

Mon 05 January 2015 [ab testing \(https://www.chrisstucchio.com/tag/ab-testing.html\)](https://www.chrisstucchio.com/tag/ab-testing.html) / [segmentation \(https://www.chrisstucchio.com/tag/segmentation.html\)](https://www.chrisstucchio.com/tag/segmentation.html)  
/ [multiple comparisons \(https://www.chrisstucchio.com/tag/multiple-comparisons.html\)](https://www.chrisstucchio.com/tag/multiple-comparisons.html)

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An experiment that seemed to be performing poorly might have actually been successful, but only for a certain segment. For example, our experiment may have shown that a variation of our mobile landing page is not performing well. When looking into the segments though, we may see that it is performing exceptionally well for Android users, but badly for iPhone users. When not looking at segments, you can miss this detail.

Segment	Filters	Color Coding	Events
Segment Type: <b>match Visits</b> Yahoo! Categories equals Technology			
Search Phrases (Direct)	Visitors	Visits	Page Views
emer kerrane	105	122	292
crepuscular light	60	62	81
judah phillips	31	37	70
ninja	27	30	36
ubc web analytics	13	13	18
michele hinojosa	12	12	15
http://d.yimg.com/ni/ey/ywa.js	11	13	13
lee isensee	10	13	25
ywa.gettracker	9	9	9
justin cutroni	9	10	14

The largest of those segments has 100 visitors! You simply do not have enough data to determine whether searches for "ninja" or "crepuscular light" will result in more conversions. Sorry, you are out of luck. Stop segmenting and don't try again until you've increased your traffic by 100x.

## Multiple goals - the same problem applies

A lot of people, in addition to segmentation, like to track multiple goals on their site. For example, newsletter signups, add item to shopping card, or save item for later. Congratulations - by using multiple sufficiently many goals, you'll definitely find a statistically significant result in one of them.

This effect is partially mitigated if your goals are correlated with each other. I.e., if people who sign up for the newsletter also tend to add an item to the shopping cart, then the issue of multiple goals is reduced. On the other hand, the more your goals are correlated with each other, the less useful information you actually get out of tracking multiple goals.

## An easy fix for multiple goals

The best way to handle the problem of multiple goals is to define One Key Metric (OKM). For example, you might define your OKM as:

$$OKM = 10 \times \text{purchase} + 1 \times \text{newsletter\_signup} + 1.5 \times \text{save\_item\_for\_later}$$

Then when making decisions, you have a single number which incorporates all the factors you are interested in. You can freely run any statistical test you like on the OKM without having to worry about multiple goals.

## How to fix the problem of multiple comparisons

Ok, you are still determined to segment your traffic or use multiple goals. Now it's time for one weird trick ([https://en.wikipedia.org/wiki/%C5%A0id%C3%A1k\\_correction](https://en.wikipedia.org/wiki/%C5%A0id%C3%A1k_correction)) to use to avoid running into the problems I've described above. It's a simple formula you can use. Suppose you want to run a segmented test with a p-value cutoff of 0.05. You can use the following formula to compute a  $p$  cutoff that works with multiple segments:

$$\text{new\_p\_cutoff} = 1 - (1 - \text{old\_p\_cutoff})^{(1/\text{number\_of\_segments})}$$

According to this formula, if we have 20 segments,  $\text{new\_p\_cutoff} = 0.00256$ . So suppose you've run a test with 20 segments. If you want to have a 5% chance of observing a false positive in the test, then you must declare any individual test to be statistically insignificant unless it yields a p-value smaller than 0.00256.

You can use the same formula with multiple goals as well. This formula is called the Sidak Correction ([https://en.wikipedia.org/wiki/%C5%A0id%C3%A1k\\_correction](https://en.wikipedia.org/wiki/%C5%A0id%C3%A1k_correction)), by the way.

It's possible your A/B testing tool has this built in, but you should not assume they do the right thing. Most do not.

## Experimenter degrees of freedom

This problem is trickier to fix. Experimenter degrees of freedom come into play when determining  $\{ \text{I exs x} \}$ . When looking for something interesting, one might first try segmenting by browser. When that fails, one might then try segmenting by location, and if that fails by demographic. The first test involves segmenting 5 ways, so the experimenter will plug  $\text{number\_of\_segments}=5$  into the Sidak Correction above. The second test involves 50 segments, so the experimenter plugs  $\text{number\_of\_segments}=50$  into the formula.

Look kosher? It's not.

