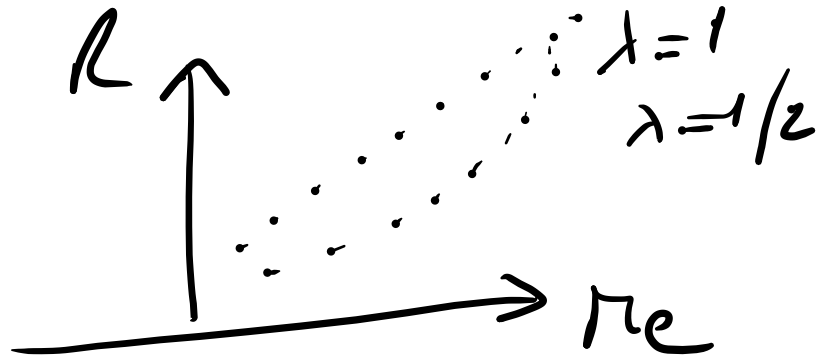


ROW - MEDIAN

$\hookrightarrow R =$

$\nearrow$  ROW  
 $\searrow$  MEDIAN

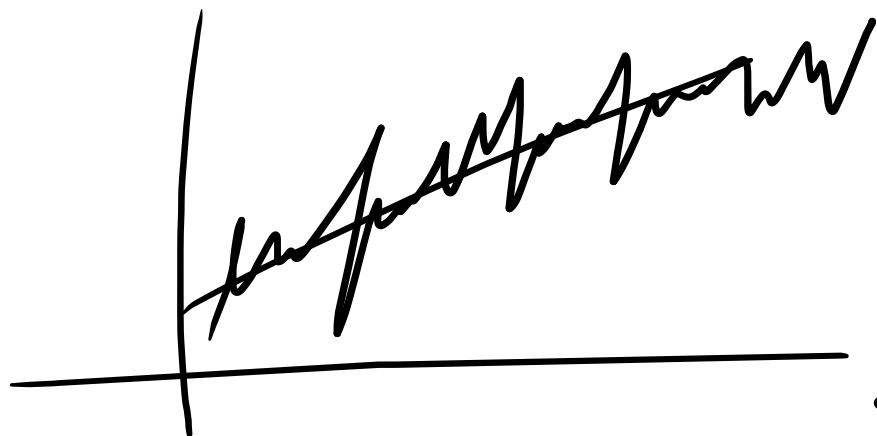
SUBCOLUMNS  $\rightarrow$  R series



no  
ESTACIONARIOS EN LA MEDIA

↳  $E[Y_t]$  no es constante

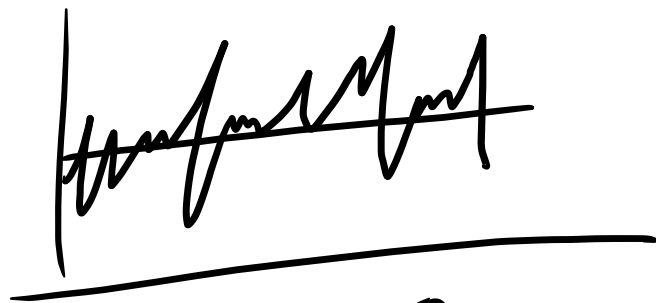
- i) Tendencias determinísticas
- ii) Tendencias estocásticas



