

Program Optimization

CS 341: Intro. to Computer Architecture & Organization

Andree Jacobson

Today

Overview

- ▶ Generally Useful Optimizations
 - Code motion/precomputation
 - Strength reduction
 - Sharing of common subexpressions
 - Removing unnecessary procedure calls
- Optimization Blockers
 - Procedure calls
 - Memory aliasing
- > Exploiting Instruction-Level Parallelism
- Dealing with Conditionals

Performance Realities

- There's more to performance than asymptotic complexity
- Constant factors matter too!
 - Easily see 10:1 performance range depending on how code is written
 - Must optimize at multiple levels:
 - · algorithm, data representations, procedures, and loops
- Must understand system to optimize performance
 - How programs are compiled and executed
 - How to measure program performance and identify bottlenecks
- How to improve performance without destroying code modularity and generality

Optimizing Compilers

- ▶ Provide efficient mapping of program to machine
 - register allocation
 - code selection and ordering (scheduling)
 - dead code elimination
 - eliminating minor inefficiencies
- ▶ Don't (usually) improve asymptotic efficiency
 - up to programmer to select best overall algorithm
 - big-O savings are (often) more important than constant factors
 - · but constant factors also matter
- Have difficulty overcoming "optimization blockers"
 - potential memory aliasing
 - potential procedure side-effects

Limitations of Optimizing Compilers

- ▶ Operate under fundamental constraint
 - Must not cause any change in program behavior
 - Often prevents it from making optimizations when would only affect behavior under pathological conditions.
- Behavior that may be obvious to the programmer can be obfuscated by languages and coding styles
 - e.g., Data ranges may be more limited than variable types suggest
- ▶ Most analysis is performed only within procedures
 - · Whole-program analysis is too expensive in most cases
- ▶ Most analysis is based only on static information
 - Compiler has difficulty anticipating run-time inputs
- ▶ When in doubt, the compiler must be conservative

Generally Useful Optimizations

- Optimizations that you or the compiler should do regardless of processor / compiler
- Code Motion
 - Reduce frequency with which computation performed
 - · If it will always produce same result
 - · Especially moving code out of loop

Compiler-Generated Code Motion void set row (double *a. double long i, long n) long ni = n*i; double *rowp = a+ni; for (j = 0; j < n; j++)for (j = 0; j < n; j++)*rowp++ = b[j]; a[n*i+j] = b[j];Where are the FP operations? testq %rcx, %rcx # Test n # If 0, goto done # rax = n x # rax *= i jle .I4 # If 0, goto done movg %rcx, %rax # rax = n imulg %rdx, %rax # rax *= i leag (%rdi,%rax,8), %rdx # rowp = A + n*i*8 mov1 50, %r8d # j = 0 # loop: movq (%rsi,%r8,8), %rax # t = b[j] # *rowp = t movq % rax, (%rdx) addq\$1, %r8 addq\$8, %rdx cmpq%r8, %rcx # j++ # rowp++ # Compare n:j jg .L3 # If >, go to loop # done:

```
Reduction in Strength

    Replace costly operation with simpler one

    Shift, add instead of multiply or divide

             --> x << 4
  16*x
  · Utility machine dependent
  · Depends on cost of multiply or divide instruction

    On Intel Nehalem, integer multiply requires 3 CPU cycles

    Recognize sequence of products

                                        int ni = 0:
  for (i = 0; i < n; i++)
                                        for (i = 0; i < n; i++)
    for (j = 0; j < n; j++)
                                          for (j = 0; j < n; j++)
      a[n*i + j] = b[j];
                                           a[ni + j] = b[j];
                                          ni \neq n;
```

Share Common Subexpressions

- Reuse portions of expressions
- Compilers not very good at exploiting arithmetic properties

```
/* Sum neighbors of i, j */
up = val[(i-1)*n + j ];
down = val[(i+1)*n + j ];
left = val[i*n + j-1];
right = val[i*n + j+1];
sum = up + down + left + right;
```

```
long inj = i*n + j;
up = val[inj - n];
down = val[inj + n];
left = val[inj - 1];
right = val[inj + 1];
sum = up + down + left + right;
```

