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Graph search

Searching a graph can have many aims:

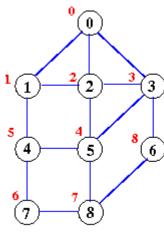
- can I reach every vertex in the graph (is it connected)?
- is one vertex reachable starting from some other vertex?
- what is the shortest path from vertex v to w?
- which vertices are reachable from a vertex? (transitive closure)
- is there a cycle that passes through all the graph? (tour)
- is there a tree that links all vertices? (spanning tree)
 - what is the *minimum* spanning tree?
- are two graphs "equivalent"? (isomorphism)

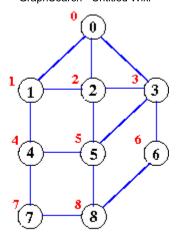
A search is almost never 'random': it uses an underlying strategy:

- depth-first search DFS
- breadth-first search BFS

Breadth-first versus Depth-first search

Example:





Depth-First Search

Breadth-First Search

Order is given by the 'red' labels

• in this example the label ordering is breadth-first (layer by layer)

DFS descends by selecting the first available unvisited node

```
• select 0
• adjacent {1,2,3}
      • select 1
      • adjacent {2, 4}
            • select 2
              adjacent {3, 5}
                  • select 3
                  ■ adjacent {5, 6}
                        • select 5
                        ■ adjacent {4, 8}
                               select 4
                                adjacent {7}
                                     • select 7
                                       adjacent {8}
                                           • select 8
                                             adjacent {6}
                                                 • select 6
                                                 adjacent {} no sites left unvisited
```

BFS descends by systematically visiting the nodes in order of level

```
• select 0
 adjacent \{1,2,3\}
      • select 1
      • adjacent {4}
       select 2
        adjacent {5}
      • select 3
       adjacent {6}
            ■ select 4
              adjacent {7}
               select 5
              adjacent {8}
              select 6
              adjacent {}
                  • select 7
                  adjacent {}
```

- select 8
- adjacent {} no sites left unvisited

These two 'strategies' actually use the <u>same</u> algorithm. They differ only in their use of data structure:

- DFS uses a stack
- BFS uses a queue

Here is the pseudo-algorithm for **Depth/Breadth**-first search:

```
push the root node onto a stack/queue
while (stack/queue is not empty) {
   pop a node from the stack/queue
   if (node is a goal node)
       return 'success'
   push all children of node onto the stack/queue
}
return 'failure'
```

If the aim is not to find a goal node, but to search the whole graph:

- leave out the conditional 'return' (i.e if (node is ...)
- return when complete

Stack-Based Depth-First Search

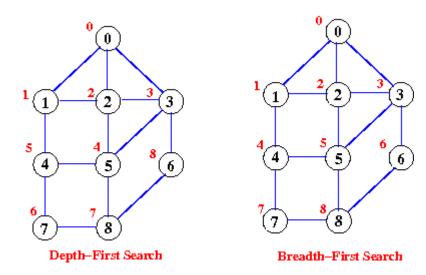
When searching we need to remember which nodes we've *visited*:

- to avoid cycles
- to make sure every node gets visited

Generally an array visited[0 .. numVertices-1] is used

- array indices correspond to vertices
- initialise all elements to -1, meaning unvisited
- when a vertex is visited, the index is set to its 'visit order' number
 - this is simply a 'count' that gets incremented each time a new node is visited

For example, here is the earlier graph again



The *visited* array starts as {-1,-1,-1,-1,-1,-1,-1,-1}

We select the root **0** first

adjacent	visit	resulting visited array
any node	0	{ 0,-1,-1,-1,-1,-1,-1,-1}
1 2 3	1	{ 0, 1,-1,-1,-1,-1,-1,-1}
0 2 4	2	{ 0, 1, 2 ,-1,-1,-1,-1,-1}
0 1 3 5	3	{ 0, 1, 2, 3,-1,-1,-1,-1}
0 2 5 6	5	{ 0, 1, 2, 3, -1, 4, -1, -1, -1}
2 3 4 8	4	{ 0, 1, 2, 3, 5, 4,-1,-1,-1}
1 5 7	7	{ 0, 1, 2, 3, 5, 4,-1, 6 ,-1}
4 8	8	{ 0, 1, 2, 3, 5, 4,-1, 6, 7}
5 6 7	6	{ 0, 1, 2, 3, 5, 4, 8 , 6, 7}

