

## Exercise 7(a)

Suppose that  $KU_A$  and  $KR_A$  are the public and private keys of a party  $A$  respectively, that  $KU_B$  and  $KR_B$  are those of a party  $B$ , and that each of  $A$  and  $B$  can use any cryptosystems.

(i) If  $A$  wants to send a very long message to  $B$ , suggest an encryption method by which only  $B$  can decrypt the message and the encryption/decryption processes are the most efficient. Make clear the role of PKI in this method design.

(ii) Can  $A$  encrypt a message so that anyone receiving the message will be assured that the message came only from  $A$  (i.e. authenticity protection)? If yes, give your method; and if not, explain why not.

(iii) Suggest an *efficient* method by which both confidentiality and authenticity protections are provided.

## Answers to Exercise 7(a)

(i)  $A$  encrypts a message  $M$  with a secret session  $k$  chosen randomly, and then  $k$  with  $B$ 's public key  $KU_B$ , i.e.  $E(k, M)$  and  $E(KU_B, k)$ .  $A$  sends both  $E(k, M)$  and  $E(KU_B, k)$  to  $B$ . Should mention that the public key should be trusted; this means before using  $B$ 's public key,  $A$  should perform all the checks to ensure that the key is trust-worthy. So what are these checks?

(ii)  $A$  encrypts the hash value of the message  $M$  with its own private key, i.e.  $M||t||E(KR_A, H(M||t))$ .

(iii) *There are three possible answers to this question:*

(1)  $A$  can send  $E(KU_B, k)$ ,  $E(k, M)$ ,  $t$ ,  $E(KR_A, H(t||E(k, M)||E(KU_B, k)))$  to  $B$ , where  $t$  is a time stamp,  $H()$  is a one-way hash function, and  $E(KR_A, H(t||E(k, M)||E(KU_B, k)))$  is  $A$ 's signature on the other items. In this solution, the signature is signed on the ciphertext.

(2)  $E(KU_B, k)$ ,  $E(k, M||t||E(KR_A, H(M||t)))$  – in this solution, the signature enjoys the confidentiality protection; the signature verification is done after the two decryptions, so this solution is more vulnerable to DoS attacks than the first solution.

(3)  $E(KU_B, k)$ ,  $E(k, M)$ ,  $t$ ,  $E(KR_A, H(t||M))$  – in this solution, the signature is on plaintext, and the signature is not confidentiality protected; the signature verification is done after two decryptions are done, so again it is more vulnerable to DoS attacks than solution (i).