3 multiplications: i*n, (i-1)*n, (i+1)*n

leaq 1(%rsi), %rax # i+1
leaq -1(%rsi), %r8 # i-1
imulq %rcx, %rsi # i*n
imulq %rcx, %rax # (i+1)*n
imulq %rcx, %ra # (i-1)*n
addq %rdx, %rsi # i*n+j
addq %rdx, %rax # (i+1)*n+j
addq %rdx, %rax # (i-1)*n+j

1 multiplication: i*n

```
imulq %rcx, %rsi # i*n
addg%rdx, %rsi # i*n+j
movq%rsi, %rax # i*n+j
subq%rcx, %rax # i*n+j-n
leaq(%rsi,%rcx), %rcx # i*n+j+n
```

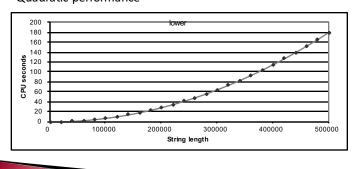
Optimization Blocker #1: Procedure Calls

▶ Procedure to Convert String to Lower Case

```
void lower(char *s)
{
  int i;
  for (i = 0; i < strlen(s); i++)
   if (s[i] >= 'A' && s[i] <= 'Z')
      s[i] -= ('A' - 'a');
}</pre>
```

Lower Case Conversion Performance

- Time quadruples when double string length
- Quadratic performance



Convert Loop To Goto Form

```
void lower(char *s)
{
    int i = 0;
    if (i >= strlen(s))
        goto done;
loop:
    if (s[i] >= 'A' && s[i] <= 'Z')
        s[i] -= ('A' - 'a');
    i++;
    if (i < strlen(s))
        goto loop;
done:
}</pre>
```

strlen executed every iteration

Calling Strlen

```
/* My version of strlen */
size_t strlen(const char *s)
{
    size_t length = 0;
    while (*s != '\0') {
    s++;
    length++;
    }
    return length;
}
```

- Strlen performance
 - Only way to determine length of string is to scan its entire length, looking for null character.
- ▶ Overall performance, string of length N
 - N calls to strlen
 - Require times N, N-1, N-2, ..., 1
 - · Overall O(N2) performance

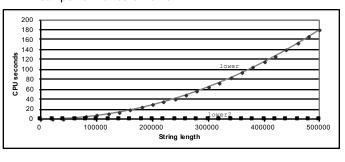
Improving Performance

```
void lower(char *s)
{
  int i;
  int len = strlen(s);
  for (i = 0; i < len; i++)
    if (s[i] >= 'A' && s[i] <= 'Z')
       s[i] -= ('A' - 'a');
}</pre>
```

- Move call to strlen outside of loop
- Since result does not change from one iteration to another
- Form of code motion

Lower Case Conversion Performance

- Time doubles when double string length
- Linear performance of lower2



Optimization Blocker: Procedure Calls

- ▶ Why couldn't compiler move strlen out of inner loop?
 - Procedure may have side effects
 - · Alters global state each time called
 - Function may not return same value for given arguments
 - · Depends on other parts of global state
 - · Procedure lower could interact with strlen
- Warning
 - Compiler treats procedure call as a black bo int lencnt = 0;
 - Weak optimizations near them
- Remedies:
 - Use of inline functions
 - GCC does this with –O2
 - · See web aside ASM:OPT
 - Do your own code motion

```
size_t strlen(const char *s)
{
    size_t length = 0;
    while (*s != '\0') {
    s++; length++;
    }
    lencnt += length;
    return length;
}
```

Memory Matters

```
/* Sum rows is of n X n matrix a
   and store in vector b */
void sum_rowsl (double *a, double *b, long n) {
   long i, j;
   for (i = 0; i < n; i++) {
      b[i] = 0;
      for (j = 0; j < n; j++)
        b[i] += a[i*n + j];
   }
}</pre>
```

```
# sum_rows1 inner loop
.L53:
    addsd (%rcx), %xmm0 # FP add
    addq$8, %rcx
    decq%rax
    movsd %xmm0, (%rsi,%r8,8) # FP store
    jne .L53
```

- Code updates b[i] on every iteration
- Why couldn't compiler optimize this away?

