

Prospects for strongly coupled atom-photon quantum nodes

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ABSTRACT

We discuss the trapping of cold atoms within microscopic voids drilled perpendicularly through the axis of an optical waveguide. The dimensions of the voids considered are between 1 and 40 optical wavelengths. By simulating light transmission across the voids, we find that appropriate shaping of the voids can substantially reduce the associated loss of optical power. Our results demonstrate that the formation of an optical cavity around such a void could produce strong coupling between the atoms and the guided light. By bringing multiple atoms into a single void and exploiting collective enhancement, cooperativities ~ 300 or more should be achievable. The simulations are carried out using a finite difference time domain method. Methods for the production of such a void and the trapping of cold atoms within it are also discussed.

Introduction

The introduction of cold atoms into microscopic holes in optical waveguides allows the integration of atomic components into otherwise purely photonic devices, with potential applications in sensing and quantum information processing [1, 2]. While alternative techniques are available for coupling guided light to cold atoms — for example the use of tapered nanofibres [3, 4, 5] or hollow core fibres [6, 7, 8] — microscopic holes offer a unique set of advantages that make them ideally suited for certain applications. Firstly, the technique of introducing cold atoms via a microscopic hole is just as applicable in a 2D waveguide chip as in a fibre, allowing the direct combination of cold atoms with photonic circuit devices. Secondly, while the overall optical depth of an atom cloud contained in a microscopic hole is likely to be less than that obtained using a nanofibre or hollow core fibre, the optical depth per unit length should be able to match that achievable in free space, which is substantially greater than that typical of hollow core fibre or nanofibre experiments. This may have important implications for spatial resolution in sensing applications. Finally, the spatial separation between the atoms

and the solid material of the waveguide can be much larger in a microscopic hole than is typical of a hollow core fibre or possible using a nanofibre. This will be important in precision sensing and spectroscopy experiments, where atom-surface interactions might otherwise adversely affect the results, as well as for any experiments involving Rydberg atoms, which are currently one of the most promising candidates for the implementation of multi-qubit gates [9, 10, 11].

In this article we simulate transmission of light across microscopic holes in optical waveguides. We focus on holes drilled perpendicular to the core of the waveguide, with diameters in the range of 1 to 40 optical wavelengths. Holes of this kind can be fabricated by pulsed laser drilling [12, 13] — see for example those shown in figure 1(d), which were fabricated by Workshop of Photonics [14] in 2015. We find that appropriate shaping of the holes can significantly improve the overlap of the transmitted light with the guided mode, thus reducing the losses associated with traversing the hole, and present results for a range of different shapes of hole. We then discuss the implications of our results with respect to the prospects of reaching the strong coupling regime for atoms confined in such a hole. We also examine the intensity distribution of the light inside the hole and use our results to show that both crossed and individual waveguides are capable of forming a full, 3D dipole trap for ultracold atoms using only guided light.

While this article focuses on the specific application of a light-atom interface, the results may also be applicable within other fields. These include fibre-based gas sensors [15, 16] and the efficient transmission of light through integrated optical or optofluidic elements [17, 18] in a fibre or waveguide chip. Coupling of light between waveguides and/or optical fibres is also an important area of application.

Simulation methods

In order to identify a geometry which allows a gap in the micrometer range with high optical transmission, simulations based on solving Maxwell’s equations were performed using Optiwave software (Optiwave Systems Inc.). For most data we use a three dimensional finite difference time domain (FDTD) method, which is a numerical solution of the full Maxwell’s equations [19].

Where applicable, we compare that to the results of a beam propagation method (BPM). While numerically less intensive than the FDTD method, the BPM we employ makes several approximations — most notably the paraxial approximation — that render it less accurate than the FDTD method. We therefore use it only as a guide to the overall trends in the system’s behaviour, which helps to highlight the most interesting areas for investigation with the more time-consuming FDTD simulations.

