

CS 154 Notes: Computer Architecture

Classes of Computers:

- Personal Computers: general purpose, variety of software [Constraints: costs, battery, size]
- Servers: the cloud; high performance, capacity, and reliability [Constraints: low cost]
- Supercomputers: high-end scientific and engineering calculations [Constraints: highest performance]
- Embedded Computers: hidden as components of systems [Constraints: tiny, zero power, minimal cost]

Applications suggest how to improve technology and provide revenue to fund development

Improved technologies make new applications possible

Cost of software development makes compatibility a major decision market in the market

Computer Components: (1) Processor, (2) Memory, (3) Input Devices, (4) Output Devices, (5) Data Storage

Motherboard Contents: IO Devices, CPU Chip, Graphics Chip, Power Connectors, Memory IO Connectors

Parts of the CPU:

- **Datapath:** ALU, registers, functional units that data moves through to perform calculations
- **Cache Memory:** small, fast memory inside the CPU with frequently used data
- (Main memory lives outside the CPU on a separate DRAM chip)
- **Control Logic:** sequencing how datapath and memory interact

Fetch-Execute Cycle:

- **Instruction Fetch (IF):** fetch the next instruction in the program (from memory)
- **Instruction Decode (ID):** the instruction (in control unit)
- **Execution (EX):** Execute the instruction (in the alu)
- **Memory (MEM):** access stored data as necessary and read/write (in memory)
- **Write Back (WB):** Write Back results to registers (in registers)

Pipelining in CPUs: pipelines can make CPUs faster (but need to prevent data hazards)

- **Instruction Level Parallelism:** allow multiple instructions to go on at once

Computer Languages and the FE Cycle:

- CPU executes machine language instructions, which need multiple cycles to run

Machine and Assembly Language:

- CPU executes machine level instructions
- Compilers/Interpreters translate higher level languages to lower level languages
- Assemblers translate lower level languages into machine language

Computer Memory: <Address: location of data, Data: the stored data>

- DRAM: dynamic RAM (prices go down with improvement in capacity)

Abstraction Layers:

Manufacturing Integrated Circuits (ICs): (1) prepare wafer, (2) apply photoresist, (3) align photomask, (4) expose to UV light, (5) develop & remove exposed photoresist, (6) etch exposed oxide, (7) remove photoresist

Cost of Manufacturing ICs:

- Cost per die = Cost per wafer / (Dies per wafer * yield)
- Dies per wafer \approx Wafer area / Die area (round down)
- Wafer cost and Die area are usually fixed values (area determined by design)
- Yield = good die / total die = $1 / [1 + (\text{Defects per area} * \text{Die Area} / 2)]^2$

Metrics:

- **Latency:** response time to complete a single fixed task (calculations emphasizes)
- **Throughput:** total work done in a fixed time (server emphasizes)

Performance Measures:

- **Execution Time:** total response time (CPU + External Memory I/O + OS + idle), which determines overall system performance
- **CPU Time:** time spent processing a given job (excludes I/O, OS times)
 - determined by program length, computer architecture, CPU clock speed
 - can improve performance by reducing number of clock cycles and increasing clock rate
 - has tradeoff between clock rate against cycle count
 - not all instructions use the same number of clock cycles
- Performance = 1 / Execution Time
- Relative performance (Speedup) of system A vs B = P_A / P_B
- Speedup Latency = Latency Old / Latency New
- Speedup Throughput = Throughput New / Throughput Old
- CPU Time = CPU Clock Cycles * Clock Cycle Time = CPU Clock Cycles / Clock Rate
- CPU Time = instructions/program * clock cycles/instruction * seconds/clock cycle
- CPU Time = instruction count * CPI * cycle time

CPU Clocking: hardware operates on a constant-rate clock

- **Clock Period:** duration of a clock cycle
- **Clock Frequency (Rate):** cycles per second
- Clock Frequency = 1 / Clock Period

Challenge: Power Consumption: market wants power consumption to decrease while increasing performance

- Power = Capacitive Load * Voltage² * Clock Frequency
- Contributes to Moore's Law Plateau

Challenge: Idle Power: CPUs draw disproportionate power when idling

Challenge: Multiple Processors: more than 1 processor per chip

- Requires explicit instruction level parallel programming (hidden from programmer)
- Need to maximize performance, balance the load, optimizing communication and synchronization

Challenge: Amdahl's Law: improve an aspect of a computer and expect a proportional overall improvement

- $T_{\text{improved}} = T_{\text{unaffected}} + T_{\text{affected}} / \text{improvement factor}$

Pitfall: MIPS as a Performance Metric: MIPS = Millions of Instructions per second

- Doesn't account for ISAs between computers (which have different efficiencies)
- Differences in complexities between instructions (weighted CPIs)
- Better to stick to CPU Time per Fixed Process

Multiplexer: M bits N inputs to 1 output

- 2:1 Mux: if S == 0, return A, else if S == 1, return B

Transpile: translating source code into another language with similar level of extraction

Hardware Description Language (HDL): used for simulation

Instruction Set Architectures (ISAs): abstract contract between software and hardware

- described with programmer-visible states, semantics/syntax and instructions
- can have many different implementations, some of which are customizable

Classification of ISAs:

- By complexity: Complex Instruction Set Computer (CISC) vs Reduced Instruction Set Computer (RISC)
 - instruction complexity (CPI), transistors, power, commercial vs embedded
 - RISC: simply instructions
 - CISC: as few lines of code as possible
- By parallelism: Very Long Instruction Word (VLIW) vs Explicit Parallel Instruction Computing (EPIC)
 - less commercial, server/supercomputer usage
- By simplification: Minimal Instruction Set Computer (MISC) vs One Instruction Set Computer (OISC)
 - proof of concept, little parallelism

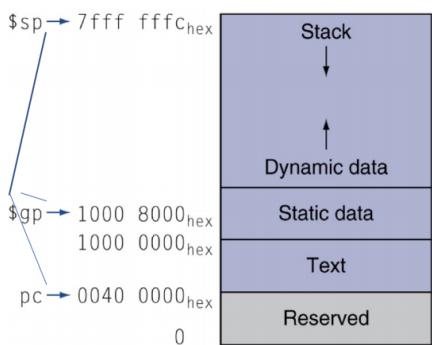
MIPS ISA: instructions in either R (register), I (immediate), or J (jumping) format represented with 32 bits

- for immediate instructions, the upper 16 bits is set to 0
- Pseudo Instructions: not core to CPU and are slower to run than core instructions

Variables: have type and storage class

- **Automatic variables:** local to part of program; created and discarded
- **Static variables:** global variables
- MIPS uses the global pointer register \$gp to access static variable block

Memory Layout:



- **Text:** program code
- **Static data:** global variables
- **Heap:** dynamic data (created and destroyed by programmer)
 - Heap is in upward direction (bottom of heap is lower memory address)
 - Stack and heap grow toward each other
- **Stack:** automatic storage of local variables (created and destroyed by compiler)
 - Stores arguments and variables when functions are called
 - Stores large local variables that don't fit in registers
 - Stack is in reverse direction (high memory is bottom of stack)

Character Data: byte-encoded character sets

- **ASCII:** 8 bits, includes all English characters but not non-English characters
- **Unicode** (-8, -16, -32); 8/16/32 minimum number of bits for variable character encoding
- Must be stored in memory (.data directive) and load them from memory (must fill to be 32 bits)

String Representations:

- 1st Choice: give length of string in the first position
- 2nd Choice: accompanying variable for length of string
- 3rd Choice: terminating EOS \0 character (C-Strings)

Branch Addressing: 16 bit immediate in WORDS

- Immediate types, can add or subtract done relative to PC Register
- Most branch targets are near branch instruction in text segment of memory
- Target Address = $PC + 4 * \text{Word Offset}$
 - Note: PC is automatically incremented by 4 when this calculation is done
- Word alignment allows us to jump further with the 16 bit immediate restriction
- If 16 bit offset is too small to encode far branch target, use jump addressing with 26 bit limit

Jump Addressing: 26 bit address in WORDS

- Encode full absolute address in instruction, not relative addressing
- Target Address = $4 * \text{Address (in Words)} \mid PC[31:28]$
 - Get 4 most significant digits from PC (If need to cross boundary, jump and add and jump)
 - Concatenate 26 bits in address; Concatenate two zeroes

Parallelism and Synchronization using Instructions

- Data Race is processors access same shared area of memory
- Need hardware support for lock and unlock
- Atomic memory operation = no other memory access allowed until atomic operation finished
- Load link (ll) and Store conditional (sc) used in sequence
 - Load link make reservation on a certain register
 - Store conditional attempts to store at register; returns value in rt (0 = fail, 1 = success)

File to Machine Code

1. **Compiler:** HLL to Assembly; may have assemblers and linkers built-in
2. **Assembler:** take care of pseudo instructions and number conversions (to hex); produces object file (machine language instruction, data, and information needed to place instructions properly in memory)
 - must determine addresses of labels and resolve labels for branching/jumping instructions
3. **Linker:** combine all object files into executable program, resolving symbols (references) as it goes along; products a single executable file with machine language instructions
4. **Loader:** OS program that takes executable code, sets up CPU memory for it, copies over the instructions to CPU memory, initializes all registers, jumps to the start routine)

Note: since a pointer is a memory address, when we simply add 4 to the address, we don't need additional instructions for indexing from an array; compilers can optimize code for this.

