# GANs and VAEs testing

## A.M. Marshall

#### August 2018

#### 1 Introduction

GANs can provide accurate representations of intractable distributions, without any prior inference [14].

Traditional GANs are an example of representation learning, training data can be unlabelled the GAN learns to create a representation of the whole data set. GAN learns to accurately represent the data without knowledge of future downstream tests the output will be scrutinized against [2].

General GAN papers [15]READ.

GANs and VAEs are implicit generative models transferring random latent variables (multiple dimensions) through a mapping function (neural network) into generated samples.

VAEs [10] can learn a disentangled representation of full sample in latent space, a small changes in latent space can induce large variations in the real space of the sample [11].

Here is presented a brief summary of the set up and procedure for GAN and VAE testing. All approaches here make heavy use of the Keras deep learning framework built on top of TensorFlow [3] [1].

https://github.com/alexmarshallbristol/Generative\_Networks

#### 1.1 Generative Models in HEP

#### 1.1.1 GANs

[5], LAGAN - jets.

[12]. "Generative models based on neural networks are highly parametrized and the model parameters have no obvious interpretation. In contrast, scientific simulators can be thought of as highly regularized generative models as they typically have relatively few parameters and they are endowed with some level of interpretation. In this setting, inference on the model parameters  $\theta$  is often of more interest than the latent variables z".

[7], WGAN to model showers in calorimters. Used  $\beta_1$  in Adam equal to 0. Other than saying which parameters they use they specify nothing about training.

[17], detector response to jets. "We did not perform a formal optimization of the neural networks architecture, but we picked a particular set of values after exploring the parameter space in terms of width and depth of the networks, based on two factors: the performance of the model and the computational times required".

[18], calorimters.

#### 1.1.2 VAEs

[16], QCD processes. [4].

### 2 Pre-processing

Data is pulled from Thomas' production files

/eos/experiment/ship/data/Mbias/background-prod-2018/pythia8\_Geant4\_10.0\_withCharmandBeauty%d000\_mu.root"%file\_number

This sample is weighted with various contribution weighted up (vector meson decay, contributions from charm and beauty). Firstly note the muons I save are muons that got to the end of the hadron absorber in the run\_fixedTarget.py production. These are muons that have hits in the vetoPoint tree. These muons are split into 4 categories and data is saved separately. The categories are as follows:

- Category 1: Positive muons vetoPoint.PdgCode() == -13 that have MCTrack.StartX() == 0 and MCTrack.StartY() == 0
- Category 2: Negative muons vetoPoint.PdgCode() == 13 that have MCTrack.StartX() == 0 and MCTrack.StartY() == 0
- Category 3: Positive muons vetoPoint.PdgCode() == -13 that have MCTrack.StartX() != 0 and MCTrack.StartY() != 0
- Category 4: Negative muons vetoPoint.PdgCode() == 13 that have MCTrack.StartX() != 0 and MCTrack.StartY() != 0

for Category 1 and Category 2 data is stored in the following format for each muon:

```
[[e.GetWeight()/768.75,e.GetStartZ(), e.GetPx(), e.GetPy(), e.GetPz()]]
```

where the value 768.75 is the largest weight in the sample and is used to normalize the e.GetWeight() value to a probability. For Category 3 and Category 4 more StartX and StartY data is also stored:

```
[[e.GetWeight()/768.75,e.GetStartX(),e.GetStartY(),e.GetStartZ(),
e.GetPx(), e.GetPy(), e.GetPz()]]
```

Category 1 and Category 2 will be the training data for generative networks with input\_dims = 4, while Category 3 and Category 4 will be for networks with input\_dims = 6.

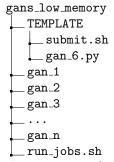
Thomas' sample is split over 66 files. To increase the speed of this pre-processing step data is pulled from all of these  $^1$ . From each file a separate array is saved containing information on the minimum and maximum values seen for each muon parameter in each file. Thomas' full sample is currently run over until  $\sim 1.8$  million muons are obtained in each Category. The distributions for muon parameters for Category 4 can be seen in figure 1.