The key parameters of the FDTD simulation method are the mesh spacing in each dimension $\Delta x, \Delta y, \Delta z$ (with the z axis corresponding to the direction of light propagation along the waveguide), the time step size Δt and the number of time steps for which the simulation was run, N_t . These are given for each case below, with the convention that all distances are given in micrometers and all times in seconds.

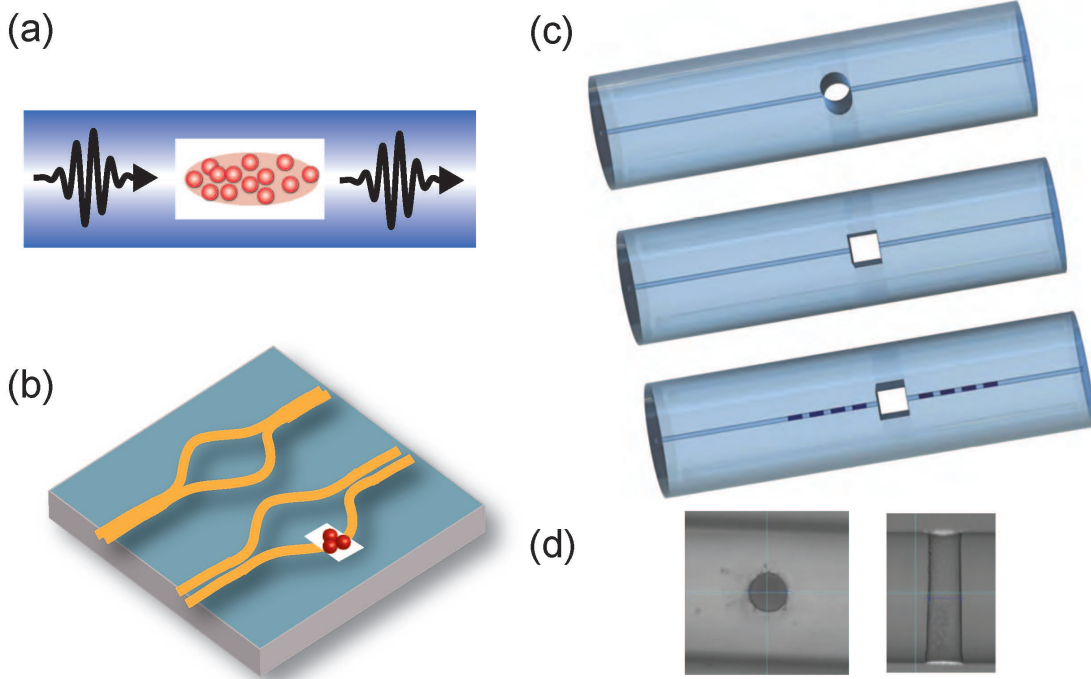


Figure 1. a) Illustration showing atoms confined within a microscopic void in an optical fibre, interacting with the guided light. b) The same method can be used to introduce cold atoms into a waveguide on a chip, thus allowing them to be integrated into more complex photonic circuits. c) Examples of possible geometries; round hole, square hole, square hole combined with fibre Bragg gratings. d) Laser drilled holes in a Thorlabs 780HP optical fibre, images produced by Workshop of Photonics.

The boundary condition used for the FDTD simulations was the built-in anisotropic, perfectly-matched layers (PML) condition, which accurately approximates a perfect absorber.

In general we consider the overlap of the transmitted light with the fundamental mode of the waveguide (MOTL), rather than the transmission coefficient. The difference between these two is the additional loss of light resulting from reflections at the glass to air/vacuum interfaces. In the case of rectangular holes interference effects are important, and the reflection coefficient varies strongly with the length of the hole. We therefore calculated reflection coefficients for several illustrative cases of rectangular hole. The maximum and minimum (excluding sub-wavelength holes where the reflection coefficient tends to zero as the length tends to zero) were 17.8% and 0.5%, occurring for holes with lengths of 4 and 1.7 micrometers respectively. Reflection coefficients for rectangular holes with lengths of 1, 5, 12, 22 and 30 micrometers were found to be 15.9, 1.6, 14.8, 15.6 and 11.9% respectively.