Let's try a different starting vertex: this time start at vertex 5:

adjacent	visit	resulting visited array
any node	5	{-1,-1,-1,-1,-1, 0 ,-1,-1,-1}
2 3 4 8	2	{-1,-1, 1 ,-1,-1, 0,-1,-1,-1}
0 1 3 5	0	{ 2 ,-1, 1,-1,-1, 0,-1,-1,-1}
1 2 3	1	{ 2, 3, 1,-1,-1, 0,-1,-1,-1}
0 2 4	4	{ 2, 3, 1,-1, 4, 0,-1,-1,-1}
1 5 7	7	{ 2, 3, 1,-1, 4, 0,-1, 5,-1}
4 8	8	{ 2, 3, 1,-1, 4, 0,-1, 5, 6 }
5 6 7	6	{ 2, 3, 1,-1, 4, 0, 7, 5, 6}
3 8	3	{ 2, 3, 1, 8 , 4, 0, 7, 5, 6}

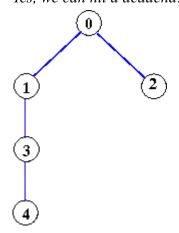
The array visited[] here is the depth-first order

• It says: { 2^{nd} , 3^{rd} , 1^{st} , 8^{th} , 4^{th} , 0^{th} , 7^{th} , 5^{th} , 6^{th} }

The visited array indicates the order of the search.

Can anything go wrong during the traversal?

• Yes, we can hit a deadend!



choice	visit	resulting visited array
any node	0	{0,-1,-1,-1,}

1 2	1	{ 0, 1,-1,-1,-1}
0 3	3	{ 0, 1,-1, 2 ,-1}
1 4	4	{ 0, 1,-1, 2, 3 }
	finished?	

- 4 is a leaf node, we can go no further
- there is still an unvisited vertex in the array

How do we 'find' it?

- we need to backtrack
 - we go back to vertex 0, and then visit vertex 2
 - this is also a leaf node
 - ... but all nodes have been visited, so we are really finished this time

Final DFS path is visited = $\{0, 1, 4, 2, 3\}$

So we cannot expect DFS to visit every vertex in a single forward traversal

• we sometimes need to backtrack

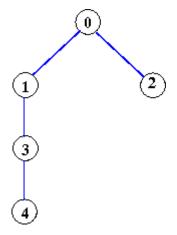
But how do we backtrack?

- we use a stack!
 - vertices are pushed onto the stack when we have 1 or more adjacent vertices to visit
 - to actually visit a vertex, we simply pop it from the stack
- only when the stack is empty have we visited everyone!

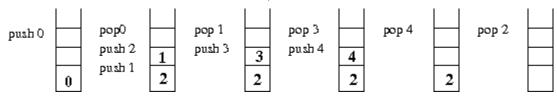
Using a stack in DFS means:

- when we *visit*, we *pop* the next vertex off the stack
- after a visit, we *push* the adjacent vertices onto the stack
- when we land on a leaf node, we cannot push any nodes onto the stack
 - we then pop a vertex instead
 - ... this is backtracking (to an earlier vertex)
- only when the stack is empty have we visited every vertex

Consider the above graph again:



The following stack operations are carried out:



dfsStack.c (for connected graphs)

```
切换行号显示
   1 // dfsStack.c: traverse a graph using DFS and stacking (graph may
be disconnected)
   2 // Compile using:
   3 //
             dcc -o dfsStack dfsStack.c IOmem.c GraphAM.c Quack.c
   4 //
   5 #include <stdio.h>
   6 #include <stdlib.h>
   7 #include "Graph.h"
   8 #include "Quack.h"
   9 #include "IOmem.h"
  10
  11 #define STARTVERTEX 0 // start the depth-first search at this
vertex
  12
  13 void dfsQuack(Graph, Vertex, int);
  14
  15 int main (void) {
        int numV;
  16
  17
         if ((numV = readNumV()) > 0) {
  18
             Graph g = newGraph(numV);
  19
             if (readBuildGraph(g)) {
  20
                 showGraph(g);
  21
                 dfsQuack(g, STARTVERTEX, numV);
  22
             }
  23
             g = freeGraph(g);
  24
             g = NULL;
  25
         }
         else {
  26
  27
             printf("Error in reading #number\n");
  28
             return EXIT FAILURE;
  29
  30
         return EXIT SUCCESS;
  31 }
  32
  33 //HANDLES CONNECTED GRAPHS ONLY
  34 void dfsQuack(Graph g, Vertex v, int numV) {
  35
       int *visited = mallocArray(numV);
  36
       Quack s = createQuack();
  37
        push(v, s);
  38
       showQuack(s);
  39
       int order = 0;
  40
       while (!isEmptyQuack(s)) {
  41
          v = pop(s);
  42
           if (visited[v] == UNVISITED) {    // we visit only unvisited
vertices
              printArray("Visited: ", visited, numV);
  43
  44
              visited[v] = order++;
  45
              for (Vertex w = numV - 1; w \ge 0; w--) { //push adjacent
vertices
                 if (isEdge(newEdge(v,w), g)) {
                                                      // ... in
  46
reverse order
                                                        // ... onto the
  47
                    push (w, s);
stack
  48
                 }
  49
              }
  50
  51
           showQuack(s);
```

```
52  }
53  printArray("Visited: ", visited, numV);
54  free(visited);
55  return;
56 }
```