The data is then combined into single .npy files and the global minimum and maximum values are found and also stored. The global minimum and maximum values are used to normalize the distributions between values of -1 and 1 (input for GAN), the VAE script takes normalised values between 0 and 1 but this is dealt with at the start of the script.

The StartX and StartY distributions in Category 3 and Category 4 are very sharply peaked around a single value, this proves difficult to model for these generative networks. To avoid this another step of pre-processing is completed to broaden these distributions. A mean value is found and subtracted from all values in each distribution, the absolute value of every point is then square rooted and correct sign is then applied. The mean value is then added back to every value and the whole distribution is again normalized. Appropriate secondary minimum, maximum values and mean values used are saved for the post-generation conversion from output to real values. In the initialization of each GAN and VAE the first dimension of these training data arrays containing weight information is split off. This is to feed into numpy.random.choice function which is used for producing each mini-batch training sample from the full training data.

## 3 Blue Crystal Training Set-up

GAN scripts are stored in organized folder structures in my home directory on Blue Crystal (/mnt/storage/home/am13743/gans\_low\_memory/) in the following structure, where gan\_1 is a copy of TEMPLATE:



Large groups of jobs testing various combinations of hyper parameters can be set up and run with shell scripts from these directories.

The training data is stored in /mnt/storage/scratch/am13743/gan\_training\_data/. The output directory is set to (/mnt/storage/scratch/am13743/low\_memory\_gan\_out/%d/test\_output)%file\_number where file\_number is set corresponding to the test number.

This set up is mimicked for VAE training.

## 4 Figure of Merit and Training Output

A function is set up in both GAN and VAE scripts to be called every n training steps to check progress of the network output. Histograms of real and generated values for each muon parameter are generated see figure 1, along with two dimensional histograms showing the correlations between each unique pair of muon parameters, see figure 3. Alignment of these plots show successful training of the network.

An accurate figure of merit (FOM) is needed to track progress and network accuracy. The approach taken is at every training step to train a classifier. Boosted decision tree (BDT) was chosen because it is fast to train and simple to implement. A BDT is trained on a selected training sample of 50k real and generated muons. Then feed the BDT 50k different real and generated muons and plot the output [25]. The measure of the goodness of the network then is the reduced  $\chi^2$  or the overlap between the BDT output distribution from the generated muons and that of the real muons. The BDT acts to systematically reduce the dimensionalality of the higher dimensional muon parameter space into just 1 dimension, see figure 5. Traditional goodness of fit methods such as  $\chi^2$  break down in high dimensions when data is sparse and almost all bins have low or no occupancy. These methods work well on this reduced space. The reduced  $\chi^2$  and the overlap between generated and real distributions is watched and training is stopped when improvement plateaus.

The BDT used currently is sklearn. GradientBoostingClassifier(n\_estimators=100, learning\_rate=0.1, max\_depth=4). If the max\_depth parameter is too low the representation of the real and generated samples on the 1D BDT output space is discontinuous. max\_depth = 4 was chosen to have as continuous as possible distributions for fastest training time.

<sup>&</sup>lt;sup>1</sup>some of the 66 files are blacklisted as they contain rouge muons originating from a bad charm production file.

#### 5 GAN Structure

Generative adversarial networks (GANs) employ two neural networks, the generator and the discriminator [8]. The generator has an input of latent space and outputs muon 'images'. The discriminator learns to distinguish between generator output images (fake images) and real training images. The generator learns from tricking the discriminator. The discriminator and generator are iteratively trained as to both become more powerful together, learning form each others output. The goal of the GAN is to produce realistic muon images.

As with all GANs, generator (G) and discriminator (D) models are stacked into one stacked\_generator\_discriminator model inside which the weights of D are frozen (D.trainable = False).

