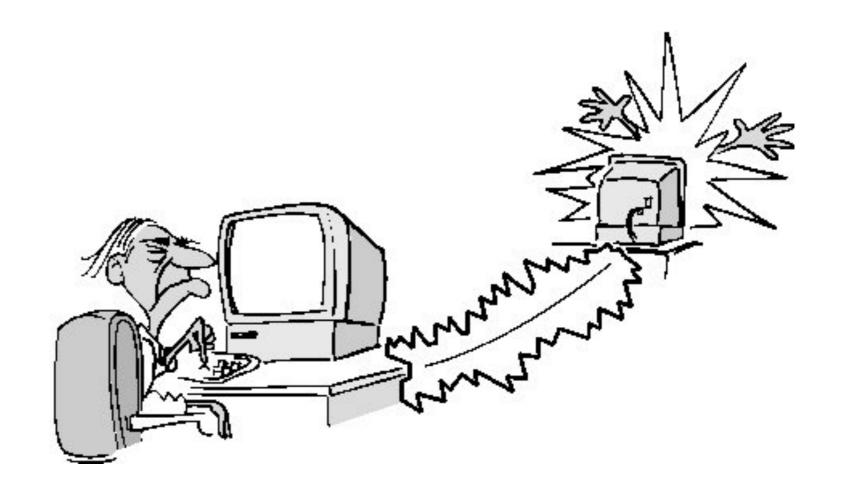
10.16.2020

### HOMEWORK 3

\* due today!



### HOMEWORK 4

\* posted today!



### **RECAP**

\* statistical power: how often a test says "significant" when there actually is an effect

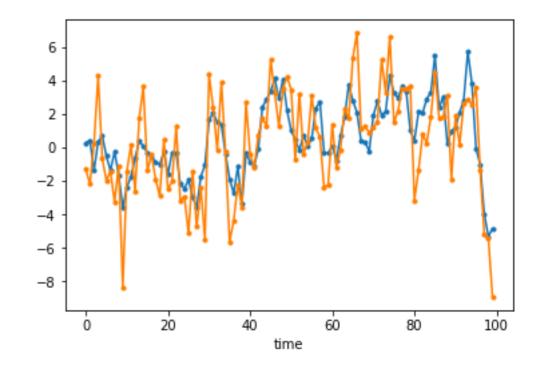
\* effect size

#### **RECAP**

- \* permutation test
  - \* "if these two samples were actually the same, it shouldn't matter if we scramble them up and then re-divide them into two new samples..."

# RELATIONSHIPS BETWEEN SAMPLES

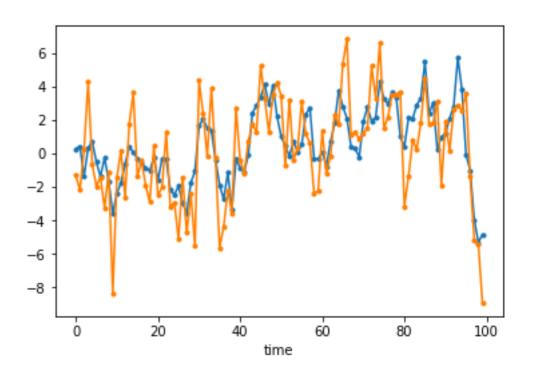
\* you record fMRI responses while someone listens to a podcast and plot the response in auditory cortex over time (orange)

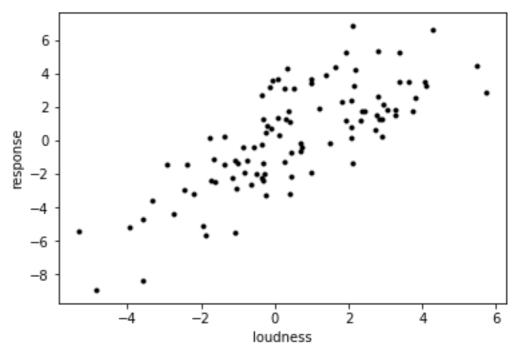


\* you also measure how loud
the sound is at every
timepoint, and plot that
(blue)

# RELATIONSHIPS BETWEEN SAMPLES

- \* you can also plot loudness vs. fMRI response in a scatter plot (bottom)
- \* these two seem related. how related? how do we measure?





