

# Multiple Linear Regression of Advertising Data

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## Abstract

This report seeks to replicate the research found in *Simple Linear Regression*, chapter 3 of the book **An Introduction to Statistical Learning** by Gareth James, et al., on a set of advertising data. I run a multiple linear regression on the data and create various functions to calculate several statistics, including the residual square error and the F-statistic.

## Introduction

The goal of this research is to use existing data to formulate a marketing plan that will result in higher product sales. To that end, we will run a multiple linear regression to model the increase of sales against the amount of money spent on marketing the product through various media - TV, radio, and newspapers. We will analyze this to determine how advertising affects sales, and how the company should budget for advertising in order to increase sales of the product.

## Data

The Advertising data set consists of the **Sales** (in thousands of units) of a particular product in 200 different markets, along with advertising budgets (in thousands of dollars) for the product in each of those markets for three different media: **TV**, **Radio**, and **Newspaper**.

```
##      X      TV Radio Newspaper Sales
## 1 1 230.1  37.8      69.2   22.1
## 2 2  44.5  39.3      45.1   10.4
## 3 3  17.2  45.9      69.3    9.3
## 4 4 151.5  41.3      58.5   18.5
## 5 5 180.8  10.8      58.4   12.9
## 6 6   8.7  48.9      75.0    7.2
```

## Methodology

We perform a simple linear regression on **Sales** for each of the three other factors.

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	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	7.03	0.46	15.36	0.00
TV	0.05	0.00	17.67	0.00

Table 1: Summary of Simple Linear Regression on TV

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	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	9.31	0.56	16.54	0.00
Radio	0.20	0.02	9.92	0.00

Table 2: Summary of Simple Linear Regression on Radio

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	12.35	0.62	19.88	0.00
Newspaper	0.05	0.02	3.30	0.00

Table 3: Summary of Simple Linear Regression on Newspaper

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We look at the relationship between **Sales** and the budgets of the various forms of media using the model:

``Sales = a + b * TV + c * Radio + d * Newspaper``

That is, we predict there to be a relationship between the amount of money spent on TV, Radio, and Newspaper advertising and the number of sales of units. We approximate the values of a, b, c, and d using a multiple linear regression under the least squares criterion.

## Results

We computed the correlation coefficients using the `lm()` function, with **TV** as a function of **Sales**.

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	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	2.94	0.31	9.42	0.00
TV	0.05	0.00	32.81	0.00
Radio	0.19	0.01	21.89	0.00
Newspaper	-0.00	0.01	-0.18	0.86

Table 4: Summary of Coefficients for All Independent Factors

The estimates of these coefficients, a, b, c, and d, are 2.9388894, 0.0457646, 0.18853, and  $-0.0010375$ , respectively. For every \$1,000 increase in spending on TV advertising, sales are projected to increase by  $4.5764645 \times 10^{-5}$  units; this means that units have to cost at least  $2.185093 \times 10^4$  in order to be profitable. For every \$1,000 increase in spending on Radio advertising, sales are projected to increase by  $1.8853002 \times 10^{-4}$  units; this means that units have to cost at least 5304.2 in order to be profitable. For every \$1,000 increase in spending on Newspaper advertising, sales are projected to increase by  $-1.037493 \times 10^{-6}$  units.

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On average, sales data will deviate from the true regression model by 1.6855 units. An  $R^2$  of 0.8972 means 89.72% of the variability is explained by the model. An F-statistic of 570.2707 means that the coefficients found by our model are very likely to be close to the true regression values.

## Conclusions

Individually, each of the factors **TV**, **Radio**, and **Newspaper** have a significant effect on the number of **Sales**. Together, only **TV** and **Radio** have significant effects; an increase in **Newspaper** budget actually decreases the number of **Sales**.

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	7.03	0.46	15.36	0.00
TV	0.05	0.00	17.67	0.00

Table 5: Summary of Simple Linear Regression on TV

There is a positive correlation between the budget for TV advertising and Sales; however, this relationship is very minimal. For every \$1,000 spent on advertising only another 48 units are sold, so each unit would have to cost at least \$20.84 in order to break even or profit off the units sold.