The loop formed by lines 40-52 eventually empty the stack

- ... suggesting that the traversal is complete ...
 - ... and that all nodes have been visited

This may not be true.

If the graph is disconnected then *isEdge()* on line 46 is insufficient ...

• ... there will be no edges to a disconnected part of the graph

We need to also check that every vertex has been visited before we return from the function

This involves:

- 1. looking for a vertex in *visited[]* that is -1
 - this vertex has not yet been visited before
- 2. push this vertex onto the stack
- 3. start a new traversal with this node as 'root'

The code of the 'disconnected version' of *dfsQuack()* is as follows:

dfsQuack() (disconnected graphs)

```
切换行号显示
  1 // HANDLES DISCONNECTED GRAPHS
  2 void dfsQuack(Graph q, Vertex rootv, int numV) {
       int *visited = mallocArray(numV);
        Quack s = createQuack();
       push(rootv, s);
       showQuack(s);
        int order = 0;
        int allVis = 0;
                                // as long as there are unvisited
  9
       while (!allVis) {
vertices
 10
           while (!isEmptyQuack(s)) {
  11
              Vertex v = pop(s);
              if (visited[v] == UNVISITED) {
                 printArray("Visited: ", visited, numV); // debug
  13
                 visited[v] = order++;
                 for (Vertex w = numV - 1; w >= 0; w--) {
  15
  16
                    if (isEdge(newEdge(v,w), g)) {
  17
                       push (w, s);
  18
  19
  20
  21
              showQuack(s);
  22
  23
           // stack is empty, but are we finished?
  24
           allVis = 1;
  25
           for (Vertex w = 0; w < numV && allVis; w++) {</pre>
  26
              if (visited[w] == UNVISITED) {
  27
                 printf("Graph is DISCONNECTED\n"); // debug
  28
                 allVis = 0; // found an unvisited vertex
  29
                 push(w, s);
                                // push vertex onto stack
```

The helper ADT IOmem

Input/output and memory management is controlled by an ADT called **IOmem**. It's interface is:

This ADT allows the amount of graph search code to be kept minimal.

We can now compile the graph search algorithm with the Graph, Quack and IOmem ADTs:

• we can either the *GraphAM* or *GraphAL* ADTs

```
dcc dfsStack.c IOmem.c GraphAM.c Quack.c

or

dcc dfsStack.c IOmem.c GraphAL.c Quack.c
```

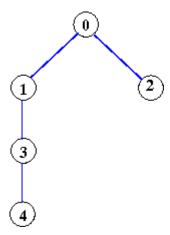
- also a choice between the array-based ADT *Quack* and linked-list version *QuackLL*
- in total, 4 combinations of *Graph* and *Quack* ADTs possible!

