GEE vs GLMM

- GEE is like studying all patients in a hospital and saying, "On average, this new epilepsy medication reduces seizure rates by 20%." It gives a broad, public health-focused conclusion without worrying about individual differences.
- GLMM is like a doctor adjusting a patient's treatment plan based on their unique seizure patterns. Some patients might have higher baseline seizure rates than others, and GLMM accounts for these individual differences.

Interpretation of Treatment Effects

- Using GEE:
 - The estimated treatment effect represents the average reduction in seizure counts across all patients.
 - Example interpretation: "On average, patients taking the new medication experience 20% fewer seizures compared to the control group."
 - This is useful if we care about **overall public health impact** rather than individual predictions.
- Using GLMM:
 - o The treatment effect accounts for **individual differences in seizure frequency** (some patients may have naturally higher or lower seizure rates).
 - Example interpretation: "For a given patient, the medication reduces their expected seizure count by 20% compared to their untreated seizure count."
 - This is useful if we want individualized predictions (e.g., estimating how a specific patient might respond).

```
data epileptic;
set epileptic_w;
array AC(1:5) CO-C4;
array Aweek(1:5) (0 2 4 6 8);
do i=1 to 5;
Count = AC[i];
week = Aweek[i];
L_per = log(2);
if i eq 1 then L_per=log(8);
output;
end;
```

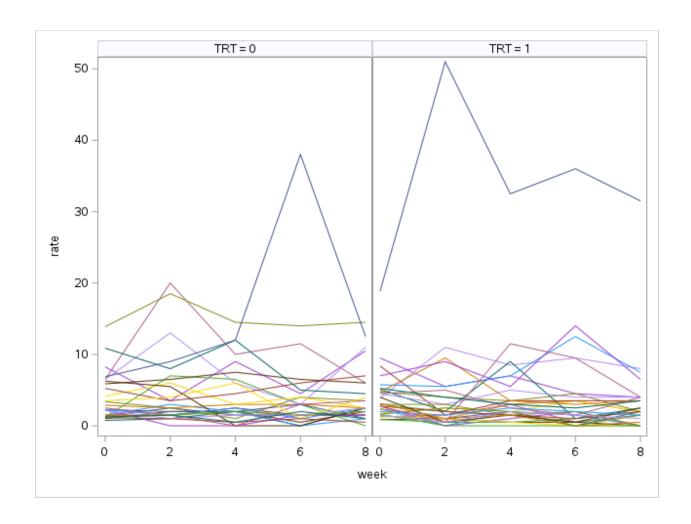
```
drop CO-C4 Aweek1 - Aweek5 i;
run;

data epileptic;
set epileptic;
  rate = Count/exp(L_per);
  l_count = log(Count+1);
  l_rate = log((Count+1)/exp(L_per));
run;

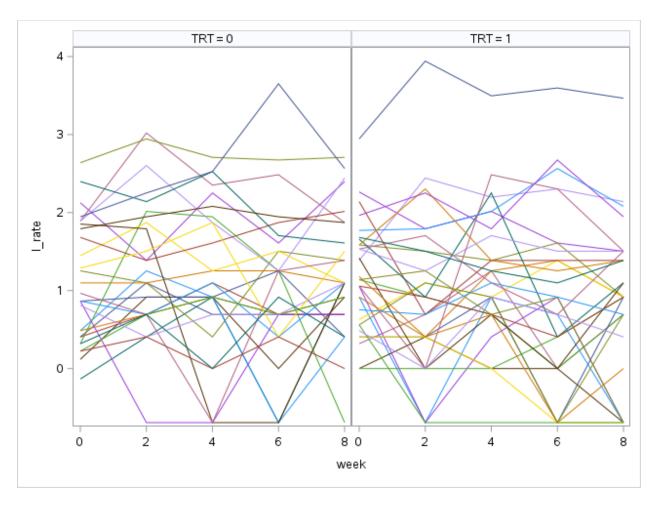
proc print data=epileptic (obs=10);
run;
```