It is also worth noting that for rectangular holes the reflected light typically overlaps well ($\sim 97\%$ intensity overlap) with the guided mode of the waveguide. Therefore, if such

a hole were placed inside an optical resonator, it would not be accurate to regard the majority of the reflected light as lost from the system.

However, calculation of accurate reflection/transmission coefficients requires a long simulation time, to allow for multiple reflections within the system. When the surfaces of the hole have even modest curvature, the poor overlap and phase averaging between the light reflected via different pathways means that interference effects are essentially negligible, and the reflection losses at each interface can be treated as independent. This yields reflection losses of $\sim 4\%$ per interface, with little variation according to the parameters of the hole. In these cases the MOTL is therefore the most interesting system property to consider.

With a specific application in mind, i.e. the interaction of photons with cesium atoms, we consider the case of 852 nm light (resonant with the D₂ line in Caesium) in a waveguide whose refractive index profile matches a commercial optical fibre (Thorlabs 780HP), as a representative example for a typical singlemode optical waveguide. However, the general trends and qualitative behaviours observed are likely to be widely applicable. We also consider a specific case based on the waveguide chip described in [1], for which we find agreement between our simulations and the work of the original authors.

Simulation results

The first hole shape considered is the simplest geometry — a cylinder, and the results are plotted in figure 2(a). Simulation parameters were: $(\Delta x, \Delta y, \Delta z, \Delta t, N_t) = (0.08, 0.08, 0.1, 1.33 \times 10^{-16}, 2289)$. The dip in MOTL between 10 and 1.5 μm is due to additional divergence caused by the concave surface curvature, and MOTL eventually tends upwards to 1 as the hole size is reduced to zero. For holes with diameters greater than about three micrometers, the highest achievable MOTL is $\sim 38\%$. This occurs at a plateau of MOTL as a function of diameter, for hole diameters from 20 to 30 micrometers.

The next case considered was a rectangular hole, as the flat faces of the rectangular hole were expected to eliminate the dip at small radii seen in the cylindrical hole due to concave lensing effects. This was indeed found to be the case, and the results are plotted in figure 2(b). Simulation parameters were: $(\Delta x, \Delta y, \Delta z, \Delta t, N_t) = (0.08, 0.08, 0.1, 1.33 \times 10^{-16}, 2289)$.

The FDTD and BPM results show a similar trend, where the FDTD result is consistently lower, owing to the remaining inaccuracy of the BPM data due to the paraxial approximation not covering all beam paths in this regime. For holes up to 10 optical wavelengths, a mode overlap $> 95\%$ is achievable.

For rectangular holes some experimental data is available in the literature [1]. This was found to yield 65% power transmission across a 16 μm gap between 4 μm square waveguides in silica. Based on the refractive index contrast (0.75%) and laser wavelength used, we simulated this situation using the FDTD method and found an