Memory Aliasing

```
/* Sum rows is of n X n matrix a
    and store in vector b */
void sum_rowsl(double *a, double *b, long n) {
    long i, j;
    for (i = 0; i < n; i++) {
        b[i] = 0;
        for (j = 0; j < n; j++)
            b[i] += a[i*n + j];
    }
}</pre>
```

```
double A[9] =
  { 0,   1,   2,
   4,   8,   16},
  32,  64,  128);
double B[3] = A+3;
sum_rows1(A, B, 3);
```

Value of B:

```
init: [4, 8, 16]

i = 0: [3, 8, 16]

i = 1: [3, 22, 16]

i = 2: [3, 22, 224]
```

- Code updates b [i] on every iteration
- · Must consider possibility that these updates will affect program behavior

Removing Aliasing

```
/* Sum rows is of n X n matrix a
    and store in vector b */
void sum_rows2(double *a, double *b, long n) {
    long i, j;
    for (i = 0; i < n; i++) {
        double val = 0;
        for (j = 0; j < n; j++)
        val += a[i*n + j];
        b[i] = val;
}</pre>
```

```
# sum_rows2 inner loop
.L66:
addsd (%rcx), %xmm0 # FP Add
addq$8, %rcx
decq%rax
jne .L66
```

No need to store intermediate results

Optimization Blocker: Memory Aliasing

- Aliasing
 - $\,^\circ\,$ Two different memory references specify single location
 - Easy to have happen in C
 - · Since allowed to do address arithmetic
 - · Direct access to storage structures
 - Get in habit of introducing local variables
 - Accumulating within loops
 - · Your way of telling compiler not to check for aliasing

Program Optimizations

Optimizing Compilers (Recap)

- ▶ Efficiently map program to machine
 - register allocation
 - code selection and ordering (scheduling)
 - dead code elimination
 - eliminating minor inefficiencies
- Don't (usually) improve asymptotic efficiency
 - Programmer should select best algorithm
 - big-O savings are (often) more important than constant factors
 - · but constant factors also matter
- ▶ Limitations: Optimization blockers dependent on runtime behavior
 - Typically static, intra-procedural analysis
 - Safe optimizations only: original program behavior must be preserved
 - Memory aliasing: two pointers to overlapping memory locations
 - · Stateful functions (with side effects): function output not solely dependent on inputs

Other (Potential Compiler) Optimizations

- Code motion
 - · reduce execution frequency of an operation
- ▶ Strength reduction
 - substitute cheap operations for costly ones
- ▶ Function inlining
 - replace function call with function body
- ▶ Sharing common sub-expressions
 - a more complex variant of code motion
- ▶ Eliminating unnecessary memory references
 - · use intermediates that compiler can store in registers

/* data structure for vectors */ typedef struct{ int len; double *data; } vec; /* retrieve vector element and store at val */ double get_vec_element(*v, idx, double *val) { if (idx < 0 || idx >= v->len) return 0; *val = v->data[idx]; return 1; }

Benchmark Computation

```
void combine1 (vec_ptr v, data_t *dest)
{
    long int i;
    *dest = IDENT;

    for (i = 0; i < vec_length(v); i++) {
        data_t val;
        get_vec_element(v, i, &val);
        *dest = *dest OP val;
    }
}</pre>
```

Compute sum or product of vector elements

Data Types

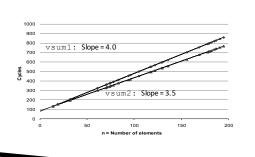
- Different declarations for data t
- int
- \circ float
- double

Operations

- Different OP and IDENT
- · + / 0
- · * / 1

Cycles Per Element (CPE)

- Convenient expression of program performance for vectors or lists
- ▶ Length = n
- ▶ In our case: CPE = cycles per OP
- ► T = CPE*n + Overhead
 - CPE is slope of line



Benchmark Performance

```
void combinel (vec_ptr v, data_t *dest)
{
   long int i;
   *dest = IDENT;
   for (i = 0; i < vec_length(v); i++) {
      data_t val;
      get_vec_element(v, i, &val);
      *dest = *dest OP val;
   }
}</pre>
```

