

prelim_sims

Setup for simulation

```
library(dplyr)
```

Attaching package: 'dplyr'

The following objects are masked from 'package:stats':

filter, lag

The following objects are masked from 'package:base':

intersect, setdiff, setequal, union

```
library(ggplot2)
```

Warning: package 'ggplot2' was built under R version 4.3.3

```
library(gt)
```

Warning: package 'gt' was built under R version 4.3.3

```
library(knitr)
```

Warning: package 'knitr' was built under R version 4.3.3

```
library(lavaan)
```

Warning: package 'lavaan' was built under R version 4.3.3

This is lavaan 0.6-18

lavaan is FREE software! Please report any bugs.

```
library(pinsearch)
library(SimDesign)
```

Warning: package 'SimDesign' was built under R version 4.3.3

```
# TODO:
# - Summarize the pattern of bias

# Define conditions: Testing different sample sizes
design <- createDesign(
  n = c(30, 100, 250, 1000, 5000)
)

# Fixed objects
set.seed(1855)

# Helper Function
# Generates a random covariance matrix
get_ucov <- function(p, scale = sqrt(0.1), n = 5) {
  W <- matrix(rnorm(p * n), nrow = n)
  WtW <- crossprod(W)
  D <- diag(1 / sqrt(diag(WtW))) * scale
  D %*% WtW %*% D
}

# Defines key parameters
fixed <- list(
  p = 6,
  lambda = c(.3, .7, .4, .5, .6, .4),
  dlambda = list(
    c(0, 0, 0, 0, 0, 0),
    c(.1, 0, 0, 0, 0, 0),
    c(.2, -.3, 0, 0, 0, 0),
```

```

      c(.3, -.3, 0, 0, 0, 0)
    ),
    nu = c(2, 3, 1.5, 3.5, 2, 3),
    alpha = c(0, -0.25, 0.25, 0.5),
    psi = c(1, 0.85, 1.15, 0.7),
    theta = c(1, 1.2, .8, .9, 1, 1) - .1,
    dtheta = matrix(
      runif(24, min = -0.2, max = 0.2),
      nrow = 4
    ),
    # ucov = replicate(4, get_ucov(6), simplify = FALSE)
    ucov = replicate(4, diag(.1, 6), simplify = FALSE),
    ninv_ind = c(1, 2)
  )
# lavaan syntax for the measurement model
fixed$mod <- paste(
  "f =~",
  paste0("y", seq_len(fixed$p), collapse = " + ")
)
# Compute implied means and covariances
fixed <- within(fixed, {
  lambdag <- lapply(dlambdas, FUN = \(x) x + lambda)
  Thetag <- lapply(seq_along(ucov),
    FUN = function(g) {
      diag(theta + dtheta[g, ]) + ucov[[g]]
    })
  covy <- mapply(\(lam, psi, th) tcrossprod(lam) * psi + th,
    lam = lambdag, psi = psi, th = Thetag,
    SIMPLIFY = FALSE)
  meany <- mapply(\(lam, al, nu) nu + lam * al,
    lam = lambdag, al = alpha, nu = list(nu),
    SIMPLIFY = FALSE)
})

# Population effect size
fixed$fmacs_pop <- local({
  pooled_sd <- lapply(fixed$covy, FUN = \(x) diag(x)) |>
    do.call(what = rbind) |>
    colMeans() |>
    sqrt()
})

```

```

fmacs(
  intercepts = matrix(rep(fixed$nu, 4),
                      nrow = 4,
                      byrow = TRUE
  ),
  loadings = sweep(
    do.call(rbind, fixed$dlambda),
    MARGIN = 2,
    STATS = fixed$lambda,
    FUN = "+"
  ),
  latent_mean = 0,
  latent_sd = 1,
  pooled_item_sd = pooled_sd
)[1:2]
})

# Function for data generation
# sim_y <- function(n, lambda, nu, alpha, psi, Theta) {
#   covy <- tcrossprod(lambda) * psi + Theta
#   meany <- nu + lambda * alpha
#   MASS::mvrnorm(n, mu = meany, Sigma = covy)
# }

