

COMP21111 Assignment 10
20 marks

Deadline: 17th Dec., time 12:00, SSO

Show your working.

Problem 1 (5 marks)

Write down LTL formulas expressing the following properties of paths:

- ▶ If F holds then sometime in the future $\neg F$ holds.
- ▶ There are infinitely many states in which F holds but G does not.
- ▶ F holds exactly at two states.
- ▶ If F holds in a state s_k then G does not hold in a previous state s_{k-1} , for $k \geq 1$.

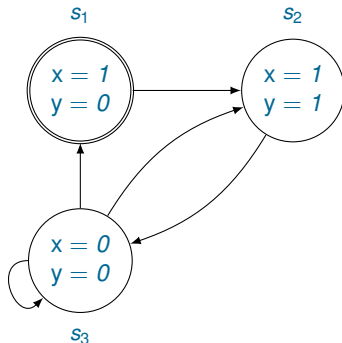
Problem 2 (5 marks)

Show that the following formulas are not equivalent by giving a path that satisfies one of them but not the other:

$$\begin{array}{c} \Box \Diamond (p \wedge q) \\ \Box \Diamond p \wedge \Box \Diamond q \end{array}$$

Problem 3 (10 marks)

Consider a transition system with the following state transition graph.



Which of the following formulas are true on all of the paths starting from the initial state? If a formula is false on a path draw one such path.

1. $\Box x \vee \Box \neg y$
2. $\Diamond(x \leftrightarrow y)$
3. $\Diamond \Box(x \rightarrow y)$
4. $\Box \Diamond(x \leftrightarrow y)$
5. $x \mathbf{U} \Diamond y$