Compute sum or product of vector elements

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Combine1 unoptimized	29.0	29.2	27.4	27.9
Combine1 -O1	12.0	12.0	12.0	13.0

Basic Optimizations

```
void combine4 (vec_ptr v, data_t *dest)
{
  int i;
  int length = vec_length(v);
  data_t *d = get_vec_start(v);
  data_t t = IDENT;
  for (i = 0; i < length; i++)
    t = t OP d[i];
  *dest = t;
}</pre>
```

- ▶ Move vec_length out of loop
- ▶ Avoid bounds check on each cycle
- ▶ Accumulate in temporary

Effect of Basic Optimizations

```
void combine4(vec_ptr v, data_t *dest)
{
  int i;
  int length = vec_length(v);
  data_t *d = get_vec_start(v);
  data_t t = IDENT;
  for (i = 0; i < length; i++)
    t = t OP d[i];
  *dest = t;
}</pre>
```

Method	Integer		Double FP	
Operation	Add Mult		Add	Mult
Combine1 -O1	12.0	12.0	12.0	13.0
Combine4	2.0	3.0	3.0	5.0

Exploiting Instruction-Level Parallelism

- More complex optimizations require at least a basic understanding of modern processor design
 - Hardware can execute multiple instructions in parallel
- ▶ Performance limited by data dependencies
- Simple transformations can yield dramatic improvements
 - Compilers often cannot make these transformations
 - Lack of associativity and distributivity in floating-point arithmetic

Register Updates Prediction OK? Register Updates Prediction OK?

Superscalar Processor

- Definition: A superscalar processor can issue and execute multiple instructions in one cycle. The instructions are retrieved from a sequential instruction stream and are usually scheduled dynamically.
- ▶ Benefit: without programming effort, superscalar processor can take advantage of the *instruction level parallelism* that most programs have
- ▶ Most CPUs since about 1998 are superscalar.
- ▶ Intel: since Pentium Pro

Nehalem CPU

- Multiple instructions can execute in parallel
 - 1 load, with address computation
 - 1 store, with address computation
 - 2 simple integer (one may be branch)
 - 1 complex integer (multiply/divide)
 - 1 FP Multiply
 - 1 FP Add
- ▶ Some instructions take > 1 cycle, but can be pipelined

Instruction	Latency	Cycles/Issue
Load / Store	4	1
Integer Multiply	3	1
Integer/Long Di vide	1121	1121
Single/Double FP Multiply	4/5	1
Single/Double FP Add	3	1
Single/Double FP Divide	1023	1023

x86-64 Compilation of Combine4

▶ Inner Loop (Case: Integer Multiply)

```
L519: # Loop:

imull (%rax,%rdx,4), %ecx # t = t * d[i]

addq $1, %rdx # i++

cmpq %rdx, %rbp # Compare length:i

jg .L519 # If >, goto Loop
```

Method	Integer		Doub	le FP
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Latency Bound	1.0	3.0	3.0	5.0

Loop Unrolling

- ▶ Increase number of elements computed per iteration
 - Reduces loop overhead
 - Exposes other optimization opportunities

Loop Unrolling

```
void unroll2a_combine(vec_ptr v, data_t *dest)
{
   int length = vec_length(v);
   int limit = length-1;
   data_t *d = get vec_start(v);
   data_t x = IDENT;
   int I;
   /* Combine 2 elements at a time */
   for (i = 0; i < limit; i+=2) {
        x = (x OP d[i]) OP d[i+1];
   }
   /* Finish any remaining elements */
   for (; i < length; i++) {
        x = x OP d[i];
   }
   *dest = x;
}</pre>
```

▶ Perform 2x more useful work per iteration

Effect of Loop Unrolling

Method	Inte	ger	Double FP	
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Unroll 2x	2.0	1.5	3.0	5.0
Latency Bound	1.0	3.0	3.0	5.0

- ▶ Helps integer multiply
 - below latency bound
 - Compiler does clever optimization
- ▶ Others don't improve. Why?
 - Still sequential dependency

x = (x OP d[i]) OP d[i+1];