Dynamic Linking: only finish linking a library procedure when it is called

- PRO: often used libraries only need to be stored in a single location and not duplicated
- PRO: Update/fixes to library can be done modularly
- PRO: Reduce compiling time
- CON: Newer version of library is not backward compatible

Java: compiled to Java bytecode instruction set; usually slower than C/C++

- Run on Java virtual machine regardless of computer architecture
- JVM is a software interpreter that simulates an ISA
- PRO: portability
- Performance can be enhanced with Just in Time compilation

Addition and Subtraction Overflow:

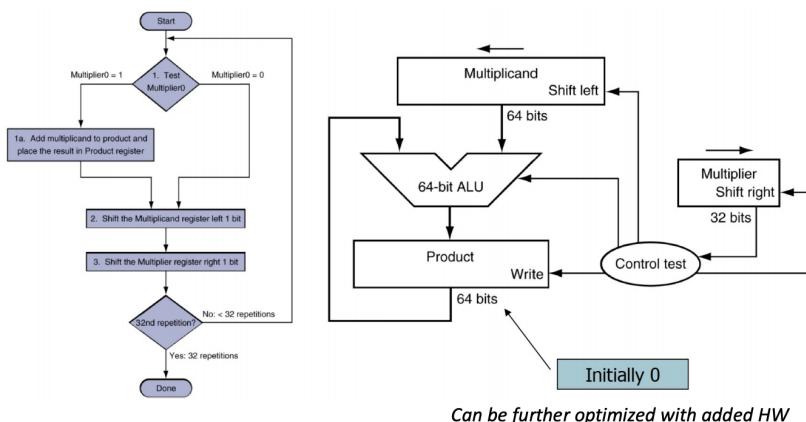
- Languages like C/C++, Java ignore overflow. Use unsigned assembly instructions to simulate this.
- Demand on CPU runtime is excessive; we can manually check in such languages.
- When using the signed operations, an exception handler is invoked:
 - PC is saved in exception program counter register
 - Jump executed to a predefined handler address

Multiplication and Division:

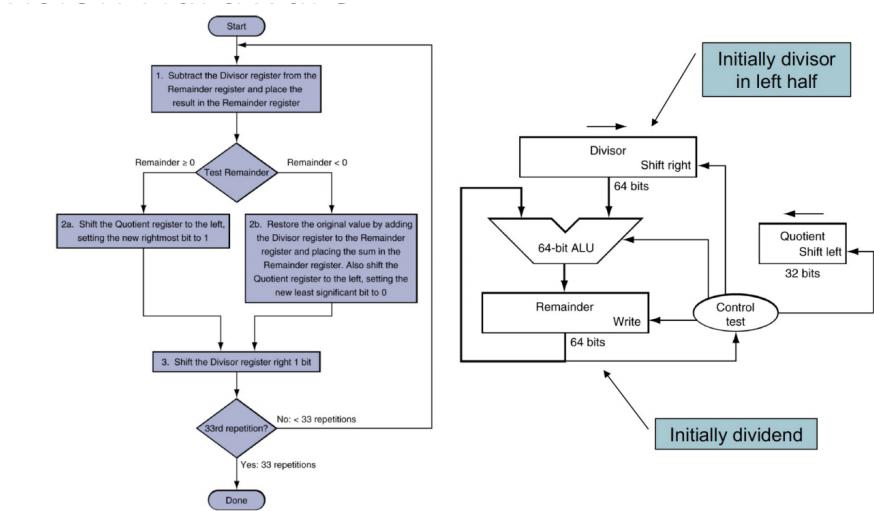
- mult multiplies 2 numbers and stores lower 32-bit result in LO and higher 32-bit result in HI
- div divides 2 numbers and stores the result in LO and quotient in HI
- use mflo and mfhi to move out of lo and hi registers
- no checking for overflow or divide by zero

Multiplication Algorithm: for $M * N$

- Initialize $P = 0$
- Loop 32 times:
 - If bit 0 of N is 1, $P += M$
 - Shift N to the right and M to the left 1 bit
- Return P (product)

**Division Algorithm:** for N / D

- Initialize $R = N$
- Loop 32 times:
 - $R = R - D$
 - If $R \geq 0$, shift Q to the left one bit and set last signed bit to be 1
 - Else, $R = R + D$ and shift Q to the left one bit
 - Shift D to the right 1 bit
- Return R (remainder) and Q (quotient)



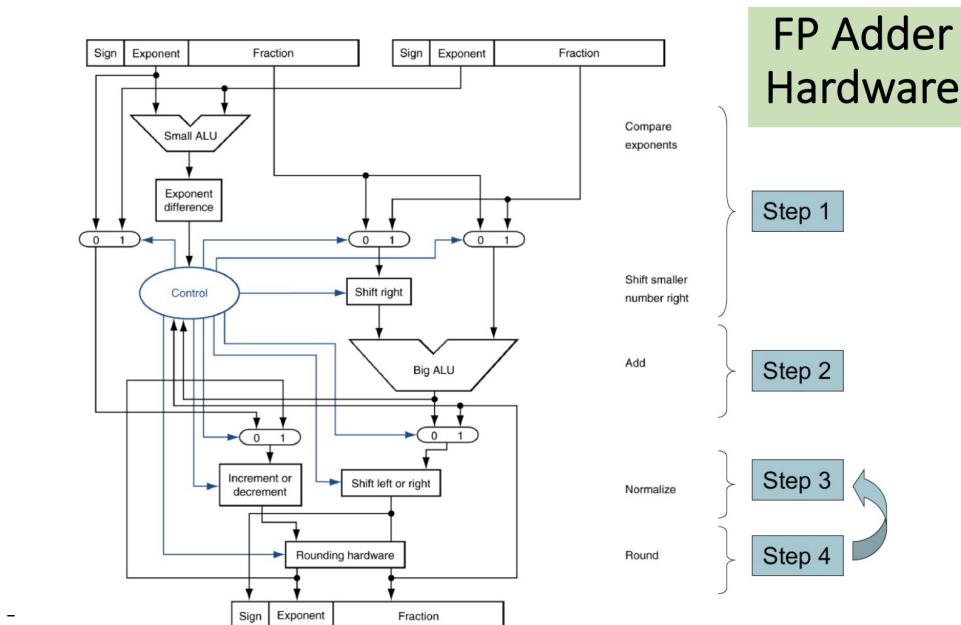
Optimization: can do addition/shift and subtraction/shift in parallel

Floating Point: representation for non integer numbers, allowing small and large representations

- normalized in binary scientific notation
- $(-1)^S \cdot (1 + \text{Fraction}) \cdot 2^{E-B}$
- 32 bits: (31) is sign, (30 - 23) is exponent, and (22 - 0) for fraction; $1 + \text{Fraction} = \text{Mantissa}$
- Overflow occurs when exponent too large and underflow when too small
- Double precision uses 64 bits with 11 bits for exponent and 52 bits for fraction
- Fraction written out as $b_1 b_2 \dots$ with implicit 1 ($b_1 = 0.5$)
- E is normal variable and B is constant (127 for single precision and 1023 for double)
- Exponents 0x00 and 0xFF are reserved for single precision numbers
- Zero represented with S = 0/1, E = 0, F = 0
- Pos/Neg Infinity represented with S = 0/1, E = 0xFF, F = 0
- Not a Number represented with S = 0/1, 0xFF, F != 0
- Denormalized numbers represented with S = 0/1, E = 0, F != 0

Floating Point Addition:

- Align decimal points by shifting smaller exponent
- Add significands
- Normalize result and check for over/underflow
- Round if necessary



Floating Point Unit:

- Specialized hardware in separate co-processor for floating point arithmetic
- Allows for floating point to integer conversions
- Operations take several cycles that should be pipelined

	<i>Single-Precision</i>	<i>Double-Precision</i>
Addition	<code>add.s</code>	<code>add.d</code>
Subtraction	<code>sub.s</code>	<code>sub.d</code>
Multiplication	<code>mul.s</code>	<code>mul.d</code>
Division	<code>div.s</code>	<code>div.d</code>
Comparisons	<code>c.xx.s</code> Where xx can be eq, neq, lt, gt, Example: <code>c.eq.s</code>	<code>c.xx.d</code>
Load	<code>lwc1</code>	<code>lwd1</code>
Store	<code>swc1</code>	<code>swd1</code>

Also, FP branch, true (**bc1t**) and branch, false (**bc1f**)

MIPS FP Instructions:

