

# PA 446

Coding for Civic Data Applications

Will be starting at 6:05pm

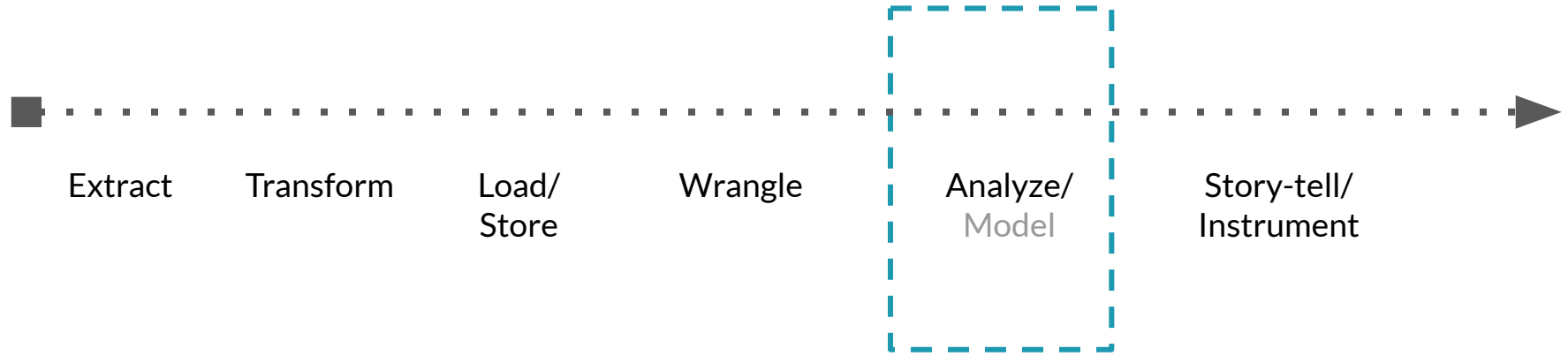
# Class #6

Logistics

# Course Logistics

- HW 4
  - Due 10/20
  - Available end of week
- HW 3, graded by EOW
- Midterm
  - Similar format as HW4
  - With a tighter time limit

# Data Science “workflow”



Focus next 3 weeks

# Where We Been: Gender Data

1. Two variable comparison
2. Two variable significance testing

# What We Found: Gender Data

Dept	Difference Between Female and Male Salaries	Female Salary Averages	Male Salary Averages
POLICE	-4834.963677	87338.2753	92173.239
FIRE	-2537.510887	103619.36	106156.871
STREETS & SAN	-7476.160747	68309.8452	75786.006
WATER MGMNT	-11322.18714	86732.6581	98054.8453
AVIATION	-9040.943804	73139.6085	82180.5523

# How Confident Were We: Gender Data

Discuss

# How Confident Were We: Gender Data

Dept	Difference Between Female and Male Salaries	Female Salary Averages	Male Salary Averages	p.value	alternative
POLICE	<b>-4834.963677</b>	87338.2753	92173.239	<b>1.96E-38</b>	two.sided
FIRE	<b>-2537.510887</b>	103619.36	106156.871	<b>0.03008956</b>	two.sided
STREETS & SAN	<b>-7476.160747</b>	68309.8452	75786.006	<b>1.54E-08</b>	two.sided
WATER MGMNT	<b>-11322.18714</b>	86732.6581	98054.8453	<b>2.92E-24</b>	two.sided
AVIATION	<b>-9040.943804</b>	73139.6085	82180.5523	<b>3.02E-11</b>	two.sided



# Takeaways: Gender Data

So What	Next Steps

# Where We Been: Race Data

1. Multiple variable comparison
2. Multiple variable significance testing

## Where We Been: Race Data

Department	api	black	hispanic	white	NA
AVIATION	89023	63501	76966	82891	77932
FIRE	90779	99732	99272	107545	106035
POLICE	85783	90703	86518	93484	90574
STREETS & SAN	66412	68870	72859	74037	72828
WATER MGMNT	94739	92964	93684	97413	96131

# How Confident Were We: Race Data

Discuss

# Where We Been: Race Data

[to coding]

## How Confident Were We: Race Data

Department	api	black	hispanic	white	NA	p.value
AVIATION	89023	63501	76966	82891	77932	5.19E-06
FIRE	90779	99732	99272	107545	106035	1.58E-11
POLICE	85783	90703	86518	93484	90574	3.37E-52
STREETS & SAN	66412	68870	72859	74037	72828	0.029837 002
WATER MGMNT	94739	92964	93684	97413	96131	0.000458 519

## How Confident Were We: Race Data

Department	api	black	hispanic	white	NA	p.value
AVIATION	89023	63501	76966	82891	77932	5.19E-06
FIRE	90779	99732	99272	107545	106035	1.58E-11
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# Takeaways: Race Data

So What	Next Steps



# Takeaways: Race Data

What Can We Do?

# In Order to Say Anything About 1 Race Relative to Another

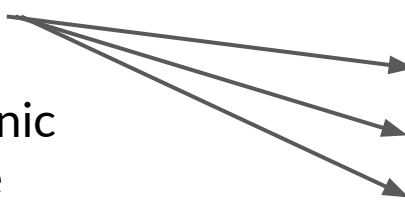
Department	api	black	hispanic	white	NA	p.value
AVIATION	89023	63501	76966	82891	77932	5.19E-06

**Salary Averages**

api  
black  
hispanic  
white

**Salary Averages**

api  
black  
hispanic  
white



# In Order to Say Anything About 1 Race Relative to Another

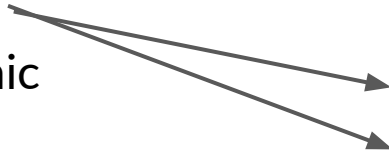
Department	api	black	hispanic	white	NA	p.value
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**Salary Averages**

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black  
hispanic  
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**Salary Averages**

api  
black  
hispanic  
white

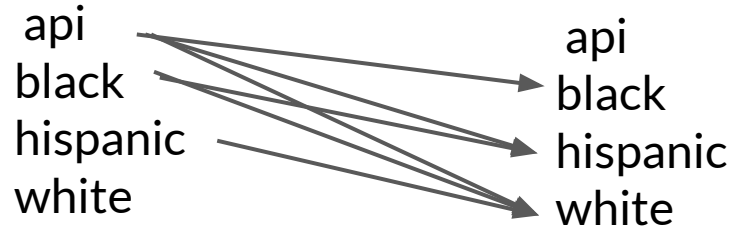


# In Order to Say Anything About 1 Race Relative to Another

Department	api	black	hispanic	white	NA	p.value
AVIATION	89023	63501	76966	82891	77932	5.19E-06

Salary Averages

Salary Averages



**Number of tests :  $(3+2+1) * \text{\# of Departments} = 30$  tests**

**A lot of work + error prone**

# In Order to Say Anything About 1 Race Relative to Another

What Can We Do?