The problem is that by the time the experimenter finished segmenting by browser,  $\{ \text{I epi eh} \}$   $\{ \text{I eh e 9} \}$   $\{ \text{gl ergi sj w i nk e jepi t swaxi} \}$ . The second segmentation attempt introduced  $\text{er sx i v}$  5% chance of making an error. So the data analyst now has a 10% chance, rather than a 5% chance, of seeing a false positive!

## How to reduce experimenter degrees of freedom

The only way to avoid this problem is to **not** know what you're looking for. Before you look at the data, decide how many segmentation attempts you will make. Ask yourself: "Self, hypothetically, if segmenting by browser doesn't give anything interesting, what will I do next?" Once you've decided this, you must then count the number of segments just to see if you're right.

So in the above example, `number_of_segments = 5 + 50 + 25` (assuming 5 browsers, 50 geographic locations and 25 demographic segments). That's the easy part.

The hard part is to **wait** after you've done it all. At this point, you failed. No matter how you kick the data around, you'll only be obtaining statistically significant results by chance.

Andrew Gelman discusses this in a lot more detail in his article, [The Garden of Forking Paths](http://www.stat.columbia.edu/~gelman/research/unpublished/p_hacking.pdf) ([http://www.stat.columbia.edu/~gelman/research/unpublished/p\\_hacking.pdf](http://www.stat.columbia.edu/~gelman/research/unpublished/p_hacking.pdf)).

## But Google and Amazon make \$ of money by segmenting and personalizing?!?

Google and Amazon have more traffic than you. They've also hired teams of statisticians to help them avoid making these mistakes.

## Conclusion

Lots of people on the internet are suggesting that you should segment your A/B testing data in order to understand things more deeply. Unfortunately, none of these people are telling you how to do it correctly. Segmentation is hard. Most of the time it doesn't give you anything useful. But unless you are very careful, of all the false positive will make it look like segmentation generated a big win.

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## Comments

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Matthew Forr · 4 years ago

Whoa, hold up there.

You started your article off citing two experts and their recommendations on segmentation and then pulled another bloggers article as evidence of why segmentation doesn't go well. If you go back to the first two articles they both argue for a much better segmentation strategy than Ms. Kirrane. Namely, segment based on source, behavior or outcome.

I wouldn't expect to see much of a difference in performance based on geography or location, they're inane ways of segmenting.

Also, your article does a great job of explaining why multiple comparisons can cause problems but that can be fixed by designing your A/B tests to be more directly related to the goal being tested.

Not saying you're totally wrong but it would have been nice if you explored the right way to segment traffic.

^ | v · Reply · Share



stucchio Mod → Matthew Forr · 4 years ago

The main point I'm trying to get across is that a lot of people who segment without being careful will run into far more false positives than real ones. Whether you segment by informative or uninformative characteristics doesn't change this - the point is simply that  $(\# \text{ segments}) \times (p\text{-value cutoff}) = (\# \text{ of false positives})$  unless you use the Sidak correction.

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Michael Chow → stucchio · 4 years ago

That's not true. You're assuming that in all segments the null hypothesis is true. For example, if in every segment the null hypothesis is false, then you will have no false positives. But also, if the null hypothesis is not a point (E.g. Something = 0), and the true value is far away from those in the alternative hypothesis, it might not be far fetched to run many segments without any false positives.

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stucchio Mod → Michael Chow · 4 years ago

Yes, I'm approaching this from a frequentist perspective - I'm computing  $P(\text{positive} | \text{null hypothesis})$ .

You are correct that  $P(\text{positive} \&\& \text{null hypothesis})$  might be different from this - you'd need to do a Bayesian calculation from some prior to find that out. In this more general case, the number of false positives will be approximately  $(p \text{ value cutoff}) \times (\# \text{ of negative segments})$ . So it's true that if  $(\# \text{ of negative segments})$  is low, you won't get many false positives.

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Michael Chow → stucchio · 4 years ago

In the second case I mentioned everything is the null hypothesis, and  $p(\text{positive} | \text{null hypothesis})$  can still be arbitrarily low! For example, if I did a one sample t-test, and was just testing the positive tail, but the true parameter was large in the negative direction.

Sorry, I don't mean to nit pick. Your comment just reminded me of the (important) fringe cases :).

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stucchio Mod → Michael Chow · 4 years ago

No worries. The main theme of this blog is nitpicking the details. The only thing that is forbidden here is platitudes and vague generalities. :)

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William Högman · 4 years ago

Thanks for raising such an important point. Loads of practitioners probably just plug their data into calculators on the web without knowing the statistics behind it, shame really.

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