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HATRICOLA: 334279
 A^{-1} = \frac{1}{141} \cdot A^{+} A^{*} = [C_{\pi \epsilon}] rc(A) = dim(R(A)) = dim(C(A))
 U4. U2 = { v 6 V 1 v = U4. U2, U4 & U4, U2 & U2} dim (U+W) = dim (U) + dim (W) - olim (UAW)
V = \bigoplus U_i \implies V = \sum U_i , \ U_k \wedge U_{\widehat{k}} = \{ \widehat{o} \} \qquad A = [u_{i|B} \mid ... \mid U_{n|B}] \rightarrow X = \sum t_i A_{c(i)} \rightarrow [A|x] \rightarrow [S|x']
In(f) ~ C(F) Ker(f) ~ Ker(F) K(f)- dim(Ker(f))

FIB<sub>ν</sub>B<sub>ω</sub> = [f(ν<sub>1</sub>)<sub>|B<sub>ω</sub></sub>|...|f(ν<sub>n</sub>)<sub>|Bω</sub>] dim(ν) = ε(f) + K(f)
                                                                                                                                                                 rc(f)= dim (1m(f))
                                                                                                                                                                 inist. e(f)= dim(V)
MB-B'=[ VAIB' | ... | VaIB'] MB-B" MB-B"
                                                                                                                                                                 sured r (f). dim(w)
VIB' = MB-3B' · VIB FIB'B' = MB-3B' · FIB-B · MB' -B.
                                                                                                                                                                 lin. re(f)= dim(v)=
 FLBV = MBY -BV FIBV MBY -BV
                                                                                                                                                                                        = dim(w)
 AB= OB- OA - BIR - AIR A [ U4 | B | ... | Unis] X= QIR + SECAC → [AIx-QIR] → [>IX]
 // \pi(\tilde{A}|\tilde{B})^{\frac{1}{2}}\pi(\tilde{A}) = n-q
\times \pi(\tilde{A}|\tilde{B}) = \pi(\tilde{A}) \times n-q \quad \left[\tilde{A}|\tilde{B}\right] = \begin{bmatrix} A & B \\ A' & B \end{bmatrix} \quad \left[A(B) \rightarrow \pi a \mu \mu. \text{ alg di } S, \quad p = \dim(S) \\ A & \mu = \pi a \mu. \text{ alg di } T, \quad q = \dim(T) \\ n = \dim(A) \quad n = \dim(A) \quad n = \dim(A)
A simile \alpha \in B se \exists S : A = S^{*}B \cdot S, A simile \alpha \in B se hanno automore coincidenti
 ngh.π(Ã/B)>π(Ã)>n-q
 A remile a B - R (A) = R(B), Br(A) = Br(B), IAI = IBI, PA(X) = PB(X) ( readice e confliciente )
V<sub>λ</sub>= Ker (A-λI) P<sub>A</sub> (λ)= (A-λI ) → C<sub>O</sub>= (Al, C<sub>n-4</sub>= (-1)<sup>n-4</sup> Gr(A), C<sub>n</sub>= (-1)<sup>n</sup>
 <u, V> = U 18 · VIB < A, B> = Gr (AT. B) < X, Y> = x 18 · GIB · YIB GIV=[ < U1, U2 >] GIB · A 18 · GIB · MES
\|U \cdot v\|_{*}^{\frac{1}{2}} \|v\|^{\frac{1}{2}} + \|v\|^{\frac{1}{2}} + \frac{2}{2} \langle v, v \rangle
U^{\perp} = \left\{ v \in V \mid \langle v, v \rangle \cdot o \right\} \qquad \rho_{U}(v) = \sum_{i=1}^{\frac{2}{2}} \frac{\langle v, u_{i} \rangle}{\|v_{i}\|^{2}} v_{i} \rightarrow \sigma_{*} \sum_{i=1}^{\frac{2}{2}} \frac{\langle v, v_{i} \rangle}{\|v_{i}\|^{2}} v_{i}

⟨ V, U @ W >= ⟨ \( \frac{\w}{\omega}, \omega \end{array} \) \( U, \end{array} \) (\( U_1 \end{array}, \omega_3 \)) = ⟨ \( U_1 \omega \unders_3 \) \( U_2 \omega \unders_3 \) \( U_4 \omega \unders_3 \unders_3 \) \( U_4 \omega \unders_3 \und
 f \in End(v), construit \rightarrow f \in O(v) O(GL(v)) O(n; \mathbb{R}) \sim O(v) Q \in O(n; \mathbb{R}) \subset Q \cdot Q^{\frac{1}{2}} I (191-24)
 3L = {AeGL(n; K) | |A|=1} -> SO=SLAO -> SO(n; R)~SO(v), SO(v) - ral.