Loop Unrolling with Reassociation

```
void unroll2aa_combine(vec_ptr v, data_t *dest)
{
   int length = vec length(v);
   int limit = length-1;
   data_t *d = get_vec_start(v);
   data_t x = IDENT;
   int I;
   /* Combine 2 elements at a time */
   for (i = 0; i < limit; i+=2) {
        x = x OP (d[i] OP d[i+1]);
   }
   /* Finish any remaining elements */
   for (; i < length; i++) {
        x = x OP d[i];
   }
   *dest = x;
}</pre>
```

Can this change the result of the computation?

FP. Why? Compare to before

x = (x OP d[i]) OP d[i+1];

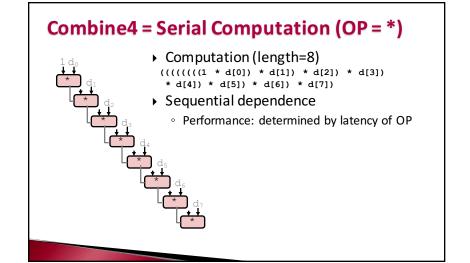
Effect of Reassociation

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Unroll 2x	2.0	1.5	3.0	5.0
Unroll 2x, reassociate	2.0	1.5	1.5	3.0
Latency Bound	1.0	3.0	3.0	5.0
Throughput Bound	1.0	1.0	1.0	1.0

- Nearly 2x speedup for Int *, FP +, FP *
 - · Reason: Breaks sequential dependency

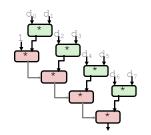
$$x = x OP (d[i] OP d[i+1]);$$

Why is that? (next slide)



Reassociated Computation

x = x OP (d[i] OP d[i+1]);



- What changed:
 - Ops in the next iteration can be started early (no dependency)
- Overall Performance
 - N elements, D cycles latency/op
 - Should be (N/2+1)*D cycles:CPE = D/2
 - Measured CPE slightly worse for FP mult

Loop Unrolling with Separate Accumulators

```
void unroll2a_combine(vec_ptr v, data_t *dest)
{
   int length = vec length(v);
   int limit = length-1;
   data_t *d = get vec_start(v);
   data_t x0 = IDENT;
   data_t x1 = IDENT;
   int T;
   /* Combine 2 elements at a time */
   for (i = 0; i < limit; i+=2) {
      x0 = x0 OP d[i];
      x1 = x1 OP d[i+1];
   }
   /* Finish any remaining elements */
   for (; i < length; i++) {
      x0 = x0 OP d[i];
   }
   *dest = x0 OP x1;
}</pre>
```

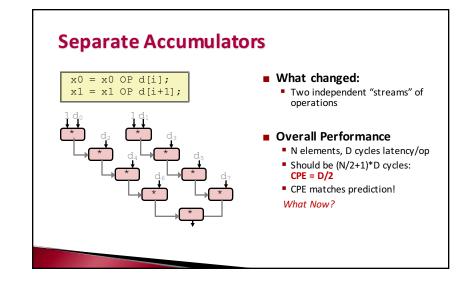
▶ Different form of reassociation

Effect of Separate Accumulators

Method	Integer		Doub	le FP
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Unroll 2x	2.0	1.5	3.0	5.0
Unroll 2x, reassociate	2.0	1.5	1.5	3.0
Unroll 2x Parallel 2x	1.5	1.5	1.5	2.5
Latency Bound	1.0	3.0	3.0	5.0
Throughput Bound	1.0	1.0	1.0	1.0

- 2x speedup (over unroll2) for Int *, FP+, FP *
 - Breaks sequential dependency in a "cleaner," more obvious way
 x0 = x0 OP d[i];

x0 = x0 OP d[i];x1 = x1 OP d[i+1];



Unrolling & Accumulating

- ▶ Idea
 - Can unroll to any degree L
 - Can accumulate K results in parallel
 - L must be multiple of K
- ▶ Limitations
 - Diminishing returns
 - · Cannot go beyond throughput limitations of execution units
 - Large overhead for short lengths
 - Finish off iterations sequentially

