

Contents

1	Derivations	2
1.1	Theoretical $Z - Z$ Cross Section σ	2
1.2	Theoretical $\gamma - Z$ Cross Section σ	3
2	Misc.	4
2.1	Feynman Diagrams	4

Chapter 1

Derivations

1.1 Theoretical $Z - Z$ Cross Section σ

Define

$$\begin{aligned}\alpha &= \frac{g_Z^4}{(32\pi)^2 s} \frac{\sqrt{1-4\varepsilon^2}}{(1-\lambda^2)^2 + (\frac{\lambda\Gamma_Z}{\sqrt{s}})}, \\ \beta &= ((C_V^e)^2 + (C_A^e)^2)((C_V^\mu)^2), \\ \Delta &= ((C_V^e)^2 + (C_A^e)^2)((C_A^\mu)^2), \\ \Gamma &= 8C_V^e C_A^e C_V^\mu C_A^\mu.\end{aligned}$$

These definitions produce the differential cross section:

$$\frac{d\sigma}{d\Omega}^{Z-Z} = \alpha(\beta(1+\cos^2\vartheta+4\varepsilon^2\sin^2\vartheta)+\Delta(1+\cos^2\vartheta)(1-4\varepsilon^2)+\Gamma\sqrt{1-4\varepsilon^2}\cos\vartheta)$$

Under the substitutions

$$\begin{aligned}\sin^2\vartheta &\rightarrow 1-\cos^2\vartheta \quad \text{and} \\ \varepsilon_\pm &= 1 \pm 4\varepsilon^2,\end{aligned}$$

we see that the integral over the solid angle $d\Omega = d\phi dx$ (with implicit change of variable $\cos\vartheta \rightarrow x$) becomes

$$\begin{aligned}\sigma &= \alpha \int_0^{2\pi} d\phi \int_{-1}^1 \beta\varepsilon_+ + \beta\varepsilon_-x^2 + \Delta\varepsilon_- + \Delta\varepsilon_-x^2 + \Gamma\sqrt{\varepsilon_-}x \, dx \\ &= 2\pi\alpha \int_{-1}^1 \beta\varepsilon_+ + \Delta\varepsilon_- + (\beta + \Delta)\varepsilon_-x^2 + \Gamma\sqrt{\varepsilon_-}x \, dx.\end{aligned}$$

The Γ term will disappear as it is symmetric in the integration limits. After simplification, the trivial integral is evaluated to

$$\sigma^{Z-Z} = 4\pi\alpha(\beta(\varepsilon_+ + \frac{1}{3}\varepsilon_-) + \frac{4}{3}\Delta\varepsilon_-).$$

1.2 Theoretical $\gamma - Z$ Cross Section σ

Define

$$\begin{aligned}\alpha &= \frac{2g_e^2 g_Z^2}{(16\pi)^2 s} \frac{(1 - \lambda^2)\sqrt{1 - 4\varepsilon^2}}{(1 - \lambda^2)^2 + (\frac{\lambda\Gamma_Z}{\sqrt{s}})}, \\ \beta &= C_V^e C_V^\mu, \\ \Delta &= 2C_A^e C_A^\mu \sqrt{1 - 4\varepsilon^2},\end{aligned}$$

These definitions lead to the differential cross section

$$\frac{d\sigma^{\gamma-Z}}{d\Omega} = \alpha(\beta(1 + \cos^2 \vartheta + 4\varepsilon^2 \sin^2 \vartheta) + \Delta \cos \vartheta)$$

Under the substitution $\sin^2 \vartheta \rightarrow 1 - \cos^2 \vartheta$, we see that the integral over the solid angle $d\Omega = d\phi dx$ (with implicit change of variable $\cos \vartheta \rightarrow x$) becomes

$$\begin{aligned}\sigma &= \alpha \int_0^{2\pi} d\phi \int_{-1}^1 \beta(1 + x^2 + 4\varepsilon^2(1 - x^2)) + \Delta x \, dx \\ &= 2\pi\alpha \int_{-1}^1 \beta(1 + 4\varepsilon^2) + \beta(1 - 4\varepsilon^2)x^2 + \Delta x \, dx.\end{aligned}$$

The antisymmetric Δx terms vanishes under integration, giving (after rearranging)s

$$\sigma = \frac{16}{3}\pi\alpha\beta(1 + 2\varepsilon^2).$$

Chapter 2

Misc.

2.1 Feynman Diagrams

Here are the Feynman diagrams for the scatterings.

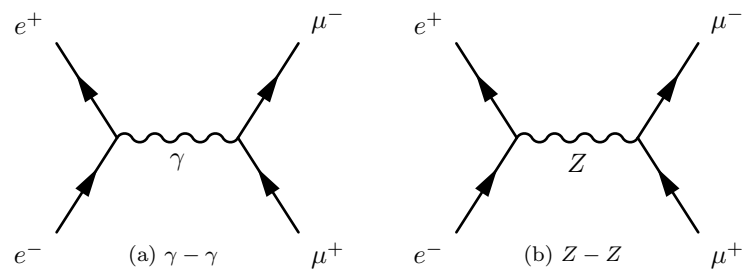


Figure 2.1: $e^-e^+ \rightarrow \mu^-\mu^+$ scattering via different bosons.