 se: { f= Idv V=v } f=-Idv V=v } |l|=1, f= Idv => dim(V,)=1 1 mude in Vi di Bro(f)=1+2 cos+
       [16] -1. Lo-Idv => dim (V_)=1 1 nitate lungo V_ 1 nucle in Vide Exc(f)=-1. 2000
 se: 161=14 => ruda di cos «= { Bech) } 161=14 => rifulle lungo V.
 1 di 1 se < fcvs. w>w = < fcvs. v>v F = F = 5 [m(4) = Korlf =) ] Jun(1 = Korlf) = Korlf) = Korlf)
 re 1+= 1 li autoagginto => 16 S(v) S(v) ~ S(n: R)
 fi ort. diag. ne 3060(n, R): D=Q*.F.Q Interde: fi outoaggiinta ne e solo se fi ort. diagon.
 S. T. milioporei: d(3,T)= \( \frac{G(\nu_1,...,\nu_n,\alpha \)}{G(\nu_1,...,\nu_n)} \) con \( \left(\nu_1,...,\nu_n \right) \) loss di U+W, PES, QET
   X = \int d(s,\tau) = 0   (s,\tau) = d(s,\tau) = d(s,\tau)   (s,\tau) = d(s,\tau)   (s,\tau) = d(s,\tau)
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r(C)	r(A)	$I_3$	$I_2$	$I_1I_3$	Forma canonica	Moduli	Nome	\[ \sum_{\text{tot}} \alpha_{ij} \x_i^2 + 2 \sum_{\text{tot}} \sum_{\text{tot}} \x_{ij} \x_{ij
- 3	2	$\neq 0$	> 0	< 0	$\frac{\tilde{x}^2}{\alpha^2} + \frac{\tilde{y}^2}{\beta^2} = 1$	$\alpha, \beta > 0$	Ellisse con punti reali	
3	2	$\neq 0$	> 0	> 0	$\frac{\tilde{x}^2}{\alpha^2} + \frac{\tilde{y}^2}{\beta^2} = -1$	$\alpha, \beta > 0$	$Ellisse\ privo\ di\ punti\ reali$	$ \begin{array}{c ccccc} A & a_{ii} & a_{ij} & B & b_i \\ \vdots & \vdots & \vdots \\ a_{pi} & a_{pq} & \vdots \\ \end{array} $ $ \begin{array}{c ccccc} B & b \\ \vdots \\ b_n \end{array} $ $ \begin{array}{c cccc} C & B \\ \hline B^T & C \end{array} $
3	2	$\neq 0$	< 0		$\frac{\tilde{x}^2}{\alpha^2} - \frac{\tilde{y}^2}{\beta^2} = 1$	$\alpha, \beta > 0$	Iperbole	
3	1	$\neq 0$	=0		$\tilde{x}^2 - 2\rho \tilde{y} = 0$	$\rho > 0$	Parabola	[azi ann ] [bn] [B' C]
2	2	= 0	> 0	= 0	$\frac{\tilde{x}^2}{\alpha^2} + \tilde{y}^2 = 0$	$\alpha > 0$	Coppia di rette incidenti con un unico punto reale	X-A-x + 2B-x+c=0
2	2	= 0	< 0	= 0	$\frac{\tilde{x}^2}{\alpha^2} - \tilde{y}^2 = 0$	$\alpha > 0$	Coppia di rette incidenti con infiniti punti reali	$Y^{\dagger} \cdot C \cdot Y = 0  \left(Y_{2} \left[\frac{x}{4}\right]\right)$
					~2		Coppia di rette parallele	$\widetilde{A} = Q^T \cdot A \cdot Q  \widehat{B} = Q^T (A \cdot T + B)$
