

2.1

$$\text{let } w^T x = w_1 x + w_2 x$$

$$h(w^T x_i + b) = \frac{1}{1 + e^{-w_1 x - w_2 x - b}}$$

$$L(v, b) = -\frac{1}{M} \sum_{i=1}^M \left[y_i \log \left(\frac{1}{1 + e^{-w_1 x - w_2 x - b}} \right) + (1 - y_i) \left(\log \left(1 - \frac{1}{1 + e^{-w_1 x - w_2 x - b}} \right) \right) \right]$$

$$\text{let } U_i = \frac{1}{1 + e^{-w_1 x - w_2 x - b}} \quad \frac{\partial U_i}{\partial w_1} = \frac{x e^{-b - w_2 x - w_1 x}}{(e^{-b - w_2 x - w_1 x} + 1)^2}$$

$$\frac{\partial U_i}{\partial w_2} = \frac{x e^{-b - w_2 x - w_1 x}}{(e^{-b - w_2 x - w_1 x} + 1)^2}$$

$$\frac{\partial v}{\partial b} = \frac{e^{b + w_1 x + w_2 x}}{(e^{b + w_1 x + w_2 x} + 1)^2}$$

$$\frac{\partial L}{\partial w_1} = -\frac{1}{M} \sum_{i=1}^M \left[y_i \log(u) + (1 - y_i) (\log(1 - u)) \right]$$

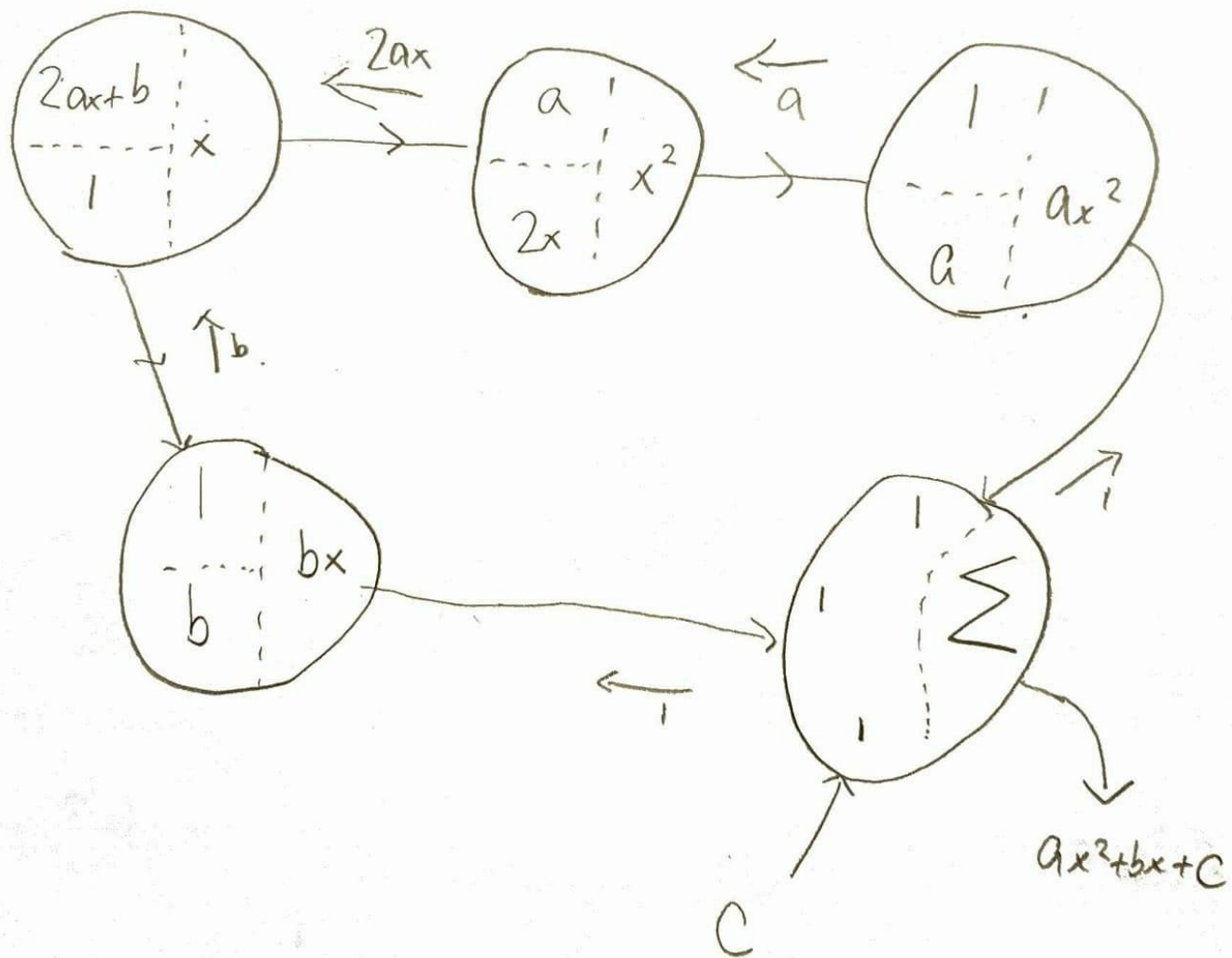
$$\frac{\partial L}{\partial u_i} = -\frac{1}{M} \sum_{i=1}^M \left[\frac{y_i}{u} + \frac{(1 - y_i)}{u - 1} \right]$$

$$\frac{\partial L}{\partial w_1} = \frac{\partial L}{\partial u_i} \cdot \frac{\partial u_i}{\partial w_1} = -\frac{1}{M} \sum_{i=1}^M \left[\frac{y_i (e^{-b - w_2 x - w_1 x} + 1)}{x e^{-b - w_2 x - w_1 x}} + \frac{(1 - y_i) (e^{-b - w_2 x - w_1 x} + 1)}{x e^{-b - w_2 x - w_1 x} - (e^{-b - w_2 x - w_1 x} + 1)} \right]$$

$$\frac{\partial L}{\partial w_2} = \frac{\partial L}{\partial u_i} \cdot \frac{\partial u_i}{\partial w_2} = -\frac{1}{M} \sum_{i=1}^M \left[\frac{y_i (e^{-b - w_2 x - w_1 x} + 1)}{x e^{-b - w_2 x - w_1 x}} + \frac{(1 - y_i) (e^{-b - w_2 x - w_1 x} + 1)^2}{x e^{-b - w_2 x - w_1 x} - (e^{-b - w_2 x - w_1 x} + 1)^2} \right]$$

$$\frac{\partial L}{\partial b} = \frac{\partial L}{\partial v} \cdot \frac{\partial v}{\partial b} = -\frac{1}{M} \sum_{i=1}^M \left[\frac{y_i (e^{b + w_1 x + w_2 x} + 1)^2}{e^{b + w_1 x + w_2 x}} + \frac{(1 - y_i) (e^{b + w_1 x + w_2 x} + 1)^2}{e^{b + w_1 x + w_2 x} - e^{b + w_1 x + w_2 x} + 1} \right]$$

2.2



2.3/2.4