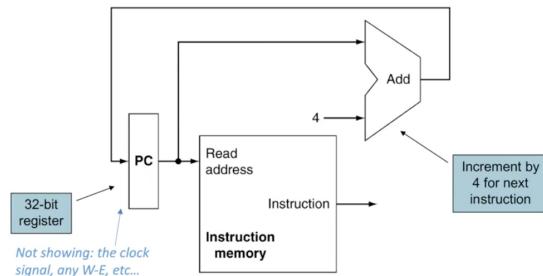
- FP instructions operate on FP registers (from FPU) at \$f0, \$f1, ...
- Floating point registers can be paired for double precision size
- FP addition takes multiple steps; longer than integer addition
- Operations not available for FP: bitshift, modulo

Implementing the Design of a CPU

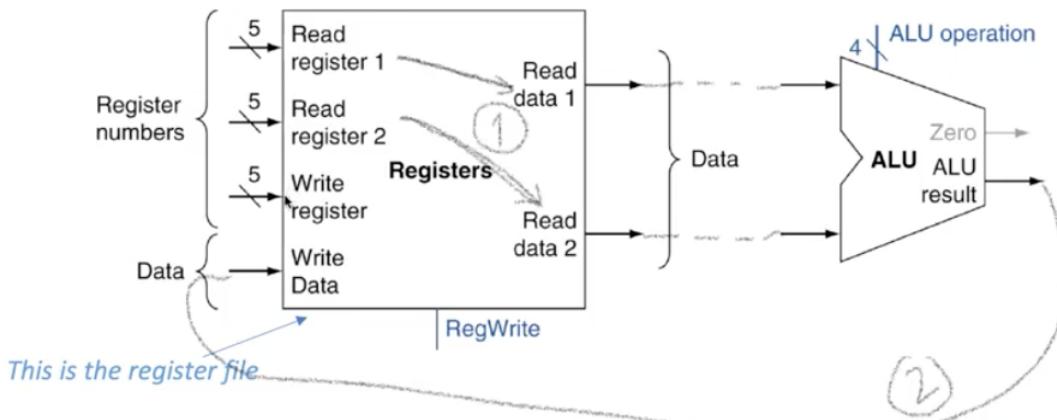
- CPU Performance Factor: Iron Law
 - Instruction Count determined by ISA and Compiler
 - CPU and Cycle Time determined by CPU Hardware
- Consider simple subset for run time
 - Memory reference: lw, sw
 - Arithmetic and logical: add, addi, sub, and, andi, or, slt
 - Control transfer: beq, j

Instruction Fetch-Execute Cycle:

- Send PC to the memory location is and fetch it; then increment PC to next instruction

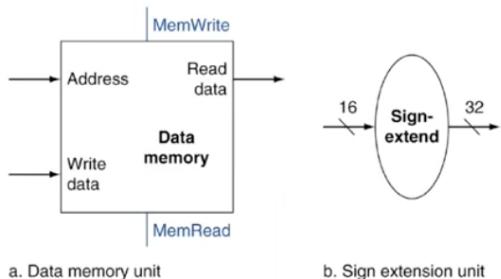


- R Type Instructions:
 - Read the two register operands rs/rt (outputs contents of register)
 - Perform ALU operation (two 32-bit input and 1 32-bit output plus a 1-bit signal if zero)
 - Write result to rd (writes on next clock edge)

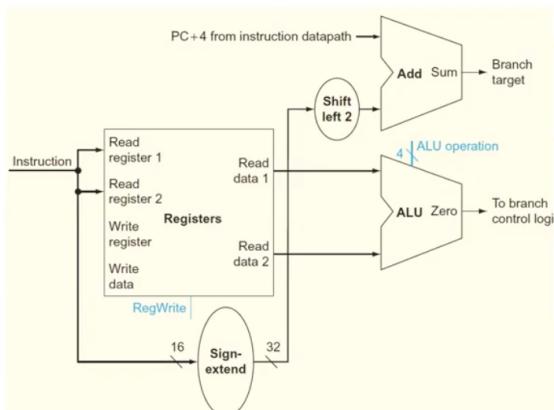


- Memory Reference Classes:
 - Read register operands rs/rt

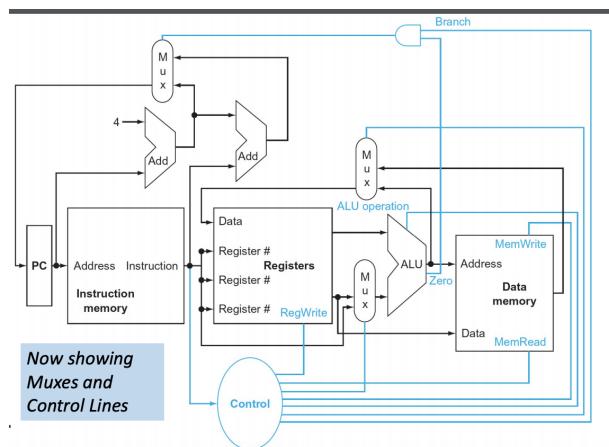
- Use ALU to find offset memory address for ALU
- Load: Read memory and update register
- Store: write register value to memory (on next clock cycle)



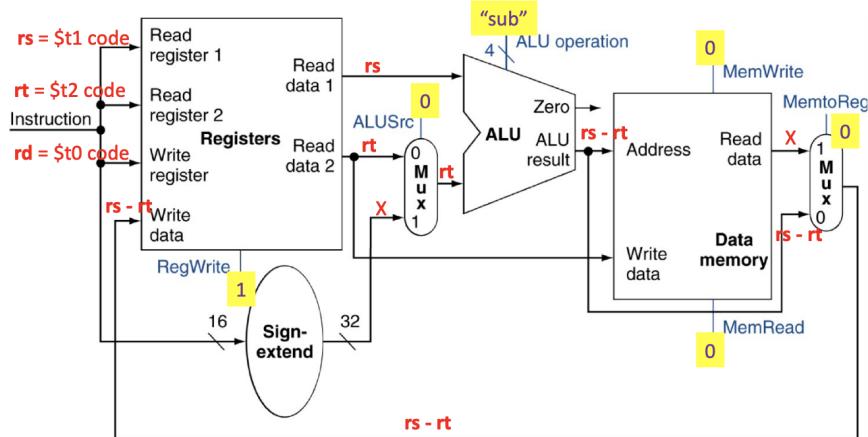
- Branching Classes:
 - Read register operands
 - Compare operands (use ALU subtract and check ALU output)
 - Use ALU to calculate target address



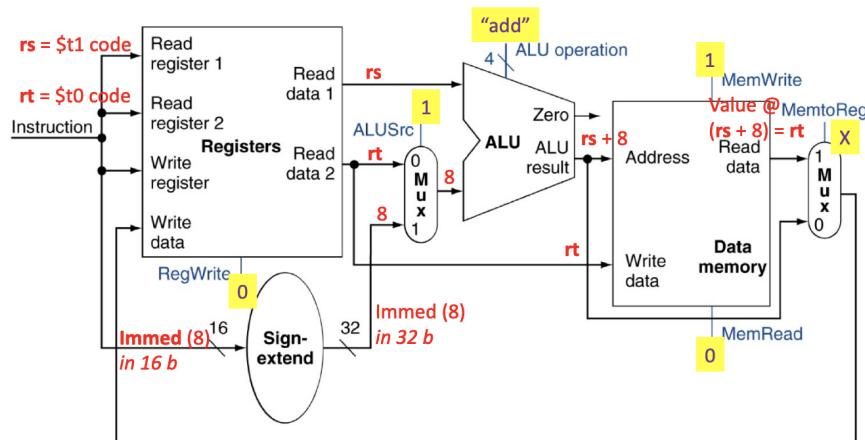
- All these data paths perform one instruction in one clock cycle
- Each datapath element can only do one function at a time
- Use multiplexer when alternate data sources are used