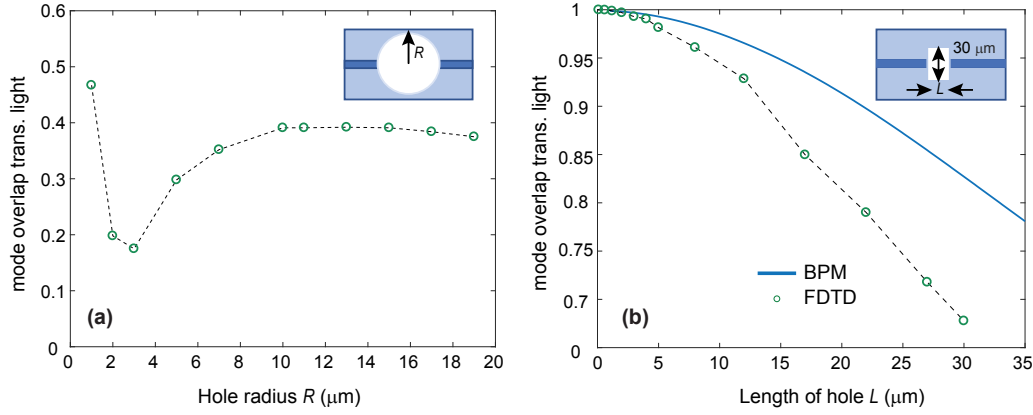


Figure 2. Fractional power overlap with the fundamental mode of the waveguide for light transmitted across a cylindrical (a) and a rectangular (b) through-hole in an optical fibre as a function of hole length. The hole is orientated perpendicular to the fibre axis, with the insets displaying the considered geometry. In both cases, the distance of closest approach between the input and output surfaces is $30\ \mu\text{m}$, the fibre parameters used match Thorlabs 780HP fibre, and the optical wavelength is $852\ \text{nm}$.

estimated transmission of 78% (including reflection losses). The theoretical result is an upper bound to what is achievable experimentally and the slightly lower result can be explained by potential imperfections in the polishing of the end facets, a small angle between the end facets or a small amount of contamination. We therefore find that these figures are consistent with our expectations.

From the two initial simulations, it was expected that the use of convex surfaces should enhance the mode overlap for larger holes, as the focal power of these surfaces will compensate for the beam divergence related to the numerical aperture of the fibre core and allow recapture of light into the guided mode.

One relevant case to consider is that of a hole with spherically-curved surfaces on the input and output facets. We simulated this case for a range of radii of curvature, with the closest approach between the input and output surfaces being locked to $30\ \mu\text{m}$. The results are plotted in figure 3(a). Simulation parameters were: $(\Delta x, \Delta y, \Delta z, \Delta t, N_t) = (0.08, 0.08, 0.1, 1.33 \times 10^{-16}, 2289)$. It can be seen from the FDTD simulations that for a radius of curvature of $\sim 16\ \mu\text{m}$ the MOTL exceeds 93%, a major improvement over the rectangular hole of $30\ \mu\text{m}$ length where the MOTL was only 68% (see figure 2(b)). As a consistency check, additional simulations were also run for radii of curvature up to 3 mm, well beyond the range of figure 3(a). It was confirmed that, as expected, the MOTL gradually drops off as the radius of curvature is increased and ultimately tends to the same value predicted for the $30\ \mu\text{m}$ rectangular hole.

With the practicalities of making a hole of this shape in mind, we also considered the effect of using cylindrically curved convex surfaces instead of spherically curved surfaces. We expect such holes to be easier to make as they have a constant cross-section. The results are shown in figure 3(b). Simulation parameters were: $(\Delta x, \Delta y, \Delta z, \Delta t, N_t) =$