2	1	=0	=0	= 0	$\frac{\tilde{x}^2}{\alpha^2} = 1$	$\alpha > 0$	con infiniti punti reali	
2	1	= 0	= 0	= 0	$\frac{\tilde{x}^2}{\alpha^2} = -1$	$\alpha > 0$	Coppia di rette parallele prive di punti reali	$\widehat{C} = T^{T} \cdot A \cdot T + 2B^{T} \cdot T + C$ $F \cdot \left[ \begin{array}{c} a & T \\ \hline & \bullet \\ \end{array} \right] \rightarrow \widehat{C} = F^{T} \cdot C \cdot F$
1	1	= 0	= 0	= 0	$\tilde{x}^2 = 0$		Retta doppia	
r(C)	r(A)	$I_4$ $I$	_	_	Forma canonica	Moduli	Nome	r(A)= r(A) , r(C)= r(E)
4		< 0   ≠	_	_	-2 ~2 =2	$\alpha, \beta, \gamma > 0$	Ellissoide con punti reali	0 (1) 0 (2) 101 121
4	3	> 0   \neq	0 >	0 < 0	$\frac{\tilde{x}^2}{\alpha^2} + \frac{\tilde{y}^2}{\beta^2} + \frac{\tilde{z}^2}{\gamma^2} = -1$	$\alpha, \beta, \gamma > 0$	Ellissoide privo di punti reali	$P_{A}(\lambda) = P_{X}(\lambda)$ , $ C  =  C $
4	3 :	> 0 \( \neq \)		0 ≥ 0	$\frac{\tilde{x}^2}{\alpha^2} + \frac{\tilde{y}^2}{\beta^2} - \frac{\tilde{z}^2}{\gamma^2} = 1$	$\alpha, \beta, \gamma > 0$	Iperboloide ad una falda od iperbolico	iv E2: I4 = En (A) Is 1C1
4	_	< 0 \ \neq		0 \le 0	$\frac{\tilde{x}^2}{\alpha^2} - \frac{\tilde{y}^2}{\beta^2} - \frac{\tilde{z}^2}{\gamma^2} = 1$	$\alpha, \beta, \gamma > 0$	Iperboloide a due falde	I2=  Al
4	_	$< 0 \neq 0$			$\frac{\tilde{x}^2}{\alpha^2} + \tilde{y}^2 - 2\rho \tilde{z} = 0$	$\alpha, \rho > 0$	od ellittico  Paraboloide ellittico	
4		> 0 =		0 = 0	$\frac{\tilde{x}^2}{\alpha^2} - \tilde{y}^2 - 2\rho \tilde{z} = 0$	$\alpha, \rho > 0$	Paraboloide iperbolico	iv 1E3: I4= Bro(A) I3= IAI
3	3 =	= 0   ≠	0 >	0 <	$\frac{\tilde{x}^2}{\alpha^2} + \frac{\tilde{y}^2}{\beta^2} + \tilde{z}^2 = 0$	$\alpha, \beta > 0$	Cono con un unico punto reale	$I_2 = I_2(P_A)$ $I_4 =  C $
3	_	= 0 ≠		_	$\frac{\tilde{x}^2}{\alpha^2} + \frac{\tilde{y}^2}{\beta^2} - \tilde{z}^2 = 0$	$\alpha, \beta > 0$	Cono con infiniti	λ <sub>4</sub> x <sub>4</sub> + ··· + λη x <sub>η</sub> = O π(c) = π(A)
3	3 =	= 0   ≠	0	≤ 0			punti reali Cilindro ellittico	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
_ 3	2 =	= 0   =	0 >	0 = 0	$\frac{\tilde{x}^2}{\alpha^2} + \frac{\tilde{y}^2}{\beta^2} = 1$	$\alpha, \beta > 0$	con punti reali	
3	2 =	= 0 =	0 >	0 = 0	$\frac{\tilde{x}^2}{\alpha^2} + \frac{\tilde{y}^2}{\beta^2} = -1$	$\alpha, \beta > 0$	Cilindro ellittico	(λ, x, + ···· λ, x, + 2ρ X, = ο π(c) - ε(A) · 2
3	2 =	= 0 =	0 <		-2 -2	$\alpha, \beta > 0$	privo di punti reali	[0 Lan. (1
3	_	= 0 =	_	_		$\rho > 0$	Cilindro iperbolico  Cilindro parabolico	
2		= 0 =			$\frac{\tilde{x}^2}{a^2} + \tilde{y}^2 = 0$	$\alpha > 0$	Coppia di piani incidenti	$ \begin{bmatrix} \lambda_{1} & 0 & 0 \\ \vdots & \lambda_{k} & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} \lambda_{1} & 0 & 0 & 0 \\ \vdots & \ddots & \vdots & \vdots \\ 0 & \dots & \lambda_{k} & 0 \\ 0 & \dots & 0 & P \end{bmatrix} $
		- 0   -	0 /	3 - 0	$\frac{\alpha^2 + y}{\alpha^2} = 0$	a > 0	con una retta di punti reali	
2	2 =	= 0 =	0 <	0 = 0	$\frac{\tilde{x}^2}{\alpha^2} - \tilde{y}^2 = 0$	$\alpha > 0$	Coppia di piani incidenti con infiniti punti reali	[6016]
2	1 =	= 0 =	0 =	0 = 0	$\tilde{x}^2$ 1	- > 0	Coppia di piani paralleli	[6,9, 10]
	1 =	= 0   =	0 = 1	J = 0	$\frac{\tilde{x}^2}{\alpha^2} = 1$	$\alpha > 0$	con infiniti punti reali	$x = Q \cdot \tilde{x} + \tau $
2	1 =	= 0 =	0 =	0 = 0	$\frac{\tilde{x}^2}{\alpha^2} = -1$	$\alpha > 0$	Coppia di piani paralleli privi di punti reali	
1	1 =	= 0 =	0 =	0 = 0	$\tilde{x}^2 = 0$		Piano doppio	hasha => restaurant
4.				7			070	C: [AI-B]
47	<b>Q</b> ₄ .	A C	יעו : פיז.	= Q4 ·	AQ, => A4	, D <sub>4</sub>	= W . B , C,=C	
2)	т. •	۷-۱	<u> </u>	1	siet _ A.	= A. B.	= A <sub>1</sub> · T <sub>2</sub> + B <sub>1</sub> , C = - \( \frac{\pi}{4} \)	$-\frac{v_{0}}{Ai} - c_{1}  \pi_{i}  X = C + t \vee_{n}  (v_{n}  a.v  d: A)$
			^		-> - +4 £ ( £ M		1,	
	ſ	_	l Ra					
3)	a, L	Д,е	而	.ii <sub>e</sub> H	4 Hh.n.4] =	A - Q	ALQ3 , B3 QT BL , C3	, • C2
						5 <sub>3</sub> = D4 ,	C4=0 ! P=   B1 p	
Ly	Q= (	Q <sub>4</sub> . Q	3	T = G	14(Qs·T4+T2)			
ROT. NUTORNO AD ASSE CILINDRO GEN. DA J / a R: COUO CON DIR. 8								
KOT	. NUT	URN(	AD	- A3	Dea Peir3	Sac.	x QeX	$\begin{cases} P_0 \in \mathcal{O} \\ \overline{VP} = \varepsilon \overline{VP_0} \end{cases}$
)	٠.	,		,	, , , , ,	1.	1, 1	10000
	11 00	: II =	II ÕP	เก้	) die aue	( e'	a // re passante per	Poex, PelE3 velE3
μ,	۷, ۵	QP > :	0		D E DANG	(th	mmo w-cho, ye, to) &	( T)
					y,, e,,)			( etimino Po = (xo, yo, zo) + t)
		-			•			