

# Introduction to OpenACC

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- OpenACC Application Program Interface describes a collection of compiler directive to specify loops and regions of code in standard C, C++ and Fortran to be offloaded from a host CPU to an attached accelerator.
- provides portability across operating systems, host CPUs and accelerators



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Introduction to OpenACC



#### The Standard for GPU Directives

Simple: Directive are the easy path to accelerate compute intensive

applications

Open: OpenACC is an open GPU directives standard, making GPU

programming straightforwards and portable across parallel and

multi-core processors

Powerful: GPU directives allow complete access to the massive parallel power

of a GPU







#### High Level

- Compiler directives to specify parallel regions in C & Fortran
  - Offload parallel regions
  - Portable across OSes, host CPUs, accelerators, and compilers
- Create high-level heterogenous programs
  - Without explicit accelerator intialization
  - Without explicit data or program transfers between host and accelerator

#### High Level · · · with low-level access

- Programming model allows programmers to start simple
- Compiler gives additional guidance
  - Loop mappings, data location and other performance details
- Compatible with other GPU languages and libraries
  - Interoperate between CUDA C/Fortran and GPU libraries
  - e.g. CUFFT, CUBLAS, CUSPARSE, etc







- Directives are easy and powerful.
- Avoid restructuring of existing code for production applications.
- Focus on expressing parallelism.

# OpenACC is not GPU Programming

OpenACC is Expressing Parallelism in your code







- Did you attend/review the trainings on C/C++ or Modern Fortran?
- Recall the following three exercises:
  - SAXPY: Generalized vector addition
  - Matrix Multiplication
  - Calculate pi by Numerical Integration





 SAXPY is a common operation in computations with vector processors included as part of the BLAS routines

$$y \leftarrow \alpha x + y$$

• Write a SAXPY code to multiply a vector with a scalar.

# Algorithm 1 Pseudo Code for SAXPY

# program SAXPY

$$n \leftarrow \text{some large number}$$

$$x(1:n) \leftarrow \text{some number say, } 1$$

$$y(1:n) \leftarrow$$
 some other number say, 2

$$a \leftarrow \text{some other number, say, } 3$$

do 
$$i \leftarrow 1 \cdots n$$

$$y_i \leftarrow y_i + a * x_i$$

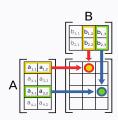
end do

end program SAXPY





- Most Computational code involve matrix operations such as matrix multiplication.
- Consider a matrix C which is a product of two matrices A and B:
   Element i,j of C is the dot product of the i<sup>th</sup> row of A and j<sup>th</sup> column of B
- Write a MATMUL code to multiple two matrices.







# Algorithm 2 Pseudo Code for MATMUL

#### program MATMUL

$$\begin{array}{l} m,n \leftarrow \text{some large number} \leq 1000 \\ \text{Define } a_{mn},b_{nm},c_{mm} \\ a_{ij} \leftarrow i+j;b_{ij} \leftarrow i-j;c_{ij} \leftarrow 0 \\ \textbf{do } i \leftarrow 1 \cdots m \\ & \textbf{do } j \leftarrow 1 \cdots m \\ & c_{i,j} \leftarrow \sum_{k=1}^n a_{i,k} * b_{k,j} \\ & \textbf{end do} \\ & \textbf{end do} \\ & \textbf{end program MATMUL} \end{array}$$





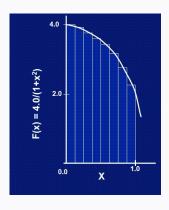
We know that

$$\int_0^1 \frac{4.0}{(1+x^2)} \, dx = \pi$$

 So numerically, we can approxiate pi as the sum of a number of rectangles

$$\sum_{i=0}^{N} F(x_i) \Delta x \approx \pi$$

Meadows et al, A "hands-on" introduction to OpenMP, SC09



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# **Algorithm 3** Pseudo Code for Calculating Pi