# In Order to Say Anything About 1 Race Relative to Another

## What Can We Do?

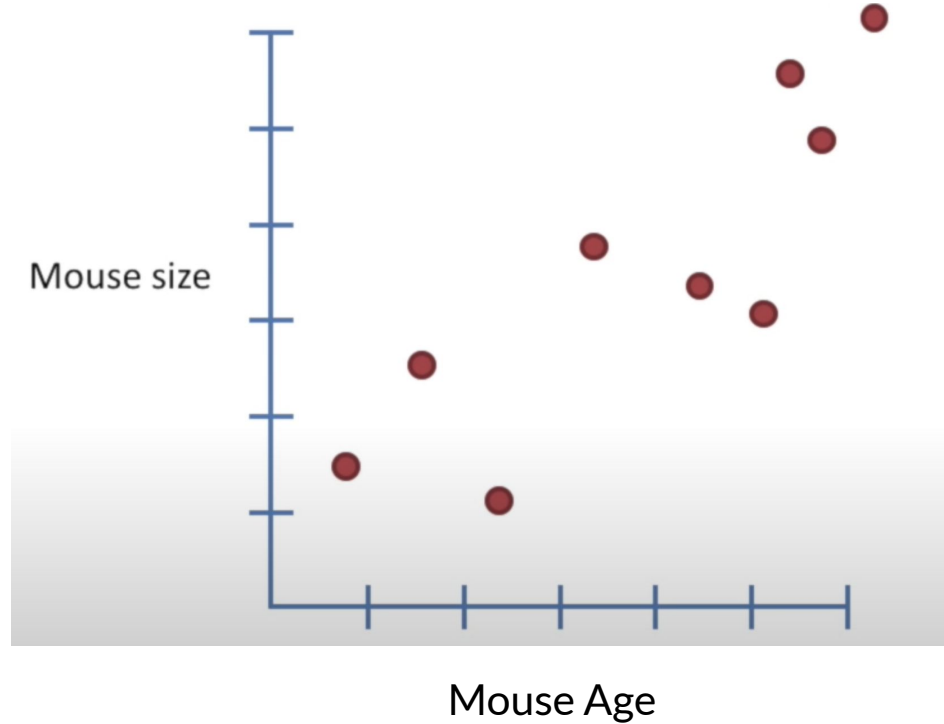
- Clarify scope with the client and compare less variables
- Use linear regressions

# Linear Regression



# Basic Linear Regression

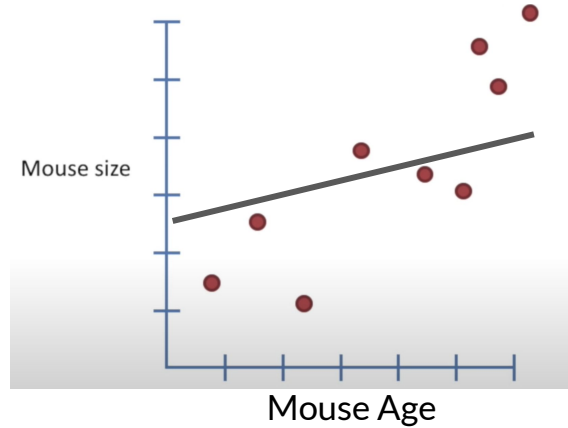
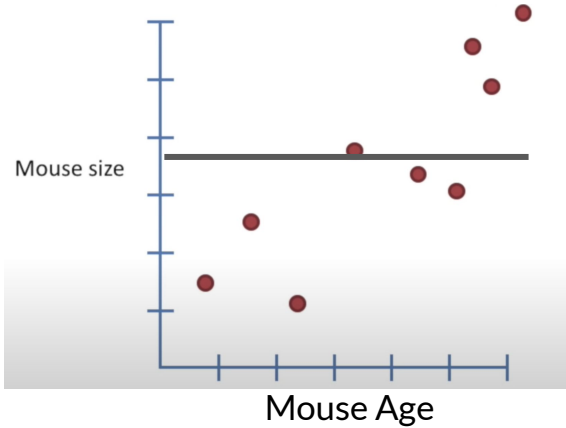
## Purpose



How does change in Mouse age impacts Mouse Size?

# Basic Linear Regression

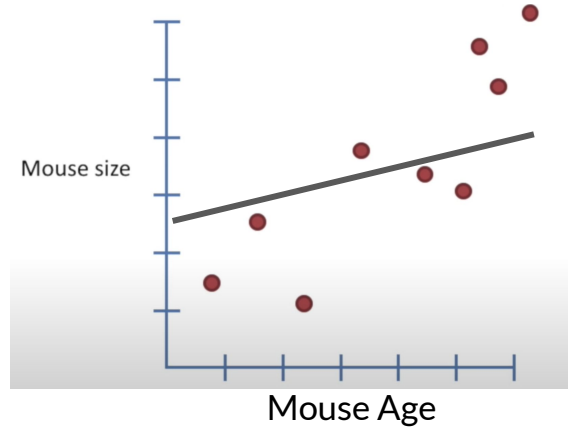
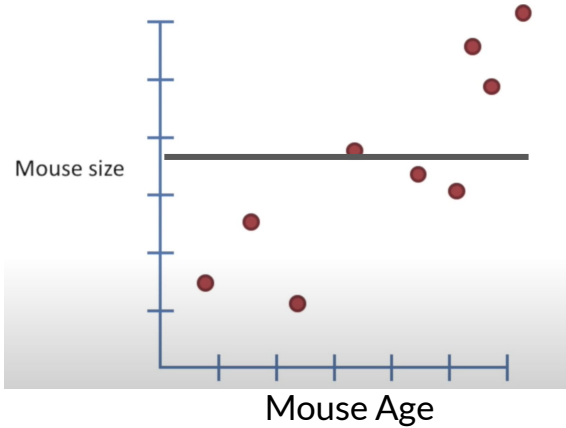
## Finding a Line Best Fit



A lot of compute power is used testing out different lines and slopes until the line best fitted to our data is determined

