

Introduction to MPI

2021 HPC Workshop: Parallel Programming

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July 13 - 15, 2021

Research Computing

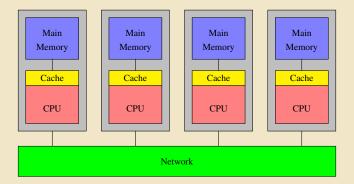


1 Introduction

Distributed Memory Model



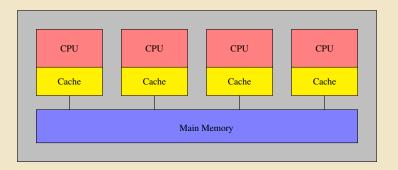
- Each process has its own address space
 - Data is local to each process
- Data sharing is achieved via explicit message passing
- Example
 - MPI



Shared Memory Model



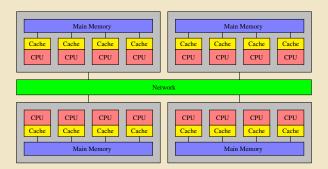
- All threads can access the global memory space.
- Data sharing achieved via writing to/reading from the same memory location
- Example
 - OpenMP
 - Pthreads



Clusters of SMP nodes



- The shared memory model is most commonly represented by Symmetric Multi-Processing (SMP) systems
 - Identical processors
 - Equal access time to memory
- Large shared memory systems are rare, clusters of SMP nodes are popular.



Shared vs Distributed



Shared Memory

- Pros
 - Global address space is user friendly
 - Data sharing is fast
- Cons
 - Lack of scalability
 - Data conflict issues

Distributed Memory

- Pros
 - Memory scalable with number of processors
 - Easier and cheaper to build
- Cons
 - Difficult load balancing
 - Data sharing is slow

Why MP1?



- There are already network communication libraries
- Optimized for performance
- Take advantage of faster network transport
 - Shared memory (within a node)
 - Faster cluster interconnects (e.g. InfiniBand)
 - TCP/IP if all else fails
- Enforces certain guarantees
 - Reliable messages
 - In-order message arrival
- Designed for multi-node technical computing

What is MP1?



- MPI defines a standard API for message passing
 - The standard includes
 - What functions are available
 - The syntax of those functions
 - What the expected outcome is when calling those functions
 - The standard does NOT include
 - Implementation details (e.g. how the data transfer occurs)
 - Runtime details (e.g. how many processes the code run with etc.)
- MPI provides C/C++ and Fortran bindings

MPI Implementations



- There are two different types of MPI implementations commonly used.
 - **MPICH**: Developed by Argonne National Laboratory.
 - used as a starting point for various commercial and open source MPI libraries
 - MVAPICH2: Developed by D. K. Panda with support for InfiniBand, iWARP, RoCE, and Intel Omni-Path. (default MPI on Sol),
 - Intel MPI: Intel's version of MPI. Part of Intel OneAPI HPC Toolkit
 - IBM MPI: for IBM BlueGene, and
 - CRAY MPI: for Cray systems.
 - OpenMPI: A Free, Open Source implementation from merger of three well know MPI implementations. Can be used for commodity network as well as high speed network.
 - FT-MPI from the University of Tennessee,
 - LA-MPI: from Los Alamos National Laboratory,
 - LAM/MPI: from Indiana University

MPI Compilers



- There is no MPI compiler available to compile programs nor is there is a compiler flag.
- Instead, you need to build the MPI scripts for a particular compiler.
- You can use MVAPICH2 and MPICH on Sol
- You should use MPICH only on Hawk.
- Each of these builds provide mpicc, mpicxx and mpif90 for compiling C, C++ and Fortran codes respectively that are wrapper for the underlying compilers

```
[alp514.sol](793): module load mvapich2
[alp514.sol](794): mpicc—show
/share/Apps/intel/2020/compilers_and_libraries_2020.3.275/linux/bin/intel64/icc—lmpi—I/share/Apps/lusoft/opt/spack/linux—
centros=house|1/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=house|1/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=house|1/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=house|1/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=house|1/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.11/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.11/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.11/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.11/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.11/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.11/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.11/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.11/intel=20.0.3/mvanich2/2.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.0.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.0.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.0.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.0.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.0.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.0.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.0.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.0.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.0.3.4_wvnudho/include=1/share/Apps/lusoft/opt/spack/linux—entros=0.0.3.4_wvnudho/include=1/share/
```