Obs	ID	TRT	Age	Count	week	L_per	rate	I_count	I_rate
1	1	0	31	11	0	2.07944	1.375	2.48491	0.40547
2	1	0	31	5	2	0.69315	2.500	1.79176	1.09861
3	1	0	31	3	4	0.69315	1.500	1.38629	0.69315
4	1	0	31	3	6	0.69315	1.500	1.38629	0.69315
5	1	0	31	3	8	0.69315	1.500	1.38629	0.69315
6	2	0	30	11	0	2.07944	1.375	2.48491	0.40547
7	2	0	30	3	2	0.69315	1.500	1.38629	0.69315
8	2	0	30	5	4	0.69315	2.500	1.79176	1.09861
9	2	0	30	3	6	0.69315	1.500	1.38629	0.69315
10	2	0	30	3	8	0.69315	1.500	1.38629	0.69315

```
Proc SGpanel data = epileptic;
PanelBy TRT / columns=2;
series y=rate x=week / group =ID LineAttrs= (pattern=1 );
run;
quit;
```



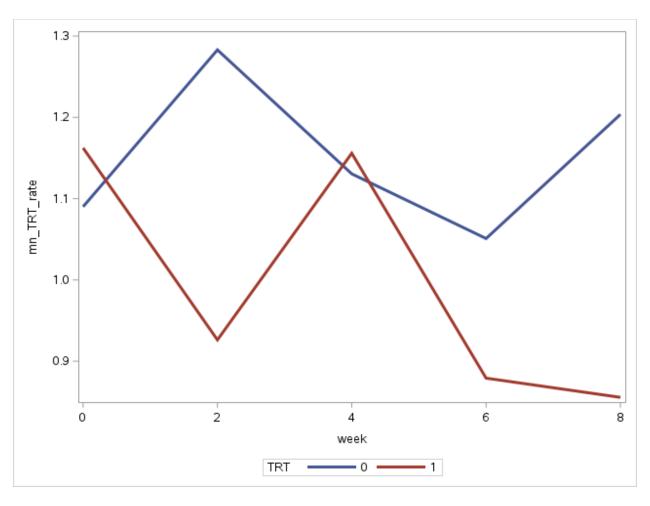
```
Proc SGpanel data = epileptic;
PanelBy TRT / columns=2;
series y=l_rate x=week / group =ID LineAttrs= (pattern=1 );
run;
quit;
```



```
proc sort data=epileptic;
by TRT week;

*Calculate the mean by week;
proc means mean data=epileptic noprint;
by TRT week;
var l_rate;
output out = MN_TRT_dat mean = mn_TRT_rate;
run;

*First, let's look at the mean by TRT group;
Proc SGplot data = MN_TRT_dat;
series x=week y=mn_TRT_rate / group =TRT LineAttrs= (pattern=1 thickness=3);
run;
```



```
proc gee data=epileptic;
class ID ;
model Count = TRT week TRT*week/d=poisson link=log offset=L_per
type3;
repeated subject=ID/type=exch corrw modelse covb ;
run;
quit;
```

The GEE Procedure

Model Info	ormation
Data Set	WORK.EPILEPTIC
Distribution	Poisson
Link Function	Log
Dependent Variable	Count

Model Info	ormation		
Offset Variable		L_	per
Number of Observat	ions Read	295	
Number of Observat	ions Used	295	

	Class Level Information				
Class	Levels	Values			
ID	59	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59			

Parameter Information			
Parameter	Effect		
Prm1	Intercept		
Prm2	TRT		
Prm3	week		
Prm4	TRT*week		

GEE Model Information			
Correlation Structure	Exchangeable		
Subject Effect	ID (59 levels)		
Number of Clusters	59		
Correlation Matrix Dimension	5		
Maximum Cluster Size	5		
Minimum Cluster Size	5		

Covariance Matrix (Model-Based)					
Prm1 Prm2 Prm3					
Prm1	0.02404	-0.02404	0.001484	-0.001484	
Prm2	-0.02404	0.04507	-0.001484	0.003109	
Prm3 0.00148		-0.001484	0.0006504	-0.000650	
Prm4	-0.001484	0.003109	-0.000650	0.001338	