```

Running the simulation

```

generate <- function(condition, fixed_objects) {
  ylist <- lapply(seq_along(fixed_objects$covy),
    FUN = function(g) {
      yg <- MASS::mvrnorm(
        condition$n,
        mu = fixed_objects$meany[[g]],
        Sigma = fixed_objects$covy[[g]]
      )
      colnames(yg) <- paste0("y", seq_len(fixed_objects$p))
      cbind(yg, group = g)
    })
  do.call(rbind, ylist)
}
sim1 <- generate(design[3, ], fixed_objects = fixed)

```

```

# Evaluate/Summarize
evaluate <- function(condition, results, fixed_objects) {
  c(
    bias = colMeans(results) - fixed_objects$fmacs_pop,
    robust_bias = apply(results, 2, mean, trim = .1) -
      fixed_objects$fmacs_pop,
    emp_sd = apply(results, 2, sd),
    emp_mad = apply(results, 2, mad)
  )
}

# Analysis
analyze <- function(condition, dat, fixed_objects) {
  # Define lavaan syntax
  pinv_fit <- cfa(
    fixed_objects$mod,
    data = dat,
    group = "group", std.lv = TRUE,
    group.equal = c("loadings", "intercepts"),
    group.partial = c(
      paste0("f=~y", fixed_objects$ninv_ind),
      paste0("y", fixed_objects$ninv_ind, "~1")
    )
  )
  as.vector(pinsearch::pin_effsize(pinv_fit))
}

out <- runSimulation(design,
  replications = 500,
  parallel = TRUE,
  generate = generate,
  analyse = analyze,
  summarise = evaluate,
  filename = "results-trial1",
  packages = c("MASS", "lavaan", "pinsearch"),
  fixed_objects = fixed
)

```

Number of parallel clusters in use: 19

Design: 1/5; RAM Used: 71.7 Mb; Replications: 500; Total Time: 0.00s
Conditions: n=30

Design: 2/5; RAM Used: 72.5 Mb; Replications: 500; Total Time: 03m 28.72s
Conditions: n=100

Design: 3/5; RAM Used: 72.5 Mb; Replications: 500; Total Time: 03m 52.28s
Conditions: n=250

Design: 4/5; RAM Used: 72.5 Mb; Replications: 500; Total Time: 04m 4.67s
Conditions: n=1000

Design: 5/5; RAM Used: 72.5 Mb; Replications: 500; Total Time: 04m 18.74s
Conditions: n=5000

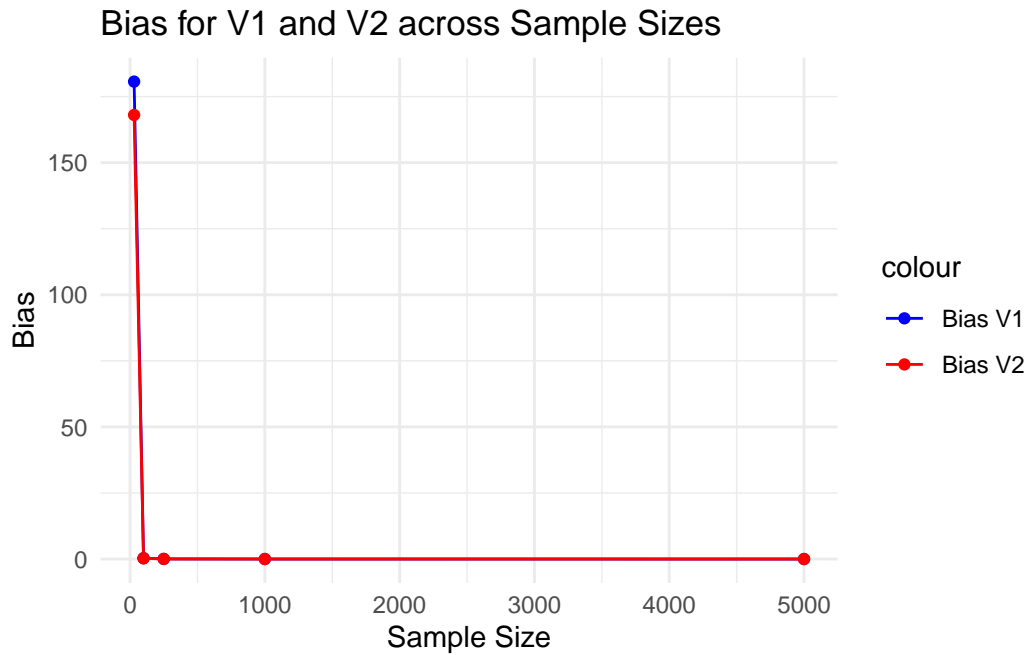
Simulation complete. Total execution time: 04m 41.61s