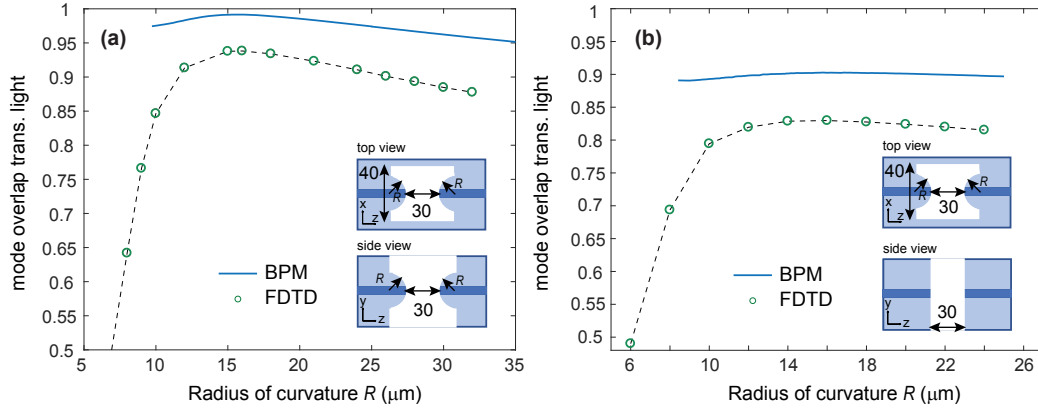


Figure 3. (a) Fractional power overlap with the fundamental mode of the waveguide for light transmitted across a through-hole in an optical fibre with spherically-curved convex input and output facets, as a function of the radius of curvature of the surface. (b) The same for cylindrically-curved input and output facets. In both cases, the distance of closest approach between the input and output surfaces is 30 μm , the fibre parameters used match Thorlabs 780HP fibre, and the optical wavelength is 852 nm.

(0.08, 0.08, 0.059, 9.74×10^{-17} , 2349).

Parabolic surface curvatures were also investigated using the FDTD method, and were found to provide even better mode overlap for the transmitted light. The results are plotted in figure 4(a). Simulation parameters were: $(\Delta x, \Delta y, \Delta z, \Delta t, N_t) = (0.084, 0.084, 0.1, 1.40 \times 10^{-16}, 2280)$. In particular, for circularly symmetric, convex, parabolic surface curvature of the hole surfaces with $\alpha = \frac{\delta z}{r^2} = 0.063 \mu\text{m}^{-1}$ we find 99.3% MOTL for a hole where the distance of closest approach is 20 μm .

The convex surfaces also lead to focusing of the light within the hole. The enhancement in peak intensity that results from this could be useful for the production of an optical dipole trap within the hole (see below), or to allow the strong coupling regime to be reached with smaller atomic ensembles as discussed in §. We observe enhancements of up to a factor of 15.5 in peak intensity, with a general trend towards greater surface curvature producing a larger peak intensity enhancement. In the example given above (parabolic curvature with $\alpha = 0.063 \mu\text{m}^{-1}$) we find that the peak intensity is increased by a factor of ~ 4 .

In order to constitute a quantum memory, or to allow longer interrogation times in sensing applications, it is advantageous to hold cold atoms within the junction, e.g. in an optical dipole trap. Where in other systems the creation of a small stable trap could be challenging, here they can be created using only light guided in the waveguides themselves. The trapping region then also automatically overlaps with the interrogation region of the probe light.

The FDTD method of simulation provides full data on the electric field as a function of position within the junction and can therefore be used to determine the light intensity, and hence the optical dipole potential, as a function of position within the junction.