Covariance Matrix (Empirical)

	Prm1	Prm2	Prm3	Prm4
Prm1	0.02749	-0.02749	0.0001172	-0.000117
Prm2	-0.02749	0.04355	-0.000117	0.0003482
Prm3	0.0001172	-0.000117	0.0005812	-0.000581
Prm4	-0.000117	0.0003482	-0.000581	0.0008272

Working	Correlation Matrix	
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	Obs 1	Obs 2	Obs 3	Obs 4	Obs 5
Obs 1	1.0000	0.7781	0.7781	0.7781	0.7781
Obs 2	0.7781	1.0000	0.7781	0.7781	0.7781
Obs 3	0.7781	0.7781	1.0000	0.7781	0.7781
Obs 4	0.7781	0.7781	0.7781	1.0000	0.7781
Obs 5	0.7781	0.7781	0.7781	0.7781	1.0000

Exchangeable Working Correlation

Correlation	0.7781

GEE Fit Cri	teria
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QIC	-561.1905
QlCu	-581.7413

Parameter Estimates for Response Model

with Empirical Standard Error Estimates

Parameter	Estimate	Standard Error	95% Confidence Limits		Z	Pr > Z
Intercept	1.2901	0.1658	0.9651	1.6150	7.78	<.0001
TRT	0.0378	0.2087	-0.3712	0.4468	0.18	0.8563
week	-0.0009	0.0241	-0.0481	0.0464	-0.04	0.9708
TRT*week	-0.0188	0.0288	-0.0751	0.0376	-0.65	0.5143

Parameter Estimates for Response Model

with Model-Based Standard Error Estimates

Parameter	Estimate	Standard Error	95% Confidence Limits		z	Pr > Z
Intercept	1.2901	0.1550	0.9862	1.5939	8.32	<.0001
TRT	0.0378	0.2123	-0.3783	0.4539	0.18	0.8587
week	-0.0009	0.0255	-0.0509	0.0491	-0.03	0.9724
TRT*week	-0.0188	0.0366	-0.0905	0.0529	-0.51	0.6081

Score Statistics For Type 3 GEE Analysis

Source	DF	Chi-Square	Pr > ChiSq
TRT	1	0.03	0.8549
week	1	0.00	0.9680
TRT*week	1	0.46	0.4967

Interpretation of interaction

Every additional week, the average seizure rate in the treatment group is multiplied by 0.9814 (or reduced by 1.86%) relative to the average seizure rate control group.

Interpretation of main effects

At the beginning of the study (week 0), the average seizure rate in the treatment group is 1.0385 times (or 3.85% higher than) the control group.

In the control group, each additional week the average seizure rate is multiplied by 0.9991 (or decreases by 0.09%).

```
proc gee data=epileptic;
class ID week (ref = '0');
model Count = TRT week TRT*week/d=poisson link=log offset=L_per
type3;
repeated subject=ID/type=exch corrw modelse covb;
run;
quit;
```

GEE Fit Criteria				
QIC	-654.5784			
QlCu	-653.6516			

Score Statistics For Type 3 GEE Analysis Source DF Chi-Square Pr > ChiSq TRT 1 0.03 0.8534 week 4 1.64 0.8012 TRT*week 4 1.80 0.7734

```
proc gee data=epileptic;
class ID ;
model Count = TRT week TRT*week/d=poisson link=log offset=L_per
type3;
repeated subject=ID/type=un corrw modelse covb ;
run;
quit;
```

	Parameter Estimates for Response Model						
	with Empirical Standard Error Estimates						
Parameter	Estimate	Standard Error	95% Confide	z	Pr > Z		
Intercept	1.1074	0.3148	0.4904	1.7243	3.52	0.0004	
TRT	0.1718	0.4013	-0.6148	0.9583	0.43	0.6687	
week	-0.0170	0.0658	-0.1460	0.1119	-0.26	0.7956	
TRT*week	-0.0031	0.0742	-0.1486	0.1423	-0.04	0.9663	

```
proc gee data=epileptic;
class ID ;
model Count = TRT week TRT*week/d=negbin link=log offset=L_per
type3;
repeated subject=ID/type=exch corrw modelse covb ;
run;
quit;
```