Unrolling & Accumulating: Double *

- Case
 - Intel Nehelam (Shark machines)
 - Double FP Multiplication

0									
Ŭ	FP *				Unrolling	Factor L			
	K	1	2	3	4	6	8	10	12
	1	5.00	5.00	5.00	5.00	5.00	5.00		
rs	2		2.50		2.50		2.50		
Accumulators	3			1.67					
nule	4				1.25		1.25		
cun.	6					1.00			1.19
Ac	8						1.02		
	10							1.01	
	12								1.00
	The same of the sa	-							

Unrolling & Accumulating: Int +

- ▶ Case
 - Intel Nehelam (Shark machines)
 - Integer addition

_									
0	FP *			Į.	Unrolling	Factor L			
	K	1	2	3	4	6	8	10	12
	1	2.00	2.00	1.00	1.01	1.02	1.03		
rs	2		1.50		1.26		1.03		
Accumulators	3			1.00					
nnl	4				1.00		1.24		
cnu	6					1.00			1.02
Ac	8						1.03		
	10							1.01	
	12								1.09
Total Contract	-								

Achievable Performance

Method	Integer		Doub	le FP
Operation	Add	Mult	Add	Mult
Scalar Optimum	1.00	1.00	1.00	1.00
Latency Bound	1.00	3.00	3.00	5.00
Throughput Bound	1.00	1.00	1.00	1.00

- Limited only by throughput of functional units
- ▶ Up to 29X improvement over original, unoptimized code

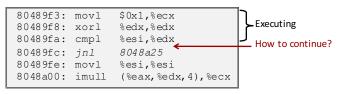
Using Vector Instructions

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Scalar Optimum	1.00	1.00	1.00	1.00
Vector Optimum	0.25	0.53	0.53	0.57
Latency Bound	1.00	3.00	3.00	5.00
Throughput Bound	1.00	1.00	1.00	1.00
Vec Throughput Bound	0.25	0.50	0.50	0.50

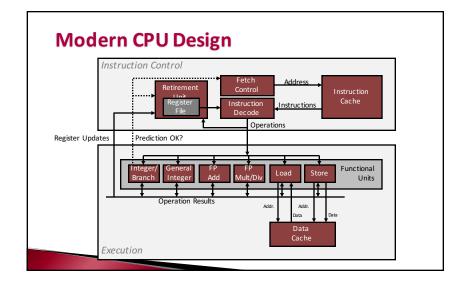
- Make use of SSE Instructions
 - Parallel operations on multiple data elements
 - See Web Aside OPT:SIMD on CS:APP web page

What About Branches?

- Challenge
 - Instruction Control Unit must work well ahead of Execution Unit to generate enough operations to keep EU busy



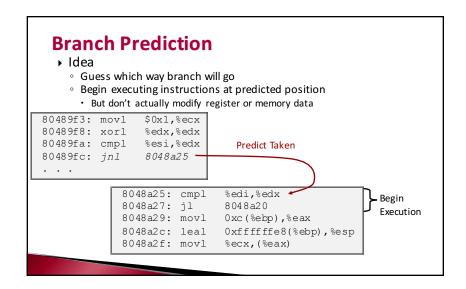
 \circ When encounters conditional branch, cannot reliably determine where to continue fetching