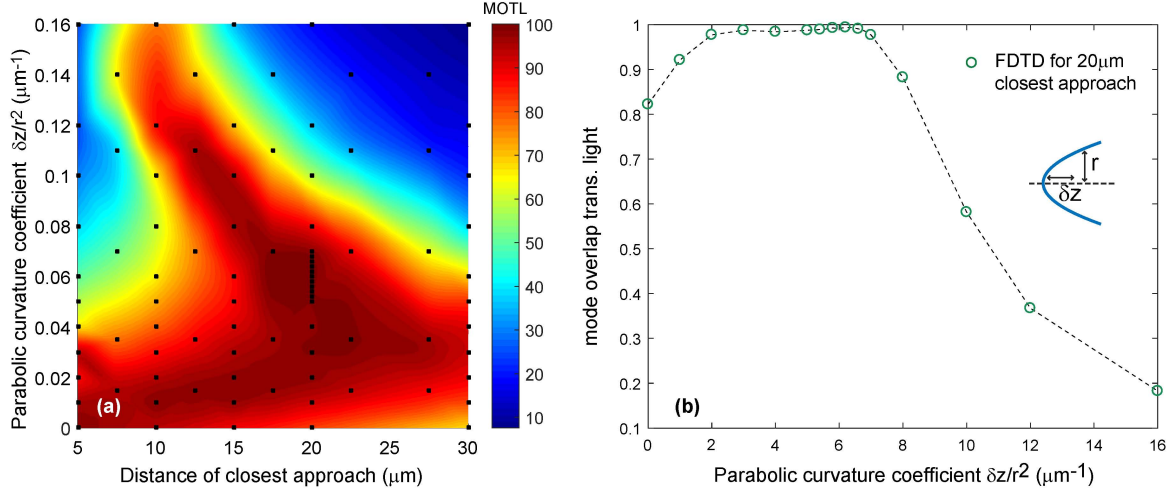


Figure 4. (a) Mode overlap for light transmitted across a through-hole in an optical fibre with parabolically-curved convex input and output facets, as a function of the coefficient of curvature of the surfaces and the distance of closest approach of the input and output faces. (b) MOTL as a function of the coefficient of curvature with the distance of closest approach equal to 20 μm . In (a) the black markers indicate the locations of the data points resulting from FDTD simulations, while the colour map is a cubic interpolation between the measured points.

Figure 5(a) shows the dipole potential generated for Cs atoms by 1 mW of light at 1064 nm crossing a 20 μm hole with convex parabolic surface curvature ($\alpha = 0.063 \mu\text{m}^{-1}$) in a waveguide with parameters matching Thorlabs 780 HP optical fibre. It can be seen from this that already a single beam forms a full 3D trap - a result of focusing of the guided light at the convex interfaces. Figure 5(b) shows the dipole potential generated in a junction formed at the intersection of two 4 μm square silica waveguides with a refractive index contrast of 0.75%. There is assumed to be 1 mW of 1064 nm light in each waveguide, with identical linear polarisations. It is worth noting that the small mode area offers an unusually high trap depth for a given optical power and wavelength.

The damage threshold for waveguides and optical fibres of this type is typically of the order of 10^{10} Wm^{-2} for visible and NIR wavelengths. This would correspond to a power of ~ 200 mW in each waveguide. As a result, the maximum trap depth that can realistically be achieved in such a junction (with a comparable detuning of the trapping laser from the relevant atomic transition) would be on the order of 10 to 15 mK.

Strong coupling regime

Reaching the strong coupling regime is of interest as it permits single-photon gate operations and allows the observation and exploitation of quantum electrodynamic effects [20, 21, 22, 23, 24]. In order to reach this regime an optical cavity would be produced around a quantum system with an appropriate optically-addressable