\* "are these two sets of numbers (linearly)
related?"



\* the (linear) correlation between two variables is their covariance divided by the produce of their standard deviations

$$r_{X,Y} = corr(X,Y) = \frac{cov(X,Y)}{\sigma_X \sigma_Y}$$

# WHAT THE HECK IS COVARIANCE

\* variance is the average squared difference from the mean

$$var(X) = \sigma_X^2 = \frac{1}{n} \sum_{i=1}^{N} (X_i - \bar{X})^2 = \frac{1}{n} \sum_{i=1}^{N} (X_i - \bar{X})(X_i - \bar{X})$$

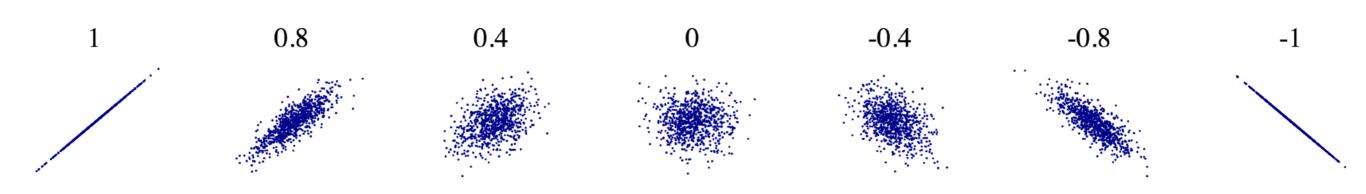
# WHAT THE HECK IS COVARIANCE

\* in covariance we replace one of the terms
with Y:

$$cov(X,Y) = \frac{1}{n} \sum_{i=1}^{N} (X_i - \bar{X})(Y_i - \bar{Y})$$

- \* is covariance, but normalized by the product of the standard deviations
- \* and thus is always in the range -1...1
  - \* which is nice

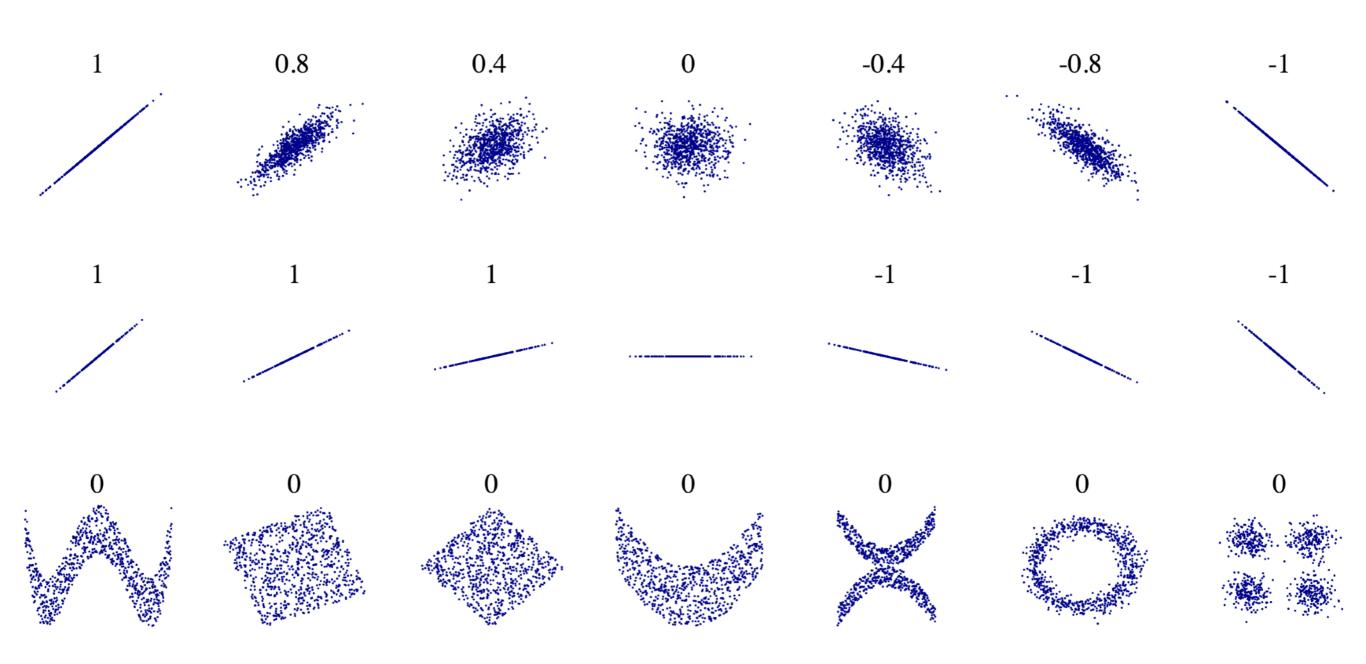
\* tells you how **linearly related** two variables are