snare/apps/intel/zew2compites_and_titorartes_zeve.3.z/s/titux/oin/intelo4/icc-lmpi — Jsnare/apps/usort/opt/spack/titux-centos8-haswell/intel—20.0.3/mwapich2/2.3.4-mguydha/ritude—L/share/Apps/lusoft/opt/spack/linux-centos8-haswell/intel—20.0.3/mwapich2/2.3.4-mguydha/lib —NI_-rpath —NI_/share/Apps/lusoft/opt/spack/linux-centos8-haswell/intel—20.0.3/mwapich2/2.3.4-mguydha/lib

[alp514.sol](795): module load mpich

Lmod is automatically replacing "mvapich2/2.3.4" with "mpich/3.3.2".

[alp514.sol](796): mpif90 —show

/share/Apps/intel/2020/compilers_and_libraries_2020.3.275/linux/bin/intel64/ifort_L/share/Apps/lusoft/opt/spack/linux-centos8haswell/intel-20,0.3/mlo/c/2_0-ep-jrs/p7/ib = 1/share/Apps/lusoft/opt/spack/linux-centos8-haswell/intel-20.0.3/mpich/3.3.2-n7f36fo/include — I/share/Apps/lusoft/opt/spack/linux-centos8-haswell/intel-20.0.3/mpich/3.3.2-n7f36fo/lib_laptfort_MI,_rpath — MI,_rpath — MI,_share/Apps/lusoft/opt/spack/linux-centos8-haswell/intel-20.0.3/mpich/3.3.2-n7f36fo/lib_laptfort_MI,_rpath — MI,_share/Apps/lusoft/opt/spack/linux-centos8-haswell/intel-20.0.3/mpich/3.3.2-n7f36fo/lib_laptfort_MI,_rpath — MI,_rpath — MI,_

Running MPI Applications



- To run MPI applications, you need to launch the application using mpirun (OpenMPI), mpirun_rsh (MPICH and MVAPICH2) or mpiexec (OpenMPI, MPICH and MVAPICH2).
- mpirun, mpirun_rsh and mpiexec are schedulers for the MPI library.
- On clusters with SLURM scheduler, srun can be used to launched MPI applications
- The MPI scheduler needs to be given additional information to correctly run MPI applications

	mpiexec	mpirun_rsh	mpirun
# Processors	-n numprocs	-n numprocs	-np numprocs
Processors List	-hosts core1,core2,	core1 core2	-hosts core1,core2,
Processor filelist	-f file	-hostfile file	-f/-hostfile file

- Run an application myapp on 72 processors on a total of 3 nodes node1, node2 and node3
 - mpirun: mpirun —np 72—f filename myapp
 - mpirun_rsh: mpirun_rsh -np 72-hostfile filename myapp
 - mpiexec: mpiexec -n 72-hosts node1,node2,node3-ppn 24myapp

MPI Program Outline



- Initiate communication between processes
 - MPI_INIT: initialize MPI environment
 - MPI_COMM_SIZE: return total number of MPI processes
 - MPI_COMM_RANK: return rank of calling process
- 2 Communicate data between processes
 - MPI_SEND: send a message
 - MPI_RECV: receive a message
- 3 Terminate the MPI environment using MPI_FINALIZE

First MPI Program



\mathbf{c}

```
// required MPI include file
#include "mpi.h"
#include <stdio.h>
int main(int arac, char *arav[]) {
  int numtasks, rank, len, rc:
 char hostname[MPI MAX PROCESSOR NAME]:
 // initialize MPI
 MPI Init(&arac.&arav):
 // get number of tasks
 MPI_Comm_size(MPI_COMM_WORLD,&numtasks);
 // get my rank
 MPI_Comm_rank(MPI_COMM_WORLD,&rank);
 // this one is obvious
 MPI_Get_processor_name(hostname, &len);
 printf ("Number of tasks= %d My rank= %d Running on %s\
          n", numtasks, rank, hostname);
  // done with MPI
 MPI_Finalize();
```