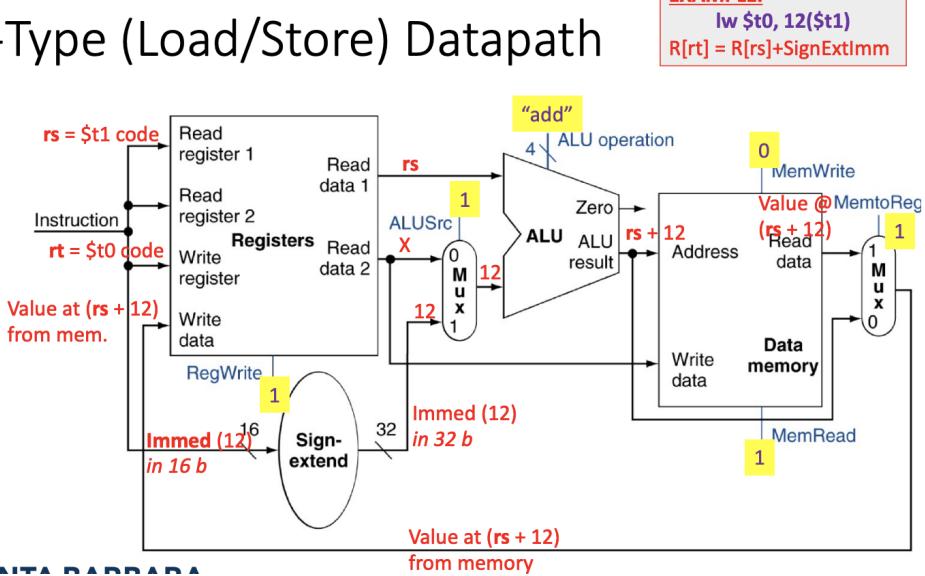
R-Type Datapath



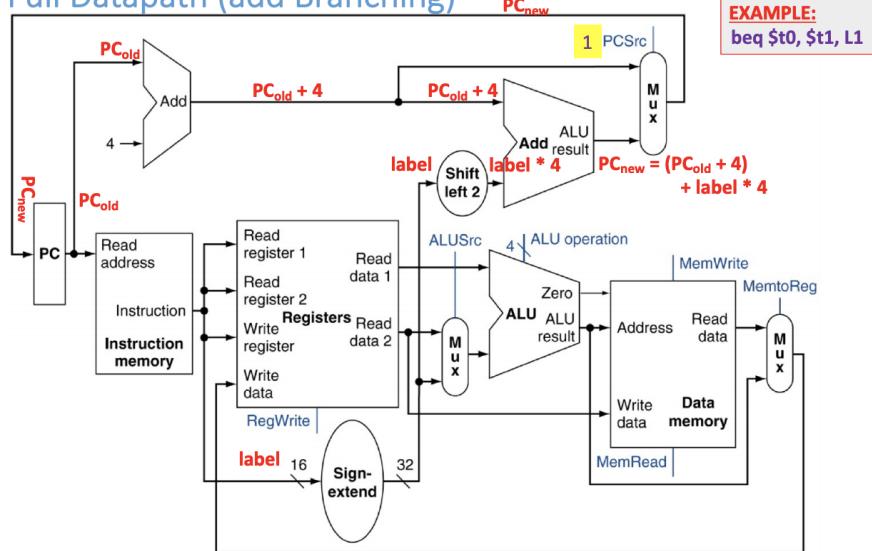
I-Type (Load/Store) Datapath



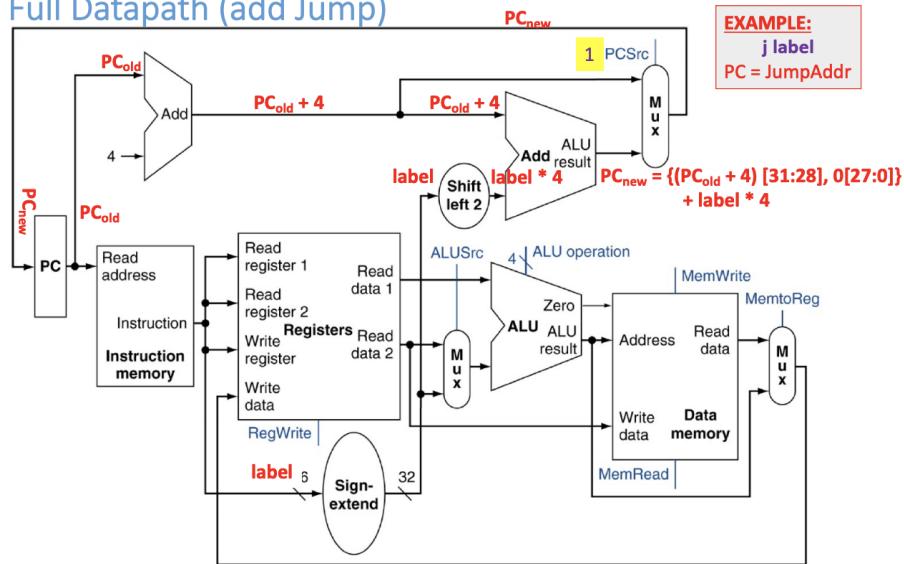
I-Type (Load/Store) Datapath



Full Datapath (add Branching)



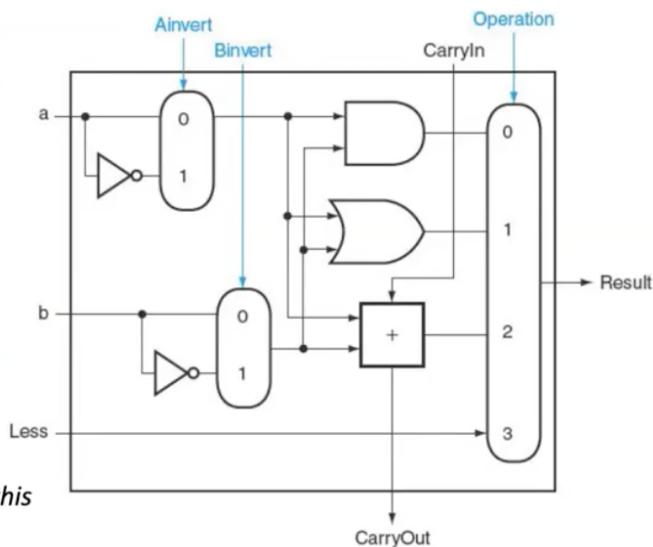
Full Datapath (add Jump)



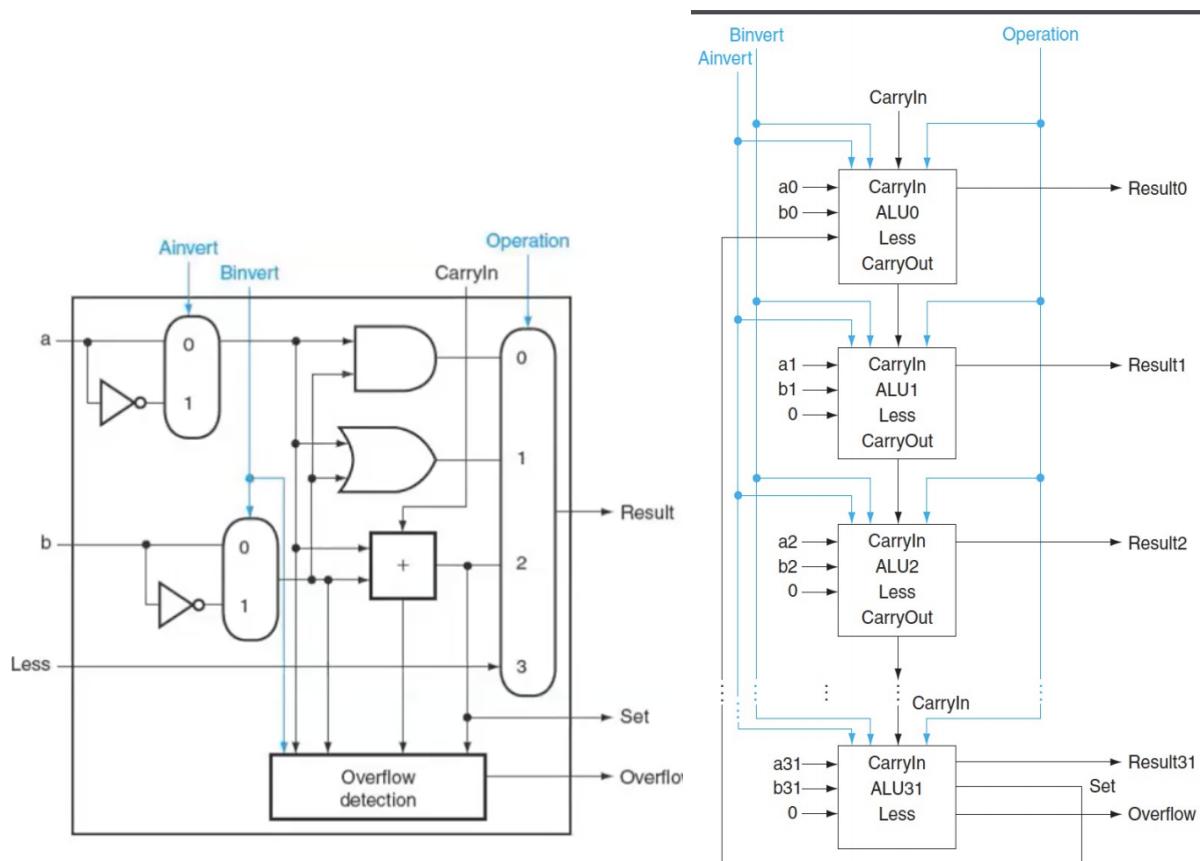
Ainv	Binv	OP[1:0]	Result
0	0	00	AND
1	1	00	NOR
0	0	01	OR
1	1	01	NAND
0	0	10	add
0	1	10	subtract
X	1	11	less*

* less: as in a flag for "set-if-less-than".

