The Skellam distribution

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Consider

 $X \sim \text{Poisson}(\lambda_1)$

and

 $Y \sim \text{Poisson}(\lambda_2)$

then

$$Z = X - Y$$

has a Skellam distribution with

$$Z \sim \text{Skellam}(\lambda_2, \lambda_2).$$

See Wikipedia. Skellam distribution http://en.wikipedia.org/wiki/Skellam_distribution Load the package

```
library('skellam')
```

Set some parameters

```
N = 5000
lambda1 = 1.5
lambda2 = 0.5
```

Simulate Poisson and Skellam random variables

```
X = rpois(N, lambda1)
Y = rpois(N, lambda2)
XminusY = X - Y
Z = rskellam(N, lambda1, lambda2)
```

Produce figures

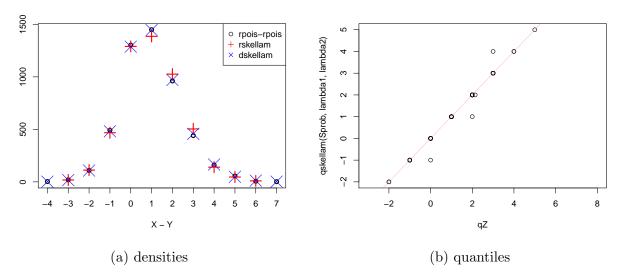


Figure 1: Differences of Poisson and Skellam with parameters 1.5 and 0.5

If the dskellam and rskellam functions are correct, the three sets points on the left will be coincident. If the qskellam function is correct the points on the right will lie on the red line.

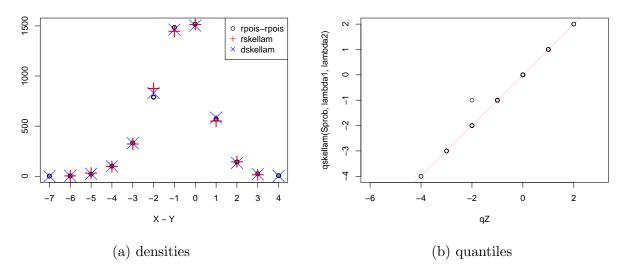


Figure 2: Differences of Poisson and Skellam with parameters 0.5 and 1.25

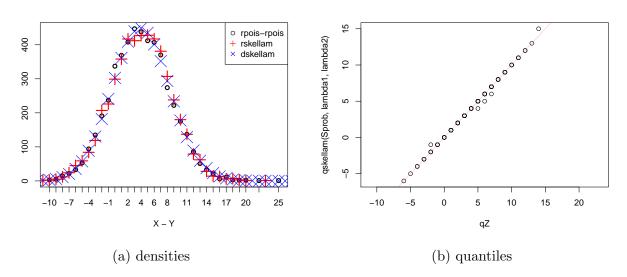


Figure 3: Differences of Poisson and Skellam with parameters 12 and 8