# Basic Linear Regression

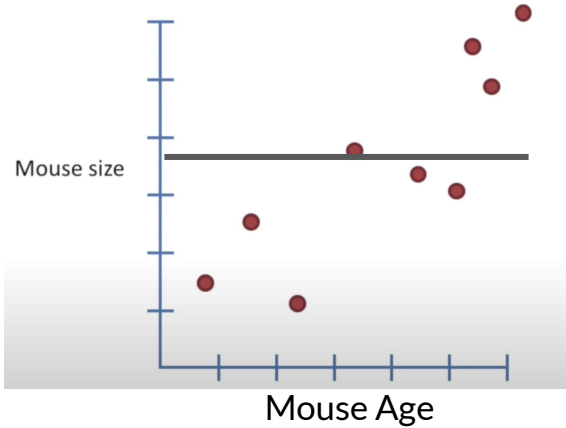
Described in Equation Form



$$y = \text{slope} * X + \text{constant (y-intercept)}$$

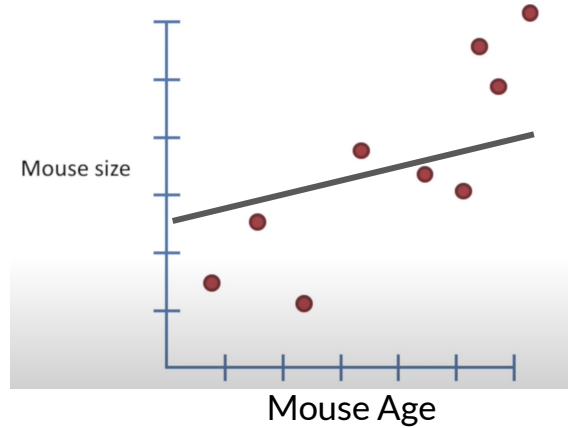
# Basic Linear Regression

Finding Relationships Between X and Y

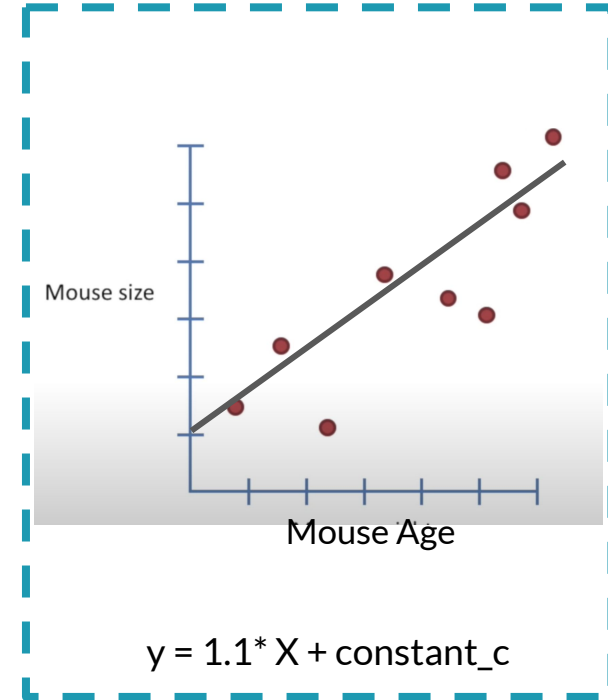


$$y = 0 * X + \text{constant\_a}$$

y = Mouse Size      X = Mouse Age



$$y = 0.5 * X + \text{constant\_b}$$



$$y = 1.1 * X + \text{constant\_c}$$

Constant = y-intercept

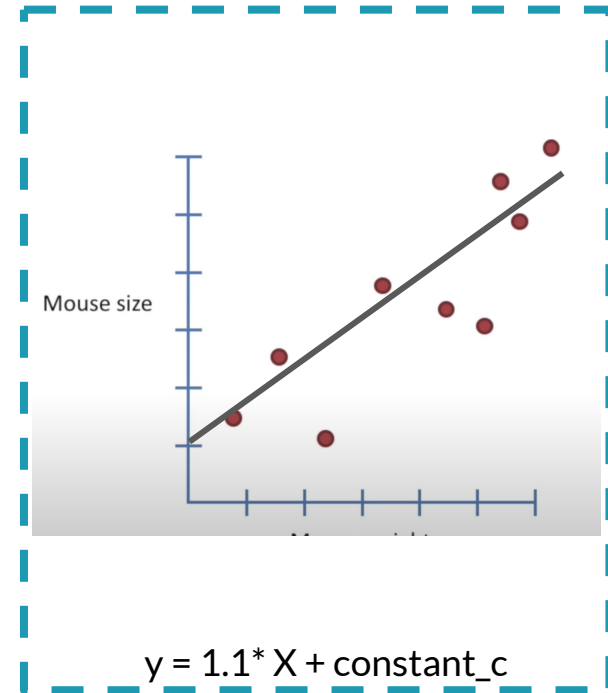
# Basic Linear Regression

## Interpreting the Formula

$$y = 1.1 * X + \text{constant\_c}$$

$1.1 * X$ : a 1 unit increase in mouse age is correlated with a 1.1 unit increase in mouse size

$\text{constant\_c}$ : at age 0, a mouse has size 1



# New Question

Within the Same Sample, Another Variable Impacts Size

$y$  = Mouse Size

$X_2$  = Whether the mouse received gene therapy (Control vs Mutant)

Now what you want to know is **how gene therapy impacts the size of the mouse**

# New Question

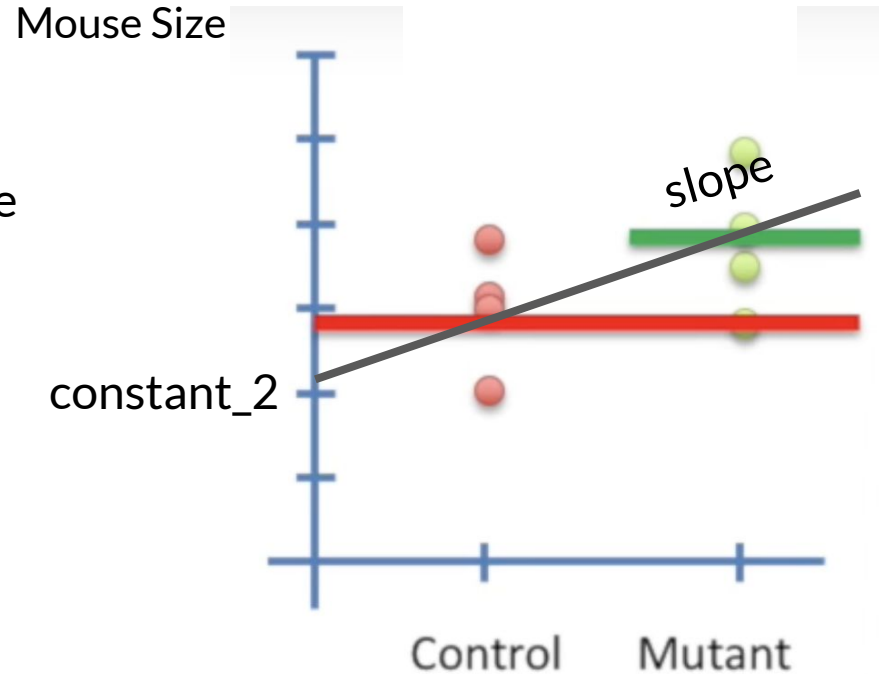
Within the Same Sample, Another Variable Impacts Size

$y = \text{Mouse Size}$

$X_2 = \text{Whether the mouse received gene therapy}$

$X_2$  is a categorical variable (Control or Mutant). How do you represent it in the linear regression equation?

