

# Sign SGD with Heavy-Tailed Noise and Differential Privacy

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## Abstract

Federated learning faces the dual challenge of ensuring fast communication and maintaining data privacy. This paper addresses these challenges by proposing a novel modification of the Sign-SGD algorithm, designed to be both communication-efficient and differentially private. Our approach is particularly suited for real-world data characterized by noise distributions with infinite variance and bounded  $k$ -th moments, where  $k$  ranges from 1 to 2. We demonstrate that our modified Sign-SGD algorithm achieves differential privacy and converges with high probability, even when the noise is heavy-tailed, asymmetric, or non-unimodal. Additionally, we show that the algorithm’s speed is comparable to existing methods. The effectiveness of our approach is validated through improved training quality and speed in Large Language Models.

**Keywords:** Sign SGD, differential privacy, high-probability convergence, federated learning, heavy-tailed noise.

## Highlights:

1. Sign Stochastic Gradient Descent can be used to train LLMs on real data.
2. Our modification of Sign Stochastic Gradient Descent keeps user data private.
3. Our modification of Sign Stochastic Gradient Descent does not require tuning.

## 1 Introduction

In the recent work [2], the authors have shown that Sign-SGD with heavy-tailed noise achieves optimal convergence rates under certain assumptions. Additionally, [1] demonstrated that Sign-SGD can be made differentially private while maintaining good convergence properties.

## 2 Theory

Present your theoretical framework, definitions, lemmas, and proofs.

## 3 Experiments

Describe your experimental setup, methodology, and results.

## 4 Conclusion

Summarize your findings and discuss future work.

## Acknowledgments

Optional acknowledgments section.

## A Additional Proofs and Results

Include detailed proofs and supplementary materials here.

## References

- [1] Richeng Jin et al. “Stochastic-Sign SGD for Federated Learning with Theoretical Guarantees”. In: *Part of this work is published in IEEE Transactions on Neural Networks and Learning Systems, 2024* 36.2 (Feb. 25, 2020), pp. 3834–3846. ISSN: 2162-2388. DOI: 10.1109/tnnls.2023.3345367. arXiv: 2002.10940 [cs.LG].
- [2] Nikita Kornilov et al. *Sign Operator for Coping with Heavy-Tailed Noise: High Probability Convergence Bounds with Extensions to Distributed Optimization and Comparison Oracle*. 2025. DOI: 10.48550/ARXIV.2502.07923.