

sim_dmacs_cat_p=6

```
library(SimDesign)
```

Warning: package 'SimDesign' was built under R version 4.3.3

```
library(lavaan)
```

Warning: package 'lavaan' was built under R version 4.3.3

This is lavaan 0.6-18

lavaan is FREE software! Please report any bugs.

```
library(pinsearch)
```

```
# TODO:
```

```
# - Increase the number of replications to 500
```

```
# - Summarize the pattern of bias
```

```
# Define conditions
```

```
design <- createDesign(  
  n = c(30, 100, 250, 1000)  
)
```

```
# Fixed objects
```

```
set.seed(1855)
```

```
# Helper
```

```
get_ucov <- function(p, scale = sqrt(0.1), n = 5) {  
  W <- matrix(rnorm(p * n), nrow = n)  
  WtW <- crossprod(W)
```

```

D <- diag(1 / sqrt(diag(WtW))) * scale
D %*% WtW %*% D
}
fixed <- list(
  p = 6,
  lambda = c(.3, .7, .4, .5, .6, .4),
  dlambdas = list(
    c(0, 0, 0, 0, 0, 0),
    c(.3, 0, 0, 0, 0, 0)
  ),
  # nu = c(2, 3, 1.5, 3.5, 2, 3),
  tau = c(0.5, -0.5, 1, 0, -2, 0),
  alpha = c(0, -0.25),
  psi = c(1, 1.15),
  ninv_ind = c(1)
)
# lavaan syntax
fixed$mod <- paste(
  "f =~",
  paste0("y", seq_len(fixed$p), collapse = " + "), "\n",
  paste0("y", seq_len(fixed$p), "~~ 1 * y", seq_len(fixed$p),
    collapse = "\n")
)
# Compute implied means and covariances
fixed <- within(fixed, {
  lambdag <- lapply(dlambdas, FUN = \(x) x + lambda)
  covy <- mapply(\(lam, psi) tcrossprod(lam) * psi + diag(length(lam)),
    lam = lambdag, psi = psi,
    SIMPLIFY = FALSE)
  meany <- mapply(\(lam, al) lam * al,
    lam = lambdag, al = alpha,
    SIMPLIFY = FALSE)
})

# Population effect size
fixed$dmacs_pop <- local({
  pooled_sd <- mapply(pinsearch::var_from_thres,
    thres = fixed$tau[1],
    mean = lapply(fixed$meany, FUN = \(x) x[1]),
    sd = lapply(fixed$covy, FUN = \(x) sqrt(x[1, 1]))
}) >

```

```

    mean() |>
    sqrt()

dmacs_ordered(
  thresholds = matrix(rep(fixed$tau, 2),
    nrow = 2,
    byrow = TRUE
  ) |> `colnames<-`(1:6),
  loadings = sweep(
    do.call(rbind, fixed$dlambda),
    MARGIN = 2,
    STATS = fixed$lambda,
    FUN = "+"
  ),
  latent_mean = 0,
  latent_sd = 1,
  pooled_item_sd = pooled_sd
)[1]
})

# Function for data generation
# sim_y <- function(n, lambda, nu, alpha, psi, Theta) {
#   covy <- tcrossprod(lambda) * psi + Theta
#   meany <- nu + lambda * alpha
#   MASS::mvrnorm(n, mu = meany, Sigma = covy)
# }

generate <- function(condition, fixed_objects) {
  ylist <- lapply(seq_along(fixed_objects$covy),
    FUN = function(g) {
      yg <- MASS::mvrnorm(
        condition$n,
        mu = fixed_objects$meany[[g]],
        Sigma = fixed_objects$covy[[g]]
      )
      yg <- vapply(seq_len(ncol(yg)), FUN = \(j) {
        findInterval(yg[, j], fixed_objects$tau[j])
      }, FUN.VALUE = integer(nrow(yg)))
      colnames(yg) <- paste0("y", seq_len(fixed_objects$p))
      cbind(yg, group = g)
    })
  do.call(rbind, ylist)
}

```

```

}
sim1 <- generate(design[3, ], fixed_objects = fixed)

# Analysis
analyze <- function(condition, dat, fixed_objects) {
  # Define lavaan syntax
  pinv_fit <- cfa(
    fixed_objects$mod,
    data = dat,
    group = "group", std.lv = TRUE,
    ordered = TRUE,
    group.equal = c("loadings", "thresholds"),
    group.partial = c(
      paste0("f=~y", fixed_objects$ninv_ind),
      paste0("y", fixed_objects$ninv_ind, "|t1")
    ),
    parameterization = "theta"
  )
  as.vector(pinsearch::pin_effsize(pinv_fit))
}

analyze_bc <- function(condition, dat, fixed_objects) {
  # Define lavaan syntax
  pinv_fit <- cfa(
    fixed_objects$mod,
    data = dat,
    group = "group", std.lv = TRUE,
    ordered = TRUE,
    group.equal = c("loadings", "thresholds"),
    group.partial = c(
      paste0("f=~y", fixed_objects$ninv_ind),
      paste0("y", fixed_objects$ninv_ind, "|t1")
    ),
    parameterization = "theta"
  )
  f_orig <- as.vector(pinsearch::pin_effsize(pinv_fit))
  f_boot <- lavaan::bootstrapLavaan(pinv_fit,
    R = 250,
    FUN = pinsearch::pin_effsize,
    parallel = "snow",