# $\begin{array}{c} \textbf{program} \; \text{CALCULATE\_PI} \\ step \leftarrow 1/n \\ sum \leftarrow 0 \\ \textbf{do} \; i \leftarrow 0 \cdots n \\ x \leftarrow (i+0.5) * step; sum \leftarrow sum + 4/(1+x^2) \\ \textbf{end do} \\ pi \leftarrow sum * step \\ \textbf{end program} \end{array}$







## Serial Code

```
program saxpy
  implicit none
  integer, parameter :: dp = selected real kind(15)
 integer, parameter :: ip = selected int kind(15)
 integer(ip) :: i,n
  real(dp), dimension(:), allocatable :: x, y
  real(dp) :: a, start_time, end_time
  n=5000000
  allocate(x(n),y(n))
  x = 1.0d0
  v = 2.0d0
  a = 2.0
  call cpu_time(start_time)
  do i = 1, n
    y(i) = y(i) + a * x(i)
  end do
  call cpu_time(end_time)
  deallocate(x,y)
 print '(a,f8.6)', 'SAXPY Time: ', end_time - start_time
end program saxpy
```

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# OpenMP Code

```
program saxpy
  implicit none
  integer, parameter :: dp = selected real kind(15)
  integer, parameter :: ip = selected int kind(15)
  integer(ip) :: i,n
  real(dp), dimension(:), allocatable :: x, y
  real(dp) :: a, start time, end time
  n=5000000000
  allocate(x(n), y(n))
  !$omp parallel sections
  !$omp section
  x = 1.0
  !$omp section
  y = 1.0
  !$omp end parallel sections
  a = 2.0
  call cpu time(start time)
  !$omp parallel do default(shared) private(i)
  do i = 1, n
     y(i) = y(i) + a * x(i)
  end do
  !$omp end parallel do
  call cpu time (end time)
  deallocate(x,y)
  print '(a,f8.6)', 'SAXPY Time: ', end_time - start_time
end program saxpy
```







# OpenACC Code

```
program saxpy
  use omp_lib
  implicit none
  integer :: i,n
  real, dimension(:), allocatable :: x, y
  real :: a, start time, end time
  allocate(x(n), y(n))
 a = 2.0
  !$acc data create(x,y) copyin(a)
  !$acc parallel
  x(:) = 1.0
  !$acc end parallel
  !$acc parallel
 y(:) = 1.0
  !$acc end parallel
  start time = omp get wtime()
  !$acc parallel loop
  do i = 1, n
    v(i) = v(i) + a * x(i)
  end do
  !$acc end parallel loop
  end_time = omp_get_wtime()
  !$acc end data
  deallocate(x,v)
  print '(a,f15.6,a)', 'SAXPY Time: ', end_time - start_time, 'in secs'
end program saxpy
```

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#### CUDA Fortran Code

```
module mymodule
contains
  attributes(global) subroutine saxpy(n, a, x, y)
    real :: x(:), y(:), a
    integer :: n, i
    attributes(value) :: a, n
    i = threadIdx%x+(blockIdx%x-1)*blockDim%x
    if (i \le n) y(i) = a \times x(i) + y(i)
  end subroutine saxpy
end module mymodule
program main
  use cudafor; use mymodule
  integer, parameter :: n = 100000000
  real, device :: x d(n), y d(n)
  real, device :: a d
  real :: start time, end time
 x d = 1.0
 v d = 2.0
  a d = 2.0
  call cpu time(start time)
  call saxpy<<<4096, 256>>>(n, a, x_d, y_d)
  call cpu time (end time)
  print '(a,f15.6,a)', 'SAXPY Time: ', end time - start time, 'in secs'
end program main
```