Note that Binv has to be 1 when using this



Note for subtraction: carry in value must be one



Overflow Detection: check when result of the adder result in overflow (at the end of the cascade)

Another output: set less than, which sets to 1 when true (at the end of the cascade)

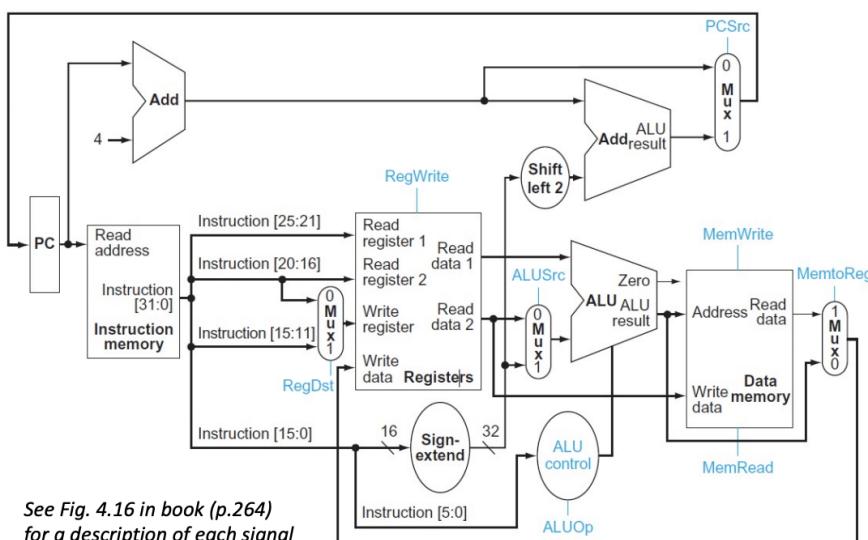
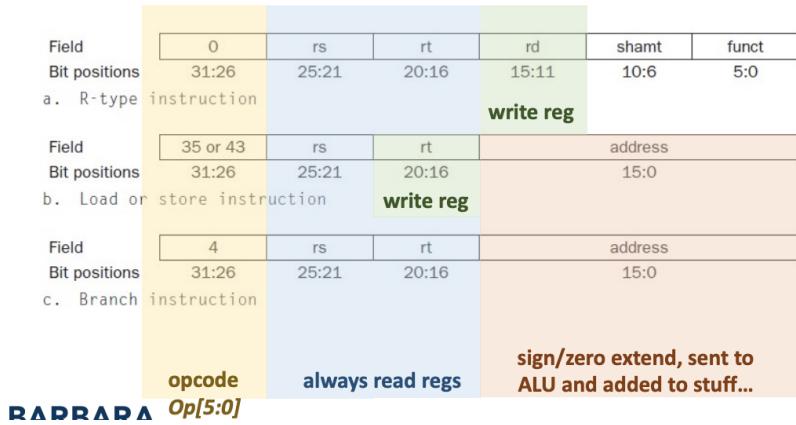
Carry in and Binvert work as same way and can be combined into a single bnegate

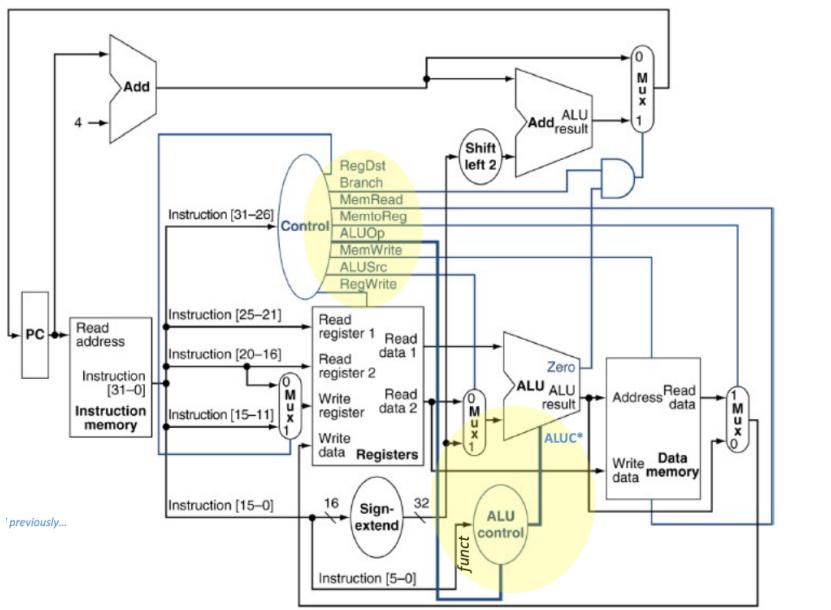
Subtraction allows equality comparison if zero bit is true

Zero gate only returns 1 if all the result bits are 0 (using a NOR gate)

ALU Control:

- sufficient information from decoded opcode and funct code from instruction to let ALU select
- ALUOp[1:0] (decode of instruction opcode) combined with Instructions[5:0] (the funct field) provides the ALU_Control[3:0] for ALU functionality





Performance Issues:

- latencies in the datapath (ignore the wires); sum of latencies is total latency
- iron clad rule: longest delay determines clock period
- critical path: load instruction (longest delay usually)
 - Instruction memory -> register file -> ALU -> data memory -> register file
- not feasible to vary period for different instructions (and complicates design)

Pipelining:

- Pipeline speedup = non-pipeline time / pipeline time = stages
- Stages need to be balanced and allotted to 1 single clock cycle
- Speed is faster due to increased throughput, but instruction latency does not change

MIPS vs Other Pipelining:

- MIPS (and RISC-types) have simpler ISAs versus CISC-types
- MIPS has same length instructions; x86 has variable length instructions
- MIPS has only 3 instruction formats; x86 has more stages bc more format types
- MIPS only has memory access for load store; x86 have other instructions

Pipeline Hazards: prevent starting the next instruction, reducing the performance

- **Structural hazards:** hardware is busy; cannot change in software (Ex: multiplication for multiple cycles)

- **Data hazards:** new instruction need to wait for previous to read/write
 - Might be able to fix in software (rewrite) or in hardware
- **Control hazard:** deciding on action depends on previous instruction (Ex: branch decisions)
 - Fetching next instruction resolves this issue
 - Resolution: add hardware to compute target early in ID Branch

Forwarding: don't wait for a result to be stored in the register

- Instead, forward the result to a stage that needs it (destination stage later in time than source stage)
- **Pipeline Stall/Bubble:** delay start of next instruction so we can forward to destination stage
- More forwarding = more overhead
- **NO OP:** an stub instruction to fill pipeline that is harmless

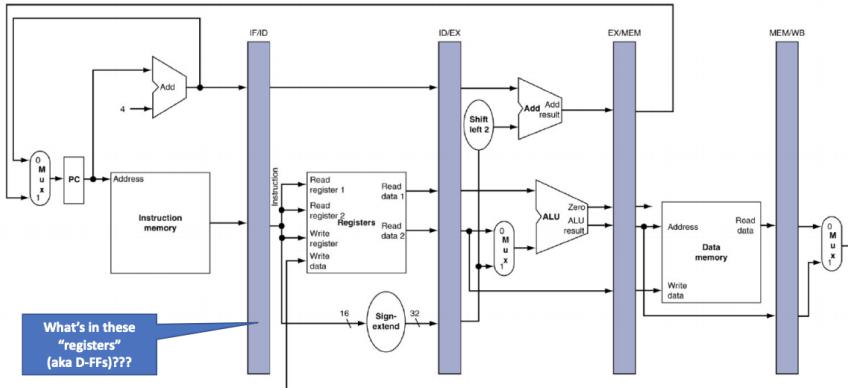
Code Scheduling: reorder code to avoid hazards

Predict the Branch Solution for Control Hazards:

- if prediction is correct, pipeline is not slowed down
- if prediction is wrong, kill the instruction after fetch and is no worse than original bubble
- **Simple Strategy:** predict branches are not taken; only when branches are taken, then we have a bubble
- **Static Predictions:** predict based on typical behavior; take loops but not branches
- **Dynamic Predictions:** hardware measures actual branch behavior based on record of recent history of each branch like a learning algorithm; assume future behavior will continue the trend

MIPS Pipelined Datapath - Simplified

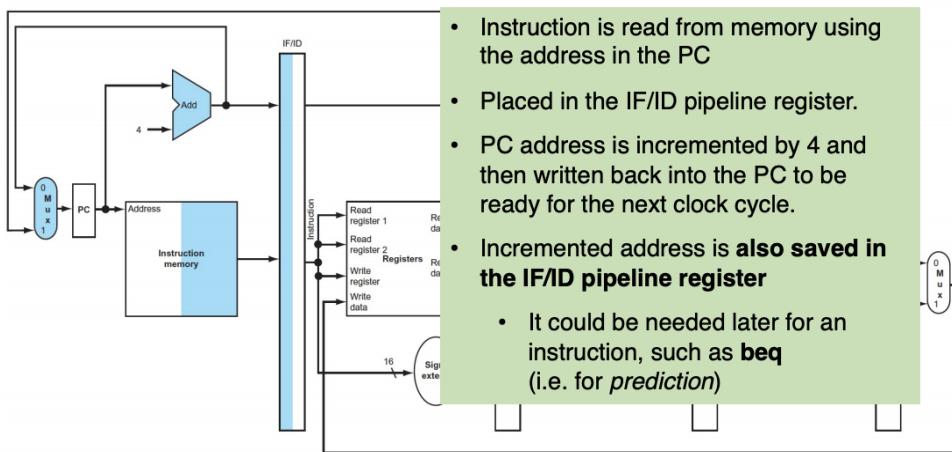
Need registers between stages to hold information produced in previous cycle