```

```

      ncpus = 19
    )
    pmax(0, 2 * f_orig - colMeans(f_boot, na.rm = TRUE))
  }

analyze_bc2 <- function(condition, dat, fixed_objects) {
  # Define lavaan syntax
  pinv_fit <- cfa(
    fixed_objects$mod,
    data = dat,
    group = "group", std.lv = TRUE,
    ordered = TRUE,
    group.equal = c("loadings", "thresholds"),
    group.partial = c(
      paste0("f=~y", fixed_objects$ninv_ind),
      paste0("y", fixed_objects$ninv_ind, "|t1")
    ),
    parameterization = "theta"
  )
  f_orig <- pinsearch::pin_effsize(pinv_fit)
  ns <- lavInspect(pinv_fit, what = "nobs")
  ng <- length(ns)
  f2_bias <- (ng - 1) / ng * sum(1 / ns)
  sqrt(pmax(0, f_orig^2 - f2_bias))
}

# Evaluate/Summarize
evaluate <- function(condition, results, fixed_objects) {
  results <- as.matrix(results)
  c(
    bias = colMeans(results) - fixed_objects$dmacs_pop,
    robust_bias = apply(results, 2, mean, trim = .1) -
      fixed_objects$dmacs_pop,
    emp_sd = apply(results, 2, sd),
    emp_mad = apply(results, 2, mad)
  )
}

SimClean()
# out <- runSimulation(design,
#   replications = 500,

```

```

#   parallel = TRUE,
#   generate = generate,
#   analyse = list(naive = analyze,
#                   bc_boot = analyze_bc,
#                   bc_form = analyze_bc2),
#   summarise = evaluate,
#   filename = "results-dmacs-cat-trial",
#   save_results = TRUE,
#   packages = c("MASS", "lavaan", "pinsearch"),
#   fixed_objects = fixed
# )

```

```

data <- readRDS("C:/Users/alex/OneDrive/Documents/results-dmacs-cat-trial.rds")

```

```

bias_table <- data.frame(
  SampleSize = data$n,
  Bias_Naive1 = data$bias.naive,
  Bias_BC_Boot1 = data$bias.bc_boot,
  Bias_BC_Form1 = data$bias.bc_form
)

```

```

robust_bias_table <- data.frame(
  SampleSize = data$n,
  Robust_Bias_Naive = data$robust_bias.naive,
  Robust_Bias_BC_Boot = data$robust_bias.bc_boot,
  Robust_Bias_BC_Form = data$robust_bias.bc_form
)

```

```

emp_sd_table <- data.frame(
  SampleSize = data$n,
  Empirical_SD_Naive = data$emp_sd.naive,
  Empirical_SD_BC_Boot = data$emp_sd.bc_boot,
  Empirical_SD_BC_Form = data$emp_sd.bc_form
)

```

```

emp_mad_table <- data.frame(
  SampleSize = data$n,
  Empirical_MAD_Naive = data$emp_mad.naive,
  Empirical_MAD_BC_Boot = data$emp_mad.bc_boot,
  Empirical_MAD_BC_Form = data$emp_mad.bc_form
)

```

```
# Create and display tables using knitr
knitr::kable(bias_table, caption = "Bias for Naive, BC Bootstrap, and Bias-Corrected across
```

Table 1: Bias for Naive, BC Bootstrap, and Bias-Corrected across Sample Sizes

SampleSize	Bias_Naive1	Bias_BC_Boot1	Bias_BC_Form1
30	0.4075979	0.3038443	0.3635886
100	0.1438503	0.0555087	0.1201242
250	0.0559425	0.0059237	0.0424477
1000	0.0075601	-0.0057407	0.0043066

```
knitr::kable(robust_bias_table, caption = "Robust Bias for Naive, BC Bootstrap, and Bias-C
```

Table 2: Robust Bias for Naive, BC Bootstrap, and Bias-Corrected across Sample Sizes

SampleSize	Robust_Bias_Naive	Robust_Bias_BC_Boot	Robust_Bias_BC_Form
30	0.3826305	0.2412953	0.3441872
100	0.1163620	0.0059315	0.0957243
250	0.0455814	-0.0097682	0.0348200
1000	0.0041979	-0.0076320	0.0014530

```
knitr::kable(emp_sd_table, caption = "Empirical Standard Deviation for Naive, BC Bootstrap
```

Table 3: Empirical Standard Deviation for Naive, BC Bootstrap, and Bias-Corrected across Sample Sizes

SampleSize	Empirical_SD_Naive	Empirical_SD_BC_Boot	Empirical_SD_BC_Form
30	0.3504513	0.4840956	0.3772408
100	0.2182071	0.2834244	0.2315206
250	0.1418793	0.1684096	0.1511943
1000	0.0837288	0.0907899	0.0856249

```
knitr::kable(emp_mad_table, caption = "Empirical MAD for Naive, BC Bootstrap, and Bias-Cor
```

Table 4: Empirical MAD for Naive, BC Bootstrap, and Bias-Corrected across Sample Sizes

SampleSize	Empirical_MAD_Naive	Empirical_MAD_BC_Boo	Empirical_MAD_BC_Form
30	0.3577492	0.5347278	0.3877167
100	0.1805724	0.2358567	0.1945414
250	0.1593400	0.1971070	0.1645365
1000	0.0834076	0.0918275	0.0848776