

Optical Pumping

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Abstract

We will show that doppler broadening due to thermal fluctuations can be alleviated in order to show spectral features that would otherwise be hidden. In this case, we will show measurement of the hyperfine states of Rubidium (whose linewidth requires higher resolution than the doppler broadening allows) in order to demonstrate this technique.

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1 Introduction

We show that it is possible to spectally resolve features of the Hyperfine structure of Rubidium that would otherwise be impossible outside some sort of atomic trap using a technique called doppler-free spectroscopy. We also show that it is possible to make use of the interference pattern of a Michelson Interferometer to make calibrations and create a conversion from time into frequency for the purposes of measurement on a time-resolved oscilloscope. This means that we can use an oscilloscope with (potentially) much better-resolved time dynamics to mimic the purpose of a spectrum analyzer.

In particular, we discuss the methods used for finding the information required, including the methods used to find the Hyperfine transitions, measure the linewidth of the resonances, and the linewidth of the doppler-broadened peak.

2 Theory

2.1 Energy of Rb

Rubidium is often used as an atom for optical experiments because it has a hydrogen-like spectrum in its ground state, which allows for the splitting and simplification of the system hamiltonian. If we ignore the relativistic effects and assume that the nucleus is much heavier than the outer electrons, we can write the Hamiltonian of the system as the sum of different parts. We have

$$\begin{aligned} H_{kin} &= \frac{p^2}{2m} \\ H_{em} &= \frac{-Z_{eff}e^2}{4\pi\epsilon_0 r} \\ H_{so} &= \frac{1}{m_e c^2} \frac{1}{r} \frac{\partial V}{\partial r} \vec{L} \\ H_{hyp,1} &= \alpha \vec{J} \cdot \vec{I} \\ H_{hyp,2} &= \frac{\beta}{2I(2I-1)j(2j-1)} \left(3(\vec{I} \cdot \vec{J})^2 + \frac{3}{2}(\vec{I} \cdot \vec{J}) - I(I+1)j(j+1) \right) \end{aligned}$$

The first three are fairly basic - they stem from the electron's motion and interactions between the electron's magnetic moment and the magnetic moment of its motion around the nucleus. They are the standard additions to the Hydrogen atom hamiltonian with the exception of the relativistic correction term.

The second two are more complex. $H_{hyp,1}$ is the hyperfine interaction that occurs between the electron's total angular momentum $\vec{J} = \vec{L} + \vec{S}$ and the atom's intrinsic nuclear spin \vec{I} . The constant α is called the magnetic hyperfine structure constant. This interaction is also present in other atoms, but we see it very prominently in atoms like Rb due to the fact that the outer valence electrons typically have very high ℓ (hereafter the quantum number associated with \vec{L}) states, which directly increases j (quantum number associated with \vec{J}), it is a magnetic dipole interaction. Along that same vein, we have $H_{hyp,2}$. It is the interaction between the electric quadrupole moment of the nucleus and the electron. The dipole moment of the interaction is given in H_{em} . As with any other separable hamiltonian, we can apply non-degenerate perturbation theory and calculate the energy shift due to the perturbation quite simply. Thus we can simply write down the energy of the system as

$$E_{tot} = E_0 + E_{hyp}$$

where we have wrapped all the non-hyperfine parts into one term, and the two hyperfine hamiltonians into the E_{hyp} term.

2.2 Electron Transitions

The ground state for 85Rb and 87Rb is the $5^2S_{1/2}$, $f = 2$ state. Recall spectroscopic notation: $n^{2s+1}\ell_j$. Since we are measuring the hyperfine transitions between the $5^2P_{1/2}$, $f = 2$ states, we need some way to get the electrons into that state. We do this with a pump beam. In the orientation that we use, we happen to use the pump beam reflected and passed through a linear polarizer as our probe beam, but this is not necessary. We pump the ensemble into the $5^2P_{1/2}$, $f = 2$ states with a 780 nm laser. From there we let the hyperfine splitting occur as it normally would.