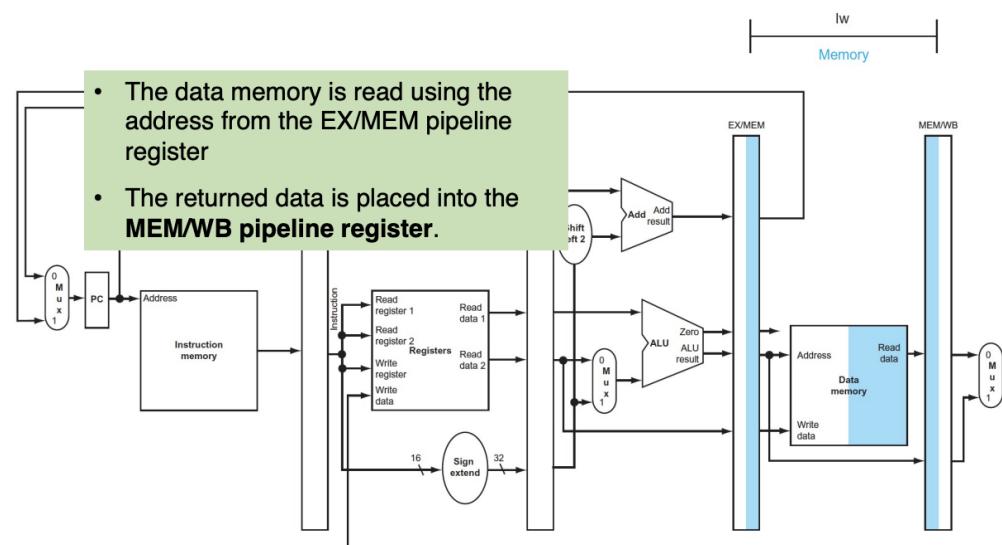
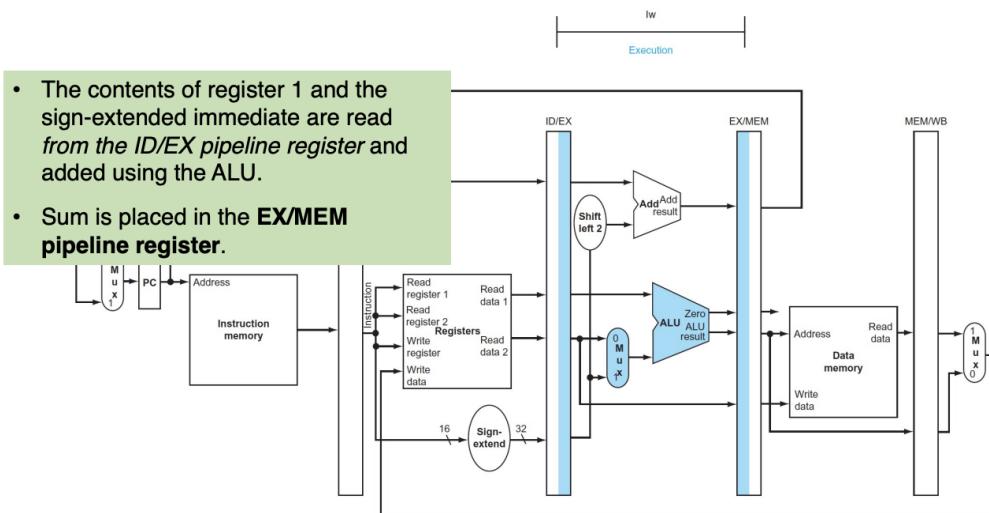
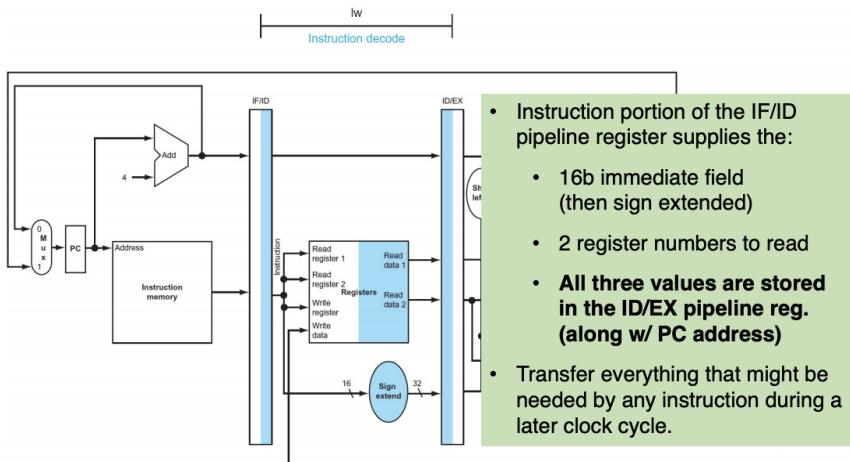
MIPS Pipelined Datapath for lw instruction: IF

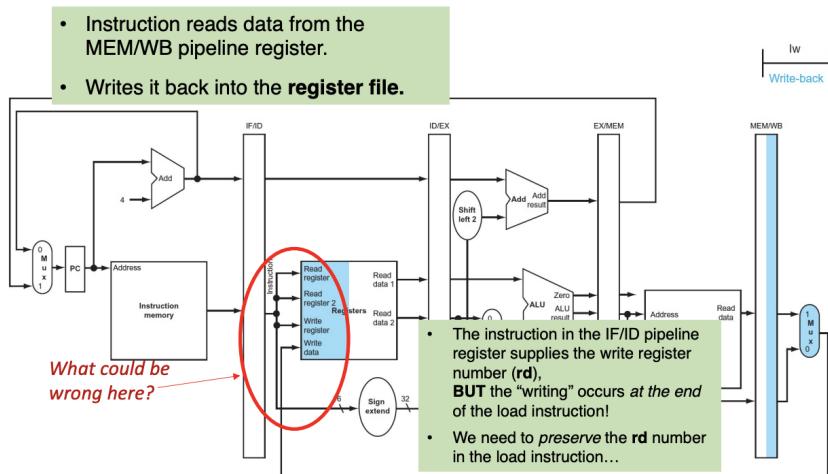
- Highlight the **right half** of registers or memory when they are being **read**
- Highlight the **left half** when they are being **written**

lw
Instruction fetch



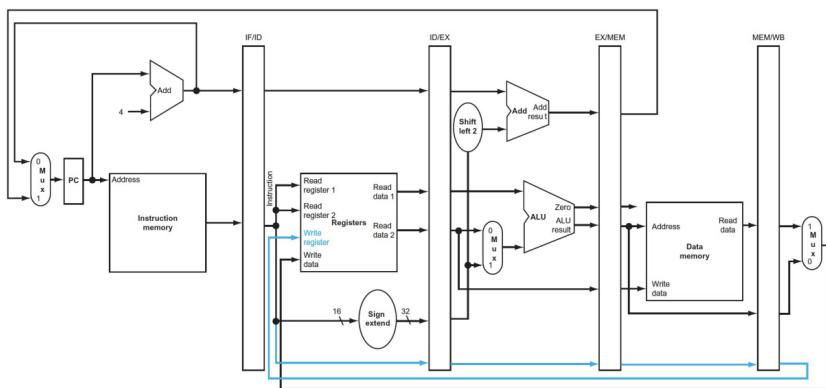
MIPS Pipelined Datapath for lw instruction: ID





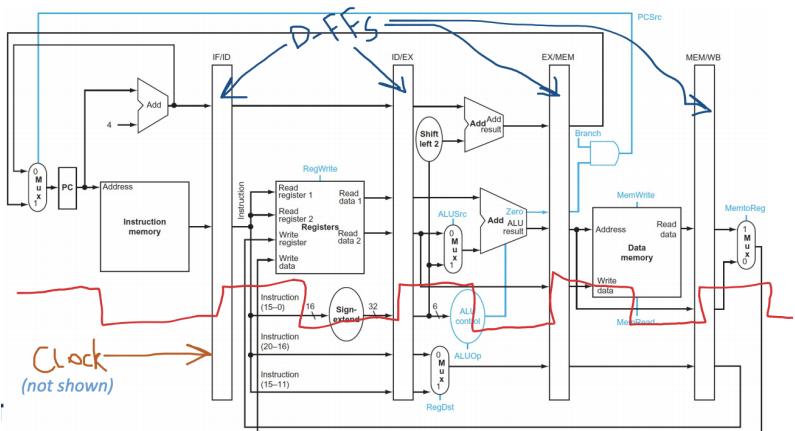
Corrected Pipelined Datapath

Otherwise load instruction wouldn't work properly...

