

# The Bayes Filter

System equation	$\mathbf{x}_k = F_{k-1}\mathbf{x}_{k-1} + \boldsymbol{\epsilon}_{k-1}$
Observation equation	$\mathbf{b}_k = A_k\mathbf{x}_k + \mathbf{e}_k$
Initial conditions Other conditions	$\boldsymbol{\epsilon}_k \sim N(\mathbf{0}, \Sigma_{\epsilon,k})$ $\mathbf{e}_k \sim N(\mathbf{0}, \Sigma_{e,k})$
Prediction of state vector Prediction of covariance matrix Covariance matrix for updating	$E\{\mathbf{x}_0\} = \hat{\mathbf{x}}_0$ $E\{(\mathbf{x}_0 - \hat{\mathbf{x}}_{0 0})(\mathbf{x}_0 - \hat{\mathbf{x}}_{0 0})^T\} = P_{0 0}$ $E\{\boldsymbol{\epsilon}_k \mathbf{e}_j^T\} = 0, \quad \text{for all } k, j$ $\hat{\mathbf{x}}_{k k-1} = F_{k-1}\hat{\mathbf{x}}_{k-1 k-1}$ $P_{k k-1} = F_{k-1}P_{k-1 k-1}F_{k-1}^T + \Sigma_{\epsilon,k}$ $P_{k k} = (P_{k k-1}^{-1} + A_k^T \Sigma_{e,k}^{-1} A_k)^{-1}$
Kalman gain matrix Updating of state vector	$K_k = P_{k k} A_k^T \Sigma_{e,k}^{-1}$ $\hat{\mathbf{x}}_{k k} = \hat{\mathbf{x}}_{k k-1} + K_k(\mathbf{b}_k - A_k \hat{\mathbf{x}}_{k k-1})$