Fortran

```
program simple
  ! required MPI include file
  include 'mpif.h'
  integer numtasks, rank, len, ierr
 character(MPI MAX PROCESSOR NAME) hostname
  ! initialize MPI
  call MPI INIT(ierr)
  ! get number of tasks
  call MPI_COMM_SIZE(MPI_COMM_WORLD, numtasks, ierr)
  ! get my rank
  call MPI_COMM_RANK(MPI_COMM_WORLD, rank, ierr)
  ! this one is obvious
 call MPI_GET_PROCESSOR_NAME(hostname, len, ierr)
 print '(a,i2,a,i2,a,a)', 'Number of tasks=',numtasks,'
          My rank=',rank,&
       ' Running on ',hostname
  ! done with MPT
  call MPI_FINALIZE(ierr)
end program simple
```

Compile & Run



```
[alp514.sol](1003): module load mvapich2/2.2/intel=17.0.3 [alp514.sol](1004): mpicc — helloc hello.c [alp514.sol](1005): mpirG — helloc hello.fp0 [alp514.sol](1005): mpirG — helloc hello.fp0 [alp514.sol](1006): srun —p eng —n 4 ./helloc Number of tasks= 4 My rank= 3 Running on sol—b110 Number of tasks= 4 My rank= 2 Running on sol—b110 Number of tasks= 4 My rank= 2 Running on sol—b110 [alp514.sol](1007): srun —p eng —n 4 ./hellof Number of tasks= 4 My rank= 3 Running on sol—b110 Number of tasks= 4 My rank= 2 Running on sol—b110 Number of tasks= 4 My rank= 2 Running on sol—b110 Number of tasks= 4 My rank= 2 Running on sol—b110 Number of tasks= 4 My rank= 8 Running on sol—b110 Number of tasks= 4 My rank= 0 Running on sol—b110 Number of tasks= 4 My rank= 0 Running on sol—b110
```

MP1 Program Structure



Header File: Required for all programs that make MPI library calls.

С	Fortran	
<pre>#include "mpi.h"</pre>	include 'mpif.h'	

- Format of MPI Calls:
 - C names are case sensitive; Fortran names are not.
 - Programs must not declare variables or functions with names beginning with the prefix MPI_ or PMPI_ (profiling interface)

C Binding		
Format	<pre>rc = MPI_Xxxxx(parameter,)</pre>	
Example	<pre>rc = MPI_Bsend(&buf,count,type,dest,tag,comm)</pre>	
Error code	Returned as "rc". MPI_SUCCESS if successful	
Fortran Binding		
Format	CALL MPI_XXXXX(parameter,, ierr)	
	call mpi_xxxxx(parameter,, ierr)	
Example	CALL MPI_BSEND(buf,count,type,dest,tag,comm,ierr)	
Error code	Returned as "ierr" parameter. MPI_SUCCESS if successful	

Communicators



A communicator is an identifier associated with a group of processes



```
MPI_Comm_size(MPI_COMM_WORLD,int &numtasks);
MPI_Comm_rank(MPI_COMM_WORLD,int &rank);

call MPI_COMM_SIZE(MPI_COMM_WORLD, numtasks, ierr)
call MPI_COMM_RANK(MPI_COMM_WORLD, rank, ierr)
```

Communicators



- A communicator is an identifier associated with a group of processes
 - Can be regarded as the name given to an ordered list of processes
 - Each process has a unique rank, which starts from 0 (usually referred to as "root")
 - It is the context of MPI communications and operations
 - For instance, when a function is called to send data to all processes, MPI needs to understand what "all"
 - MPI_COMM_WORLD: the default communicator contains all processes running a MPI program
 - There can be many communicators
 - e.g., MPI_Comm_split(MPI_Commcomm, intcolor, int, kye, MPI_Comm* newcomm)
 - A process can belong to multiple communicators
 - The rank is usually different

Communicator Information



- Rank: unique id of each process
 - C: MPI_Comm_Rank(MPI_Comm comm, int *rank)
 - Fortran: MPI_COMM_RANK(COMM, RANK, ERR)
- Get the size/processes of a communicator
 - C: MPI_Comm_Size(MPI_Comm comm, int *size)
 - Fortran: MPI_COMM_SIZE(COMM, SIZE, ERR)