The GAN has the G and D models both having inverted pyramid structure with the number of nodes increasing deeper into the network, the base number of nodes is the same. Every layer is a dense fully connected layer. The number of nodes is structured as follows, in order of depth in the layer: 256\*n, 512\*n, 1024\*n, 2048\*n (where n is the node factor, -nG or -nD for G and D respectively, editable with argparse). This inverted pyramid structure is not at all required. I will experiment with a flat structure soon.

Dropout layers are added between each dense layer to help prevent over fitting [24] (understand what is meant by noise from dropout).

Batch normalization is used in every layer. This reduces the shift in features inside hidden layers, allowing each layer to learn more independently. This can increase stability at higher learning rates and add regularization which can help prevent over fitting [9].

G has a latent space input of size (n,100) where n is the number of 'images' to generate. The value of 100 is picked arbitrarily.

Two loss functions are used in the GAN, standard binary\_crossentropy (measuring the difference between input and output labels) from Keras and \_loss\_generator which is user defined as:

```
K.mean(-(K.log(y_pred)), axis=-1)
```

where y\_pred is the output of D.

D is complied with the binary\_crossentropy loss function, D sees the input labels and output labels are tested against this. Loss function is high if the output of D does not accurately match the labels. G and the stacked\_generator\_discriminator are complied with \_loss\_generator, although note G is never directly trained. Labels throughout the GAN are such that if stacked\_generator\_discriminator is outputting a high mean label the \_loss\_generator loss function is lower. In this setup real data is labeled 1 and generated data is labeled 0.

The training order is as followed:

- Fake images are sampled from G, these are synthetic\_images.
- D is trained to distinguish synthetic\_images from training sample (legit\_images).
- stacked\_generator\_discriminator is trained on normal latent noise which is miss-labeled as true images (label = 1). Back propagation works here to reduce the loss function \_loss\_generator. This is minimal if the mean discriminator output is closer to 1, which is equivalent to more generated images staying mislabeled as true images. D is frozen at this point so the weights of G are updated to minimize this loss function.
- Repeat, this time however the fake images from G will be slightly improved.

Two techniques are employed to prevent over fitting and mode collapse. Mode collapse is a common failure in GANs, where the generator locks onto one particularly successful output image which is able to constantly trick the discriminator, this single output acts like a local minimum. Firstly the labels on both legit\_images and synthetic\_images that are seen by D are blurred with Gaussian noise of  $\mu=0$  and  $\sigma=0.3$ , [22] suggests only smearing positive labels. Secondly, the true values for muon parameters in the training sample are blurred with a very small amount of Gaussian noise ( $\mu=0$  and  $\sigma=0.001$ ) every time a mini-batch sample is created. The GAN gain gain stability when it's job is made harder [23]. Testing will be undertaken to understand the effectiveness of these approaches, this will occur when a final structure for the GAN is settled on.

It is often good practice along with normalizing neural network training data, to also shift mean value to 0. This step is not included here, there are some strict physical boundaries in the data. For example no muon can have a StartZ value before the start of the target. The GANs seem not to have a problem with non centred inputs.

### 6 VAE Structure

VAE structure has the encoder and decoder built up of dense fully connected layers. The encoder has the goal of transferring input muon 'images' into a latent space. This latent space is of lower dimensions. Via a KL-divergence term in the loss function the encoder is forced into molding the full samples' representation in latent space into an uncorrelated multivariate Gaussian. This latent space representation is then fed to the decoder which learns to transfer it back into real space, recreating the samples originally fed to the encoder. The requirement for reconstruction of the same samples means the encoder has a complex job of creating a latent space that makes sense to the decoder.

Forcing the full sample to have an uncorrelated multivariate Gaussian representation in latent space is what makes generation of new muons possible. The KL-divergence term encourages these Gaussian distributions (one in each dimension of latent space) to have  $\mu=0$  and  $\sigma=1$  [6]. Generating data then only

requires sampling simple  $\mu = 0$  and  $\sigma = 1$  normal distributions to create latent samples and running these through the decoder network.