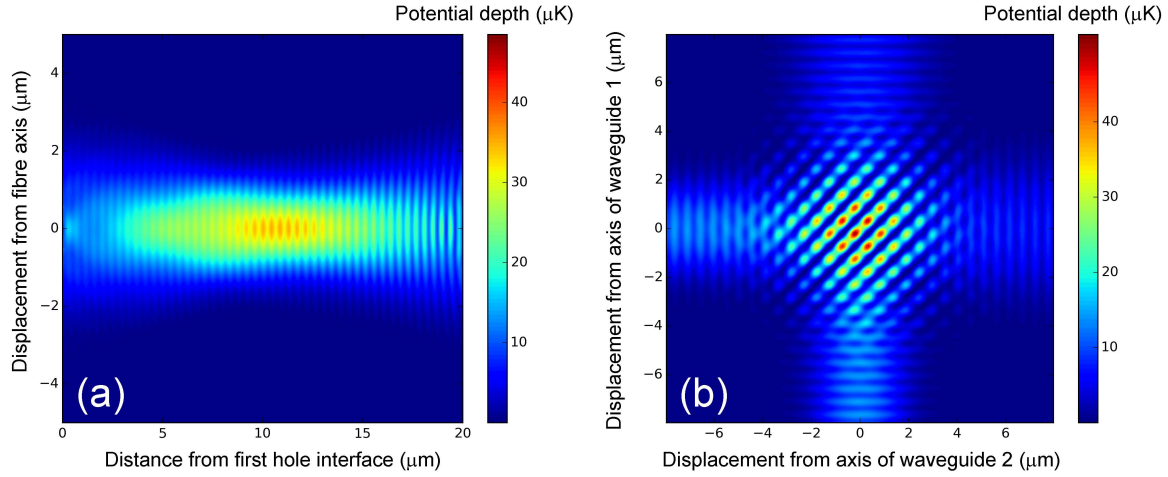


Figure 5. Simulated trapping potentials for Cs atoms in two example waveguides. Part (a) represents a 20 μm long hole with convex parabolic surface curvature ($\alpha = \frac{\delta z}{r^2} = 0.063 \mu\text{m}^{-1}$) in a waveguide with parameters matching Thorlabs 780 HP optical fibre. Part (B) represents the intersection of two 4 μm square silica waveguides with a refractive index contrast of 0.75%. In both cases each waveguide carries 1 mW of 1064 nm light propagating in the positive x or z direction as appropriate.

transition, in this case via the use of laser-written Bragg gratings [20, 25] on either side of the hole. Different regimes can then be reached, depending on the cavity length and the choice of hole type. The strong coupling regime is defined as the regime in which the atom-cavity coupling constant g significantly exceeds the atomic decay rate γ and the cavity decay rate κ . The Purcell regime, in which the cooperativity $C = g^2/(\kappa\gamma)$ is large but $g < \kappa$, is also of interest — particularly with regard to the production of single photon sources [26]. The maximum value of the atom-cavity coupling constant is given according to [2]

$$g_1 = \zeta \sqrt{\frac{\omega_c}{2\hbar\epsilon_0 V}} \phi(\vec{r}), \quad (1)$$

where ζ is the dipole matrix element for the atomic transition being addressed, ω_c is the resonant frequency of the cavity and V the volume of the cavity mode [27]. The mode volume is defined such that $V = \int \phi^2(\vec{r}) d^3\vec{r}$.

We assume a $1/e^2$ intensity radius of 2.5 μm , which is representative of most waveguides of the kind we consider herein, and analyse examples for different cavity lengths. In [20] fibre Bragg gratings with a reflectivity of 99.5% were used, and even higher reflectivities are achievable [20, 21]. For now we assume that the mode profile in the hole does not differ significantly from that in the waveguide, although the focal effects of surfaces with convex curvature discussed in the previous section could in principle be used to enhance the coupling strength. In the case of a single Caesium atom addressed on the D_2 line ($F = 4, m_F = 4 \rightarrow F' = 5, m'_F = 5$), trapped inside a rectangular void with a length of $L = 5 \mu\text{m}$ inside a cavity with length $l_c = 5 \text{ mm}$, this gives a value

of $g = 263$ MHz and $\kappa = 609$ MHz. Here g clearly exceeds the atomic decay rate of $\gamma = 16.4$ MHz [28] (where γ is equal to half of the spontaneous decay rate Γ , to allow for the atomic population distribution) and the cooperativity equates to $C = 3.5$, thus placing this system within the Purcell regime [29]. Note that for rectangular holes we consider only losses associated with imperfect MOTL. This is because, in the case of rectangular holes, the reflected light was found to overlap well with the mode of the waveguide *and* the reflection coefficient could be reduced to $\sim 0.5\%$ through appropriate local tuning of the hole length. When considering holes with other shapes reflection losses are taken into account.

In order to enter the strong coupling regime it is also necessary that $g > \kappa$. This would be reached for a single Cs atom in a rectangular void of $L = 5$ μm and a cavity length of $l_c = 50$ mm, again for a cooperativity of $C = 3.5$ and a coupling rate of $g = 83$ MHz and $\kappa = 61$ MHz. For longer rectangular holes, up to a size of $L = 12$ μm (8 % losses), cooperativities with $C=1.5$ and a cavity length of $l_c = 300$ mm with $g = 34$ MHz and $\kappa = 23.5$ MHz are possible. While introducing a large ensemble of cold atoms into such a space is difficult, introducing a single trapped atom into a hole of this size is plausible, and small rectangular holes may therefore permit strong coupling of single atoms to guided light. Furthermore, the development of an anti-reflection coating technique for the interior hole surfaces would greatly expand the range of options available. For example, without reflection losses appropriate convex surface curvature would allow the strong coupling regime to be reached for single atoms in holes over 20 μm in length.