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# Simple Example V



#### Compile

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```
[apacheco@mikel 2013-LONI]$ pgf90 -o saxpy saxpy.f90
[apacheco@mikel 2013-LONI]$ pgf90 -mp -o saxpy_omp saxpy_omp.f90
[apacheco@mikel 2013-LONI]$ pgf90 -acc -ta=nvidia -o saxpy_acc saxpy_acc.f90
[apacheco@mikel 2013-LONI]$ pdf90 -o saxpy cuda saxpy.cuf
```

# Speed Up

Algorithm	Device	Time (s)	Speedup
Serial	Xeon E5-2670	0.986609	1
OpenMP (8 threads)	Xeon E5-2670	0.241465	4.1x
OpenACC	M2090	0.059418	16.6x
CUDA	M2090	0.005205	189 5x

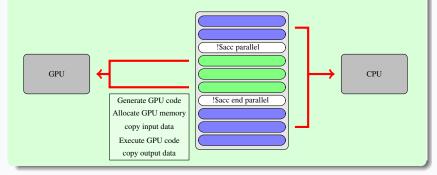


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# OpenACC Execution Model



- Application code runs on the CPU (sequential, shared or distributed memory)
- OpenACC directives indicate that the following block of compute intensive code needs to be offloaded to the GPU or accelerator.



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# **Building Block of OpenACC**



- Program directives
  - Syntax
    - C/C++: #pragma acc <directive> [clause]
    - Fortran: !\$acc <directive> [clause]
  - Regions
  - Loops
  - Synchronization
  - Data Structure
  - ...
- Runtime library routines







- if (condition)
- async (expression)
- data management clauses
  - copy(···), copyin(···), copyout(···)
  - create(···), present(···)
  - present\_or\_copy{,in,out}(...) or pcopy{,in,out}(...)
  - present\_or\_create(···) or pcreate(···)
- reduction(operator:list)



#### Runtime Libraries



- System setup routines
  - acc\_init(acc\_device\_nvidia)
  - acc\_set\_device\_type (acc\_device\_nvidia)
  - acc\_set\_device\_num(acc\_device\_nvidia)
- Synchronization routines
  - acc\_async\_wait(int)
  - acc\_async\_wait\_all()





# OpenACC kernels directive



# C: #pragma acc kernels [clause]

#### Fortran !Sacc kernels [clause]

- The kernels directive expresses that a region may contain parallelism and the compiler determines what can be safely parallelized.
- The compiler breaks code in the kernel region into a sequence of kernels for execution on the accelerator device.
- For the codes on the right, the compiler identifies 2 parallel loops and generates 2 kernels.
- What is a kernel? A function that runs in parallel on the GPU.
- When a program encounters a kernels contruct, it will launch a sequence of kernels in order on the device.

```
!Sacc kernels
do i = 1, n
   x(i) = 1.0
   y(i) = 2.0
end do
do i = 1, n
   v(i) = v(i) + a * x(i)
end do
!Sacc end kernels
#pragma acc kernels
  for (i = 0; i < n; i++) {
    x[i] = 1.0;
    y[i] = 2.0;
  for (i = 0; i < n; i++){
    y[i] = a * x[i] + v[i];
```







- The **parallel** directive identifies a block of code as having parallelism.
- Compiler generates a parallel kernel for that loop.

C: #pragma acc parallel [clauses]

Fortran: !\$acc parallel [clauses]

```
!$acc parallel
do i = 1, n
   x(i) = 1.0
  y(i) = 2.0
end do
do i = 1, n
  y(i) = y(i) + a * x(i)
end do
!$acc end parallel
#pragma acc parallel
  for (i = 0; i < n; i++) {
    x[i] = 1.0:
   v[i] = 2.0;
  for (i = 0; i < n; i++) {
    v[i] = a*x[i] + v[i];
```



# OpenACC Loop Directive



- Loops are the most likely targets for Parallelizing.
- The Loop directive is used within a parallel or kernels directive identifying a loop that can be executed on the accelerator device.

C: #pragma acc loop [clauses]

Fortran: !\$acc loop [clauses]

 The loop directive can be combined with the enclosing parallel or kernels

C:

#pragma acc kernels loop [clauses]

Fortran: !\$acc parallel loop [clauses]

 The loop directive clauses can be used to optimize the code. This however requires knowledge of the accelerator device.

Clauses: gang, worker, vector, num\_gangs, num\_workers