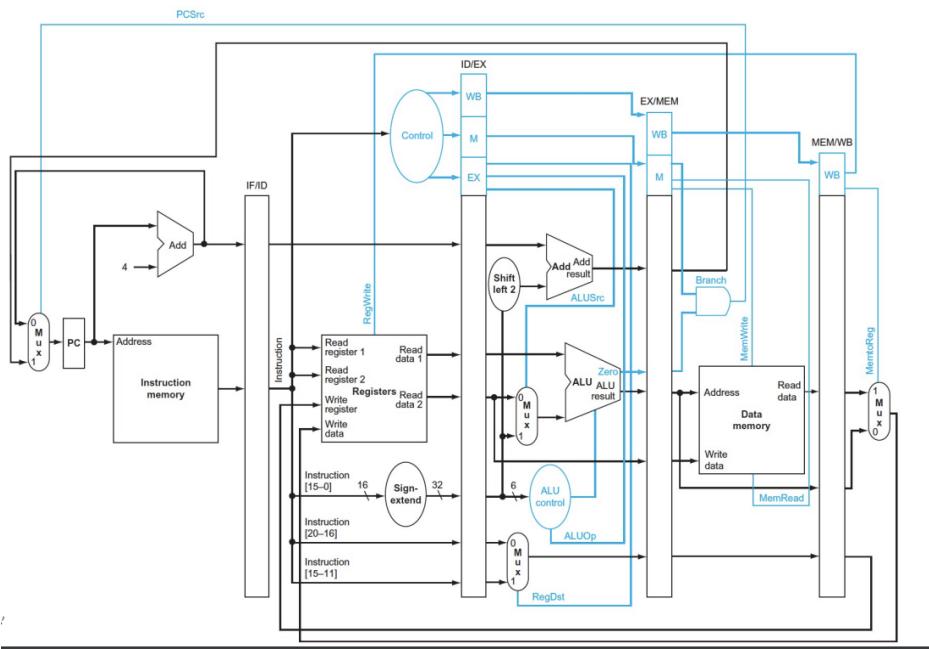


Pipeline Summary:

- One logical component can be only used for a single pipeline stage at a time
 - Multiclock Cycles Diagram: good for high level overview and details
 - Single Clock Cycle Diagram: full details of 5 instructions



Pipelined Datapath Showing Control Signals



Forwarding vs Stalling: can forward data to any stage that needs it as soon as the write back happens

- Data Hazards Occur When...
 - EX/MEM.RegisterRD = ID/EX.RegisterRS
 - EX/MEM.RegisterRD = ID/EX.RegisterRT
 - MEM/WB.RegisterRD = ID/EX.RegisterRS
 - MEM/WB.RegisterRD = ID/EX.RegisterRT
- Check RegWrite control signal for when registers will be written to
- If RS/RT are the zero registers, RD cannot be overridden (even tho it won't throw an error)
- Note: must stall when read is performed after a load word command writes to a register

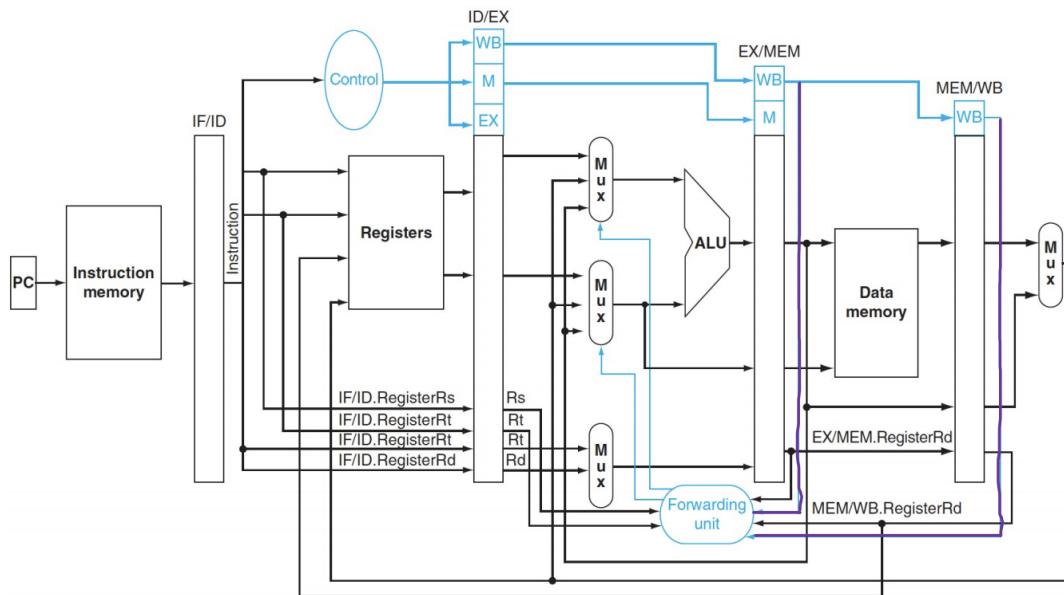
Double Data Hazard: if more than one cause a data hazard, only use the most recent value

|EX hazard

- if (EX/MEM.RegWrite and (EX/MEM.RegisterRd ≠ 0)
and (EX/MEM.RegisterRd = ID/EX.RegisterRs))
ForwardA = 10
- if (EX/MEM.RegWrite and (EX/MEM.RegisterRd ≠ 0)
and (EX/MEM.RegisterRd = ID/EX.RegisterRt))
ForwardB = 10

MEM hazard

- if (MEM/WB.RegWrite and (MEM/WB.RegisterRd ≠ 0)
and not (EX/MEM.RegWrite and (EX/MEM.RegisterRd ≠ 0))
and (EX/MEM.RegisterRd = ID/EX.RegisterRs))
and (MEM/WB.RegisterRd = ID/EX.RegisterRs))
ForwardA = 01
- if (MEM/WB.RegWrite and (MEM/WB.RegisterRd ≠ 0)
and not (EX/MEM.RegWrite and (EX/MEM.RegisterRd ≠ 0))
and (EX/MEM.RegisterRd = ID/EX.RegisterRt))
and (MEM/WB.RegisterRd = ID/EX.RegisterRt))
ForwardB = 01



Hazard Detection for Stalling:

```

if (ID/EX.MemRead and
    ((ID/EX.RegisterRt = IF/ID.RegisterRs) or
     (ID/EX.RegisterRt = IF/ID.RegisterRt)))
    stall the pipeline
  
```

How to Stall:

- Force control values in ID/EX to be 0 so that EX, MEM, and WB will do a no-op
- Prevent update of PC and IF/ID register
 - current instruction decoded again, following instruction is fetched again
 - this cycle allows MEM to read data for lw and then can subsequently forward to EX stage
- For compilers to resolve stalls, they must know the hardware info to fix stalling

Branch Types:

- Direct: label has fixed PC; Indirect: label is in register with address
- Unconditional: jump always taken; Conditional: depend on register/immediate values

Control Hazards:

want to mitigate latency

- Misprediction gets flushed, rather than an incorrect instruction execution
- **Misprediction Penalty:** amount of cycles needed before branch outcome is determined
- Fixing with compiler with branch delay does not work well due to inaccuracy
- Fixing with compiler using branch hint is also inaccurate

Predictions:

- Branch outcome, determined after execute stage
- Branch address, known after decode stage (direct branches) or execute stage (indirect branches)
- Scheme 1: branch not taken by default; if branch taken, flush away (assume flushing is negligible)
- Scheme 1.5: move branch execution earlier in pipeline
 - move branch adder from EX stage to the ID stage (or add pre-decode stage)
 - evaluate branch decision earlier (harder to do while maintaining short cycle time); need two register reads for equality check using simple gates, but adds more potential hazards
- Scheme 2: based on typical branch behavior (increases to about 70% accuracy)

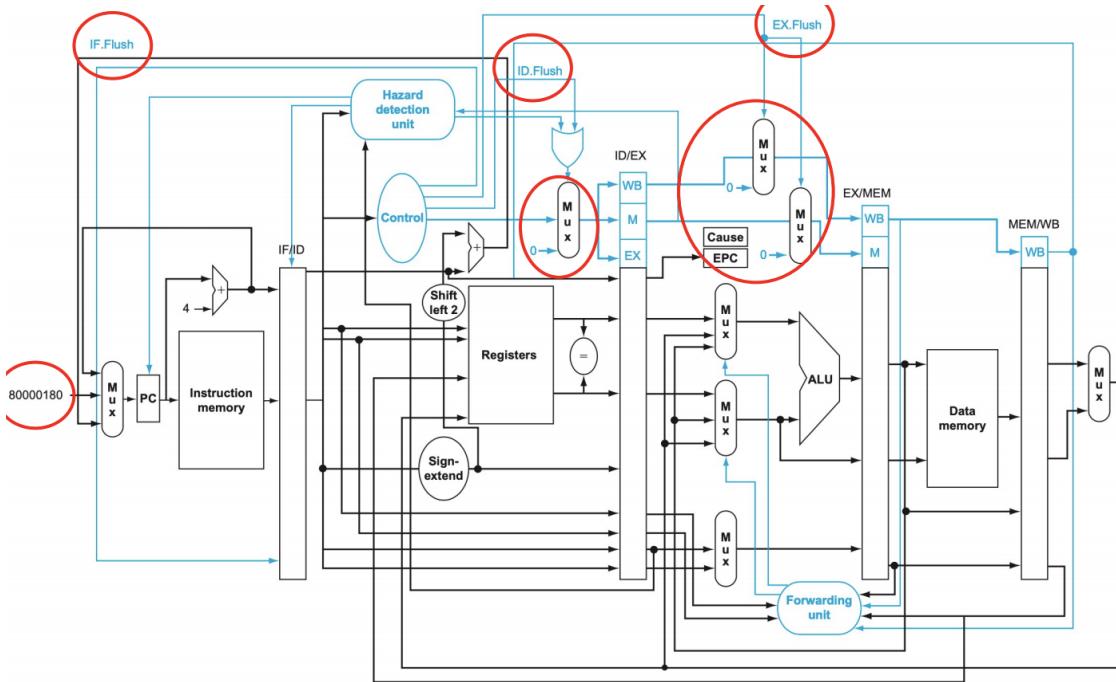
- Prediction schemes not related to the ISA; part of the microarchitecture implementation
- Dynamic Scheme: create branch history table to store past outcome; given a PC, return past result and assume same outcome happens like last time; update prediction if wrong
 - Branch prediction buffer small memory: 1-bit that states take or not take
 - Issue: nested loop construct that can result in a sequence of wrong predictions
 - Two Bit Predictor: only change prediction after two successive mispredictions