Saving simulation results to file: results-trial1.rds

```
data <- readRDS("results-trial1.rds")
```

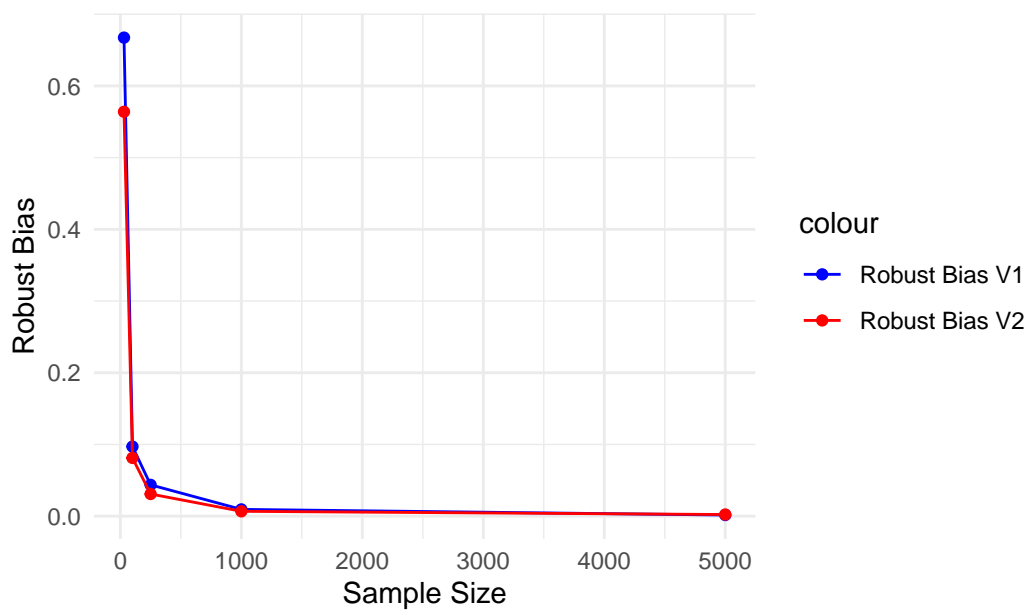
Graphs to visualize simulation results

```
ggplot(out, aes(x = n)) +  
  geom_line(aes(y = bias.V1, color = "Bias V1")) +  
  geom_point(aes(y = bias.V1, color = "Bias V1")) +  
  geom_line(aes(y = bias.V2, color = "Bias V2")) +  
  geom_point(aes(y = bias.V2, color = "Bias V2")) +  
  labs(title = "Bias for V1 and V2 across Sample Sizes",  
        x = "Sample Size", y = "Bias") +  
  scale_color_manual(values = c("Bias V1" = "blue", "Bias V2" = "red")) +  
  theme_minimal()
```