$$Y = \text{slope} * X_2 + \text{constant}_2$$



# Categorical X Values Must be Converted to “Dummy” Vars

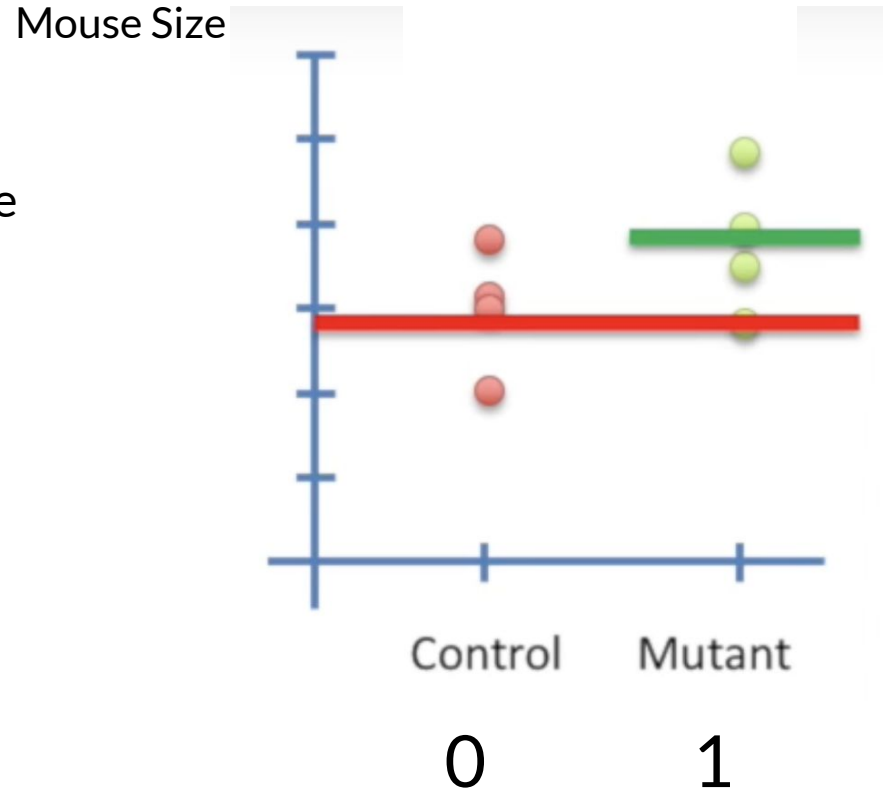
Control or Mutant → 1 or 0

$y = \text{Mouse Size}$

$X_2 = \text{Whether the mouse received gene therapy}$

When  $X_2=0$ ,  $Y = \text{slope} * 0 + \text{constant}_2$

When  $X_2=1$ ,  $Y = \text{slope} * 1 + \text{constant}_2$





# New Question

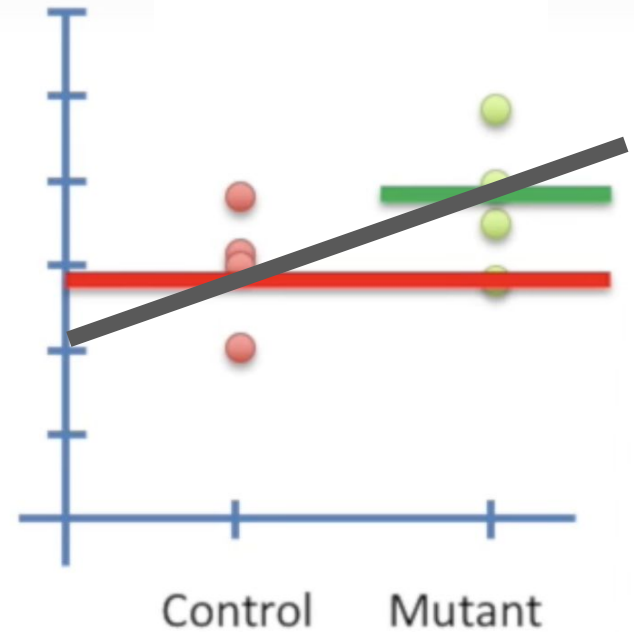
## Another Linear Regression

$y = \text{Mouse Size}$

$X_2 = \text{Whether the mouse received gene therapy}$

$Y = 0.5 * X_2 + \text{constant}_2$

Mouse Size



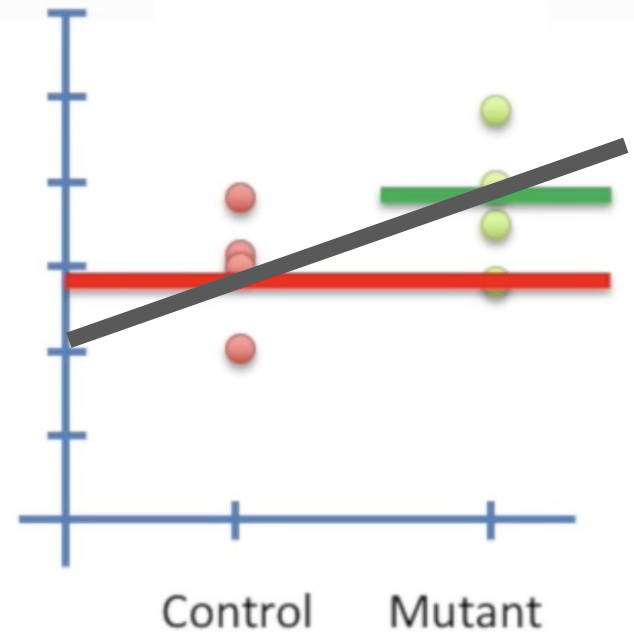
# New Question

## Complications

You just determined the relationship between gene therapy and mouse size ( $Y = 0.5 * X_2 + \text{constant}_2$ ).

But remember, you are using the same sample as before. What might you have overlooked?

Mouse Size

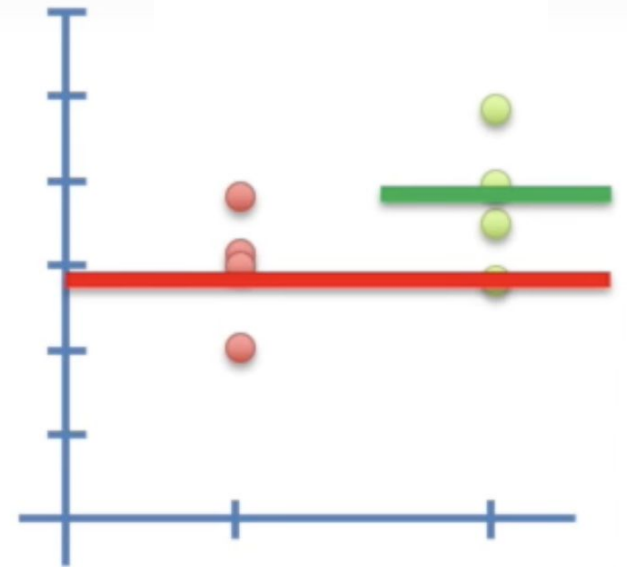


# New Question

## How to Control for Age?

Is there some way to control for age, when comparing the mouse size of control and mutant mice?

Mouse Size



Control

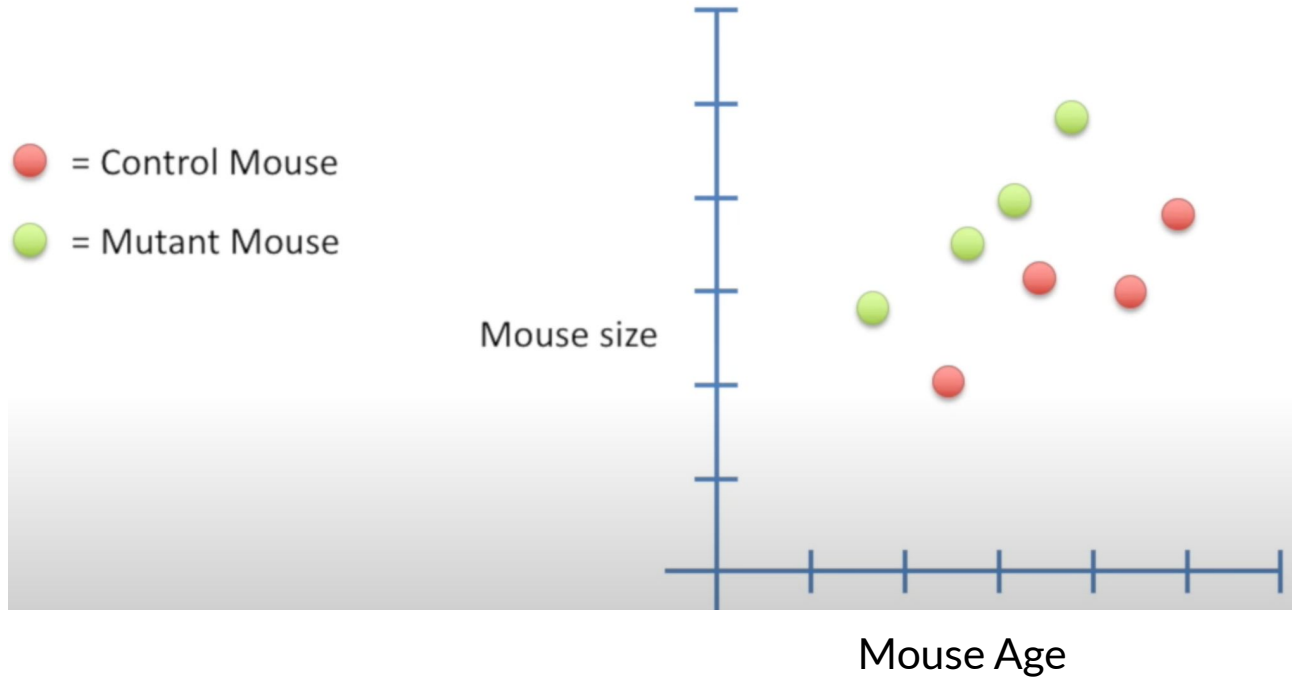
Mutant

0

1

# Multiple Regression

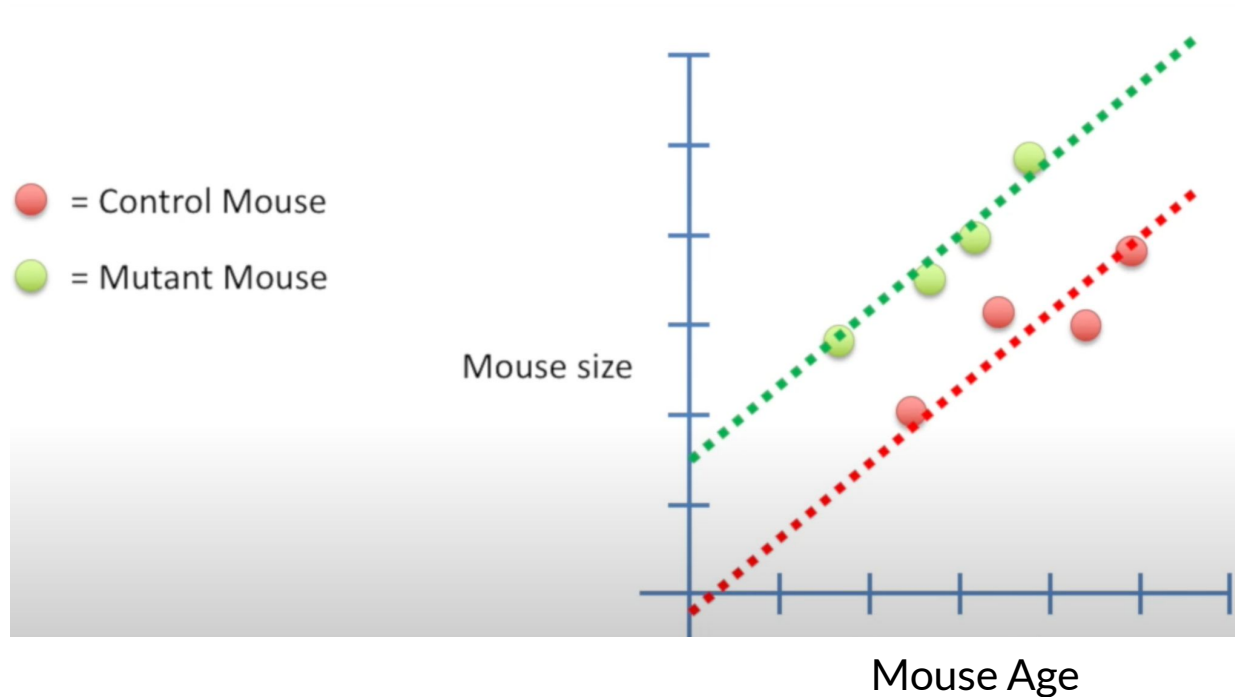
Finding Relationships Between X and Y, Controlling for X2



What relationship do you see?