```
!$acc loop
do i = 1, n
    y(i) = y(i) + a * x(i)
end do
!$acc end loop

#pragma acc loop
for (i = 0; i < n; i++) {
    y[i] = a*x[i] + y[i];
}</pre>
```





#### PARALLEL

- Requires analysis by programmer to ensure safe parallelism.
- Straightforward path from OpenMP

#### **KERNELS**

- Compiler performs parallel analysis and parallelizes what it believes is safe.
- Can cover larger area of code with single directive.

Both approaches are equally valid and can perform equally well.









```
program saxpy
  use omp_lib
  implicit none
  integer :: i.n
  real, dimension(:), allocatable :: x, y
  real :: a, start_time, end_time
  allocate(x(n),y(n))
  a = 2.0
  x(:) - 1.0
  v(:) - 1.0
  start_time - omp_get_wtime()
  !$acc parallel loop
  do i - 1, n
     y(i) - y(i) + a * x(i)
  end do
  !$acc end parallel loop
  end_time = omp_get_wtime()
  deallocate(x, v)
  print '(a,f15.6)', 'SAXPY Time: ', end_time - start_time
end program saxpy
```

```
#include <stdio.h>
#include <time.h>
#include <omp.h>
int main() {
 long long int i, n=5000000000:
 float a=2.0;
 float x[n];
 float v[n]:
 double start_time, end_time;
 a = 2.0;
 for (i = 0; i < n; i++) {
  x[i] = 1.0;
 start_time = omp_get_wtime();
#pragma acc kernels loop
   for (i = 0; i < n; i++){}
     y[i] = a \times x[i] + y[i];
 end_time - omp_get_wtime();
 printf ("SAXPY Time: %f\n", end_time - start_time);
```



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## **Compilation**



• C:

pgcc -acc [-Minfo=accel] [-ta=nvidia] -o saxpyc\_acc saxpy\_acc.c

• Fortran 90:

pgf90 -acc [-Minfo=accel] [-ta=nvidia] -o saxpyf\_acc saxpy\_acc.f90

```
Compiler Output
[apacheco@mikel nodataregion] $ pgcc -acc -ta=nvidia -Minfo=accel -o saxpyc acc saxpy acc.c
main:
     19, Generating present or copyin(x[0:500000000])
         Generating present or copy(y[0:500000000])
         Generating NVIDIA code
         Generating compute capability 1.0 binary
         Generating compute capability 2.0 binary
         Generating compute capability 3.0 binary
     21, Loop is parallelizable
         Accelerator kernel generated
         21, #pragma acc loop gang, vector(128) /* blockIdx.x threadIdx.x */
[apacheco@mikel nodataregion] $ pgf90 -acc -ta=nvidia -Minfo=accel -o saxpvf acc saxpv acc.f90
saxpy:
     17, Accelerator kernel generated
         18, !$acc loop gang, vector(256) ! blockidx%x threadidx%x
     17, Generating present_or_copy(y(1:500000000))
         Generating present or copyin(x(1:500000000))
         Generating NVIDIA code
         Generating compute capability 1.0 binary
         Generating compute capability 2.0 binary
         Generating compute capability 3.0 binary
[apacheco@mikel nodataregion]$
```





# Running



 The PGI compiler provides automatic instrumentation when PGI\_ACC\_TIME=1 at runtime