When multiple atoms are trapped inside a void and therefore confined in such a cavity, there is a collective enhancement of the coupling constant by a factor equal to the square root of the number of atoms present $g_N = \sqrt{N}g_1$ [30, 31]. Considering the trapping volumes involved ($\sim 1 - 1000$ μm^3) and the densities typically achievable in a dipole trap (~ 1 μm^{-3} without evaporative cooling or ~ 1000 μm^{-3} with [32]), atom numbers between $1 - 10^6$ should be achievable. With, for example, optimal convex parabolic curvature in a 20 μm long void these would yield collective cooperativities $C_N = g_N^2/(\kappa\gamma)$ in the range of $1.5 - 1.5 \times 10^6$. Under these conditions trapping of e.g. ~ 260 Cs atoms within the hole, a plausible number even without using evaporative cooling, would yield $C_N = 384$.

Other quantum systems such as quantum dots [33] or semiconductor vacancy centres [34] could be placed into much smaller holes, and potentially even into holes which are then filled with index-matching fluid, as is done in [35]. Bringing these systems into the strong coupling or Purcell regimes should therefore also be possible in microscopic voids of this kind.

Outlook

The transmission of light across holes in optical waveguides, with sizes in the range 1 to 30 micrometers, has been studied via numerical simulation. Most attention was

given to losses resulting from mode mismatch, since for curved surfaces reflection losses remain roughly constant, at about 8% for two uncoated glass surfaces. The results are found to be consistent with previous experimental results and reproduce the correct limiting behaviour as variables become large or small and calculation of the transmission becomes trivial.

The results show that for a given length of hole the losses due to mode mismatch can be greatly reduced through appropriate hole shaping, with appropriate convex parabolic curvature of the input and output faces of a 20 micrometer long hole reducing losses due to mode-mismatch from $\sim 15\%$ in the case of flat end faces to $< 0.7\%$. Shaping of holes to maximise power transmission may have applications in fibre-based sensors as well as in quantum optics experiments involving cold atoms.

It is also shown that dipole traps for ultracold atoms can be formed within such holes using only guided light, with maximum depths in the range of ten to fifteen mK for typical silica waveguides and trapping laser detunings of ~ 200 nm. Furthermore, our calculations suggest that construction of optical cavities around such holes should allow the strong coupling regime to be reached for single atoms trapped in holes up to ~ 10 μm in length. Exploiting collective enhancement to increase the coupling strength allows the use of larger voids and permits higher cooperativities — for example an ensemble of 300 Cs atoms in a 20 μm long hole with appropriate surface curvature could yield a cooperativity of more than 400. This could make holes of this kind an ideal component for interfacing light and cold atoms as part of an integrated quantum information system.

Future work will include determining suitable methods for the smoothing and anti-reflection coating of the interior hole surfaces. For example, smoothing is expected to be possible using either ion beam milling or plasma assisted chemical etching [36]. Additionally, shaping of the waveguide's refractive index profile on either side of the junction will be investigated. Previous experimental work has demonstrated the plausibility of shaping such waveguides [37, 38], and the additional dimension this approach adds to the space of free parameters available when designing a waveguide-void interface should allow for extremely high transmission coefficients to be achieved.

Data Availability Statement

Any relevant data not presented in the manuscript is available from the authors upon reasonable request.

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Author contributions

L.H. and N.C. provided the initial ideas for the work. C.B. commenced the simulation work, which was then significantly expanded by N.C.. M.G. provided advice on the efficient use of the simulation software. E.D., V.N. and L.H. assisted N.C. with manuscript preparation and review of the relevant literature. All authors reviewed the final manuscript.

Additional information

The authors declare no competing interests.