The loss function for the VAE (vae\_loss) is:

```
xent_loss = original_dim * objectives.binary_crossentropy(x, x_decoded_mean)
kl_loss = - 0.5 * K.sum(1 + z_log_var - K.square(z_mean) - K.exp(z_log_var), axis=-1)
vae_loss = xent_loss*xent_factor + kl_loss
```

xent\_loss is the standard binary crossentropy loss, this is high if the output images from the decoder are far from the input images fed to the encoder. The kl\_loss term is high if distributions of samples in each dimensions of latent space are far from unit Gaussians. xent\_factor refers to a weighting. Without the xent\_factor value, variations in the kl\_loss term dominate the progress of the loss function and the output of the VAE is nonsense.

The training of the VAE is simple, it is fed the training sample which is labeled with itself:

```
vae.train_on_batch(legit_images, legit_images)
```

Currently experimenting with adding batch normalization and dropout to layers of VAE. READ [28].

TALK ABOUT VAE SAMPLING

# 7 GAN Training

The GAN script is built with argparse allowing easy change of hyper parameters, controlling GAN architecture and training.

The GAN takes the following options:

- $\bullet\,$  -l, learning rate, default set to 0.0002
- -o, optimizer choice, default set to Adam with amsgrad=True
- -nG, node factor, default set to 1
- ullet -nD, node factor, default set to 1
- $\bullet$  -layers G, number of layers in generator, default set to 3
- -layersD, number of layers in discriminator, default set to 3

Preliminary testing proved learning was most stable with default optimizer Adam with amsgrad=True instead of alternatives of Adam without amsgrad=True [20] and RMSprop. So for testing since then I have focused on default optimizer. A lower learning rate increases stability of training, a lower than default value of 0.00005 was found in preliminary testing to be stable whilst not making training too slow. The Adam optimizer uses momentum to speed up training. A momentum controlling parameter  $_1$  can be varied which is shown to provide mixed results, I currently use  $_1=0.5$  as suggested by Radford et. al [19]. I will play with this.

The -layersO and -layersD parameters control the numbers of layers in each network. These are found to be optimal when they are both set equal to 2. Combinations of values were checked between 1 to 4 for each parameter.

The -nG and -nD hyper parameters controls the number of nodes in each layer of corresponding networks. Performance appears to be improved when -nG -nD, optimum appears to be when -nG = 6 and -nD = 3 for the 6 dimensional GAN case (training on Category 3 and Category 4 from section 2).

Batch size is also important for training. This parameter controls the difference between gradient descent (GD), stochastic GD and min-batch GD [21]. It was found in preliminary testing that a value of  $\sim 100$  was good, 1000 being too high and 10 too low.

#### 8 VAE Training

The VAE script is also built with argparse.

The VAE takes the following options:

- -lr, learning rate, default set at 0.001 (higher than GAN)
- $\bullet\,$  -x, cross-entropy factor, default set at 1000
- -iE, intermediate dimensions (nodes) in every layer of encoder (E), default set to 100
- -iD, intermediate dimensions (nodes) in every layer of decoder (D), default set to 100
- $\bullet\,$  -layers E, number of layers in E, default set to 3
- -layersD, number of layers in D, default set to 3

the choice of value for the learning rate is very dependent on the optimizer chosen, currently running with a high learning rate value for the Adam optimizer but this needs investigation.

The number of dimensions in latent space is variable, in preliminary tests it was found if this value was too small ( $\sim$  2), output was worse, probably too much information was lost and VAE found it harder to produce good output from decoder. Currently the number of dimensions in latent space is set to 4.

The cross-entropy factor -x as discussed in section 6 this should be high,  $\sim 1000$ .

The number of nodes in each layer of each network needs to be optimized.

The number of layers in each network needs to be optimized.

[23]

### 9 GAN Output

Follows is currently the best achieved output from a 6 input dimension GAN, this was trained on Category 4 (from section 2) training data. The values for relevant hyperparameters were:

- -nG = 6
- -nD = 2
- -layersG = 2
- -layersD = 2

this is the output after 2,710,000 training steps,  $\sim 30$  hours of training on Blue Crystal.