TSP  
Trend  
stationary  
process

$$Y_t = \underbrace{\alpha + \beta t}_{f(t)} + \phi_1 Y_{t-1} + \epsilon_t$$

$|\phi_1| < 1$



$$\hat{T}(t) = \alpha + \hat{\beta} t \rightarrow \hat{y}_t = y_t - \hat{T}_t$$

$y_t \rightarrow \text{lin (Linear model)}$

$$y_t \sim t.t$$

Tendencias  
Estocásticas → Assumptions  
stocks no  
convergentes

Random Walk

$$Y_t = Y_{t-1} + \epsilon_t$$

$$t=1 \quad Y_1 = \underline{Y_0 + \epsilon_1}$$

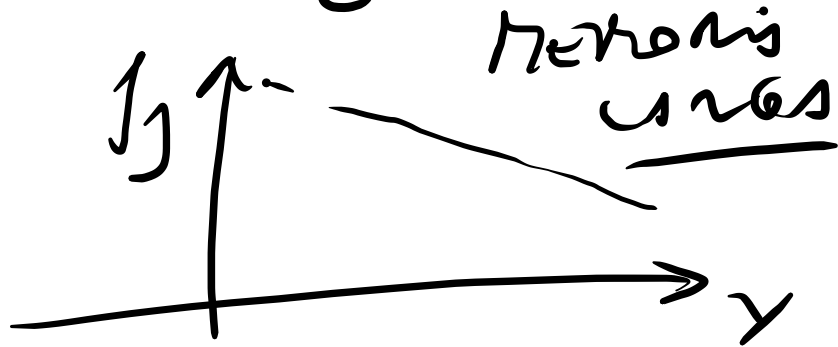
$$t=2 \quad Y_2 = Y_1 + \epsilon_2 = Y_0 + \epsilon_1 + \epsilon_2$$

$$Y_t = \underline{Y_0} + t \sum_{j=1}^t \varepsilon_j$$

~~Corresponding~~

$$E[Y_t] = Y_0$$

$$\text{Var}(Y_t) = t \cdot \sigma_\varepsilon^2$$



$$Y_t = Y_{t-1} + \varepsilon_t$$

$$Y_t - Y_{t-1} = \varepsilon_t$$



$$\nabla Y_t = \varepsilon_t$$

$$E(\nabla Y_t) = 0$$

$$\text{Var}(\nabla Y_t) = \sigma^2_\varepsilon$$



Wird  
benutzt



Estimation

- (1)  $Y_t = \alpha + \beta t + \phi_1 \cdot Y_{t-1} + \epsilon_t$

$$\nabla Y_t = Y_t - Y_{t-1}$$

$$(2) Y_{t-1} = \alpha + \beta \cdot (t-1) + \phi_1 \cdot Y_{t-2} + \epsilon_{t-1}$$

$$(1) - (2) \rightarrow \nabla Y_t = \beta \cdot (\cancel{t} - \cancel{t} + 1) + \phi_1 \cdot (\underbrace{Y_{t-1} - Y_{t-2}}_{\nabla Y_{t-1}}) + \underbrace{(\epsilon_t - \epsilon_{t-1})}_{\downarrow \text{MA}(1) \text{ INU.}}$$



$$Y_t: I(1)$$



INTEGRAL of order 1

$$\int_a^b f(x) dx$$

→ INTEGRAL

$$\lim \sum f(x)$$

→ SUM

transmission  $\rightarrow I(\omega)$

$$\phi_1 = 0.59$$



$$\frac{\text{Value Not  
Resort}}{\text{Value Not  
Resort}} = \frac{\text{Value Not  
Resort}}{\text{Index (Adjusted)}}$$

Sum (\$)\$ → Result

# SARIMA (p, d, q)

$$\underbrace{(1 - \phi_1 B - \phi_2 B^2 - \dots - \phi_p B^p)}_{\text{red}} \underbrace{(1 - B)^d}_{\text{yellow}} Y_t = \phi_0 + \underbrace{(1 - \theta_1 B - \theta_2 B^2 - \dots - \theta_q B^q)}_{\text{green}} \epsilon_t$$


