hw1

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R Markdown

```
cars=read.csv("mtcars.csv")
head(cars)
##
                 model mpg cyl disp hp drat
                                                wt qsec vs am gear carb
## 1
             Mazda RX4 21.0
                              6 160 110 3.90 2.620 16.46
                                                          0
                                                             1
## 2
         Mazda RX4 Wag 21.0
                              6 160 110 3.90 2.875 17.02
           Datsun 710 22.8
## 3
                              4 108 93 3.85 2.320 18.61
                                                                       1
        Hornet 4 Drive 21.4
                                258 110 3.08 3.215 19.44
## 4
                              6
                                                                       1
                                360 175 3.15 3.440 17.02
                                                                       2
## 5 Hornet Sportabout 18.7
                             8
                                                         0
## 6
              Valiant 18.1
                              6 225 105 2.76 3.460 20.22 1 0
                                                                       1
```

$\mathbf{Q}\mathbf{1}$

```
v1 = mean(cars$mpg)
v2 = mean(cars$cyl)
v3 = mean(cars$disp)
v4 = mean(cars$hp)
v5 = mean(cars$drat)
v6 = mean(cars$wt)
v7 = mean(cars$qsec)
v8 = mean(cars$vs)
v9 = mean(cars$am)
v10 = mean(cars$gear)
v11 = mean(cars$carb)
tab <- matrix(c(v1, v2, v3, v4, v5, v6, v7, v8, v9, v10, v11), ncol=11)
colnames(tab) <- c("mpg", "cyl", "disp", "hp", "drat", "wt", "qsec", "vs", "am", "gear", "carb")</pre>
rownames(tab) <- c("mean")</pre>
library(knitr)
kable(tab)
```

```
df = as.data.frame(cars)
df <- df[ , -which(names(df) %in% c("model"))]</pre>
result 1 = cov(df)
result_2 = cor(df)
result 1
##
                        cyl
                                 disp
                                             hp
                                                       drat
                                                                   wt
              mpg
## mpg
        36.324103 -9.1723790 -633.09721 -320.732056
                                                 2.19506351 -5.1166847
        -9.172379 3.1895161 199.66028 101.931452 -0.66836694
## disp -633.097208 199.6602823 15360.79983 6721.158669 -47.06401915 107.6842040
      -320.732056 101.9314516 6721.15867 4700.866935 -16.45110887 44.1926613
## drat
        2.195064 -0.6683669 -47.06402 -16.451109 0.28588135 -0.3727207
                 1.3673710 107.68420
## wt
        -5.116685
                                      44.192661 -0.37272073 0.9573790
## qsec 4.509149 -1.8868548 -96.05168 -86.770081 0.08714073 -0.3054816
         2.017137 -0.7298387 -44.37762 -24.987903
                                                 0.11864919 -0.2736613
## vs
        1.803931 -0.4657258 -36.56401 -8.320565
## am
                                                 0.19015121 -0.3381048
## gear
       2.135685 -0.6491935 -50.80262 -6.358871
                                                0.27598790 -0.4210806
## carb -5.363105 1.5201613 79.06875 83.036290 -0.07840726 0.6757903
                   vs am
             qsec
                                              gear
                                                         carb
                  2.01713710 1.80393145
## mpg
        4.50914919
                                         2.1356855 -5.36310484
       -1.88685484 -0.72983871 -0.46572581 -0.6491935 1.52016129
## cyl
## disp -96.05168145 -44.37762097 -36.56401210 -50.8026210 79.06875000
       -86.77008065 -24.98790323
                             -8.32056452 -6.3588710 83.03629032
       ## drat
## wt
       -0.30548161 -0.27366129 -0.33810484 -0.4210806 0.67579032
## qsec 3.19316613 0.67056452 -0.20495968 -0.2804032 -1.89411290
## vs
       ## am
       ## gear -0.28040323 0.07661290 0.29233871 0.5443548 0.32661290
## carb -1.89411290 -0.46370968 0.04637097 0.3266129 2.60887097
result_2
                               disp
                      cyl
                                          hp
                                                   drat
             mpg
       1.0000000 -0.8521620 -0.8475514 -0.7761684 0.68117191 -0.8676594
## cyl -0.8521620 1.0000000 0.9020329 0.8324475 -0.69993811 0.7824958
## disp -0.8475514 0.9020329 1.0000000 0.7909486 -0.71021393 0.8879799
      -0.7761684   0.8324475   0.7909486   1.0000000   -0.44875912   0.6587479
## drat 0.6811719 -0.6999381 -0.7102139 -0.4487591 1.00000000 -0.7124406
      -0.8676594 0.7824958 0.8879799 0.6587479 -0.71244065 1.0000000
## qsec 0.4186840 -0.5912421 -0.4336979 -0.7082234 0.09120476 -0.1747159
       0.6640389 \ -0.8108118 \ -0.7104159 \ -0.7230967 \ \ 0.44027846 \ -0.5549157
       0.5998324 \ -0.5226070 \ -0.5912270 \ -0.2432043 \ \ 0.71271113 \ -0.6924953
## gear 0.4802848 -0.4926866 -0.5555692 -0.1257043 0.69961013 -0.5832870
## carb -0.5509251 0.5269883 0.3949769 0.7498125 -0.09078980 0.4276059
##
             qsec
                       vs
                                  am
                                          gear
## mpg
```