The pump beam pumps the atoms into a certain state, but the probe beam is what we measure. What we actually measure is the intensity of the probe beam as it passes through the sample, and then invert that signal on our instrumentation in order to plot the atoms' absorption of photons as a function of time (and since the laser sweeps frequencies as a function of time, frequency as well). In the particular case of the hyperfine transition peaks, for example, we see absorption dips at the

transition energies, because the atoms have nowhere to go and thus the photons simply pass through. We can then find the difference in frequency between hyperfine states by measuring the difference between the times at each peak tip and from that converting into frequency. We measure the splitting between the $5^2P_{1/2}$, $f = 0$ and the $5^2P_{1/2}$, $f = 3$ in integer increments in this way.

2.3 Doppler Broadening

Since the atoms are moving back and forth quite quickly at room temperature inside the vapor cell, there must be a consideration of the doppler shift on photons from the laser as seen by the atoms as well as photons emitted from the atoms. In both cases, if there is a component of velocity pointed parallel or antiparallel to the pump/probe beams, we will see a broadened spectrum that is essentially useless. There are a few methods to take care of this issue. The first is to stop the atoms. This is usually accomplished with a MOT (Magneto-Optical Trap), which uses magnetic fields and radiation pressure with lasers to cool the atoms to lower kinetic energy states. This is usually the path taken to study the physics of ultracold atoms, and to study properties such as the Bose-Einstein condensate. Atoms can be further cooled in order to reduce their velocity even more with evaporative cooling which involves simply allowing the 'hot' atoms to simply escape the trap.

Clearly we are not going to that much trouble in this particular experiment, we have a different objective. We want to measure an effect with a linewidth of roughly 36 MHz which is not terrible compared to other effects in atomic physics (for example, Rydberg transition linewidths which are commonly in the kHz range). Thus we use this technique of Doppler-Free Spectroscopy. The idea is that if we pass the same laser through the atoms twice, first as a pump beam and then at reduced intensity as the probe beam, we will be able to see dips in absorption at the finer spectral features. If the pump beam fully saturates the sample, then we will see less absorption of the probe beam at the energies where the hyperfine states live. These states corresponds to the atoms that are not moving - there is a perpendicular doppler shift, so the atoms must truly not be moving almost at all. If an atom is in resonance with a doppler-shifted beam, then it will not be in resonance with the beam that is reflected in the probe, so there will be no attenuation of absorption at that frequency.

Thus we are able to pick out the individual hyperfine states by essentially picking the spectrum from only the atoms that don't move, removing the need for a MOT by simply choosing the ones that we want to look at.

We can characterize the doppler broadening in terms of frequency, and write the full width at half max as

$$\Gamma = 2 \frac{\nu_0}{c} \left(\frac{2k_B T}{M} \ln 2 \right)^{1/2}.$$

We can derive this relation from the Boltzmann distribution - given that the atoms are in some thermal state we can describe the probability distribution of their velocities with the Boltzmann distribution. We will refrain from deriving this relation here, however.

2.4 Crossover Frequencies

Occasionally there are atoms whose transitions are in resonance with a doppler-shifted frequency, and there will be another transition that is in resonance with the frequency with the opposite doppler shift. This will cause what are known as crossover frequencies, which occur exactly halfway between two hyperfine transitions. This becomes important as we begin to examine the spectrum, but in essence as long as we realize that the outermost features are hyperfine features, and knowing that the crossovers happen at exactly halfway between hyperfine features we can pinpoint which are hyperfine and which are crossover features.

3 Experimental Methods

3.1 Apparatus

It will be much simpler to explain the components of the optical setup if there is something to refer to, so here we will show a rendering of the optical table as seen from above.

If we refer to Figure 1, we will notice that we use a Michelson Interferometer to perform both a calibration and the Doppler-Free Spectroscopy. In performing the spectroscopy, we can simply trace the beam from its source. All the components that lead the laser into the interferometer are simply to send the laser into this particular experiment as opposed to a setup that is across the table.