Test 1

The input file we use is:

```
#5
0 1 0 2 1 3 3 4
```

which corresponds to the simple graph we saw before:



Executing *a.out* using this input file results in the following:

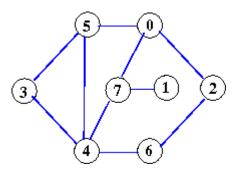
```
V=5, E=4
<0 1> <0 2>
<1 0> <1 3>
<2 0>
<3 1> <3 4>
<4 3>
Quack: <<0>>
Visited: {-1, -1, -1, -1}
Quack: <<1, 2>>
Visited: {0, -1, -1, -1, -1}
Quack: <<0, 3, 2>>
Quack: <<3, 2>>
Visited: \{0, 1, -1, -1, -1\}
Quack: <<1, 4, 2>>
Quack: <<4, 2>>
Visited: \{0, 1, -1, 2, -1\}
Quack: <<3, 2>>
Quack: <<2>>
Visited: \{0, 1, -1, 2, 3\}
Quack: <<0>>
Ouack: << >>
Visited: {0, 1, 4, 2, 3}
```

Here we see:

- the starting vertex 0 is pushed
- 0 is popped and its neighbours 1 and 2 are pushed
 - visited $[0] = \mathbf{0}$
- 1 is popped and its neighbours 0 and 3 are pushed
 - \circ visited[1] = 1
- 0 is popped and ignored as it is in array visited
- 3 is popped and its neighbours 1 and 4 are pushed
 - \circ visited[3] = 2
- 1 is popped and is ignored
- 4 is popped and its neighbour 3 is pushed
 - \circ visited[4] = 3
- 3 is popped and is ignored
- 2 is popped and its neighbour 0 is pushed
 - \circ visited[2] = 4
- 0 is popped
- quack is empty

Test 2

What about a more substantial graph:



It is represented by the input data:

```
#8
0 2 0 5 0 7 2 6 1 7 4 7 4 6 4 3 3 5 4 5
```

If we want to do a DFS starting from vertex 0 (remember: a #define in the code):

```
V=8, E=10
<0 2> <0 5> <0 7>
<1 7>
<2 0> <2 6>
<3 4> <3 5>
<4 3> <4 5> <4 6> <4 7>
<5 0> <5 3> <5 4>
<6 2> <6 4>
<7 0> <7 1> <7 4>
Quack: <<0>>
Visited: \{-1, -1, -1, -1, -1, -1, -1, -1\}
Quack: <<2, 5, 7>>
Visited: {0, -1, -1, -1, -1, -1, -1, -1}
Quack: <<0, 6, 5, 7>>
Quack: <<6, 5, 7>>
Visited: {0, -1, 1, -1, -1, -1, -1, -1}
Quack: <<2, 4, 5, 7>>
Quack: <<4, 5, 7>>
Visited: \{0, -1, 1, -1, -1, -1, 2, -1\}
Quack: <<3, 5, 6, 7, 5, 7>>
Visited: {0, -1, 1, -1, 3, -1, 2, -1}
Quack: <<4, 5, 5, 6, 7, 5, 7>>
Quack: <<5, 5, 6, 7, 5, 7>>
Visited: {0, -1, 1, 4, 3, -1, 2, -1}
Quack: <<0, 3, 4, 5, 6, 7, 5, 7>>
Quack: <<3, 4, 5, 6, 7, 5, 7>>
Quack: <<4, 5, 6, 7, 5, 7>>
Quack: <<5, 6, 7, 5, 7>>
Quack: <<6, 7, 5, 7>>
Quack: <<7, 5, 7>>
Visited: \{0, -1, 1, 4, 3, 5, 2, -1\}
Quack: <<0, 1, 4, 5, 7>>
Quack: <<1, 4, 5, 7>>
Visited: {0, -1, 1, 4, 3, 5, 2, 6}
Quack: <<7, 4, 5, 7>>
Quack: <<4, 5, 7>>
Quack: <<5, 7>>
Quack: <<7>>
Quack: << >>
Visited: {0, 7, 1, 4, 3, 5, 2, 6}
```

Test 3: a disconnected graph

The third test is a disconnected graph *exdiscon.inp*:

```
#6
0 1 0 2
1 2
3 4 3 5
4 5
```

In essence, this graph consists of 2 subgraphs, which are triangles.

Executing *a.out* using this input file results in the following:

```
V=6, E=6
<0 1> <0 2>
<1 0> <1 2>
<2 0> <2 1>
<3 4> <3 5>
<4 3> <4 5>
<5 3> <5 4>
Ouack: <<0>>>
Visited: \{-1, -1, -1, -1, -1, -1\}
Quack: <<1, 2>>
Visited: {0, -1, -1, -1, -1, -1}
Quack: <<0, 2, 2>>
Quack: <<2, 2>>
Visited: {0, 1, -1, -1, -1, -1}
Quack: <<0, 1, 2>>
Quack: <<1, 2>>
Quack: <<2>>
Quack: << >>
Graph is disconnected
Quack: <<3>>
Visited: \{0, 1, 2, -1, -1, -1\}
Quack: <<4, 5>>
Visited: \{0, 1, 2, 3, -1, -1\}
Quack: <<3, 5, 5>>
Quack: <<5, 5>>
Visited: \{0, 1, 2, 3, 4, -1\}
Quack: <<3, 4, 5>>
Quack: <<4, 5>>
Quack: <<5>>
Quack: << >>
Visited: {0, 1, 2, 3, 4, 5}
```

Notice that after traversing the first 'triangle', the program detects the program is disconnected.