# Multiple Regression

Finding Relationships Between X1, X2 and Y



## ➤ Formula

$$y = 1.1 * \text{Mouse age} + 0.5 * \text{Mutant mouse} + \text{constant}$$

Interpretation:  
Mutant mice are 0.5 size larger than control mouse, **controlling for mouse age**

A 1 unit increase in mouse age is correlated with a 1.1 unit increase in mouse size, **controlling for the mouse' gene status**

# Multiple Regression

Finding Relationships Between  $X_1$ ,  $X_2$  and  $Y$

Linear regressions works for numeric  $X$ 's and/or categorical  $X$ 's

Let's try 1 more time with exclusively categorical  $X$ 's: mice gene therapy and gender

## Multiple Binary Variables: Control v Mutant

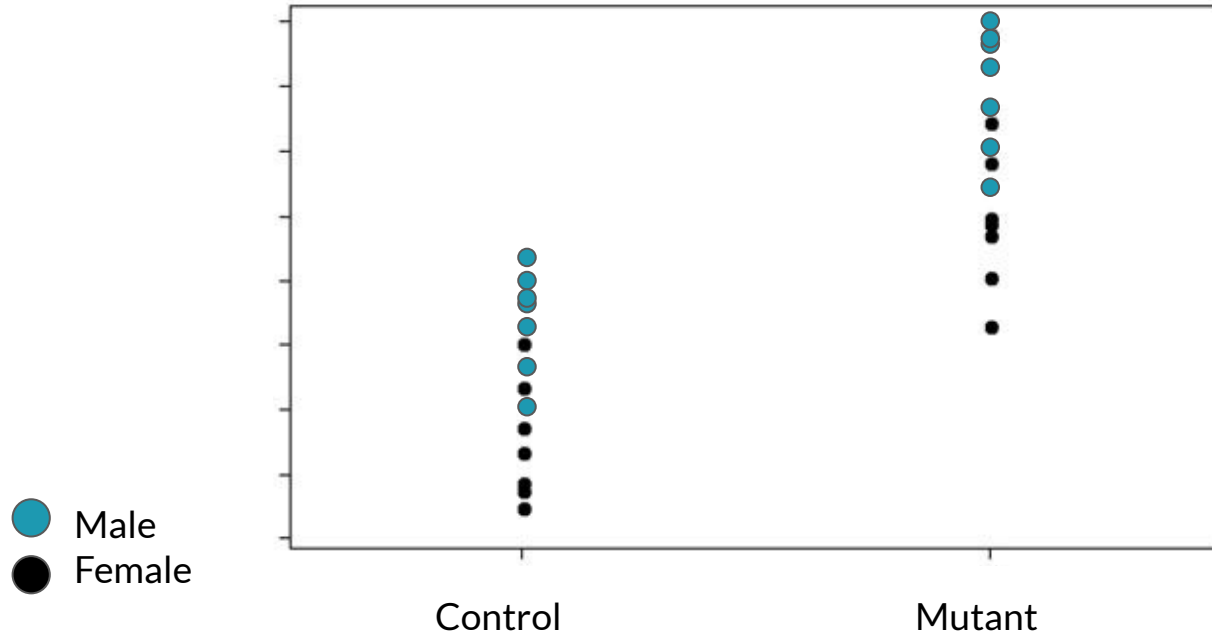
Mutant

39

# Multiple Regression: Categorical

Multiple Binary Variables: Control v Mutant and Male v Female

Mouse Size

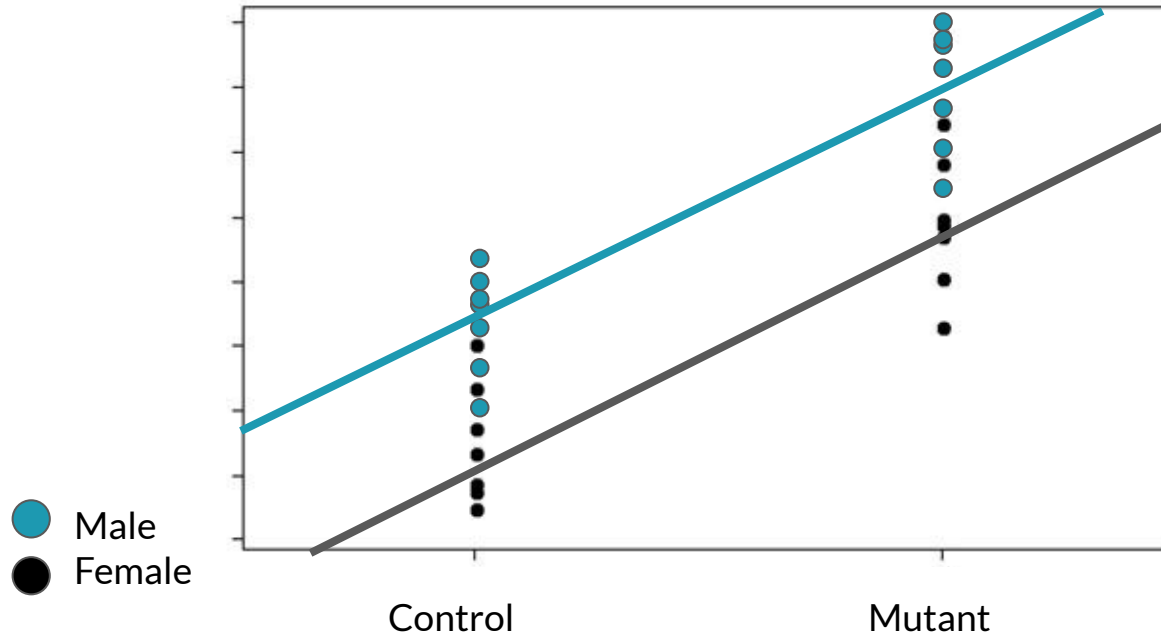




# Multiple Regression

Multiple Binary Variables: Control v Mutant and Male v Female

Mouse Size



➤ Final Formula

$$y = 1.5 * \text{Mutant mouse} + 2 * \text{gender} + \text{constant}$$

Interpretation:  
Male mice are 2 sizes larger than female mice, controlling for gene status

Mutant mice are 0.5 sizes larger than control mice, controlling for gender

**10-minute break, be  
back by 7:15pm**

# How Does This Help with Our Problem with Race?

## Discuss

<b>Mouse Size</b>	Gender (1= M, 0=F)	gene type (1=Mutant, 0 = Control)	mouse age
<b>4</b>	1	1	2.4
<b>3.6</b>	1	0	1.5
<b>6</b>	0	0	3.0
<b>4.8</b>	0	1	3.8
<b>5</b>	1	1	5.1
<b>3</b>	0	0	2.2

<b>Salary</b>	Department	race	gender
<b>118998</b>	POLICE	white	M
<b>109662</b>	FIRE	black	M
<b>121272</b>	DAIS	NA	NA
<b>119712</b>	WATER MGMNT	API	M
<b>92352</b>	TRANSPORT	hispanic	M
<b>72510</b>	POLICE	NA	F

I omitted name and job title

# Wrangling Needed Before Running a Regression

## Discuss

- 1.