cyl -0.59124207 -0.8108118 -0.52260705 -0.4926866 0.52698829 ## disp -0.43369788 -0.7104159 -0.59122704 -0.5555692 0.39497686 ## hp -0.70822339 -0.7230967 -0.24320426 -0.1257043 0.74981247

```
0.09120476
                     0.4402785
                                0.71271113  0.6996101  -0.09078980
##
        -0.17471588 -0.5549157 -0.69249526 -0.5832870
                                                       0.42760594
  wt.
  qsec
         1.0000000
                     0.7445354 -0.22986086 -0.2126822 -0.65624923
         0.74453544
                     1.0000000
                                0.16834512
                                             0.2060233 -0.56960714
##
  VS
##
  am
        -0.22986086
                     0.1683451
                                1.00000000
                                             0.7940588
                                                        0.05753435
  gear -0.21268223
                     0.2060233
                                0.79405876
                                             1.0000000
                                                        0.27407284
## carb -0.65624923 -0.5696071
                                0.05753435
                                             0.2740728
                                                        1.00000000
```

Explanation:

Based on the variance-covariance matrix, it can be interpreted that the diagonal is the variance of the variable. A positive covariance means that two variables increase or decrease at the same time. For example, the covariance of disp and cyl is 199.66028 which means when disp increases cyl tends to increase too. Some other pairs of variable that have a positive covariance are hp and cyl, qsec and mpg, and drat and vs. A negative covariance means that two variables means that when one of the variables increases the other one decreases. Some examples are disp and mpg whose covariance is -633.09721, drat and cyl whose covariance is -0.69993811, and hp and qsec whose covariance is -0.70822339. The correlation matrix tells us the correlation between two variables. A large and positive correlation means that two variables have a strong correlation and that they increase simultaneously. Examples for strong positive correlations are drat and mpg, disp and cyl, carb and hp. A small correlation that is close to 0 means that two variables are unlikely to be correlated. Pairs of variables that are not correlated are am and hp, qsec and wt, gear and vs. Negative and large correlations indicate that two variables change oppositely. While one variable decreases, the other increases. Examples of pairs of variables that have this correlation are drat and wt, wt and mpg, and vs and disp.