Compiling MPI Programs



- Not a part of the standard
 - Could vary from platform to platform
 - Or even from implementation to implementation on the same platform
 - mpicc/mpicxx/mpif77/mpif90: wrappers to compile MPI code and auto link to startup and message passing libraries

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Compiling MPI Programs



- Not a part of the standard
 - Could vary from platform to platform
 - Or even from implementation to implementation on the same platform
 - mpicc/mpicxx/mpif77/mpif90: wrappers to compile MPI code and auto link to startup and message passing libraries
- Unlike OpenMP and OpenACC, you cannot compile a MPI program for running in serial using the serial compiler
- The MPI program is not a standard C/C++/Fortran program and will split out errors about missing libraries



- Environment management functions
 - MPI_INIT
 - 2 MPI COMM SIZE
 - MPI_COMM_RANK
 - MPI_ABORT: Terminates all MPI processes
 - MPI_GET_PROCESSOR_NAME: Returns the processor name.
 - MPI_GET_VERSION: Returns the version and subversion of the MPI standard
 - MPI_INITIALIZED: Indicates whether MPI_Init has been called
 - MPI_WTIME: Returns an elapsed wall clock time in seconds
 - MPI_WTICK: Returns the resolution in seconds of MPI_WTIME
 - MPI_FINALIZE

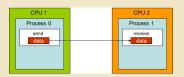
```
MPI_Init (&orgc,&orgv)
MPI_comm_size (comm,&size)
MPI_comm_rank (comm,&orank)
MPI_Abort (comm,errorcode)
MPI_Abort (comm,errorcode)
MPI_Get_processor_name (&name,&resultlength)
MPI_Get_version (&version,&subversion)
MPI_Initialized (&flag)
MPI_Wtick ()
MPI_Wtick ()
MPI_MICK ()
```

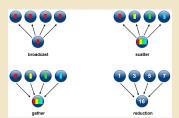
```
MPI_INIT (ierr)
MPI_COMM_SAIRE (comm, size, ierr)
MPI_COMM_RANK (comm, ronk, ierr)
MPI_ABORT (comm, error code, ierr)
MPI_GET_VERSION (version, subversion, ierr)
MPI_GET_VERSION (version, subversion, ierr)
MPI_NITIALIZED (flag, ierr)
MPI_WITICK ()
MPI_WITICK ()
MPI_WITICK ()
MPI_WITICK (ierr)
```

MP1 Functions



- Point-to-point communication functions
 - Message transfer from one process to another
- Collective communication functions
 - Message transfer involving all processes in a communicator





Point-to-point Communication



- MPI point-to-point operations typically involve message passing between two, and only two, different MPI tasks.
- One task is performing a send operation and the other task is performing a matching receive operation.
- There are different types of send and receive routines used for different purposes.
 - Blocking send / blocking receive
 - 2 Non-blocking send / non-blocking receive
 - Synchronous send

Point-to-point Communication



Blocking vs. Non-blocking:

- Blocking send / receive
 - send will "return" after it is safe to modify the application buffer (your send data) for reuse
 - send can be synchronous i.e. handshake with the receive task to confirm a safe send
 - send can be asynchronous if a system buffer is used to hold the data for eventual delivery to the receive.
 - receive only "returns" after the data has arrived and is ready for use by the program.
- Non-blocking send / receive
 - behave similarly they will return almost immediately.
 - do not wait for any communication events to complete, such as message copying from user memory to system buffer space or the actual arrival of message.
 - operations simply "request" the MPI library to perform the operation when it is able.
 - The user can not predict when that will happen.
 - communications are primarily used to overlap computation with this world Security Security