• it then starts at the lowest unvisited vertex (3) and traverses the second triangle.

Performance

- number of pushes and pops
 - should be the same (stack is empty at the end)
- number of pushes of a vertex v = vertex degree of v
- total number of pushes
 - = sum of all the vertex degrees of vertices v in the graph

```
The sum of vertex degrees is equal to twice the number of edges.
```

- this means the complexity is linear in the number of edges, O(E)
 - o what does this mean? ...
 - how many edges are there?

- the worst case is a dense graph: E = V*(V-1)/2
- so the complexity is quadratic in V: i.e. $O(V^2)$
- if it is sparse, then it will be less than quadratic
- often said that DFS is linear in the size of the graph ...
 - ... where 'size' is the number of edges
 - ... which is another way of saying quadratic in the number of vertices

Recursive Depth-First Search

DFS above used our own stack to 'remember' which path it was traversing and do backtracking.

The system also has a stack, called a call stack, which is used to execute functions

- a function call causes a *function frame* to be pushed onto the call stack
 - ... upon a function return, the *frame* is popped off the call stack

This works even for recursive functions of course.

The call stack can be used instead of the 'stack' ADT we used above

• so when we compile we do not need the ADT quack

It works by recursion:

- a function dfsR() calls itself recursively ...
- in essence adjacent vertices are being *pushed* onto the system 'call' stack
 - the for-loop in dfsR() is over all all unvisited adjacent vertices
 - in the *for-loop*, *dfsR()* is called for every vertex
 - these calls *stack up* as you descend down the tree

dfsRec.c (disconnected graphs)

```
切换行号显示
   1 // dfsRec.c: traverse a graph using DFS (graph may be
disconnected)
  2 // Compile using:
             dcc -o dfsRec dfsRec.c IOmem.c GraphAM.c
   3 //
   4 //
   5 #include <stdio.h>
   6 #include <stdlib.h>
  7 #include "Graph.h"
  8 #include "IOmem.h"
  10 #define START 0 // the start vertex
  11
  12 void dfs (Graph, Vertex, int);
  13 void dfsR(Graph, Vertex, int, int *, int *);
  14
  15 int main(void) {
  16 int numV;
       if ((numV = readNumV()) >= 0) {
  17
  1.8
           Graph g = newGraph (numV);
  19
           if (readBuildGraph(g)) {
  20
               showGraph(g);
               dfs(g, START, numV); // DEPTH-FIRST SEARCH FROM START
  21
  22
  23
            g = freeGraph(g);
```

```
g = NULL;
  24
  25
       else {
  26
  27
        return EXIT_FAILURE;
  28
  29
       return EXIT_SUCCESS;
  30 }
  31
  32 void dfs(Graph g, Vertex rootv, int numV) {//'wrapper' for
recursive dfs
       int *visited = mallocArray(numV); // ... handles disconnected
graphs
  34
       int order = 0;
  35
       Vertex startv = rootv;
                                          // this is the starting
vertex
  36 int allVis = 0;
                                          // assume not all visited
  37
      while (!allVis) {
                                           // as long as there are
vertices
  38
          dfsR(g, startv, numV, &order, visited);
  39
          allVis = 1;
                                          // are all visited now?
 40
          for (Vertex w = 0; w < numV && allVis; w++) { // look for</pre>
more
41
42
43
44
45
             if (visited[w] == UNVISITED) {
                printf("Graph is disconnected\n"); // debug
                allVis = 0; // found an unvisited vertex startv = w; // next loop dfsR this vertex
             }
  47
      }
       printArray("Visited: ", visited, numV);
  48
  49
       free (visited);
  50
       return;
  51 }
  52
  53 void dfsR(Graph g, Vertex v, int numV, int *order, int *visited) {
       visited[v] = *order;
  54
                                           // records the order of
visit
  55
       *order = *order+1;
  56
      for (Vertex w = 0; w < numV; w++) {
  57
       if (isEdge(newEdge(v,w), g) && visited[w]==UNVISITED) {
  58
             dfsR(g, w, numV, order, visited);
  59
      }
  60
  61
       return;
  62 }
```