# Generating Dummy Variables

## Discuss

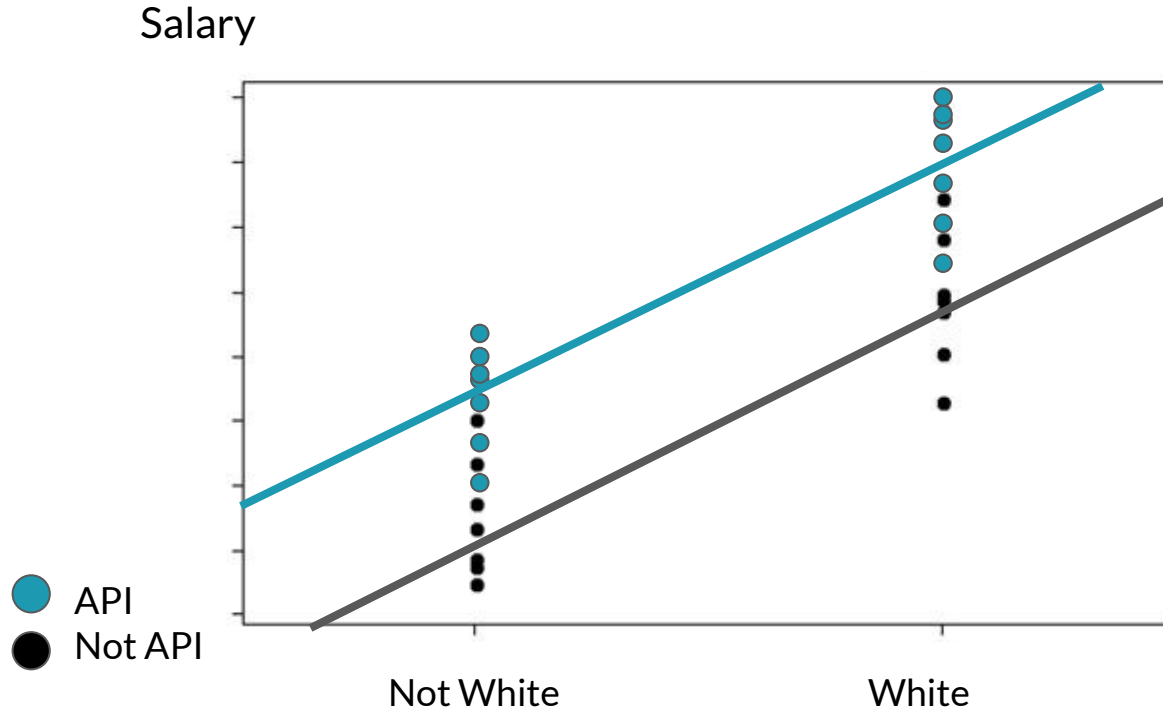
race
white
black
white
API
hispanic
NA



race_white	race_black	race_api	race_hispanic	race_aian
1	0	0	0	0
0	1	0	0	0
1	0	0	0	0
0	0	1	0	0
0	0	0	1	0
0	0	0	0	0

# Multiple Regression

What If We Isolated to Only White and API



➤ Final Formula

Much harder to visualize multiple regressions after 2 variables because you will need a 3D space

# Data Quality Checks for Linear Regressions

NA's Are Usually Bad

1. Impute (average, median etc)
2. Remove the NA rows
3. Remove the columns with NAs

# Data Quality Checks for Linear Regressions

No categorical variables for linear regression

All numerics

- Dummy (1's and 0's) - remember to exclude 1 category, otherwise you have collinearity
- Doubles (any numbers)



# Applying to Race Data

# Data Quality Checks for Linear Regressions

No categorical variables for linear regression

All numerics

- Dummy (1's and 0's) - remember to exclude 1 category, otherwise you have collinearity
- Doubles (any numbers)

# Regression Results: Aviation Department

term	estimate	std.error	statistic	p.value
(Intercept)	83247.2	1064.9	78.2	0.00
final_race_two_api	6283.4	4665.3	1.3	0.18
final_race_two_black	-12266.4	2799.8	-4.4	0.00
final_race_two_hispanic	-6127.9	1692.4	-3.6	0.00

Interpretation:

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Interpretation: the average salary of final\_race\_two\_white = 1

# Regression Results

term	estimate	std.error	statistic	p.value
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final_race_two_api	6283.4	4665.3	1.3	0.18
final_race_two_black	-12266.4	2799.8	-4.4	0.00
final_race_two_hispanic	-6127.9	1692.4	-3.6	0.00

Interpretation: the average salary of final\_race\_two\_api = 1 is \$6283.4 higher than final\_race\_two\_white = 1. The result is not statistically significant at 95% confidence level

# Data Quality Checks for Linear Regressions

No categorical variables for linear regression

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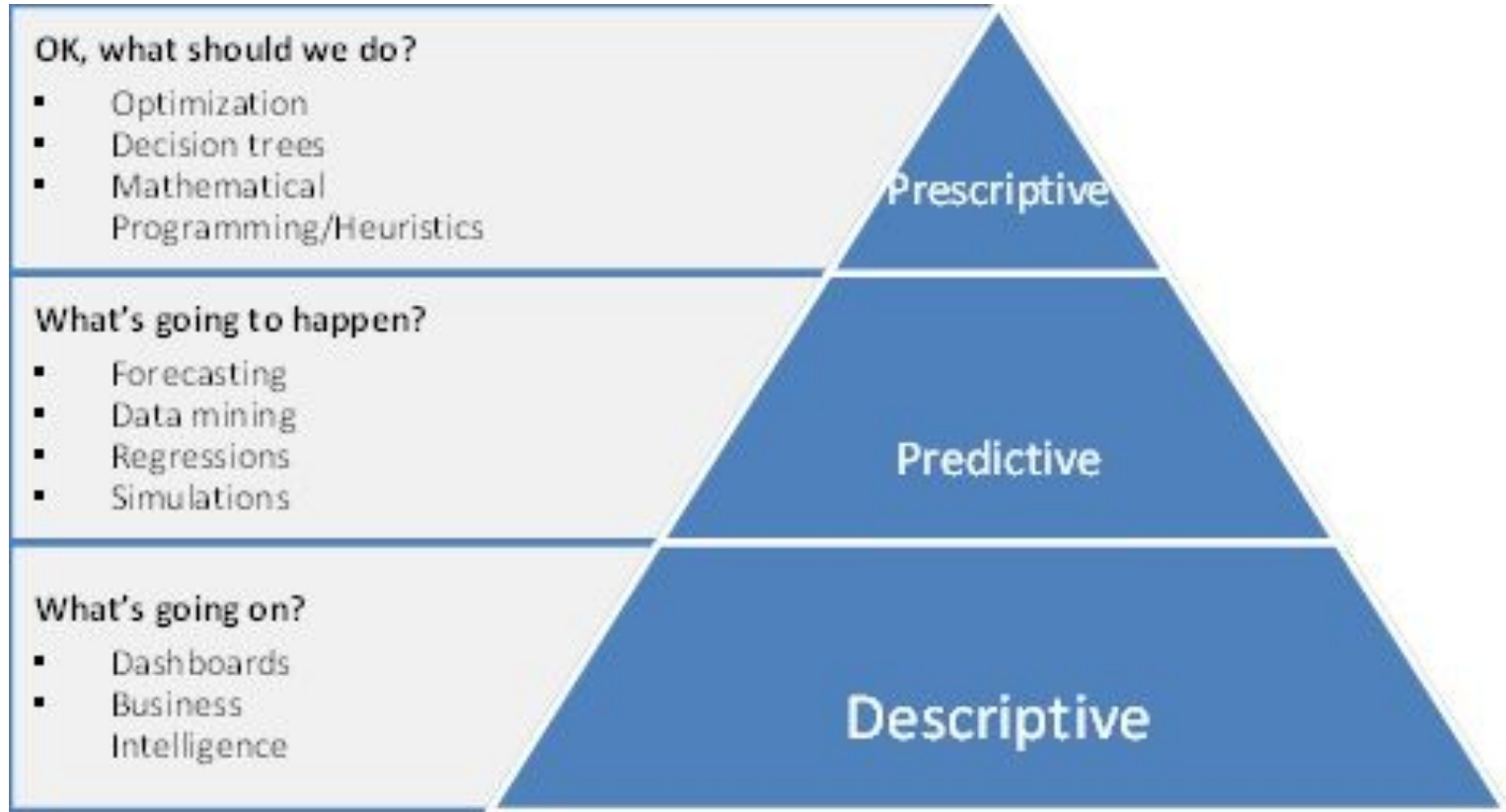
Descriptive