Blocking Message Passing Example



```
#include "mpi.h"
#include <stdio.h>
main(int arac, char *arav[]) {
  int numtasks, rank, dest, source, rc, count, tag-1:
 char inmsa, outmsa='x':
 MPI Status Stat: // required variable for receive routines
 MPI Init(&grac,&gray):
 MPI Comm size(MPI COMM WORLD, &numtasks):
 MPI Comm rank(MPI COMM WORLD, &rank):
 // task 0 sends to task 1 and waits to receive a return message
  if (rank - 0) {
   dest - 1:
    source - 1:
    MPI Send(&outmsg. 1. MPI CHAR, dest. tog. MPI COMM WORLD):
    MPI Recy(&inmsg. 1, MPI CHAR, source, tag, MPI COMM WORLD, &Stat):
 // task 1 waits for task 0 message then returns a message
 else if (rank -- 1) {
   dest = 0;
    source = 0;
    MPI_Recv(&inmsg, 1, MPI_CHAR, source, tag, MPI_COMM_WORLD, &Stat);
    MPI_Send(&outmsq, 1, MPI_CHAR, dest, tag, MPI_COMM_WORLD);
 // query recieve Stat variable and print message details
 MPI_Get_count(&Stat, MPI_CHAR, &count);
 printf("Task %d: Received %d char(s) from task %d with tag %d \n",
  rank, count, Stat.MPI_SOURCE, Stat.MPI_TAG);
 MPT Finalize():
```

```
program pina
 include 'mpif.h'
 integer :: numtasks, rank, dest, source, count, tag, ierr
 integer :: stat(MPI STATUS SIZE) ! required variable for receive routines
 character :: inmsg, outmsg
 outnsa - 'x'
 tag - 1
 call MPI INIT(ierr)
 call MPI_COMM_RANK(MPI_COMM_WORLD, rank, ierr)
 call MPI COMM SIZE(MPI COMM WORLD, numtasks, ierr)
 ! task 0 sends to task 1 and waits to receive a return message
 if (rank .eq. 0) then
    dest - 1
    source - 1
    call MPI SENDCoutmsa, 1, MPI CHARACTER, dest. top. MPI COMM WORLD, ierr)
    call MPI RECV(inmsa, 1, MPI CHARACTER, source, tag, MPI COMM WORLD, stat.
                ierr)
    ! task 1 waits for task 0 message then returns a message
 else if (rank .eq. 1) then
    dest = 0
    source - 0
    call MPI_RECV(inmsq, 1, MPI_CHARACTER, source, tag, MPI_COMM_WORLD, stat, err
    call MPI_SEND(outmsq, 1, MPI_CHARACTER, dest, tag, MPI_COMM_WORLD, err)
 ! query recieve Stat variable and print message details
 call MPI_GET_COUNT(stat, MPI_CHARACTER, count, ierr)
 print *, 'Task ',rank,': Received', count, 'char(s) from task', &
      stat(MPI_SOURCE), 'with tag', stat(MPI_TAG)
 call MPI_FINALIZE(ierr)
end program ping
```

Blocking Message Passing Example



```
#include "mpi.h"
#include <stdio.h>
main(int argc, char *argv[]) {
  int numtosks, rank, right, left, bufF21, tag1=1, tag2=2;
 MPI_Request reqs[4]; // required variable for non-blocking calls
 MPI_Status stats[4]; // required variable for Waitall routine
 MPI_Init(&argc,&argv);
 MPI Comm size(MPI COMM WORLD, &numtasks):
 MPI Comm rank(MPI COMM WORLD, &rank):
 // determine left and right neighbors
  left = ronk-1:
 right = rank+1;
 if (rank -- 0) left - numtasks-1;
 if (rank -- (numtasks-- 1)) right - 0:
 // post nom blocking receives and sends for neighbors
 MPI_Irecv(&buf[0], 1, MPI_INT, left, tag1, MPI_COMM_WORLD, &regs[0]);
 MPI_Irecv(&buf[1], 1, MPI_INT, right, tag2, MPI_COMM_WORLD, &reqs[1]);
 MPI_Isend(&rank, 1, MPI_INT, left, tag2, MPI_COMM_WORLD, &reqs[2]);
 MPI Isend(&rank, 1, MPI INT, right, too1, MPI COMM WORLD, &regs[3]):
 // wait for all nom-blocking operations to complete
 MPI Waitall(4, reas, stats):
 printf("Task %d: Received from task %d with tag %d and from task %d with tag %d\
   rank, left, tag1, right, tag2);
   rank, left, tag2, right, tag1);
 MPI_Finalize();
```

```
program ringtopo
 include 'mpif.h'
 integer numtasks, rank, next, prev, buf(2), tag1, tag2, ierr, count
 integer regs(4) ! required variable for non-blocking calls
 integer stats(MPI STATUS SIZE.4) ! required variable for WAITALL routine
 tag1 - 1
 tag2 = 2
 call MPI INIT(ierr)
 call MPI_COMM_RANK(MPI_COMM_WORLD, rank, ierr)
 call MPI_COMM_SIZE(MPI_COMM_NORLD, numtasks, ierr)
 ! determine left and right neighbors
 prev = rank-1
 next = rank + 1
 if (rank .eq. 0) then
   prev = numtosks--- 1
 if (rank ea numtasks-1) then
   next = 0
 I nost nom-blocking receives and sends for neighbors
 ! Receive 1 from left and 2 from right
 call MPI_IRECV(buf(1), 1, MPI_INTEGER, prev, tag1, MPI_COMM_WORLD, regs(1), ierr
  call MPI IRECV(buf(2), 1, MPI INTEGER, next, tag2, MPI COMM WORLD, regs(2), ierr
 ! Send 1 to right and 2 to legft
 call MPI ISEND(rank, 1, MPI INTEGER, prev, tag2, MPI COMM WORLD, reas(3), ierr)
 call MPI ISEND(rank, 1, MPI INTEGER, next, tag1, MPI COMM WORLD, reas(4), ierr)
 ! wait for all nom-blocking operations to complete
 call MPI WAITALL(4, reas, stats, ierr):
  print '(5(a,i2))', 'Task ',rank,': Received from task', prev, ' with tag',tag1,
        and from task', next, ' with tag',tag2
  print '(5(a,i2))', 'Task ',rank,': Send to task', prev, ' with tag',tag2, &
       and to task', next, ' with tag', tag1
 call MPI_FINALIZE(ierr)
```