```
[apacheco@mike407 nodataregion] $ PGI ACC TIME=1 ./saxpyc acc
SAXPY Time: 6.369176
Accelerator Kernel Timing data
/ddnB/work/apacheco/2013-LONI/openmp/saxpy/nodataregion/saxpy acc.c
  main NVIDIA devicenum=0
    time(us): 1,029,419
    19: compute region reached 1 time
        19: data copyin reached 2 times
             device time(us): total=667,515 max=339,175 min=328,340 avg=333,757
        21: kernel launched 1 time
            grid: [65535] block: [128]
            device time(us): total=57,999 max=57,999 min=57,999 avg=57,999
            elapsed time(us): total=58,014 max=58,014 min=58,014 avg=58,014
        25: data copyout reached 1 time
             device time(us): total=303,905 max=303,905 min=303,905 avg=303,905
[apacheco@mike407 nodataregion] $ PGI_ACC_TIME=1 ./saxpvf acc
SAXPY Time.
                   6 488910
Accelerator Kernel Timing data
/ddnB/work/apacheco/2013-LONI/openmp/saxpy/nodataregion/saxpy_acc.f90
  saxpv NVIDIA devicenum=0
    time(us): 1.018.988
    17: compute region reached 1 time
        17: data copvin reached 2 times
             device time(us): total=655,958 max=327,991 min=327,967 avg=327,979
        17: kernel launched 1 time
            grid: [65535] block: [256]
             device time(us): total=59,148 max=59,148 min=59,148 avg=59,148
            elapsed time(us): total=59,165 max=59,165 min=59,165 avg=59,165
        21: data copyout reached 1 time
             device time(us): total=303,882 max=303,882 min=303,882 avg=303,882
```





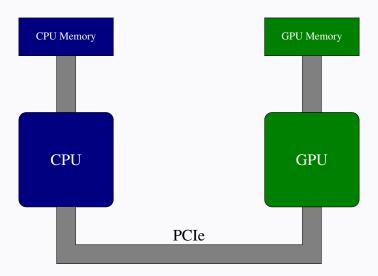
Execution	С		Fortran	
	Time	SpeedUp	Time	Speedup
Serial	0.511232		0.969819	
OpenMP (8 Threads)	0.180301	2.84	0.237585	4.08
OpenACC (M2090)	9.211521	0.06	9.188178	0.11

- What's going with OpenACC code?
- Why even bother with OpenACC if performance is so bad?







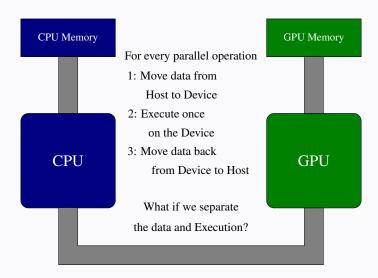


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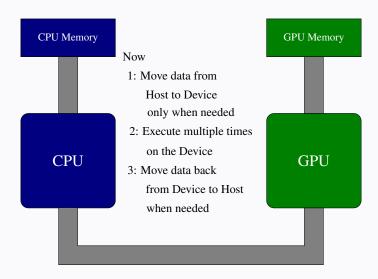




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 The data construct defines a region of code in which GPU arrays remain on the GPU and are shared among all kernels in that region

```
!$acc data [clause]
    !$acc parallel loop
    ...
    !$acc end parallel loop
```

Arrays used within the data region will remain on the GPU until the end of the data region.



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#### Data Clauses



- copy(list) Allocates memory on GPU and copies data from host to GPU when entering region and copies data to the host when exiting region.
- copyin(list) Allocates memory on GPU and copies data from host to GPU when entering region.
- copyout(list) Allocates memory on GPU and copies data to the host when exiting region.
  - create(list) Allocates memory on GPU but does not copy.
- present(list) Data is already present on GPU from another containing data region.
- Other clauses: present\_or\_copy[inlout], present\_or\_create, deviceptr.







- Compiler sometime cannot determine size of arrays
  - Must specify explicitly using the data clauses and array "shape"

