

MATHEMATICS

Linear Algebra II

# Eigenvalues and Eigenvectors

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#### Chapter 1

## Eigenvalues and Eigenvectors

#### 1.1 The vector space of linear combinations

Let  $\mathcal{T}$  be the set of all linear transformations from V into W, and let  $L(V, W) = \{T | T \in \mathcal{T}\}$ , then L(V, W) is a vector space where its operations are defined as:

• Vector addition. Let  $T_1, T_2 \in L(V, W)$  then for every  $v_1 \in V$ 

$$(T_1 + T_2)(v_1) = T_1(v_1) + T_2(v_1)$$

• Scalar multiplication. Let  $T \in L(V, W)$  and let  $\alpha \in F$ , then for all  $v_1 \in V$ 

$$(\alpha T)(v_1) = \alpha T(v_1)$$

#### 1.2 Eigenvalues and Eigenvectors