end program ringtopo

Blocking Message Passing Example



```
[alp514.sol](1110): mpicc—o ringc ring.c [alp514.sol](1113): srun—p eng—n 4./ringc Task 0: Received from task 3 with tag 1 and from task 1 with tag 2 Task 0: Send to task 3 with tag 2 and to task 1 with tag 1 Task 1: Received from task 0 with tag 1 and from task 2 with tag 2 Task 1: Send to task 0 with tag 2 and to task 2 with tag 1 Task 2: Received from task 1 with tag 1 and from task 3 with tag 2 Task 2: Send to task 1 with tag 2 and to task 3 with tag 1 Task 3: Received from task 1 with tag 2 and to task 3 with tag 1 Task 3: Received from task 2 with tag 2 and to task 3 with tag 2 Task 3: Received from task 2 with tag 1 and from task 0 with tag 2 Task 3: Send to task 2 with tag 2 and to task 3 with tag 2 Task 3: Send to task 2 with tag 2 and to task 9 with tag 2
```

```
[alp514.sol](1111): mpif90—o ringf ring.f90
[alp514.sol](1114): run—p eng—n 4 /ringf
Task 3: Received from task 2 with tag 1 and from task 0 with tag 2
Task 3: Send to task 2 with tag 2 and to task 0 with tag 1
Task 0: Received from task 3 with tag 1 and from task 1 with tag 2
Task 0: Send to task 3 with tag 2 and to task 1 with tag 1
Task 1: Received from task 0 with tag 1 and from task 2 with tag 2
Task 1: Send to task 0 with tag 2 and to task 2 with tag 1
Task 2: Received from task 0 with tag 1 and from task 3 with tag 2
Task 2: Received from task 1 with tag 2 and to task 3 with tag 2
Task 2: Received from task 1 with tag 2 and to task 3 with tag 2
```

Further Reading



- Tutorials
 - MPI: https://computing.llnl.gov/tutorials/mpi/
 - 2 Advanced MPI:

https://hpc.llnl.gov/sites/default/files/DavidCronkSlides.pdf

- Output
 Output<
- XSEDE HPC Monthly Workshop Series: https://psc.edu/xsede-hpc-series-all-workshops
- MPI Tutorial: http://mpitutorial.com/
- Books
 - Beginning MPI (An Introduction in C) by Wesley Kendall
 - 2 Parallel Programming with MPI by Peter Pacheco (No relation)
 - Using MPI 2nd Edition: Portable Parallel Programming with the Message Passing Interface (Scientific and Engineering Computation) by William Gropp
 - Parallel Programming in C with MPI and Openmp by Michael J. Quinn
 - MPI: The Complete Reference by Marc Snir et. al.