As the laser enters the interferometer, we will notice that the beam is split in two directions. In one direction, the beam simply reflects off a retroreflecting mirror and returns to the beam splitter to recombine with the other arm. The vapor cell

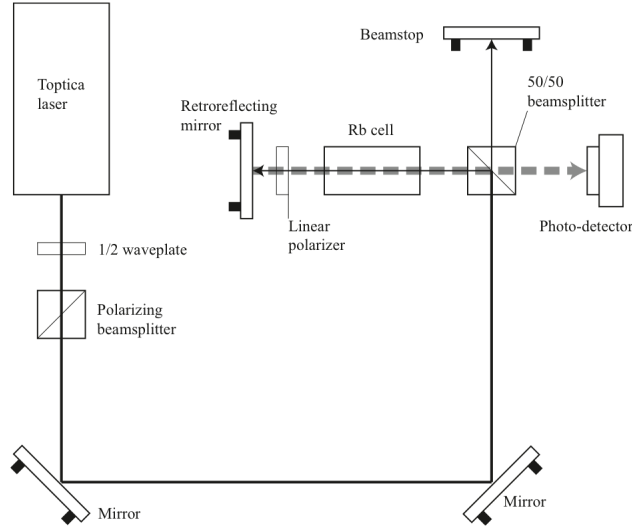


Figure 1: A depiction of the optical table as seen from above. The dark dashed arrow corresponds to the pump beam, while the lighter dashed arrow corresponds to the probe beam.

arm of the interferometer consists of the vapor cell itself, a linear polarizer and another retroreflecting mirror. After the pump beam passes through the vapor cell, it passes through a linear polarizer to reduce the intensity of the reflected beam which we use to probe the system. The probe beam and the reflected beam from the other arm of the interferometer recombine at the beam splitter and from there head into the detector. The detector sends a voltage signal to the oscilloscope, which then displays the signal in a time-resolved way.

The laser sweeps over a range of frequencies in a saw-tooth pattern, such that at some given time (modulo one period) the laser will be at a given frequency. We can calibrate this with the Michelson interferometer. We must realize that the scope trace - the absorption spectrum - is importantly time-resolved because the atoms are resonant at certain laser frequencies, which will correspond to different times in our calibration.

3.2 Michelson Interferometer Calibration

We can calibrate the time axis of the scope trace using the interference pattern given by the Michelson interferometer. There is a simple formula to calculate the difference in frequency between the two interferometer arms having to do with the phase difference:

$$\Delta\phi = \frac{4\pi f}{c}(L_1 - L_2)$$

which leads to the relation (given that the spacing between maxima on the interference pattern is a multiple of 2π)

$$\Delta f = \frac{c}{2(L_1 - L_2)} \quad (1)$$

Making use of Eq. 1, we can calculate a value for the frequency spacing between interference maxima given lengths for our particular interferometer. We measured

$$\begin{aligned} L_1 &= 29.5 \pm 0.5 \text{ cm} \\ L_2 &= 10.5 \pm 0.5 \text{ cm} \end{aligned}$$

which results in a frequency spacing between maxima of

$$790 \pm 40 \text{ MHz}. \quad (2)$$

In order to get the other part of the conversion, we take the interference spectrum (Figure 2), find the peaks and take the distances between them. From our procedure used to find the peaks we can define the uncertainty in the peak locations as something like the standard deviation of the mean of the gaussian filter. A very small number to be sure, but it is nonzero. From this uncertainty and mean, we generate a random distribution of peak locations centered at each peak on the spectrum with a standard deviation of the error on each peak. We then calculate differences between the peaks for each run (selecting a random point from this distribution each time) and average to find our best value. The uncertainty in this value will simply be the standard deviation of the sample. In order to properly populate the histogram we run this test 5000 times.