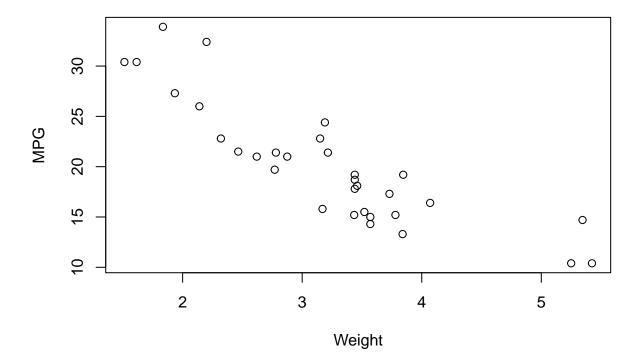
Q3

```
d = read.csv("mtcars.csv")
d
```

```
##
                                            hp drat
                                                            qsec vs am gear carb
                     model mpg cyl
                                      disp
                                                        wt
## 1
                 Mazda RX4 21.0
                                     160.0 110 3.90 2.620 16.46
                                                                            4
                                                                                 4
## 2
            Mazda RX4 Wag 21.0
                                   6 160.0 110 3.90 2.875 17.02
                                                                            4
                                                                                 4
                                                                   0
                                                                      1
## 3
               Datsun 710 22.8
                                   4 108.0
                                            93 3.85 2.320 18.61
                                                                            4
                                                                                 1
## 4
           Hornet 4 Drive 21.4
                                     258.0 110 3.08 3.215 19.44
                                                                      0
                                                                            3
                                                                                 1
## 5
        Hornet Sportabout 18.7
                                   8 360.0 175 3.15 3.440 17.02
                                                                            3
                                                                                 2
                                                                      0
                                                                            3
## 6
                   Valiant 18.1
                                   6 225.0 105 2.76 3.460 20.22
                                                                                 1
                                                                   1
                                                                      0
##
  7
                Duster 360 14.3
                                   8 360.0 245 3.21 3.570 15.84
                                                                            3
                                                                                 4
                                                                                 2
                 Merc 240D 24.4
                                   4 146.7
                                            62 3.69 3.190 20.00
                                                                            4
## 8
                                                                   1
                                                                      0
##
  9
                  Merc 230 22.8
                                   4 140.8
                                            95 3.92 3.150 22.90
                                                                   1
                                                                      0
                                                                            4
                                                                                 2
## 10
                  Merc 280 19.2
                                   6 167.6 123 3.92 3.440 18.30
                                                                      0
                                                                            4
                                                                                 4
                                                                   1
                 Merc 280C 17.8
## 11
                                   6 167.6 123 3.92 3.440 18.90
                                                                            4
                                                                                 4
## 12
                Merc 450SE 16.4
                                   8 275.8 180 3.07 4.070 17.40
                                                                            3
                                                                                 3
                                                                   0
                                                                      0
## 13
               Merc 450SL 17.3
                                   8 275.8 180 3.07 3.730 17.60
                                                                   0
                                                                      0
                                                                            3
                                                                                 3
  14
                                                                                 3
##
               Merc 450SLC 15.2
                                   8 275.8 180 3.07 3.780 18.00
                                                                   0
                                                                            3
  15
       Cadillac Fleetwood 10.4
                                   8 472.0 205 2.93 5.250 17.98
                                                                   0
                                                                            3
                                                                                 4
                                                                            3
                                                                                 4
##
   16
      Lincoln Continental 10.4
                                   8 460.0 215 3.00 5.424 17.82
                                                                   0
                                                                      0
## 17
        Chrysler Imperial 14.7
                                   8 440.0 230 3.23 5.345 17.42
                                                                   0
                                                                      0
                                                                            3
                                                                                 4
## 18
                  Fiat 128 32.4
                                      78.7
                                             66 4.08 2.200 19.47
                                                                            4
                                                                                 1
## 19
              Honda Civic 30.4
                                     75.7
                                            52 4.93 1.615 18.52
                                                                            4
                                                                                 2
                                   4
```

```
## 20
           Toyota Corolla 33.9
                                  4 71.1 65 4.22 1.835 19.90
                                                                               1
## 21
            Toyota Corona 21.5
                                  4 120.1 97 3.70 2.465 20.01
                                                                          3
                                                                               1
## 22
                                                                               2
         Dodge Challenger 15.5
                                  8 318.0 150 2.76 3.520 16.87
                                                                          3
                                  8 304.0 150 3.15 3.435 17.30
                                                                          3
                                                                               2
## 23
              AMC Javelin 15.2
## 24
               Camaro Z28 13.3
                                  8 350.0 245 3.73 3.840 15.41
                                                                          3
                                                                               4
## 25
         Pontiac Firebird 19.2
                                  8 400.0 175 3.08 3.845 17.05
                                                                          3
                                                                               2
## 26
                Fiat X1-9 27.3
                                  4 79.0
                                           66 4.08 1.935 18.90
                                                                               1
                                                                               2
            Porsche 914-2 26.0
                                           91 4.43 2.140 16.70
                                                                          5
## 27
                                  4 120.3
                                                                  0
## 28
             Lotus Europa 30.4
                                     95.1 113 3.77 1.513 16.90
                                                                  1
                                                                          5
                                                                               2
## 29
                                  8 351.0 264 4.22 3.170 14.50
                                                                          5
                                                                               4
           Ford Pantera L 15.8
## 30
             Ferrari Dino 19.7
                                  6 145.0 175 3.62 2.770 15.50
                                                                          5
                                                                               6
                                  8 301.0 335 3.54 3.570 14.60
                                                                               8
## 31
            Maserati Bora 15.0
                                                                          5
                                                                  0
## 32
               Volvo 142E 21.4
                                  4 121.0 109 4.11 2.780 18.60
                                                                               2
plot(x = d\$wt,
     y = d pg,
     xlab = "Weight",
     ylab = "MPG",
     main = "Weight vs MGP")
```