# DANGERS OF CORRELATION

\* just computing correlation can be dangerous when your variables are related in weird non-linear ways

# DANGERS OF CORRELATION

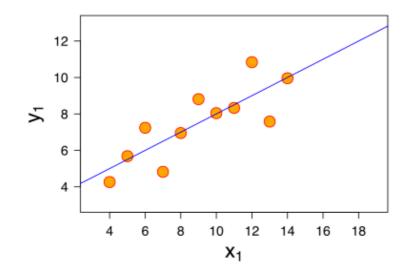


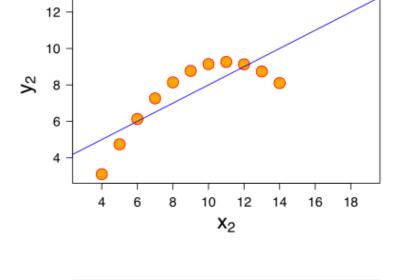
# ANSCOMBE'S QUARTET

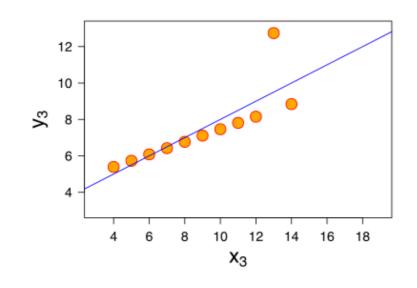


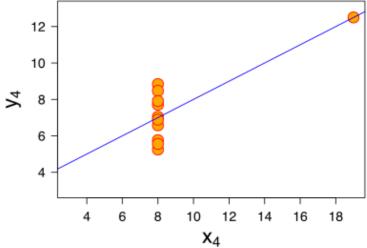
Frank

- \* 4 datasets with identical:
  - \* correlation
  - \* mean
  - \* variance
  - \* slope
  - \* R<sup>2</sup>









#### COMPUTING CORRELATION

- \* np.corrcoef(arr1, arr2)
  - \* computes the correlation between two arrays
  - \* but weirdly, gives you a 2x2 array back, e.g.:
    - \* [[1., 0.76], [0.76, 1.]]

#### COMPUTING CORRELATION

- \* np.corrcoef([arr1, arr2, arr3, ...])
  - \* computes the correlation between many arrays
  - \* for N arrays, gives you back an NxN
    matrix of correlations

## CORRELATION SIGNIFICANCE

- \* suppose the correlation between X and Y
  is 0.15
- \* is this "real", or is it something you'd see by chance?
- \* how do we figure this out?

## CORRELATION SIGNIFICANCE

- \* permutation test:
  - \* correlation depends on X and Y being ordered the same way. but if they are actually uncorrelated, then it shouldn't matter if we re-order them randomly

## CORRELATION SIGNIFICANCE

- \* "exact" test:
  - \* if we assume that X and Y are gaussian RVs, then there is an exact formula for what the distribution of correlations look like assuming they are unrelated
  - \* this can be used to find a p-value
  - \* implemented in scipy.stats.pearsonr

## END