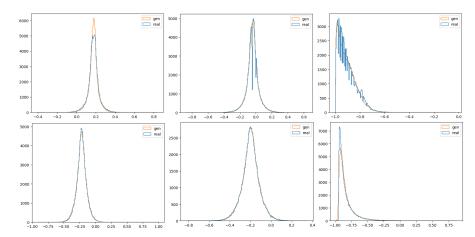


Figure 1: One dimensional histograms of output for each the 6 muon parameters overlayed against training sample. Distributions 0 and 1 here are displayed post-broadening as they are fed to the GAN.

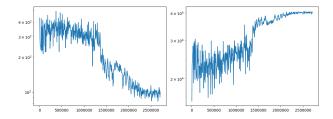


Figure 2: Left: progress of reduced  $\chi^2$  estimator for the distance between distributions in figure 5. Right: progress of overlap between distributions in figure 5.

I have begun optimization testing on 4 dimension GANs, in theory this should be an easier optimization.

#### 10 VAE Output

Do not yet have an optimized VAE for 4 dimensions or 6 dimensions.

### 11 Generation and Benchmarking

Generation will require 4 fully trained and optimized networks. When this achieved generation will be completed in accordance to the ratios of appearance of muons in the full sample using Poisson sampling.

If the a high fraction of events in a single category are weighted up this could cause a problem. You generate based on weights of full samples to avoid this?

Benchmarking must include full I/O to ROOT files. A technique must be developed to make this as fast as possible.

## 12 Generating Dangerous Region

Train VAE on full sample, see where in latent space dangerous muons are, generate latent noise in this region and feed to decoder. GAN alternative is conditional GANs [14], or only training a GAN on dangerous muons.

[27] gan struggles to reach nash equilibrium and avoides over fitting.

## 13 Discussion and Comparison of Methods

Is there a problem with BDT approach to FOM with GAN generating bulk of distribution well and this tricking BDT?

Currently appears like GAN is about to trick BDT much better than VAE. If BDT is creating an accurate FOM this implies GAN is better for this task.

Discontinuous fine structure of the target (seen in StartZ distribution) probably is too detailed to learn, can justify that this doesn't affect performance of the GAN for SHiP with simple argument.

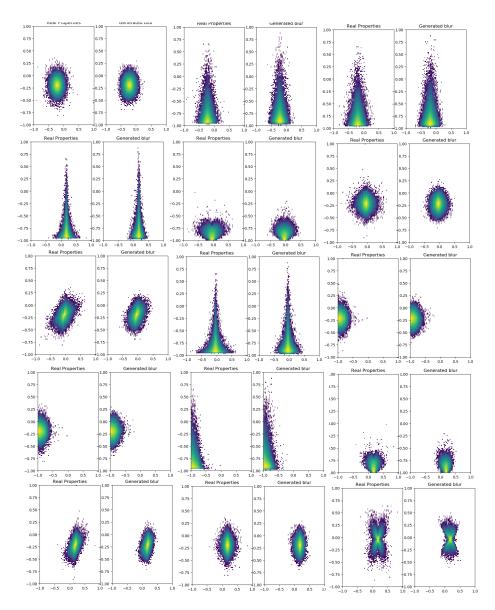


Figure 3: Two dimensional histograms displaying the correlations between each unique pair of the 6 muon parameters, generated and training samples are paired up.

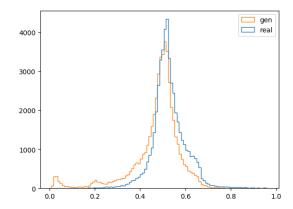


Figure 4: Output distributions of BDT for both fake and real images.

Can tails of distribution be better modeled if we normalize between -0.9 and 0.9? DO THIS - then scan latent space, make heat map of BDT predction to evaluate the greater than 0.9 region

Is label and data smearing helping?

GAN less prone to over fitting [27].

Less latent dimensions? [27] bigger better?? Careful as too high could create dead spaces, unseen in training [26].