Exceptions and Interrupts: unexpected events that require change of flow

- Exceptions arise in the CPU (undefined instructions, invalid addresses, overflow, syscall, break instruction, accessing missing coprocessor, floating point exceptions, etc.)
- Interrupts are from external I/O controller (timers, other processors, external devices)
- Dealing with them without sacrificing performance is hard

Handling Exceptions/Interrupts: need to store issues to get back to original location after handling

- Managed by System Control Coprocessor (CPO)
- Set PC value of instruction in the Exception Program Counter (EPC)
- One method: store problem in a status controller
- Other method: vectored interrupt to go to address based on cause of exception
- **Actions:** transfer to relevant handler; if restartable, take corrective action; otherwise, terminate program
- MIPS treats this similar to a control hazard



Computer Memory: programs access only a small portion of their address space at one time

- **Temporal locality:** if an item is referenced, it will tend to be referenced soon again (i.e., loops)
- **Spatial locality:** if an item is referenced, neighbors will tend to be accessed soon (i.e., array access)
- To take advantage of locality, implement a memory hierarchy
 - everything stored in secondary storage (HDD/SSD) worst case
 - copy recent (and nearby) items to smaller DRAM main memory
 - copy more recently accessed (and nearly) items to SRAM cache memory attached to CPU
 - cache is levelled with higher level at the top
 - block/line = unit of copying (can be multiple words)
 - **Hit ratio:** accessed data in upper level / accesses (hits + absences)
 - **Miss penalty:** time taken to access absent data
 - **Miss Ratio** = 1 - hit ratio

Memory Technology

- **Static RAM (SRAM):** most cache rem is SRAM; 0.5ns - 2.5ns; \$1000 - \$5000 per GB
- **Dynamic RAM (DRAM):** not in CPU but on motherboard; 10ns - 20ns; \$3 - \$20 per GB
- **External Storage (HDD/SSD):** secondary; 5 - 10ms; \$0.05 GB for HHD; 5 - 100 micros \$0.08 per GB SSD

Cache Memory: levels of memory hierarchy closest to CPU

- **Direct Cache Mapping:** each block only has one possible map in the cache
- Scheme: index % blocks (uses lower order bits for indexing)
- Store tags in cache (higher order bits) to reduce storage space
- Add valid bit to confirm whether data is valid (1 = present)
- Temporal locality: new items replace old items if they exist
- Map size must be a power of 2; cache index size is 2^n blocks; n bits used for caching index
- Block (Data) size is 2^m words (2^{m+2} bytes) where m is bits allocated for block offset
- Tag Field is $32 - (n + (m + 2))$
- Total number of bits = $2^n * (2^m * 32 + (32 - n - m - 2) + 1) = 2^n * (2^{m+5} + 31 - n - m)$
- Size of a cache excludes the tag / valid field: 2^{m+5}

Block Size Considerations

- Larger blocks reduce miss rate (practical limit to block / cache size)
- For fixed size cache, larger blocks = fewer blocks = increased miss rate

Cache Misses: stall the CPU pipeline; fetch block from next level down; complete data access/restart IS fetch

- have both instruction and data caches
- on cache hit, CPU proceeds normally

Cache Performance: reduces idealness of CPU time

- CPU Time = (CPU execution cycles + Memory stall cycles) * Clock cycle
- Memory Stall Cycles = Miss Penalty * Miss Rate * Memory Access Per Program
- Memory Stall Cycles = Miss Penalty * Misses Per Instruction * Instructions Per Program
- **Average Memory Access Time (AMAT)** = Hit Time + Miss Rate * Miss Penalty
- When CPU performance increases, miss penalty become more significant since hardware needs to improve for fetching; decreasing base CPI/increasing clock rate does not fix memory stalls
- **Compulsory Miss:** first use of a block
- **Capacity Miss:** cache is too small
- **Conflict Miss:** collisions due to less than full associativity

Multi Level Caches:

- Level 1 primary cache attached to CPU (small, fast)
- Level 2 larger slower but faster than DRAM
- L1 focuses on minimizing hit time for shorter clock cycle; L2 cache focuses on reducing miss penalty

Cache Associativity:

- Memory access patterns can cause CPU to repeatedly access addresses to map to the same index
- One location = direct map; Any location = fully associative; N location = set associative
- Fewer index bits used for same cache size
- Data in each cache set is differentiated by tags (tags looked at in parallel)

Virtual Machine: emulation method of a standard software interface

- A host computer emulates a guest OS and machine resources
- Apps can't tell they are running in a VM
- Improves isolation of multiple guests, sharing (cloud computing); users are isolated from each other
- A single computer can run several different OSes
- Additional layer of security beyond standard OS
- Computers are fast so virtualization isn't too expensive

Virtual Machine Monitor (VMM)/Hypervisor: software that supports VMs

- Maps virtual resources to physical resources (memory, i/o devices, cpus)
- Guest code can run on native machine in user mode
- Allows guest OS to be different from host OS

Hypervisor Requirements:

- Guest software should behave on a VM exactly as on native hardware
- Guest software should not be able to change allocation of the real system's resources directly
- Hypervisor must be at a higher privilege than the guest (subset of instructions for system)

Options for Hypervisor: virtualization has overhead

- When guests access a device, the hypervisor must step in
- Provide illusion of real device is tricky (need to cause exception with every access)
- Can provide fake devices that are easier to map to hypervisor
- Can adopt para-virtualization (API for guests, additional to existing ISA)
- **Note:** recursive virtualization is possible with ISA/hardware support

Virtual Memory: not virtual machines

- **Translation:** virtual addresses into physical addresses by CPU and OS
- **Protection:** application permissions to access data at an address
- **Disk Cache:** use main memory as cache of secondary storage
- Programs share main memory
- Each application gets private virtual address; protected from other programs
- Takes control of memory addressing and lets each application function as if it had unlimited memory

Memory Pages:

- Translations stored in page tables, with key = virtual address and value = mapping to physical address
- Takes 4 bytes per entry to store, so storing every address would take $4 * 2^{32}$ space
- If we only store words, it still takes the same amount of space as physical memory
- Want large page size so the page table can be smaller

Virtual Addressing: Virtual Page Number + Offset gets translated to Physical Page Number + Offset

- Upper portion of address is page number, lower portion is page offset
- Page Size = $2^{\# \text{ of page offset bits}}$
- Does not need 1:1 mapping with physical addresses
- Loading virtual addressed with valid = 0 causes page fault

Page Faults:

- page must be fetched from secondary storage (HDD/SSD)
- can take millions of clock cycles; handled by OS code

- want to minimize page fault rates by making pages large enough, optimize organization of memory, involve smart algorithms for retrieval
- page table entries have tags and valid bits too; when valid bit is off, page fault
- usually OS keeps swap space in secondary storage with pages from memory
- OS manages which processes/addresses use each physical space
- If replacements need to be done, some prediction scheme has to be used (like branching)

Write Through vs Write Back

- When writing to memory and that memory location is a copy of something further down:
 - **Write Through** if write to both cached copy and original place in memory
 - **Write Back** if writing to only cached memory and doing rest later
- **Dirty Bit:** indicate if data present in the cache/page was modified (Dirty); for write back only
- To reduce page fault rate, prefer least recently used (LRU) replacement
 - Reference/use bit in page table set to 1 on page access
 - Periodically cleared to 0 (not used recently) by OS
- Disk writes take million of cycles, write block at once not individual locations

Translation-Lookaside Buffer (TLB): cache of valid page table entries

- CPU include a special cache of recently used translations (different from instruction/data cache)
- Usually fully associative with 16-128 entries
- TLB reach = # of entries * page size (how much memory can be read without missing)
- TLB meant to make virtual memory access faster
- If TLB too small or too many processes in use, thrashing occurs: frequent TLB misses, new cached page displaces one that will be soon used again, degrade overall performance
- Used before instruction fetch and data load/store since those contain virtual addresses

Hierarchical Page Tables: make structure smaller by making levels to split it up, but causes multiple accesses