Here the function *dfs()* is called by *main()*

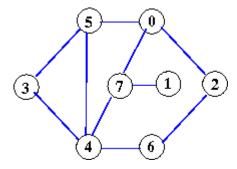
- this function is a wrapper
- it does 'housekeeping' (initialising *order* and the array *visited*)
- it calls the recursive function *dfsR()*

Remember: in the stack version the main function called *dfsQuack()*

- it does 'housekeeping' (initialising *order* and the array *visited*)
- pops and pushes off/on the quack until the quack is empty

Test 1

Let's run this recursive DFS on the graph we had above:



Remember, it is represented by the input data:

```
#8
0 2 0 5 0 7 2 6 1 7 4 7 4 6 4 3 3 5 4 5
```

Compiling:

```
dcc -o dfsRec dfsRec.c IOmem.c GraphAM.c
```

notice, no Quack ADT, and executing

```
V=8, E=10
<0 2> <0 5> <0 7>
<1 7>
<2 0> <2 6>
<3 4> <3 5>
<4 3> <4 5> <4 6> <4 7>
<5 0> <5 3> <5 4>
<6 2> <6 4>
<7 0> <7 1> <7 4>
Visiting vertex 0 in order 0
Visiting vertex 2 in order 1
Visiting vertex 6 in order 2
Visiting vertex 4 in order 3
Visiting vertex 3 in order 4
Visiting vertex 5 in order 5
Visiting vertex 7 in order 6
Visiting vertex 1 in order 7
Visited: {0, 7, 1, 4, 3, 5, 2, 6}
```

Comparing that with the stack version, the last lines are shown again below:

```
.
.
Visited: {0, -1, 1, 4, 3, 5, 2, 6}
Quack: <<7, 4, 5, 7>>
Quack: <<4, 5, 7>>
Quack: <<5, 7>>
Quack: <<7>>
Quack: <<7>>
Visited: {0, 7, 1, 4, 3, 5, 2, 6}
```

In summary:

- we've seen 2 versions of depth-first search:
 - an explicit stack version dfsStack.c that uses a Quack ADT
 - a call-stack version *dfsRec.c* that uses recursion

You could argue that the stack version:

- requires much less system resources (no recursion)
- does backtracking in an iterative manner, so will be much faster

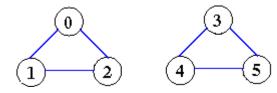
Test 2: a disconnected graph

We saw in dfsRec.c that the recursion handles disconnected graphs

Let's check that.

```
#6
0 1 0 2 1 2 3 4 3 5 4 5
```

corresponding to:



and assuming the starting vertex is 0, then *dfsRec* produces:

```
V=6, E=6
<0 1> <0 2>
<1 0> <1 2>
<2 0> <2 1>
<3 4> <3 5>
<4 3> <4 5>
<5 3> <5 4>

Visiting vertex 0 in order 0
Visiting vertex 1 in order 1
Visiting vertex 2 in order 2
Graph is disconnected
Visiting vertex 3 in order 3
Visiting vertex 4 in order 4
Visiting vertex 5 in order 5
Visited: {0, 1, 2, 3, 4, 5}
```

Notice:

- the first (sub) graph's DFS search begins at vertex 0
- the second (sub) graph's DFS search begins at vertex 3

Global variables

Crucial in both versions is the array visited[] and integer variable order

- *visited[]* records unvisited vertices and the *order* of visiting
- stop cycles occurring (remember, we are dealing with graphs)

In dfsRec.c:

- *visited[]* and *order* are initialised in the 'wrapper'
- are parameters to the recursive call
 - a vertex is visited on every call so they will change every call

```
切换行号显示

1 void dfsR(Graph g, Vertex v, int numV, int *order, int *visited) {
```

It is easier to implement them as global variables (most people do this)

• ... don't need to pass them to dfsR()

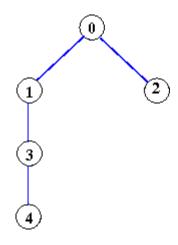
GraphSearchDFSglobal

Breadth First Search

All adjacent vertices are visited before moving to another vertex

• each level of vertices is visited before the next level's vertices are considered