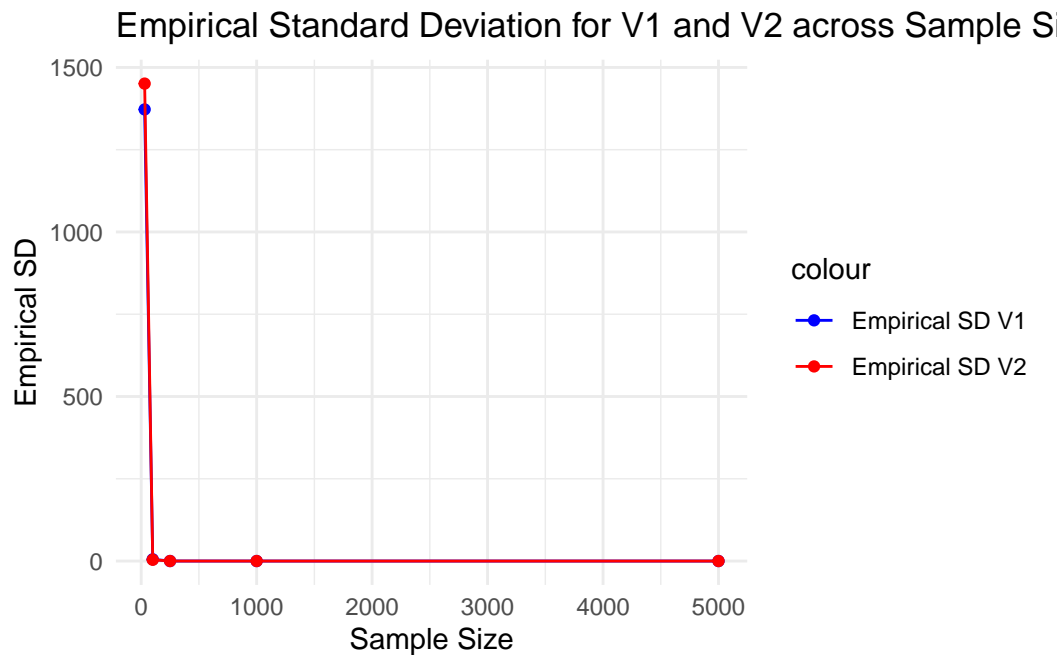


```
# Robust Bias for V1 and V2
ggplot(out, aes(x = n)) +
  geom_line(aes(y = robust_bias.V1, color = "Robust Bias V1")) +
  geom_point(aes(y = robust_bias.V1, color = "Robust Bias V1")) +
  geom_line(aes(y = robust_bias.V2, color = "Robust Bias V2")) +
  geom_point(aes(y = robust_bias.V2, color = "Robust Bias V2")) +
  labs(title = "Robust Bias for V1 and V2 across Sample Sizes",
        x = "Sample Size", y = "Robust Bias") +
  scale_color_manual(values = c("Robust Bias V1" = "blue", "Robust Bias V2" = "red")) +
  theme_minimal()
```

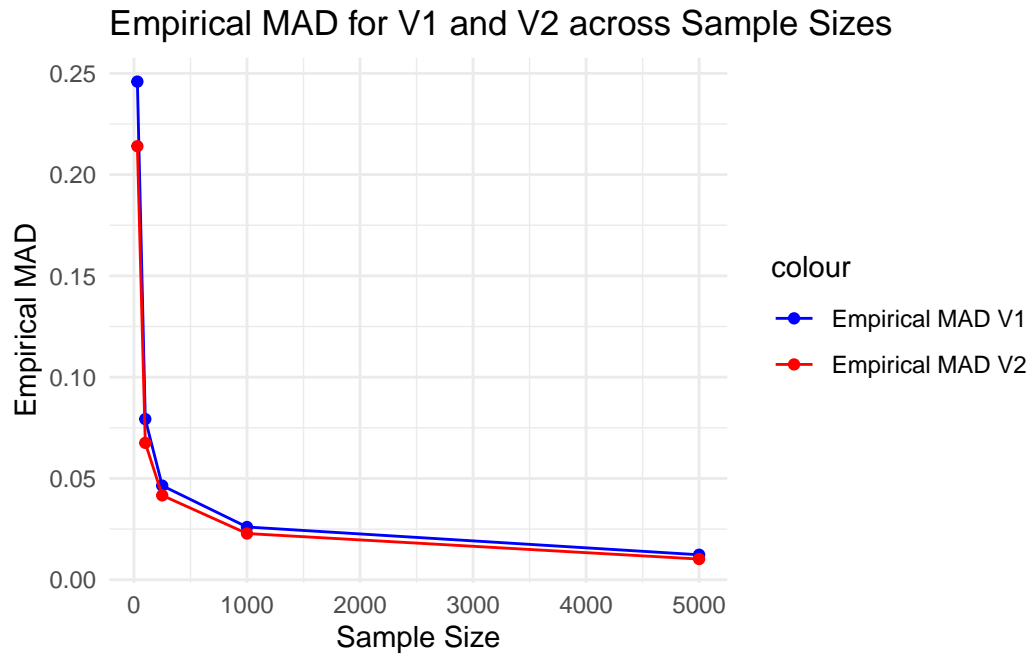
Robust Bias for V1 and V2 across Sample Sizes



```
# Empirical Standard Deviation for V1 and V2
ggplot(out, aes(x = n)) +
  geom_line(aes(y = emp_sd.V1, color = "Empirical SD V1")) +
  geom_point(aes(y = emp_sd.V1, color = "Empirical SD V1")) +
  geom_line(aes(y = emp_sd.V2, color = "Empirical SD V2")) +
  geom_point(aes(y = emp_sd.V2, color = "Empirical SD V2")) +
  labs(title = "Empirical Standard Deviation for V1 and V2 across Sample Sizes",
        x = "Sample Size", y = "Empirical SD") +
  scale_color_manual(values = c("Empirical SD V1" = "blue", "Empirical SD V2" = "red")) +
  theme_minimal()
```

```
# Empirical MAD for V1 and V2
ggplot(out, aes(x = n)) +
  geom_line(aes(y = emp_mad.V1, color = "Empirical MAD V1")) +
  geom_point(aes(y = emp_mad.V1, color = "Empirical MAD V1")) +
  geom_line(aes(y = emp_mad.V2, color = "Empirical MAD V2")) +
  geom_point(aes(y = emp_mad.V2, color = "Empirical MAD V2")) +
  labs(title = "Empirical MAD for V1 and V2 across Sample Sizes",
        x = "Sample Size", y = "Empirical MAD") +
  scale_color_manual(values = c("Empirical MAD V1" = "blue", "Empirical MAD V2" = "red"))
  theme_minimal()
```