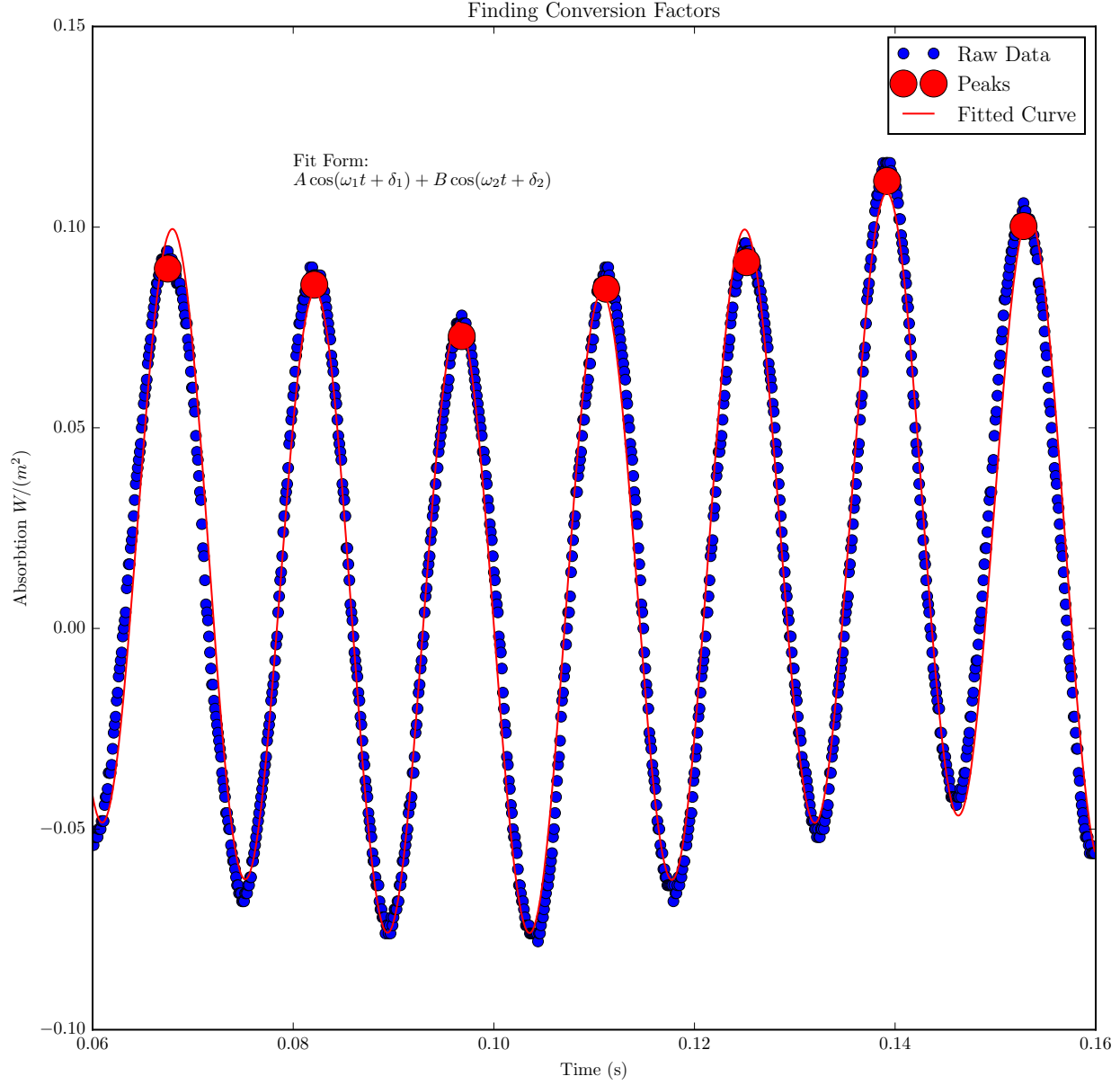


Figure 2: We have fit to the form shown in order to clean up the data. From there, we have applied a gaussian filter for increasing values of the kernel standard deviation (see the documentation for `numpy.gaussian_filter` for more information) in order to determine the correct coordinates for the peaks on the time axis. The other axis is more or less irrelevant. We have superimposed two cosine waves, because there appears to be some lower frequency oscillation in the system. Since the fit is not crucial (we only use it as a first smoothing of the data to find the peaks), we do not cite a $\tilde{\chi}^2$ value, but visually the fit is good. Also note that this is the cleanest part of the interferometer spectrum, and is shown because it is so clean.

Since the laser sweeps frequency (roughly) linearly, the conversion should be linear. Thus, we have

$$\Delta f = k \times \Delta t.$$

Given the fact that we have values for δt and δf , we calculate k as:

$$k \pm \delta k = 55.5315 \text{ GHz/s} \pm 5.73\%. \quad (3)$$

The inquisitive reader might question why there isn't a constant offset in our determination for k . Since we are only concerned with differences in time and frequency, such a constant offset would simply cancel anyway. We must be careful - this calibration can only be used to relate **differences** in time to **differences** in frequency. It is not an absolute conversion, nor is it perfect - the laser has idiosyncrasies that cause mode hops - a phenomenon that causes discontinuities in the spectrum and makes the saw tooth shape of the laser's frequency sweep distort significantly from the linear (modulo one period). It is however, good enough especially when we can see that the region of interest is free of discontinuities. So, we can use this value for k in the future to make the necessary conversions.