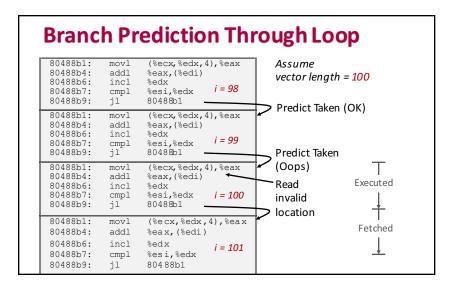


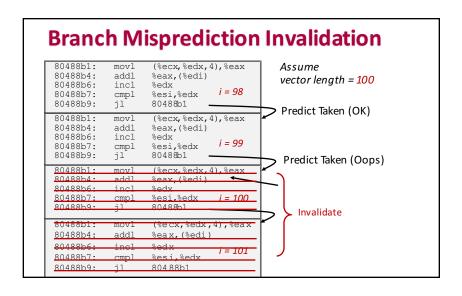
Branch Outcomes

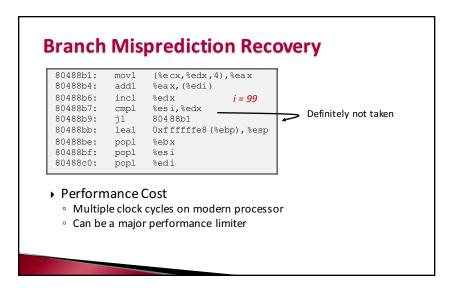
- When encounter conditional branch, cannot determine where to fetch
 - Branch Taken: Transfer control to branch target
 - Branch Not-Taken: Continue with next instruction in sequence
- Cannot resolve until outcome determined by branch/integer unit

```
80489f3: movl
               $0x1,%ecx
80489f8: xorl
               %edx,%edx
80489fa: cmpl %esi,%edx
                           Branch Not-Taken
               8048a25
80489fc: inl
80489fe: movl %esi,%esi
                                        Branch Taken
8048a00: imull (%eax, %edx, 4), %ecx
        8048a25: cmpl %edi,%edx
        8048a27: jl
                        8048a20
        8048a29: movl 0xc(%ebp),%eax
        8048a2c: leal 0xffffffe8(%ebp),%esp
        8048a2f: movl
                       %ecx,(%eax)
```









Effect of Branch Prediction

- ▶ Loops
 - Typically, only miss when hit loop end
- Checking code
 - Reliably predicts that error won't occur

Method	Inte	ger	Double FP	
Operation	Add Mult		Add	Mult
Combine4	2.0	3.0	3.0	5.0
Combine4b	4.0	4.0	4.0	5.0

Getting High Performance

- ▶ Good compiler and flags
- Don't do anything stupid
 - Watch out for hidden algorithmic inefficiencies
- Write compiler-friendly code
- Watch out for optimization blockers: procedure calls & memory references
- Look carefully at innermost loops (where most work is done)
- Tune code for machine
 - Exploit instruction-level parallelism
 - Avoid unpredictable branches
 - Make code cache friendly (Covered later in course)

GCC Optimizations

- ▶ -O1 (same as -O): reduce program size and time, quick optimizations
 - -fcompare-elim: identify instructions that compute processor flags, eliminate explicit comparison
 - -fcprop-registers: copy propagation to reduce dependencies
 - · -fce: dead code elimination
 - · -fdse: dead store elimination
 - -fdelayed-branch: exploit slot after branch delay
 - -fguess-branch-probability: based on heuristics and CFG
 - -fif-conversion: conditional jumps to branchless (cond. moves)equivalents -fif-conversion2
 - -ftree-ccp: conditional constant propagation
 - -ftree-dce: dead code elimination
 - -ftree-dominator-opts: dominator tree based optimizations (constant/copy propagation, redundancy elimination, ...) -fmerge-constants: across modules
 - · -fipa-pure-const: identify pure or constant procedures
 - ۰ ...

GCC Optimizations (cont'd)

- -O2 (optimizations that don't bloat program)
 - -fcaller-saves
 - -fcrossjumping: unifies equivalent code
 - -fcse-*: common sub-expression elimination optimizations
 - -fexpensive-optimizations
 - -fsched-spec: speculative motion of non-loads instructions
 - -freorder-blocks: Reorder basic blocks: reduce taken branches and improve locality
 - -fstrict-aliasing: different types don't overlap
 - · -freorder-functions
 - ۰ ...

GCC Optimizations (cont'd)

-O3: All optimizations

- -finline-functions
- -funswitch-loops: Move branches with loop invariant conditions out of the loop
- -fpredictive-commoning: reusing computations (especially memory loads and stores) performed in previous iterations of loops
- -fipa-cp-clone: Perform function cloning to make interprocedural constant propagation stronger

Other Considerations

- → Insufficient registers (register spilling)
- ▶ Load/Store Costs
- ▶ Amdahl's Law: only speedups to bottlenecks matter!
- ▶ Profiling Tools
 - gprof