Set up for tables

```
bias_table <- data.frame(  
  SampleSize = out$n,  
  Bias_V1 = out$bias.V1,  
  Bias_V2 = out$bias.V2  
)  
  
robust_bias_table <- data.frame(  
  SampleSize = out$n,  
  Robust_Bias_V1 = out$robust_bias.V1,  
  Robust_Bias_V2 = out$robust_bias.V2  
)  
  
emp_sd_table <- data.frame(  
  SampleSize = out$n,  
  Empirical_SD_V1 = out$emp_sd.V1,  
  Empirical_SD_V2 = out$emp_sd.V2  
)  
  
emp_mad_table <- data.frame(  
  SampleSize = out$n,
```

```

    Empirical_MAD_V1 = out$emp_mad.V1,
    Empirical_MAD_V2 = out$emp_mad.V2
  )

# Inline tables
knitr::kable(bias_table, caption = "Bias for V1 and V2 across Sample Sizes")

```

Table 1: Bias for V1 and V2 across Sample Sizes

SampleSize	Bias_V1	Bias_V2
30	180.6725954	168.0517972
100	0.3518730	0.2667248
250	0.0478055	0.0317518
1000	0.0105088	0.0070487
5000	0.0016523	0.0022065

```

knitr::kable(robust_bias_table, caption = "Robust Bias for V1 and V2 across Sample Sizes")

```

Table 2: Robust Bias for V1 and V2 across Sample Sizes

SampleSize	Robust_Bias_V1	Robust_Bias_V2
30	0.6673828	0.5639481
100	0.0970547	0.0811938
250	0.0436491	0.0309130
1000	0.0094398	0.0067654
5000	0.0015737	0.0022893

```

knitr::kable(emp_sd_table, caption = "Empirical Standard Deviation for V1 and V2 across Sa

```

Table 3: Empirical Standard Deviation for V1 and V2 across Sample Sizes

SampleSize	Empirical_SD_V1	Empirical_SD_V2
30	1372.4076599	1450.8974411
100	5.2639797	3.8151992
250	0.0529399	0.0424741
1000	0.0263212	0.0244311
5000	0.0122347	0.0104357

```
knitr::kable(emp_mad_table, caption = "Empirical MAD for V1 and V2 across Sample Sizes")
```

Table 4: Empirical MAD for V1 and V2 across Sample Sizes

SampleSize	Empirical_MAD_V1	Empirical_MAD_V2
30	0.2459071	0.2140147
100	0.0793031	0.0675686
250	0.0464374	0.0416447
1000	0.0260422	0.0228123
5000	0.0123308	0.0102229