4 Data and Uncertainty Analysis

4.1 Doppler Broadened Spectrum

The doppler-broadened spectrum is not very pretty. We are simply using a version of the spectrum where the vapor cell is inside the interferometer to make alignment easier, as well as to clean up the spectrum. The overall width of the peak (the large peak, not the hyperfine dips) is still the same as the doppler-broadened peak that would occur outside the interferometer, just easier to see.

The 87Rb $F = 1$ peak has somehow collapsed - this is due to the fact that it is almost crashing into the laser's back sweep (the noise on either side). Since this gave us the best resolution on the first three peaks, we decided to use this spectrum for further analysis.

If we want to look closer at a given peak, we choose the 87Rb $F = 2$ peak. We can zoom in and identify all the transitions, shown in Figure ??

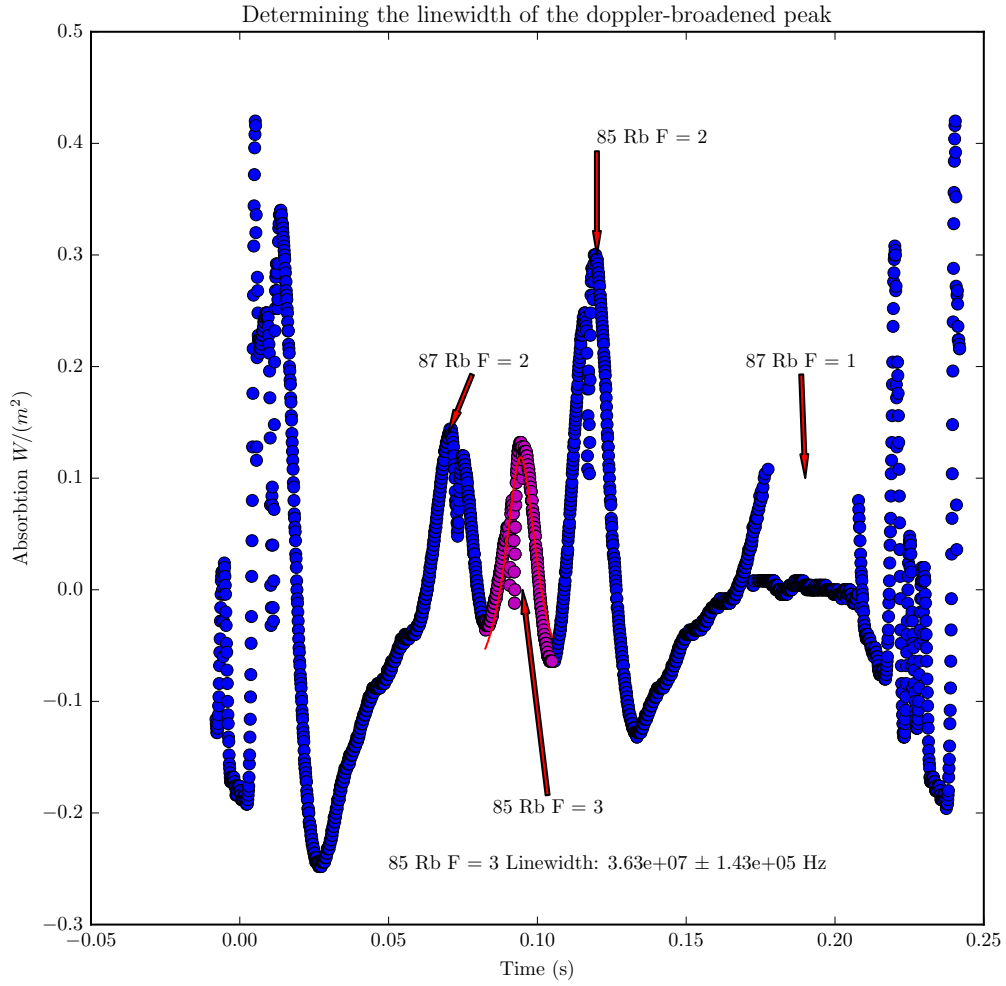


Figure 3: For this fit we simply found the maximum again using a very rough gaussian filter and fit using manual adjustment of the other fit parameters. The uncertainty in the linewidth comes from the covariance matrix element corresponding to the full width at half max of the fit form, suitably converted into frequency with Eq. 3 (taking into account uncertainty in k).

