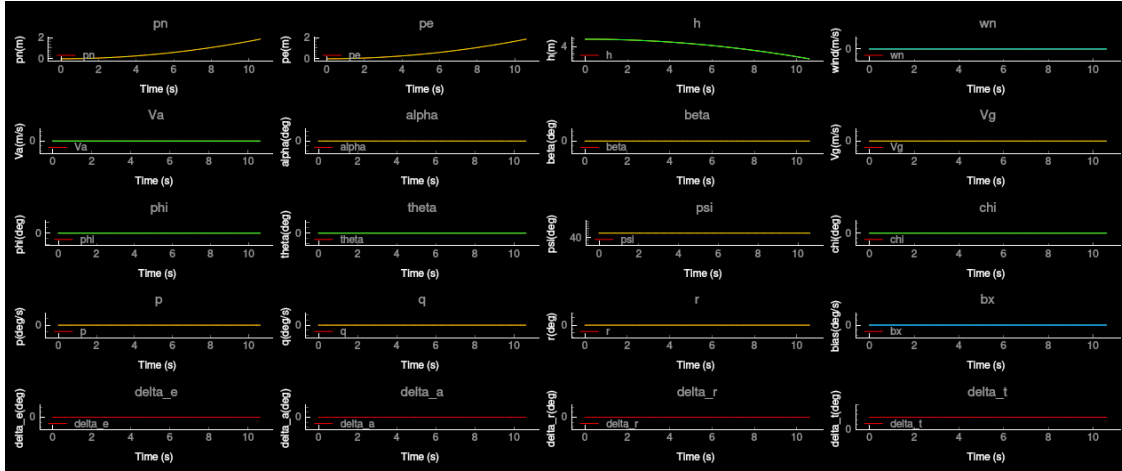
**0.5.2 Question:** Was the behavior as expected. If not, what did you observe differently from what you thought you would? Why did this difference occur?

**Answer:** plane will move forward and down

```
[5]: # Initialize the simulation parameters
sim_params = MsgSimParams(end_time=20.) # Sim ending in 10 seconds
state = DynamicState(state=np.zeros([13,1])) # State initialized to zeros
state.set_attitude_euler(0., 0., math.pi/4)
fm = ForceMoments(force_moment=np.zeros([6,1])) # Set all forces equal to zero
print('Need to choose parameters')

fm.fx = fm.fz = 0.5
state.down = -5
# Run the simulation and display the data
run_sim_and_display(sim_params, state, fm)
```

Need to choose parameters  
Press Command-Q to exit...



## 0.6 Problem 5: Constant Torque Inputs

For this problem, you will test the dynamics function with zero initial conditions and constant force inputs. Set the initial conditions such that the vehicle starts at zero north and east position, and an altitude of 5 meters. Set the initial attitude (yaw) to  $\frac{\pi}{4}$  and zero roll and pitch. Set all velocities to zero. Define the torque about the  $x$ -axis as 0.1 with all other torques and forces zeroed out.