```
C #pragma acc data copyin(a[0:size]), copyout(b[s/4:3*s/4])
```

```
Fortran !$acc data copyin(a(1:size)), copyout(b(s/4:3*s/4))
```

Note: data clauses can be used on data, parallel or kernels



# **Update Construct**



- Used to update existing data after it has changed in its corresponding copy (e.g. upate device copy after host copy changes).
- Move data from GPU to host, or host to GPU.
- Data movement can be conditional and asynchronous.
- Fortran

```
\verb|!| \verb| acc update [clause \cdots]|
```

C

```
#pragma acc update [clause ···]
```

- Clause
  - host(list)
  - device(list)
  - if(expression)
  - async(expression)







```
program saxpy
  use omp_lib
  implicit none
  integer :: i,n
  real, dimension(:), allocatable :: x, v
  real :: a, start_time, end_time
  n-500000000
  allocate (x(n), y(n))
  a = 2.0
  !$acc data create(x,y) copyin(a)
  !$acc parallel
  x(:) - 1.0
  !Sacc end parallel
  !$acc parallel
  v(:) - 1.0
  !Sacc end parallel
  start_time - omp_get_wtime()
  !$acc parallel loop
  do i - 1, n
    v(i) = v(i) + a * x(i)
  end do
  !$acc end parallel loop
  end_time = omp_get_wtime()
  !$acc end data
  deallocate(x, v)
  print '(a,f15.6,a)', 'SAXPY Time: ', end_time - start_time, '
end program saxpy
```

```
#include <stdio.h>
#include <time.h>
#include <omp.h>
int main() {
  long long int i, n=500000000;
 float a=2.0:
 float x[n];
 float y[n];
  double start time, end time;
 a = 2.0:
#pragma acc data create(x[0:n],v[0:n]) copvin(a)
#pragma acc kernels loop
     for (i = 0; i < n; i++) {
 x[i] = 1.0;
 v[i] = 2.0:
     1
      start_time - omp_get_wtime();
#pragma acc kernels loop
 for (i - 0; i < n; i++) {
    v[i] = a \times x[i] + v[i];
      end_time - omp_get_wtime();
 printf ("SAXPY Time: %f\n", end_time - start_time);
```



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Execution	С		Fortran	
	Time	SpeedUp	Time	Speedup
Serial	0.510000		0.986609	
OpenMP (8 Threads)	0.179959	2.83	0.241465	4.09
OpenACC (M2090)	0.058131	8.77	0.059418	16.61

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## Exercise: Matrix Multiplication



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Execution	Time	SpeedUp	GFlops/s
Serial	6.227		0.964
OpenMP (8 Threads)	0.823	7.566	7.290
OpenMP (16 Threads)	0.445	13.993	13.493
OpenACC	0.188	33.122	31.917

## Fortran

Execution	Time	SpeedUp	GFlops/s
Serial	7.112		0.844
OpenMP (8 Threads)	0.931	7.639	6.445
OpenMP (16 Threads)	0.494	14.397	12.146
OpenACC	0.214	33.234	28.037









• Reduction clause is allowed on *parallel* and *loop* constructs

```
Fortran

!$acc parallel reduction(operation: var)
    structured block with reduction on var
!$acc end parallel

C

#pragma acc kernels reduction(operation: var) {
    structured block with reduction on var
}
```



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Fortran					
Execution	Time	SpeedUp			
Serial	133.782	1			
OpenMP (8 Threads)	17.303	7.73			
OpenACC	0.149	897.87			
C					
Execution	Time	SpeedUp			
Serial	134.214	1			
OpenMP (8 Threads)	17.3379	7.74			
OpenACC	0.151	888.83			

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## Further Speedups



- OpenACC gives us more detailed control over parallelization
  - Via gang, worker and vector clauses
- By understanding more about specific GPU on which you're running, using these clauses may allow better performance.
- By understanding bottlenecks in the code via profiling, we can reorganize the code for even better performance.



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## General Principles: Finding Parallelism in Code



- (Nested) for/do loops are best for parallelization
- Large loop counts are best
- Iterations of loops must be independent of each other
  - To help compiler: restrict keyword (C), independent clause
  - Use subscripted arrays, rather than pointer-indexed arrays
- Data regions should avoid wasted bandwidth
  - Can use directive to explicitly control sizes
- Various annoying things can interfere with accelerated regions.
  - Function calls within accelerated region must be inlineable.
  - No IO





## OpenACC: Is it worth it?



- High-level. No involvement of OpenCL, CUDA, etc
- Single source. No forking off a separate GPU code. Compile the same program for accelerators or serial, non-GPU programmers can play along.
- Efficient. Experience shows very favorable comparison to low-level implementations of same algorithms.
- Performance portable. Supports GPU accelerators and co-processors from multiple vendors, current and future versions.
- Incremental. Developers can port and tune parts of their application as resources and profiling dictates. No wholesale rewrite required. Which can be quick.



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Lecture derived from slides and presentations by

- Michael Wolfe, PGI
- Jeff Larkin, NVIDIA
- John Urbanic, PSC

Search for OpenACC presentations at the GPU Technology Conference Website for further study

http://www.gputechconf.com/gtcnew/on-demand-gtc.php







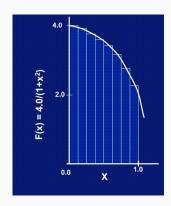
We know that

$$\int_0^1 \frac{4.0}{(1+x^2)} \, dx = \pi$$

 So numerically, we can approxiate pi as the sum of a number of rectangles

$$\sum_{i=0}^{N} F(x_i) \Delta x \approx \pi$$

Meadows et al, A "hands-on" introduction to OpenMP, SC09



Introduction to OpenACC



# Algorithm 1 Pseudo Code for Calculating Pi

# $\begin{array}{c} \textbf{program CALCULATE\_PI} \\ step \leftarrow 1/n \\ sum \leftarrow 0 \\ \textbf{do } i \leftarrow 0 \cdots n \\ x \leftarrow (i+0.5) * step; sum \leftarrow sum + 4/(1+x^2) \\ \textbf{end do} \\ pi \leftarrow sum * step \\ \textbf{end program} \end{array}$







SAXPY is a common operation in computations with vector processors included as part
of the BLAS routines

$$y \leftarrow \alpha x + y$$

• Write a SAXPY code to multiply a vector with a scalar.

## Algorithm 2 Pseudo Code for SAXPY

# program SAXPY

$$n \leftarrow \text{some large number}$$

$$x(1:n) \leftarrow \text{some number say, } 1$$

$$y(1:n) \leftarrow \text{some other number say, } 2$$

$$a \leftarrow \text{some other number ,say, } 3$$

do 
$$i \leftarrow 1 \cdots n$$

$$y_i \leftarrow y_i + a * x_i$$

## end do

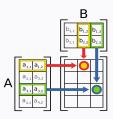
end program SAXPY





- Most Computational code involve matrix operations such as matrix multiplication.
- Consider a matrix C which is a product of two matrices A and B:

  Element i,j of C is the dot product of the  $i^{th}$  row of A and  $j^{th}$  column of B
- Write a MATMUL code to multiple two matrices.





## **Algorithm 3** Pseudo Code for MATMUL

## program MATMUL

$$\begin{array}{l} m,n \leftarrow \text{some large number} \leq 1000 \\ \text{Define } a_{mn},b_{nm},c_{mm} \\ a_{ij} \leftarrow i+j;b_{ij} \leftarrow i-j;c_{ij} \leftarrow 0 \\ \textbf{do } i \leftarrow 1 \cdots m \\ & \textbf{do } j \leftarrow 1 \cdots m \\ c_{i,j} \leftarrow \sum_{k=1}^n a_{i,k} * b_{k,j} \\ \textbf{end do} \\ \textbf{end do} \\ \textbf{end program } \text{MATMUL} \end{array}$$

