Parameter Minimization using the Levenberg-Marquardt algorithm

Do some fitting

1.1 Introduction

The Levenberg-Marquardt plugin is used to fit a SBML models parameters to experimental data.

The plugin has numerous properties to allow the user full control over the internal fitting engine, as well as access to generated fitted data after a minimization session. In addition, various statistical properties, such as standardized residuals, Q-Q data, ChiSquare and reduced ChiSquare are made accessible to the user. The resulting parameter values do also come with estimated confidence limits.

The current implementation is based on the lmfit C library by Joachim Wuttke¹.

Plugin properties are documented in the next section.

¹The package lmfit is distributed under the FreeBSD License:

⁻ Copyright (c) 2013 Joachim Wuttke All rights reserved. -

1.2 Plugin Properties

Available properties in the Levenberg-Marquardt plugin are listed in the table below.

Property Name	Data Type	Default Value	Description
SBML	string	N/A	SBML document as a string. Model to be used in the
			fitting.
ExperimentalData	telluriumData	N/A	Input data.
${\bf FittedData}$	telluriumData	N/A	Output data.
Input Parameter List	listOfProperties	N/A	Parameters to fit.
${\bf Output Parameter List}$	listOfProperties	N/A	List of fitted parameters.
Experimental-	stringList	N/A	Species selection list for experimental data.
DataSelectionList			
${\bf Fitted Data Selection Lis}$	st stringList	N/A	Selection list for model data.
Norm	double	N/A	Norm of fitting. An estimate of goodness of fit.
Norms	telluriumData	N/A	The norm is calculated throughout a fitting session.
			Each Norm value is stored in the Norms (read-only)
			property.
ConfidenceLimits	listOfProperties	N/A	Confidence limits for each fitted parameter. The confi-
			dence limits are calculated at a 95% confidence level.
Hessian	matrix	N/A	Hessian matrix. The Hessian is calculated using approx-
			imation at a found parameter minimum.

CovarianceMatrix	matrix	N/A	Covariance matrix. Calculated as the inverse of the Hes-
			sian.
Residuals	telluriumData	N/A	Residuals data.
${\bf Standardized Residuals}$	telluriumData	N/A	Standardized Residuals.
NormalProb-	telluriumData	N/A	Normal Probability of Residuals.
${\it ability} Of Residuals$			
ChiSquare	double	N/A	The ChiSquare at the minimum.
${\bf Reduced Chi Square}$	double	N/A	The Reduced ChiSquare at the minimum.
${\bf Status Message}$	string	N/A	Message from the internal fitting engine, communicating
			the status of the obtained fit.
NrOfIter	int	N/A	Number of iterations.

The following properties are used internally by the fitting engine. They are preset with default values.

Depending on the minimization problem at hand, they may need to be tweaked.

ftol	double	machine dep.	Relative error desired in the sum of squares.
xtol	double	machine dep.	Relative error between last two approximations.
gtol	double	machine dep.	Orthogonality desired between fvec and its derivs.
epsilon	double	machine dep.	Step used to calculate the jacobian.
stepbound	double	100.0	Initial bound to steps in the outer loop.

patience	double	100	Used for setting maximum number of iterations, calcu-
			lated as patience*(nr_of_parameters +1).

Table 1.1: LM fit plugin parameters

1.3 Plugin Events 5

1.3 Plugin Events

The Levenberg-Marquardt plugin are using all of a plugins available plugin events, i.e. the *PluginStarted*, *PluginProgress* and the *PluginFinished* events.

The available data variables for each event are internally treated as *pass trough* variables, so any data, for any of the events, assigned prior to the plugins execute function (in the assingOn.. family of functions), can be retrieved unmodified in the corresponding event function.

Event	Arguments	Purpose and argument types
PluginStarted	void*, void*	Signal to application that the plugin has started.
		Both parameters are pass trough parameters and
		are unused internally by the plugin.
PluginProgress	void*, void*	Communicating progress of fitting. Both param-
		eters are <i>pass trough</i> parameters and are unused internally by the plugin.
PluginFinished	void* void*	Signals to application that execution of the plugin
r rugiiir iiiisiica	void , void	has finished. Both parameters are pass trough pa-
		rameters and are unused internally by the plugin.

Table 1.2: Plugin callbacks

1.4 Python example

The following Python script illustrate how the plugin can be used.

```
1
  from telplugins import *
3
  # Load Plugins
4
  chiPlugin
                 = Plugin("tel_chisquare")
                 = Plugin("tel_levenberg_marquardt")
5
                 = Plugin("tel_test_model")
   modelPlugin
7
   addNoisePlugin = Plugin("tel_add_noise")
8
9
      10
      def myEvent(dummy): #We are not capturing any data from the plugin, so
11
         just pass a dummy
          print 'Iteration, Norm = ' + 'lm.getProperty("NrOfIter")' + ', ' +
12
              'lm.getProperty("Norm")'
13
14
      #Setup progress event function
15
      progressEvent = NotifyEventEx(myEvent)
16
      assignOnProgressEvent(lm.plugin, progressEvent)
```

1.4 Python example

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```
#-----
17
18
19
       #Create model data, with and without noise using the test_model plugin
20
       modelPlugin.execute()
21
22
       #Setup lmfit properties.
23
       lm.SBML
                           = modelPlugin.Model
24
       lm.ExperimentalData = modelPlugin.TestDataWithNoise
25
26
       # Add the parameters that we're going to fit and an initial 'start'
          value
27
       lm.setProperty("InputParameterList", ["k1", .3])
       lm.setProperty("FittedDataSelectionList", "[S1] [S2]")
28
29
       lm.setProperty("ExperimentalDataSelectionList", "[S1] [S2]")
30
31
       # Start minimization
32
       lm.execute()
33
34
       print 'Minimization finished. \n==== Result ===='
       print 'Fit engine status: ' + 'lm.getProperty('StatusMessage')'
35
36
       print 'Hessian Matrix'
37
38
       print lm.getProperty("Hessian")
39
40
       print 'Covariance Matrix'
       print lm.getProperty("CovarianceMatrix")
41
42
                                      + 'lm.getProperty("ChiSquare")'
43
       print 'ChiSquare = '
44
       print 'Reduced ChiSquare = ' + 'lm.getProperty("ReducedChiSquare")'
45
46
       #This is a list of parameters
47
       parameters = tpc.getPluginProperty (lm.plugin, "OutputParameterList")
       confLimits = tpc.getPluginProperty (lm.plugin, "ConfidenceLimits")
48
49
50
       #Iterate trough list of parameters and confidence limits
51
       para = getFirstProperty(parameters)
52
       limit = getFirstProperty(confLimits)
53
       while para and limit:
           print getPropertyName(para) + ' = ' + 'getPropertyValue(para)' + '
54
              +/- ' + 'getPropertyValue(limit)'
55
           para = getNextProperty(parameters)
56
           limit = getNextProperty(confLimits)
57
58
59
       # Get the fitted and residual data
60
       fittedData = lm.getProperty ("FittedData").toNumpy
61
       residuals = lm.getProperty ("Residuals").toNumpy
62
63
       # Get the experimental data as a numpy array
       experimentalData = modelPlugin.TestDataWithNoise.toNumpy
64
65
                                         [:,[0,1]], "blue", "-",
66
       telplugins.plot(fittedData
          S1 Fitted")
       telplugins.plot(fittedData
                                          [:,[0,2]], "blue", "-",
67
          S2 Fitted")
```

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```
telplugins.plot(residuals
                                           [:,[0,1]], "blue", "None", "x",
68
          S1 Residual")
69
       telplugins.plot(residuals
                                           [:,[0,2]], "red", "None", "x",
          S2 Residual")
70
       telplugins.plot(experimentalData
                                           [:,[0,1]], "red", "",
          S1 Data")
                                           [:,[0,2]], "blue", "",
71
       telplugins.plot(experimentalData
          S2 Data")
72
       telplugins.plt.show()
73
   except Exception as e:
74
       print 'Problem.. ' + 'e'
75
```

Listing 1.1: Minimization example.

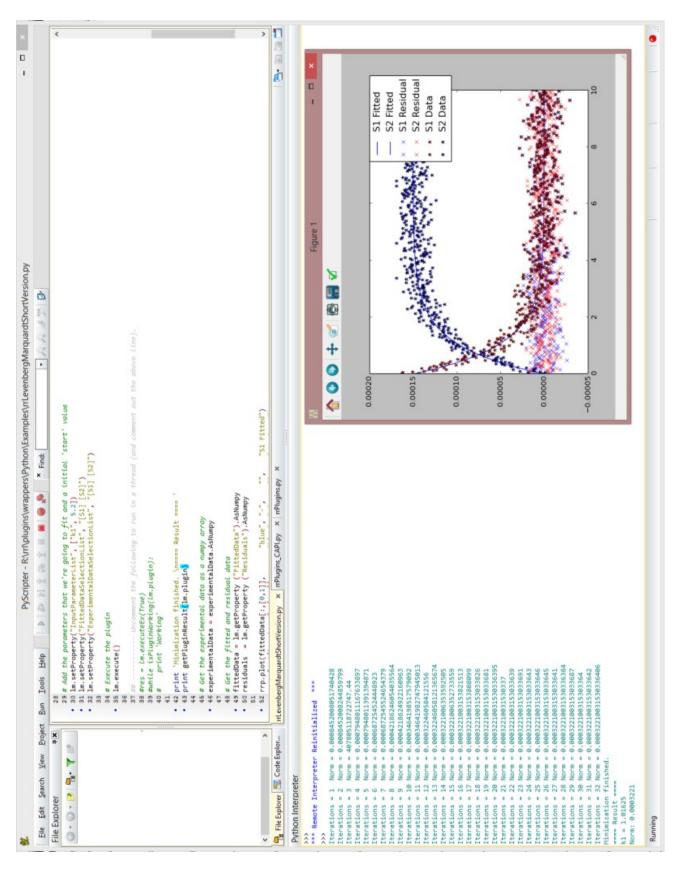


Figure 1.1: Typical output for the example script above.