**0.6.1 Question:** What behavior do you expect (try to be explicit in terms of what different states will do)?

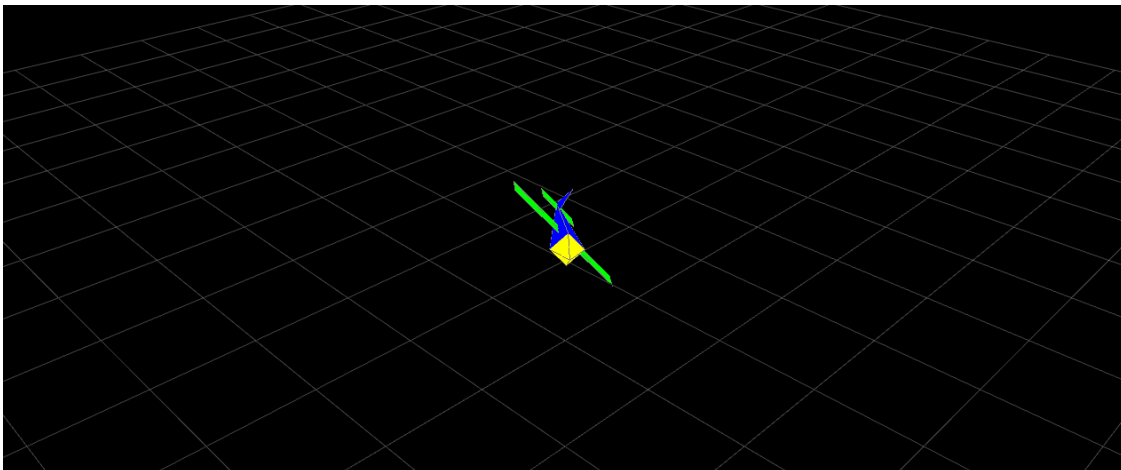
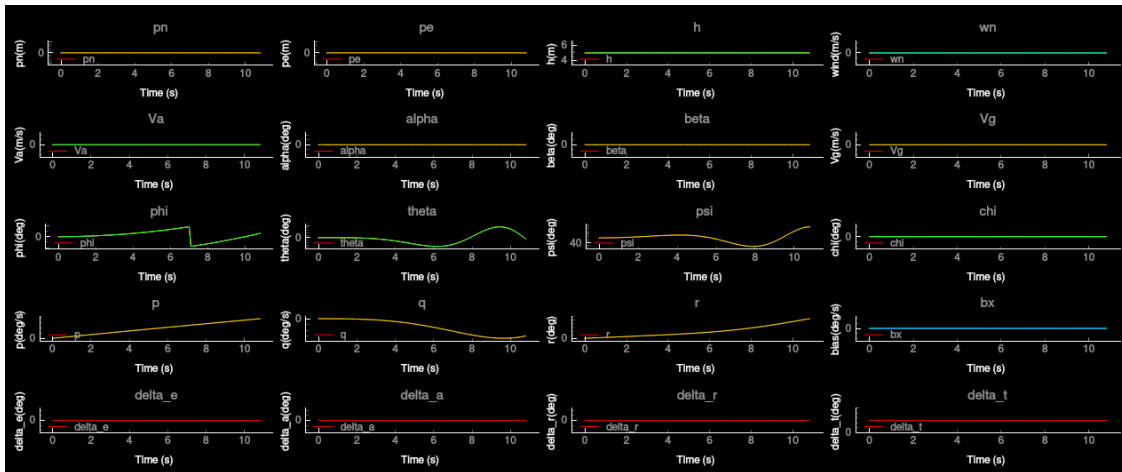
**Answer:** (Answer before completion)

**0.6.2 Question:** Was the behavior as expected. If not, what did you observe differently from what you thought you would? Why did this difference occur?

**Answer:** (Answer after completion)

```
[6]: # Initialize the simulation parameters
sim_params = MsgSimParams(end_time=20.) # Sim ending in 10 seconds
state = DynamicState(state=np.zeros([13,1])) # State initialized to zeros
state.set_attitude_euler(0., 0., math.pi/4)
fm = ForceMoments(force_moment=np.zeros([6,1])) # Set all forces equal to zero
fm.l = 0.1
state.down = -5
# Run the simulation and display the data
run_sim_and_display(sim_params, state, fm)
```

Press Command-Q to exit...





## 0.7 Simple code checking

The following code does not need to change. It should just be used as a sanity check so that you know the code is implemented properly. The output should not have any lines reading Failed test!

```
[7]: from mav_sim.unit_tests.ch3_derivatives_test import derivatives_test
     derivatives_test()
```

Starting derivatives test

Calculated output:

```
[[25.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]]
```

Expected output:

```
[[25.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]
 [ 0.]]
```

Passed test

Calculated output:

```
[[ 7.01608606e-06]
 [ 3.06165726e-04]
 [ 7.17877791e-05]
 [-6.90909091e+00]
 [-3.10818182e+02]
 [ 2.93272727e+02]
 [-1.63000000e+02]
```

```
[ 4.25000000e+01]
[ 5.10000000e+01]
[ 5.05000000e+01]
[-9.94076590e+01]
[ 1.27248458e+02]
[-3.73793531e+01]]
```

Expected output:

```
[[ 7.01608606e-06]
 [ 3.06165726e-04]
 [ 7.17877791e-05]
 [-6.90909091e+00]
 [-3.10818182e+02]
 [ 2.93272727e+02]
 [-1.63000000e+02]
 [ 4.25000000e+01]
 [ 5.10000000e+01]
 [ 5.05000000e+01]
 [-9.94076590e+01]
 [ 1.27248458e+02]
 [-3.73793531e+01]]
```

Passed test

End of test

[ ]: