## Random Effects ANOVA

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First, let's read in the data and look at the variables.

```
library(tidyverse)
BP_data_wide <- read.csv("BP_data.csv")
BP_data_wide</pre>
```

ID	BP1	BP2	BP3	BP4	BP5	BP6	BP7	BP8	BP9	BP10
1	130	136	124	121	128	138	130	126	136	133
2	123	116	117	120	117	113	111	124	110	116
3	144	139	136	142	142	133	140	138	140	139
4	128	133	127	124	132	130	134	124	131	128
5	128	128	122	120	121	123	132	130	126	132

To fit the random effects ANOVA model we're going to use the lmer function in the lme4 package. This function is very similar to the gls function except we won't use the correlation statement or weights statements much.

Here, the random effects are put in the formula portion of the model.

```
library(lme4)
?lmer
```

```
## Fit Linear Mixed-Effects Models
##
## Description:
##
## Fit a linear mixed-effects model (LMM) to data, via REML or
## maximum likelihood.
##
## Usage:
##
## lmer(formula, data = NULL, REML = TRUE, control = lmerControl(),
```

## start = NULL, verbose = OL, subset, weights, na.action, ## offset, contrasts = NULL, devFunOnly = FALSE) ## ## Arguments: ## formula: a two-sided linear formula object describing both the ## fixed-effects and random-effects part of the model, with the ## response on the left of a '~' operator and the terms, ## separated by '+' operators, on the right. Random-effects ## terms are distinguished by vertical bars ('|') separating ## ## expressions for design matrices from grouping factors. Two vertical bars ('||') can be used to specify multiple ## uncorrelated random effects for the same grouping variable. ## (Because of the way it is implemented, the '||'-syntax \_works ## ## only for design matrices containing numeric (continuous) ## predictors\_; to fit models with independent categorical ## effects, see 'dummy' or the 'lmer\_alt' function from the ## 'afex' package.) ## ## data: an optional data frame containing the variables named in 'formula'. By default the variables are taken from the ## ## environment from which 'lmer' is called. While 'data' is optional, the package authors \_strongly\_ recommend its use, ## especially when later applying methods such as 'update' and ## 'drop1' to the fitted model (\_such methods are not guaranteed ## ## to work properly if 'data' is omitted\_). If 'data' is ## omitted, variables will be taken from the environment of 'formula' (if specified as a formula) or from the parent ## ## frame (if specified as a character vector). ## ## REML: logical scalar - Should the estimates be chosen to optimize ## the REML criterion (as opposed to the log-likelihood)? ## control: a list (of correct class, resulting from 'lmerControl()' or ## ## 'glmerControl()' respectively) containing control parameters, ## including the nonlinear optimizer to be used and parameters ## to be passed through to the nonlinear optimizer, see the ## '\*lmerControl' documentation for details. ## ## start: a named 'list' of starting values for the parameters in the model. For 'lmer' this can be a numeric vector or a list ## ## with one component named '"theta"'. ## verbose: integer scalar. If '> 0' verbose output is generated during ## the optimization of the parameter estimates. If '> 1' ## ## verbose output is generated during the individual penalized ## iteratively reweighted least squares (PIRLS) steps. ## ## subset: an optional expression indicating the subset of the rows of 'data' that should be used in the fit. This can be a logical ## ## vector, or a numeric vector indicating which observation ## numbers are to be included, or a character vector of the row ## names to be included. All observations are included by ## default.

```
##
   weights: an optional vector of 'prior weights' to be used in the
##
             fitting process. Should be 'NULL' or a numeric vector.
##
             Prior 'weights' are _not_ normalized or standardized in any
##
##
             way. In particular, the diagonal of the residual covariance
             matrix is the squared residual standard deviation parameter
##
             'sigma' times the vector of inverse 'weights'. Therefore, if
##
             the 'weights' have relatively large magnitudes, then in order
##
##
             to compensate, the 'sigma' parameter will also need to have a
##
             relatively large magnitude.
##
## na.action: a function that indicates what should happen when the data
##
             contain 'NA's. The default action ('na.omit', inherited from
             the 'factory fresh' value of 'getOption("na.action")') strips
##
##
             any observations with any missing values in any variables.
##
##
     offset: this can be used to specify an _a priori_ known component to
##
             be included in the linear predictor during fitting. This
##
             should be 'NULL' or a numeric vector of length equal to the
##
             number of cases. One or more 'offset' terms can be included
##
             in the formula instead or as well, and if more than one is
             specified their sum is used. See 'model.offset'.
##
##
## contrasts: an optional list. See the 'contrasts.arg' of
##
             'model.matrix.default'.
## devFunOnly: logical - return only the deviance evaluation function.
             Note that because the deviance function operates on variables
##
             stored in its environment, it may not return _exactly_ the
##
##
             same values on subsequent calls (but the results should
##
             always be within machine tolerance).
library(lmerTest) # Added to get p-values
RE_form <- BP ~ 1 | ID
re_anova <- lmer( formula = RE_form , data = BP_data)</pre>
summary(re_anova)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: RE form
##
      Data: BP_data
##
## REML criterion at convergence: 301.7
##
## Scaled residuals:
##
        Min
                  10
                       Median
                                    30
## -2.09154 -0.72981 -0.00817 0.68723 1.79650
##
## Random effects:
                         Variance Std.Dev.
## Groups
             Name
             (Intercept) 64.14
                                  8.009
                         19.12
                                  4.372
## Residual
## Number of obs: 50, groups: ID, 5
##
## Fixed effects:
```

```
## Estimate Std. Error df t value Pr(>|t|)
## (Intercept) 128.300   3.635   4.000   35.3   3.84e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
round( confint(re_anova), 2)
```

	2.5~%	97.5 %
.sig01	4.12	15.78
.sigma	3.60	5.46
(Intercept)	120.48	136.12