The GEE Procedure

Model Information						
woder information						
Data Set	WORK.EPILEPTIC					
Distribution	Negative Binomial					
Link Function	Log					
Dependent Variable	Count					
Offset Variable	L_per					
Number of Observation	295					
Number of Observations Used						

	Class Level Information					
Class	Levels	Values				
ID	59	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59				

Parameter Information				
Parameter	Effect			
Prm1	Intercept			
Prm2	TRT			
Prm3	week			
Prm4	TRT*week			

GEE Model Information				
Correlation Structure	Exchangeable			
Subject Effect	ID (59 levels)			
Number of Clusters	59			
Correlation Matrix Dimension	5			
Maximum Cluster Size	5			
Minimum Cluster Size	5			

Covariance Matrix (Model-Based)						
	Prm1 Prm2 Prm3 Prr					
Prm1	0.06288	-0.06288	-0.001524	0.001524		
Prm2	-0.06288	0.11962	0.001524	-0.002855		
Prm3	-0.001524	0.001524	0.0004494	-0.000449		
Prm4	0.001524	-0.002855	-0.000449	0.0008587		

	Covariance Matrix (Empirical)						
	Prm1 Prm2 Prm3 Prm						
Prm1	0.02748	-0.02748	-0.000386	0.0003865			
Prm2	-0.02748	0.07472	0.0003865	0.001479			
Prm3	-0.000386	0.0003865	0.0004222	-0.000422			
Prm4	0.0003865	0.001479	-0.000422	0.0006613			

Working Correlation Matrix					
	Obs 1	Obs 2	Obs 3	Obs 4	Obs 5
Obs 1	1.0000	0.7486	0.7486	0.7486	0.7486
Obs 2	0.7486	1.0000	0.7486	0.7486	0.7486
Obs 3	0.7486	0.7486	1.0000	0.7486	0.7486
Obs 4	0.7486	0.7486	0.7486	1.0000	0.7486
Obs 5	0.7486	0.7486	0.7486	0.7486	1.0000

Exchangeable Working Correlation

Correlation 0.7486

GEE Fit Criteria

QIC -8251.4951

QICu -8258.4515

Parameter Estimates for Response Model

with Empirical Standard Error Estimates

Parameter	Estimate	Standard Error	95% Confide	ence Limits	Z	Pr > Z
Intercept	1.4214	0.1658	1.0965	1.7463	8.57	<.0001

Parameter Estimates for Response Model with Empirical Standard Error Estimates **Standard** 95% Confidence Limits **Parameter Estimate** Error Z | Pr > |Z| **TRT** 0.0183 0.2733 -0.5175 0.5540 0.07 0.9467 0.0009 0.0205 -0.0393 0.0412 0.05 0.9633 week TRT*week -0.0187 0.0257 -0.0691 0.0317 -0.73 0.4660 **Parameter Estimates for Response Model** with Model-Based Standard Error Estimates Standard Parameter **Estimate** Error 95% Confidence Limits Z | Pr > |Z| Intercept 0.2508 0.9300 1.9129 5.67 <.0001 1.4214 **TRT** 0.0183 0.3459 -0.6596 0.6962 0.05 0.9579 week 0.0009 0.0212 -0.0406 0.0425 0.04 0.9645

-0.64

0.0387

0.5224

C	Statistics	E T	2 0 5 5	A malazaia
Score	STATISTICS	For Type	3 GEE	Anaivsis

0.0293

-0.0762

-0.0187

TRT*week

Source	DF	Chi-Square	Pr > ChiSq
TRT	1	0.00	0.9477
week	1	0.00	0.9644
TRT*week	1	0.50	0.4779