$$\underbrace{\Phi(B) (1 - B)^d}_{z_t} Y_t = \phi_0 + \Theta(B) \epsilon_t$$

$$(1 - B)^d \equiv \nabla^d \rightarrow$$

$$(1 - B) = \nabla$$

$$z_t : \text{ARIMA}(p, q)$$

$$\nabla Y_t : I(d)$$

$$ARIMA(p, 0, q) \equiv ARMA(p, q)$$


$X_t: ARIMA(0, 1, 0) \rightarrow$  random  
walk

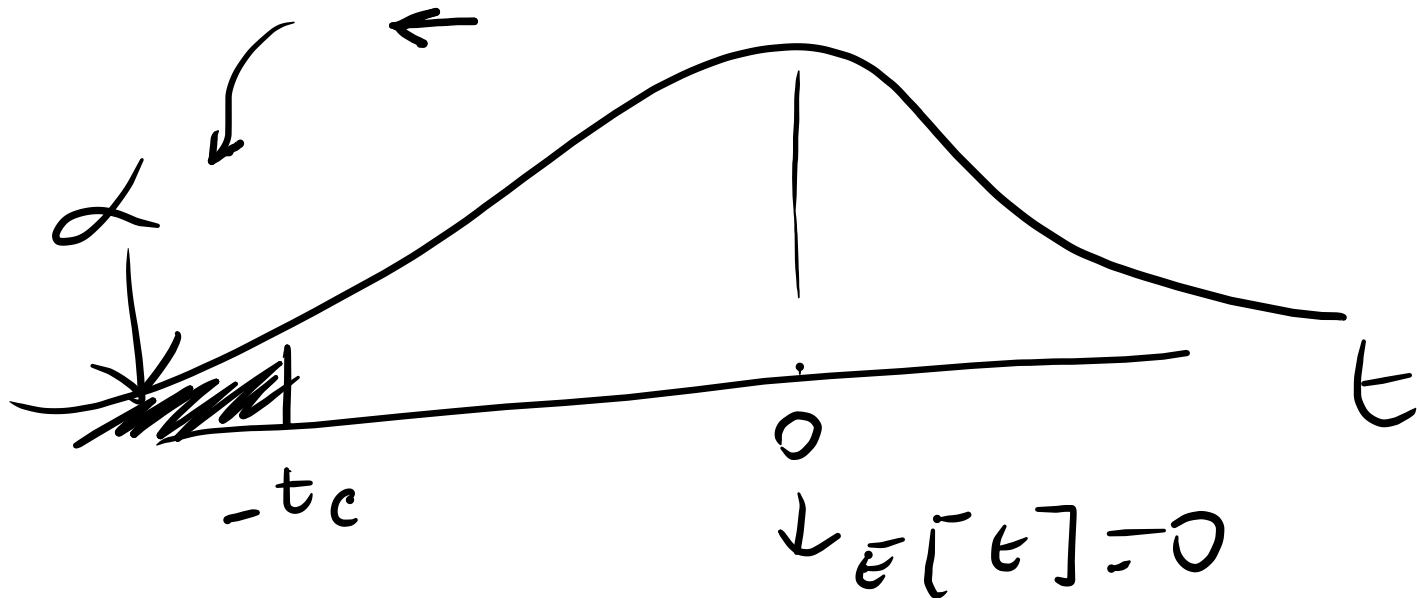
$\nabla X_t: ARIMA(0, 0, 0) \rightarrow$  white  
noise

$$\text{ANMA}(3, 0, 0) \equiv \text{AN}(3)$$

$$\text{ANMA}(0, 0, 3) \equiv \underline{\underline{\text{MA}(3)}}$$

$$H_0: \phi_1 = 1 \rightarrow \phi_1 - 1 = 0 \quad \varepsilon_1 \sim \omega \sim \omega$$

$$H_1: \phi_1 < 1 \quad \varepsilon_1 \sim \omega \sim \omega$$



$$Y_t = \phi_1 Y_{t-1} + \varepsilon_t \quad \text{AR}(1)$$

$$\nabla Y_t = (\phi_1 - 1) Y_{t-1} + \varepsilon_t$$

EC . Dickey Fuller

$$H_0: \phi_1 - 1 = 0 \quad I(1)$$

$$H_1: \phi_1 - 1 < 0 \quad I(0)$$





$$\frac{An(2)}{Y_t} = \underbrace{\phi_1}_{\substack{\downarrow \\ (\phi_1 + \phi_2)}} Y_{t-1} + \underbrace{\phi_2}_{\text{green}} Y_{t-2} + \epsilon_t$$


$$+ \underbrace{\phi_2}_{\text{blue}} Y_{t-1} - \underbrace{\phi_2}_{\text{green}} Y_{t-1}$$

$$Y_t = (\phi_1 + \phi_2) Y_{t-1} - \phi_2 (\overbrace{Y_{t-1} - Y_{t-2}}^{\nabla Y_{t-1}})$$

$$\nabla Y_t = \underbrace{(\phi_1 + \phi_2 - 1)}_{\phi_1^*} Y_{t-1} + \dots + \epsilon_t$$

~~H<sub>0</sub>~~: - - - I(3)

H<sub>1</sub>: - - -  $\begin{cases} I(2) \\ I(1) \\ I(0) \end{cases}$



H<sub>0</sub>: - - - I(2)  
H<sub>1</sub>: - - -  $\begin{cases} I(1) \\ I(0) \end{cases}$