[13]

[2], "GANs are highly unstable and prone to miss modes. We argue that these bad behaviors of GANs are due to the very particular functional shape of the trained discriminators in high dimensional spaces, which can easily make training stuck or push probability mass in the wrong direction, towards that of higher concentration than that of the data generating distribution". "although the generators produce meaningful samples, these samples are often from just a few modes (small regions of high probability under the data distribution). many modes of the data generating distribution are not at all represented in the generated samples, yielding amuch lower entropy distribution, with less variety than the data generating distribution". "In other words, since the discriminator's output is nearly 0 and 1 on fake and real data respectively, the generator is not penalized for missing modes."

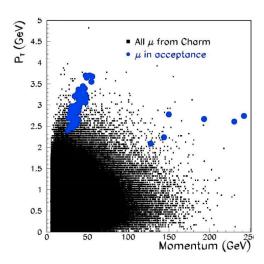


Figure 5: Dangerous muons as in early SHiP production.

Vanishing gradient - "As an example, Denton et al. (2015) noted a common failure pattern for training GANs which is the vanishing gradient problem, in which the discriminator D perfectly classifies real and fake examples, such that around the fake examples, D is nearly zero. In such cases, the generator will receive no gradient to improve itself." [2]

Understanding GAN latent space: grid search over 2 out of the 100 dimensions, run samples through BDT and plot BDT output values. Search for dead space. Plot heat map.

### References

- [1] Martín Abadi, Paul Barham, Jianmin Chen, Zhifeng Chen, Andy Davis, Jeffrey Dean, Matthieu Devin, Sanjay Ghemawat, Geoffrey Irving, Michael Isard, et al. Tensorflow: a system for large-scale machine learning. In *OSDI*, volume 16, pages 265–283, 2016.
- [2] Xi Chen, Yan Duan, Rein Houthooft, John Schulman, Ilya Sutskever, and Pieter Abbeel. Infogan: Interpretable representation learning by information maximizing generative adversarial nets. In *Advances in neural information processing systems*, pages 2172–2180, 2016.
- [3] François Chollet et al. Keras. https://keras.io, 2015.
- [4] Marco Cristoforetti, Giuseppe Jurman, Andrea I Nardelli, and Cesare Furlanello. Towards meaningful physics from generative models. arXiv preprint arXiv:1705.09524, 2017.
- [5] Luke de Oliveira, Michela Paganini, and Benjamin Nachman. Learning particle physics by example: location-aware generative adversarial networks for physics synthesis. *Computing and Software for Big Science*, 1(1):4, 2017.
- [6] Carl Doersch. Tutorial on variational autoencoders. arXiv preprint arXiv:1606.05908, 2016.
- [7] Martin Erdmann, Jonas Glombitza, and Thorben Quast. Precise simulation of electromagnetic calorimeter showers using a wasserstein generative adversarial network. arXiv preprint arXiv:1807.01954, 2018.
- [8] Ian Goodfellow, Jean Pouget-Abadie, Mehdi Mirza, Bing Xu, David Warde-Farley, Sherjil Ozair, Aaron Courville, and Yoshua Bengio. Generative adversarial nets. In Advances in neural information processing systems, pages 2672–2680, 2014.
- [9] Sergey Ioffe and Christian Szegedy. Batch normalization: Accelerating deep network training by reducing internal covariate shift. arXiv preprint arXiv:1502.03167, 2015.
- [10] Diederik P Kingma and Max Welling. Auto-encoding variational bayes. arXiv preprint arXiv:1312.6114, 2013.
- [11] Tejas D Kulkarni, William F Whitney, Pushmeet Kohli, and Josh Tenenbaum. Deep convolutional inverse graphics network. pages 2539–2547, 2015.
- [12] Gilles Louppe and Kyle Cranmer. Adversarial variational optimization of non-differentiable simulators.  $arXiv\ preprint\ arXiv:1707.07113,\ 2017.$
- [13] Luke Metz, Ben Poole, David Pfau, and Jascha Sohl-Dickstein. Unrolled generative adversarial networks. arXiv preprint arXiv:1611.02163, 2016.
- [14] Mehdi Mirza and Simon Osindero. Conditional generative adversarial nets.  $arXiv\ preprint$   $arXiv:1411.1784,\ 2014.$
- [15] Shakir Mohamed and Balaji Lakshminarayanan. Learning in implicit generative models. arXiv preprint arXiv:1610.03483, 2016.
- [16] James William Monk. Deep learning as a parton shower. arXiv preprint arXiv:1807.03685, 2018.