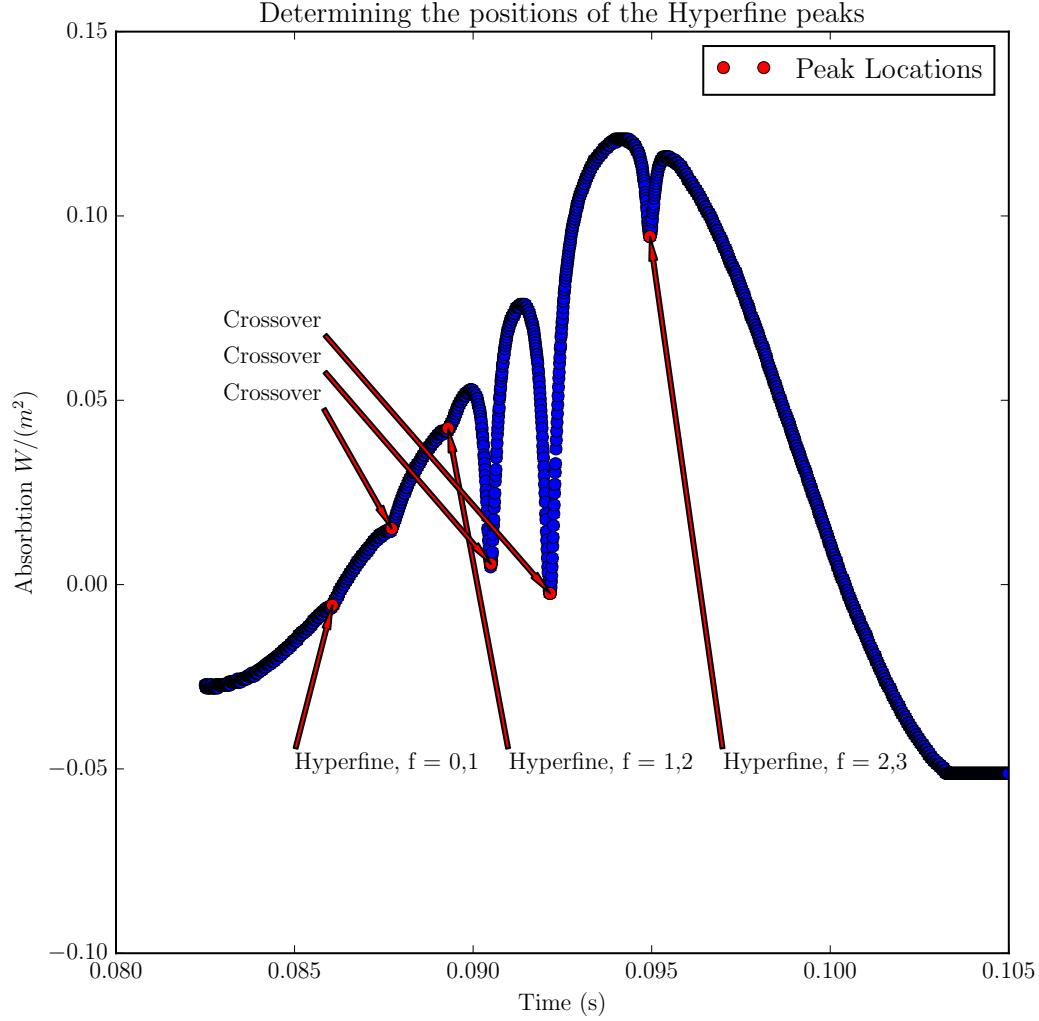


Figure 4: Finding the peaks exactly on this plot caused much consternation. We found that in order to find the smaller peaks on the left, we had to first apply 5 iterations of the gaussian filter, and give each section a linear offset before being able to determine the local minimum that defined the peak. The better-resolved peaks were quite simple, it was easy to apply a single filter and find the minimum that way. Unfortunately, two of the very well-resolved peaks were crossover features, but sometimes that's just how life goes.