Weight vs MGP

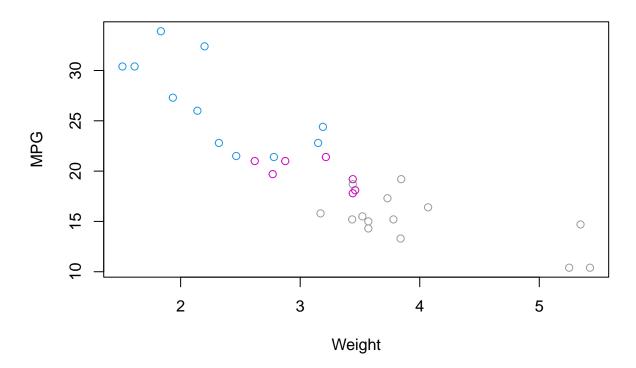


 $\mathbf{Q4}$

Blue is 4 cylinder, Purple is 6 cylinder, and Gray is 8 cylinder

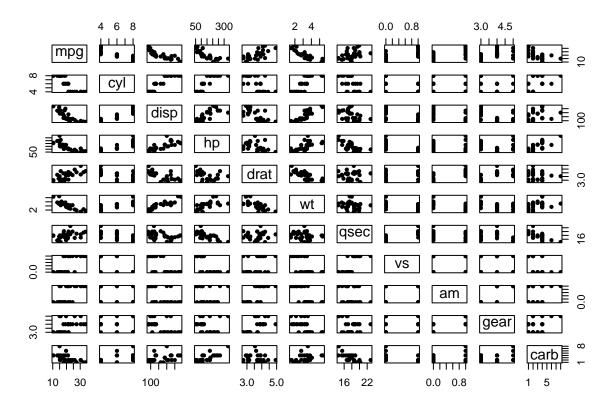
```
plot(x = d$wt,
    y = d$mpg,
    col = d$cyl,
    xlab = "Weight",
    ylab = "MPG",
    main = "Weight vs MGP VS # of Cylinders")
```

Weight vs MGP VS # of Cylinders



 $\mathbf{Q5}$

```
cars_num=subset(cars,select=-c(model))
pairs(cars_num, pch=20)
```



Q6

There is a relationship between wt and mpg and it is subject to the number of cylinders. As shown in the colored scatter plot, vehicles that weigh less and have 4 cylinders have the highest MPG. The second group is the 6 cylinder vehicles with medium weight and they have medium MPG. The last group is the heavy vehicles with the most cylinders and they have the lowest MPG.