For example:



- 1. visit vertex 0
- 2. visit vertex 1 and 2
- 3. visit vertex 3
- 4. visit vertex 4

In essence, the vertices are processed *in order* (top to bottom, left to right)

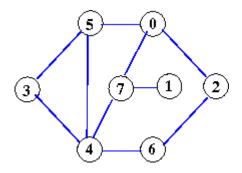
- DFS used a stack:
 - we *push* all the adjacent vertices of a vertex onto a stack
 - we pop off the top until the stack is empty (this allows backtracking)
 - vertices are being pushed and popped off the 'same place'
- BFS instead uses a queue:
 - we *qush* all the adjacent vertices onto a queue (not a stack)
 - ... so they get added to the bottom
 - we *pop* off the top
 - all adjacent vertices are handled 'together'
- the change from stack to queue is almost trivial:
 - just 4 changes

bfsQuack() (connected)

切换行号显示

```
1 void bfsQuack(Graph g, Vertex v, int numV) { //name change
     int *visited = mallocArray(numV);
 3
      Quack q = createQuack();
 4
      qush(v, q);
                                                //qush, not push
 5
      showQuack(q);
 6
      int order = 0;
7
      while (!isEmptyQuack(q)) {
8
         v = pop(q);
         if (visited[v] == UNVISITED) {
9
10
            printf("Visit %d\n", v); // debug
11
            visited[v] = order++;
12
            for (Vertex w = 0; w < numV; w++) {//vertex order</pre>
13
               if (isEdge(newEdge(v,w), g)) {
14
                   qush(w, q);
                                                 //qush, not push
15
16
17
18
         showQuack(q);
19
      printArray("Visited: ", visited, numV);
20
21
      free (visited);
22
      makeEmptyQuack(q);
23
      return;
24 }
```

Test it using the graph:



This is the file *exsedg.inp*.

```
#8
0 2 0 5 0 7 2 6 1 7 4 7 4 6 4 3 3 5 4 5
```

Compile and execute:

```
dcc bfsQueue.c IOmem.c GraphAM.c Quack.c
./a.out < exsedg.inp
Quack: <<0>>
Visit 0
Quack: <<2, 5, 7>>
                            <=== 2, 5, 7  qushed
Visit 2
Quack: <<5, 7, 0, 6>>
                              <===0,6 qushed
Visit 5
Quack: <<7, 0, 6, 0, 3, 4>>
                                <=== 0,3,4 \text{ qushed}
Visit 7
Quack: <<0, 6, 0, 3, 4, 0, 1, 4>> <==== 0,1,4, qushed
Quack: <<6, 0, 3, 4, 0, 1, 4>>
Visit 6
Quack: <<0, 3, 4, 0, 1, 4, 2, 4>>
Quack: <<3, 4, 0, 1, 4, 2, 4>>
Visit 3
Quack: <<4, 0, 1, 4, 2, 4, 4, 5>>
Visit 4
Quack: <<0, 1, 4, 2, 4, 4, 5, 3, 5, 6, 7>>
```

```
Quack: <<1, 4, 2, 4, 4, 5, 3, 5, 6, 7>>
Visit 1
Quack: <<4, 2, 4, 4, 5, 3, 5, 6, 7, 7>>
Quack: <<2, 4, 4, 5, 3, 5, 6, 7, 7>>
Quack: <<4, 4, 5, 3, 5, 6, 7, 7>>
Quack: <<4, 5, 3, 5, 6, 7, 7>>
Quack: <<4, 5, 3, 5, 6, 7, 7>>
Quack: <<5, 3, 5, 6, 7, 7>>
Quack: <<5, 3, 5, 6, 7, 7>>
Quack: <<5, 6, 7, 7>>
Quack: <<5, 6, 7, 7>>
Quack: <<7, 7>>
Quack: <<7, 7>>
Quack: <<7, 7>>
Quack: <<7>>
Quack: <<7>>
Visited: {0, 7, 1, 5, 6, 2, 4, 3}
```

Note:

- 0 is a level-0 vertex
- 2 5 7 are level-1
- 6 3 4 1 are level-2

DFS generated the following:

• $Visited[] = \{0, 7, 1, 4, 3, 5, 2, 6\}$

GraphSearch (2019-07-25 17:36:42由AlbertNymeyer编辑)