- [17] Pasquale Musella and Francesco Pandolfi. Fast and accurate simulation of particle detectors using generative adversarial neural networks. arXiv preprint arXiv:1805.00850, 2018.
- [18] Michela Paganini, Luke de Oliveira, and Benjamin Nachman. Accelerating science with generative adversarial networks: an application to 3d particle showers in multilayer calorimeters. *Physical review letters*, 120(4):042003, 2018.
- [19] Alec Radford, Luke Metz, and Soumith Chintala. Unsupervised representation learning with deep convolutional generative adversarial networks. arXiv preprint arXiv:1511.06434, 2015.
- [20] Sashank J Reddi, Satyen Kale, and Sanjiv Kumar. On the convergence of adam and beyond. 2018.
- [21] Sebastian Ruder. An overview of gradient descent optimization algorithms. arXiv preprint arXiv:1609.04747, 2016.
- [22] Tim Salimans, Ian Goodfellow, Wojciech Zaremba, Vicki Cheung, Alec Radford, and Xi Chen. Improved techniques for training gans. In Advances in Neural Information Processing Systems, pages 2234–2242, 2016
- [23] Casper Kaae Sønderby, Jose Caballero, Lucas Theis, Wenzhe Shi, and Ferenc Huszár. Amortised map inference for image super-resolution. arXiv preprint arXiv:1610.04490, 2016.
- [24] Nitish Srivastava, Geoffrey Hinton, Alex Krizhevsky, Ilya Sutskever, and Ruslan Salakhutdinov. Dropout: a simple way to prevent neural networks from overfitting. *The Journal of Machine Learning Research*, 15(1):1929–1958, 2014.
- [25] Constantin Weisser and Mike Williams. Machine learning and multivariate goodness of fit. arXiv preprint arXiv:1612.07186, 2016.
- [26] Tom White. Sampling generative networks. arXiv preprint arXiv:1609.04468, 2016.
- [27] Yuhuai Wu, Yuri Burda, Ruslan Salakhutdinov, and Roger Grosse. On the quantitative analysis of decoder-based generative models. arXiv preprint arXiv:1611.04273, 2016.
- [28] Serena Yeung, Anitha Kannan, Yann Dauphin, and Li Fei-Fei. Tackling over-pruning in variational autoencoders. arXiv preprint arXiv:1706.03643, 2017.

# 14 Appendix

#### 14.1 Dropout

Randomly ignoring neurons during training phase, this is to say all other weights are adapted as normal as if they were the whole network. Helps prevent over fitting. During training neurons can develop codependence, in this state their individual power is reduced. Dropout roughly doubles the time taken for network to converge

### 14.2 Batch normalization

Normalization of every hidden layer input values. This reduces the extent to which values shift around. Inputs are normalized to have a mean value of 0. If each layer is considered a new network, and for the first layers input it is good practice to normalize the input, why wouldn't you want to do it for all. Practically activations (values after each node) are normalized on a batch basis, the input for the whole network is completed on full sample. This process allows network to train faster, accommodates higher learning rates. Adds small amount of noise which acts as regul

#### 14.3 Activation Layers

Weighted sum of inputs plus bias, output is determined from activation shape. LeakyRELU avoids gradient vanishing.

## 14.4 Mini-batch gradient descent

Gradient descent uses full sample for each training step. Stochastic gradient descent shows one sample for each step. Mini-batch gradient descent is an intermediate, gives small batches each step. Showing less of the sample each training step leads to faster training and avoidance of local minima, randomness in the sample selection can kick NN out of a local minima.

### 14.5 Optimziers

AMSgrad

#### 14.6 Loss functions