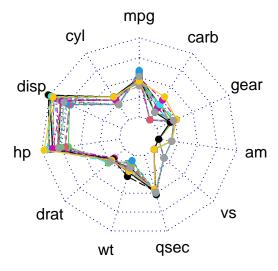
Q7

```
library(fmsb)
\max_{min} \leftarrow \text{data.frame}(\text{mpg} = c(6, 0), \text{cyl} = c(6, 0), \text{disp} = c(6, 0), \text{hp} = c(6, 0), \text{drat} = c(6, 0), \text{wt} = c(6, 0)
rownames(max_min) <- c("max", "min")</pre>
df=data.frame(cars_num)
df <- log(df[ , -which(names(df) %in% c("am","vs"))])</pre>
df$vs <- cars_num$vs
df$am <- cars_num$am
df <- rbind(max_min, df)</pre>
df
##
                         cyl
                                                         drat
              mpg
                                   disp
                                                hp
                                                                       wt
                                                                                qsec vs am
## max 6.000000 6.000000 6.000000 6.000000 6.000000 6.000000
```

```
3.044522 1.791759 5.075174 4.700480 1.360977 0.9631743 2.800933
       3.044522 1.791759 5.075174 4.700480 1.360977 1.0560527 2.834389
                                                                         0
## 3
       3.126761 1.386294 4.682131 4.532599 1.348073 0.8415672 2.923699
## 4
       3.063391 1.791759 5.552960 4.700480 1.124930 1.1678274 2.967333
## 5
       2.928524 2.079442 5.886104 5.164786 1.147402 1.2354715 2.834389
       2.895912 1.791759 5.416100 4.653960 1.015231 1.2412686 3.006672
## 6
                                                                            Ω
       2.660260 2.079442 5.886104 5.501258 1.166271 1.2725656 2.762538
       3.194583 1.386294 4.988390 4.127134 1.305626 1.1600209 2.995732
## 8
                                                                         1
                                                                            0
## 9
       3.126761 1.386294 4.947340 4.553877 1.366092 1.1474025 3.131137
## 10
       2.954910 1.791759 5.121580 4.812184 1.366092 1.2354715 2.906901
       2.879198 1.791759 5.121580 4.812184 1.366092 1.2354715 2.939162
       2.797281 2.079442 5.619676 5.192957 1.121678 1.4036430 2.856470
##
       2.850707 2.079442 5.619676 5.192957 1.121678 1.3164082 2.867899
                                                                         0
                                                                            0
  13
       2.721295 2.079442 5.619676 5.192957 1.121678 1.3297240 2.890372
       2.341806 2.079442 6.156979 5.323010 1.075002 1.6582281 2.889260
## 15
                                                                         0
                                                                            0
## 16
       2.341806 2.079442 6.131226 5.370638 1.098612 1.6908336 2.880321
                                                                         0
                                                                            0
       2.687847 2.079442 6.086775 5.438079 1.172482 1.6761615 2.857619
##
                                                                         0
  17
       3.478158 1.386294 4.365643 4.189655 1.406097 0.7884574 2.968875
       3.414443 1.386294 4.326778 3.951244 1.595339 0.4793350 2.918851
##
       3.523415 1.386294 4.264087 4.174387 1.439835 0.6070445 2.990720
## 21
       3.068053 1.386294 4.788325 4.574711 1.308333 0.9021918 2.996232
                                                                            Λ
       2.740840 2.079442 5.762051 5.010635 1.015231 1.2584610 2.825537
       2.721295 2.079442 5.717028 5.010635 1.147402 1.2340169 2.850707
## 23
                                                                         0
                                                                            0
       2.587764 2.079442 5.857933 5.501258 1.316408 1.3454724 2.735017
## 24
## 25
       2.954910 2.079442 5.991465 5.164786 1.124930 1.3467736 2.836150
       3.306887 1.386294 4.369448 4.189655 1.406097 0.6601073 2.939162
       3.258097 1.386294 4.789989 4.510860 1.488400 0.7608058 2.815409
## 27
  28
       3.414443 1.386294 4.554929 4.727388 1.327075 0.4140944 2.827314
                                                                            1
       2.760010 2.079442 5.860786 5.575949 1.439835 1.1537316 2.674149
       2.980619 1.791759 4.976734 5.164786 1.286474 1.0188473 2.740840
                                                                            1
## 31
       2.708050 2.079442 5.707110 5.814131 1.264127 1.2725656 2.681022
                                                                         0
                                                                            1
##
  32
       3.063391 1.386294 4.795791 4.691348 1.413423 1.0224509 2.923162 1
##
           gear
## max 6.000000 6.0000000
## min 0.000000 0.0000000
## 1
       1.386294 1.3862944
## 2
       1.386294 1.3862944
## 3
       1.386294 0.0000000
## 4
       1.098612 0.0000000
## 5
       1.098612 0.6931472
## 6
       1.098612 0.0000000
## 7
       1.098612 1.3862944
## 8
       1.386294 0.6931472
## 9
       1.386294 0.6931472
## 10
       1.386294 1.3862944
       1.386294 1.3862944
## 11
## 12
       1.098612 1.0986123
## 13
       1.098612 1.0986123
       1.098612 1.0986123
## 14
## 15
       1.098612 1.3862944
## 16
       1.098612 1.3862944
## 17
       1.098612 1.3862944
## 18
      1.386294 0.0000000
## 19 1.386294 0.6931472
```

```
1.386294 0.0000000
## 20
## 21
       1.098612 0.0000000
## 22
       1.098612 0.6931472
## 23
       1.098612 0.6931472
##
  24
       1.098612 1.3862944
## 25
       1.098612 0.6931472
## 26
       1.386294 0.0000000
## 27
       1.609438 0.6931472
## 28
       1.609438 0.6931472
##
  29
       1.609438 1.3862944
##
   30
       1.609438 1.7917595
       1.609438 2.0794415
##
  31
## 32
       1.386294 0.6931472
```

radarchart(df)



Explanation: I can't tell from the chart since there are so many cars in the chart and they are pretty close on the chart.