Predictive

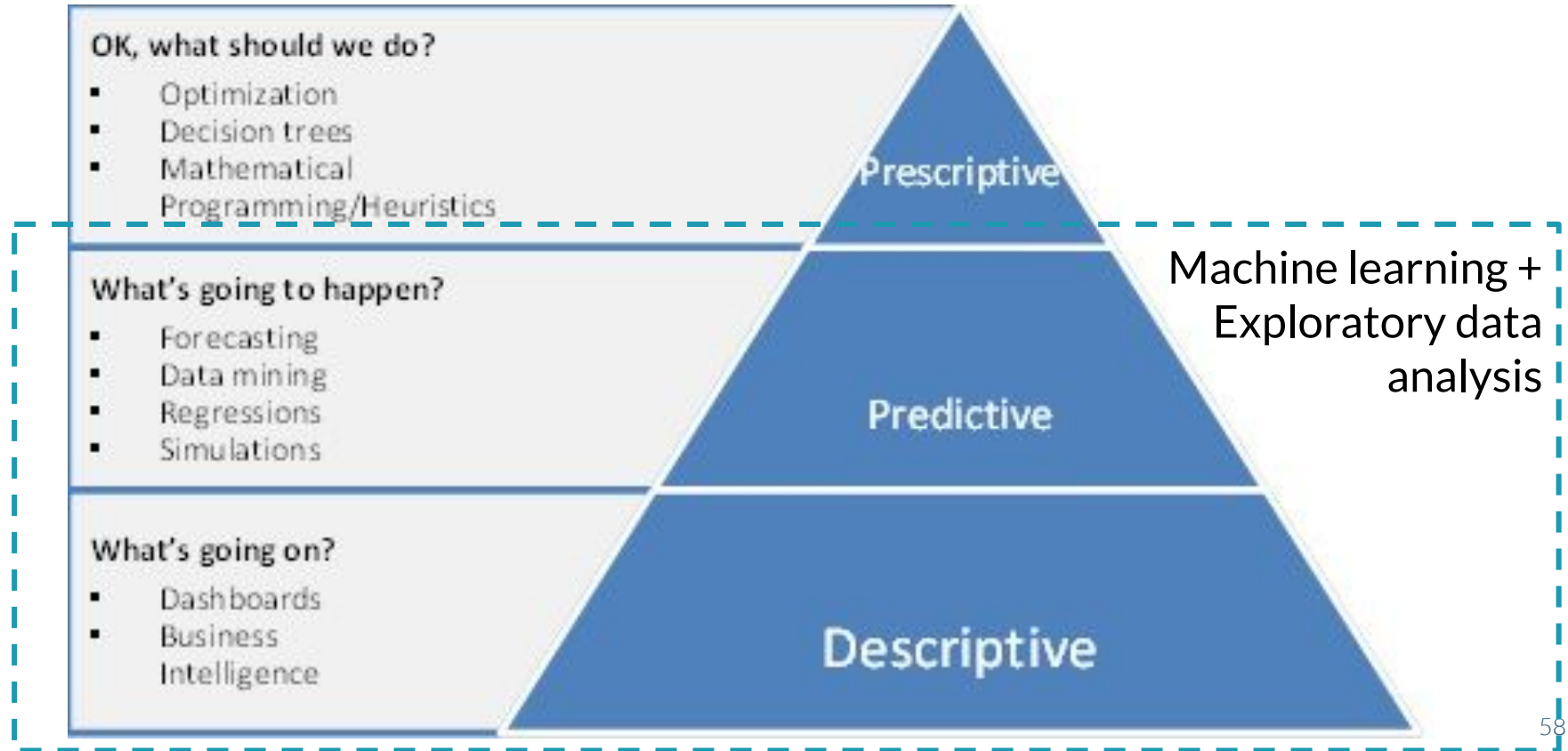
Prescriptive



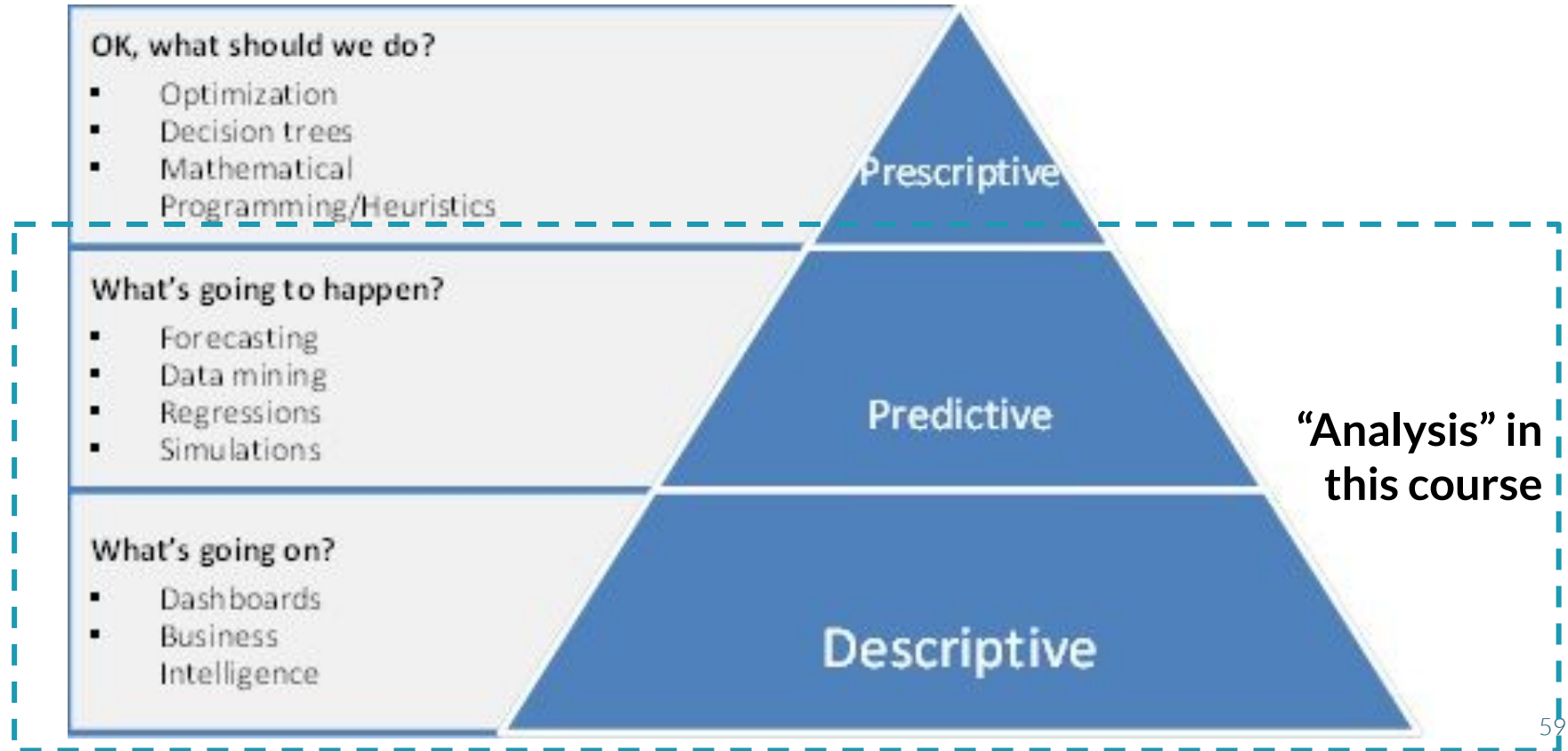
# Hierarchy of Analysis



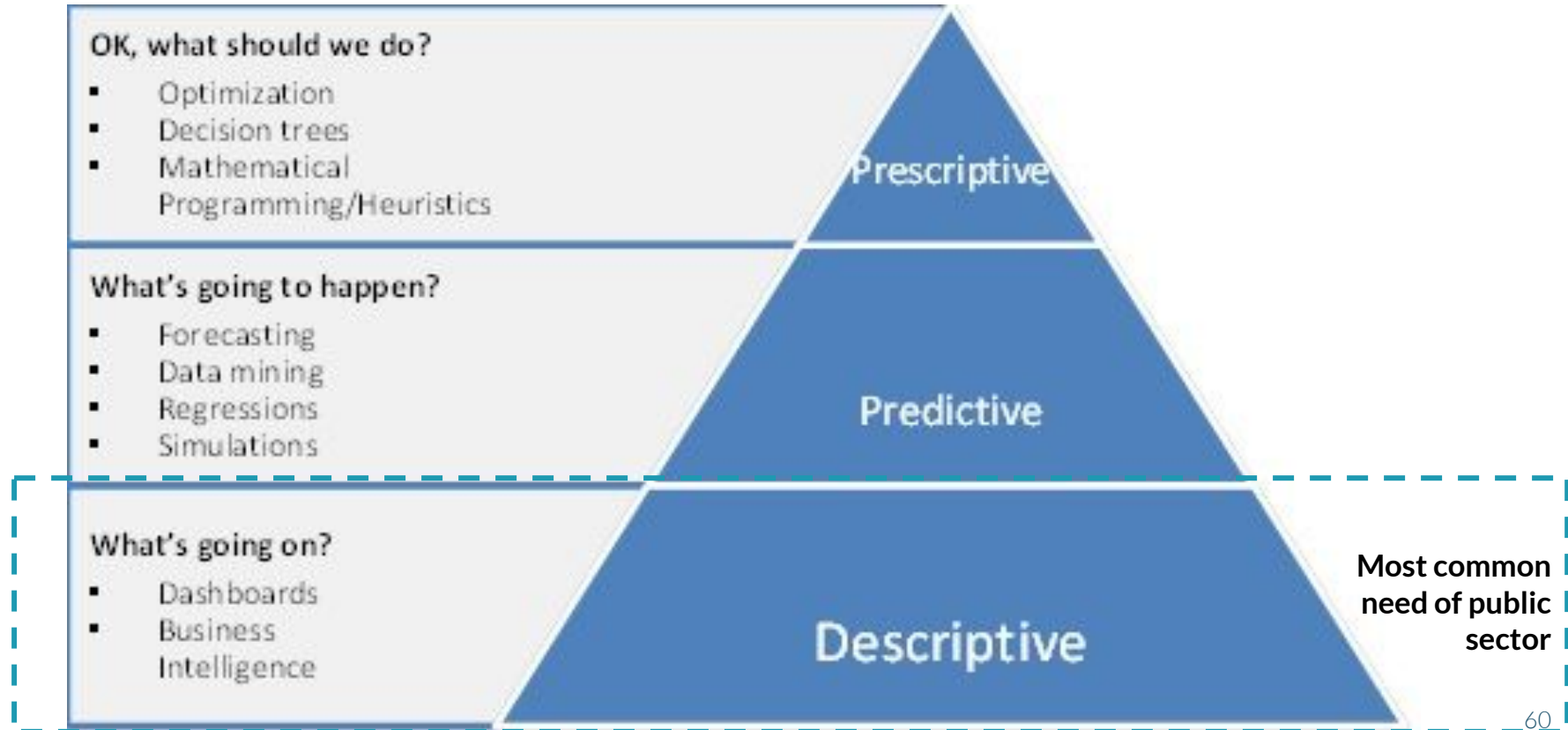
# Hierarchy of Analysis



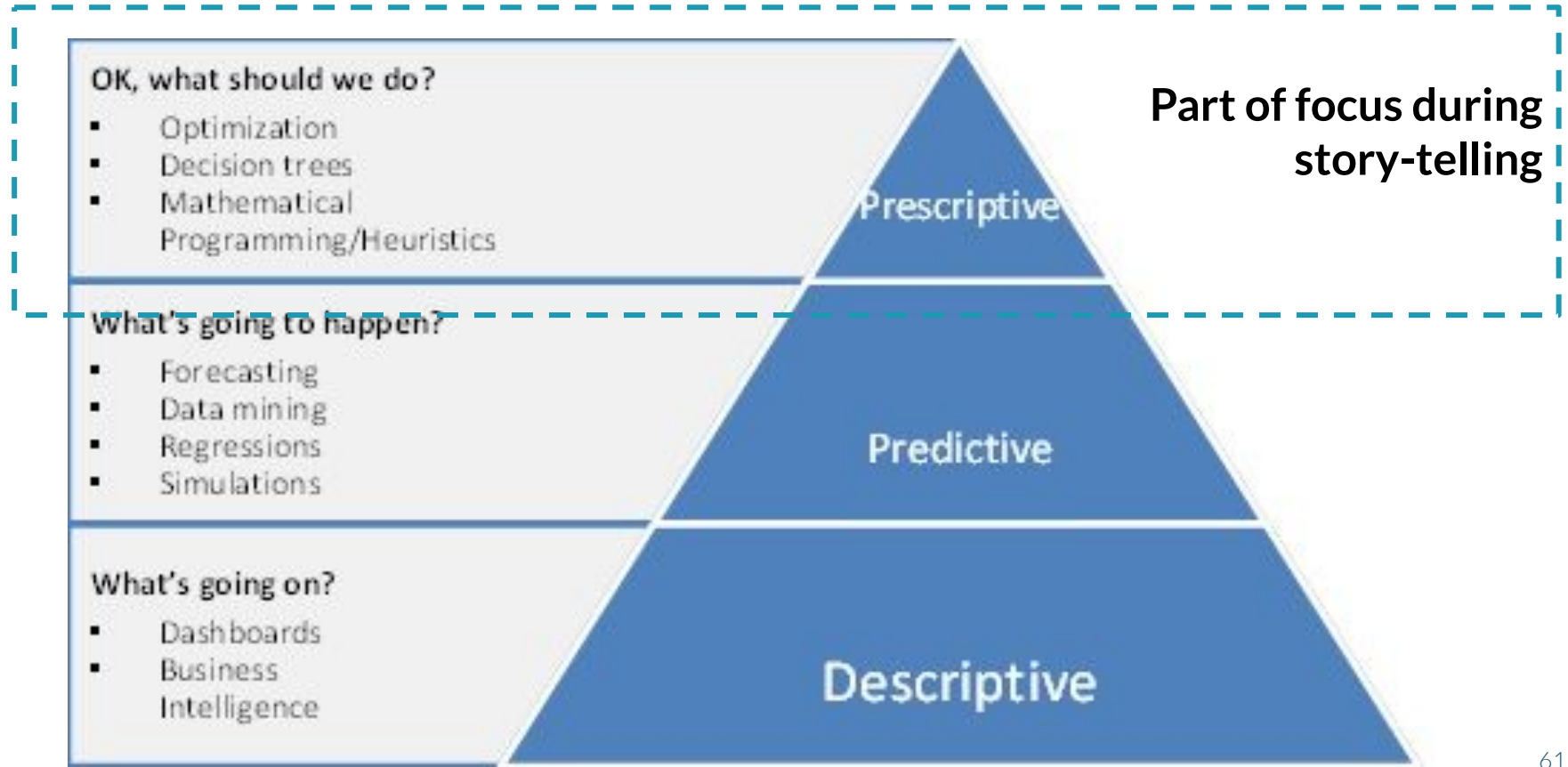
# Hierarchy of Analysis



# Hierarchy of Analysis



# Hierarchy of Analysis



# In Summary

1. Review of ANOVA
2. Isolated the impact of different races on salary data
  - a. Introduction to machine learning