

Supporting material for “Inferring epidemiological dynamics with Bayesian coalescent inference: The merits of deterministic and stochastic models”

1 Sampling from the prior

In order to assess the correctness of our implementation of the deterministic coalescent SIR and stochastic coalescent SIR models, for each model we used the MCMC algorithm to sample trees from the corresponding distribution $f(\mathcal{T}|\eta)$, and compared these samples with coalescent trees simulated directly under the model.

The chosen η included $\beta = 7.5 \times 10^{-4}$, $\gamma = 0.3$, $S_0 = 999$ and $z_0 = 30$. The comparisons were performed for trees generated from 20 leaves, sampled at integer times 0 through 19, inclusive.

For the deterministic coalescent SIR model, the direct simulation involved numerically solving the Eqs. (1)–(3) in the main text for $t \in [0, 30]$ and using this solution in combination with Eq. (10) in the main text to determine the instantaneous coalescent rate $\lambda(\tau)$. This rate was used to simulate each of the coalescent trees in the usual fashion for heterochronous leaf times. In the case that the MRCA was not reached before the origin time of the epidemic, the tree was discarded and the simulation repeated.

The direct simulation proceeded in a similar way for the stochastic coalescent SIR model, the major difference being that the stochasticity of this model required each coalescent tree to be simulated under a distinct realization of the stochastic trajectory.

Comparisons between the direct simulation and MCMC results are shown in Figures S1 and S2 for three different summary statistics and show very close agreement.

2 Validation through simulated data analysis

As part of the validation of our implementation of the two coalescent SIR models, trees were simulated by their own methods (using stochastically- and deterministically-generated SIR trajectories, as discussed in the Methods section of the main paper), and relevant epidemiological parameters were inferred

using the stochastic and deterministic coalescent SIR models. Tables 1 and 2 show the results of these analyses, indicative of correct implementations.

Analyses for varying R_0 (and necessarily, slightly varied other parameters, such as the birth rate β) are provided in Tables S3 and S4. Results from tests of the influence of broader priors (with larger standard deviations in log space) are shown in Table S4. It appears that allowance of broader priors reduces 95% HPD coverage in some cases (e.g., for parameter R_0) when using the deterministic coalescent SIR inference model, as they increase error and bias.

Finally, it was noticed that even for the higher true parameter values of $R_0 = 2.50$ and $S_0 = 999$, under which deterministic coalescent SIR is expected to perform relatively well, there was an inability to accurately estimate the origin parameter z_0 . Figure S3 provides some insight into this conundrum by examining the trajectories used for tree simulation and subsequent analysis.

2.1 H1N1 data selection

Initially, the H1N1 dataset contained 45 sequences. The ages of the inferred trees (Figure S4) using the original 45 sequences extended more than 1.5 years into the past for each of the SIR models, which is contrary to what we expect for a single, current strain of seasonal influenza. Three taxa (labelled 32197, 31893, and 31988) were hypothesized to belong to a unique strain, e.g., an additional seeding from outside the Canterbury region or a low-lying previous strain. Removing these three taxa caused the inferred trees to behave as expected, i.e., tree heights and epidemic origin z_0 less than a year old. It also raised the estimated R_0 values for all three SIR models (initially 1.24, 1.10, and 1.55 for stochastic coalescent SIR, deterministic coalescent SIR, and BDSIR, respectively), as well as those for γ (initially 8.74, 12.65, and 11.33 for stochastic coalescent SIR, deterministic coalescent SIR, and BDSIR, respectively).

It will be interesting to further investigate the interplay between influenza strains and its contribution to the overall dynamics. For the closed SIR models discussed in this manuscript, however, this additional complexity leads to increased chance of model misspecification and misleading results. Therefore, we focused our attention on the analyses using 42 sequences.

2.2 HIV-1 data analysis

The original HIV-1 dataset (HUÉ *et al.* 2005) was agglomerated from both acute and chronic infections sampled in the United Kingdom (UK) and constitutes six phylogenetic clusters, from which the five used here (Clusters 1-4 and 6) were drawn. These particular clusters, with the omission of Cluster 5, were chosen simply for the purpose of direct comparison with KÜHNERT *et al.* (2014). Our extension to the models allowed us to imprint respective tip dates on the sequence data, sampled from 1999 to 2003, for inclusion in the likelihood computation.

For the selected five clusters, the nucleotide alignments contained 41, 62, 29, 26, and 35 sequences, respectively, each with 952 sites. The substitution

scheme chosen for phylogenetic analysis was the symmetric and independent general time reversible model (GTR), with gamma distributed rate variation and explicit proportion of invariable sites (GTR+G+I). Following HUÉ *et al.* (2005), the substitution rate was set to 2.55E-4 substitutions per site per year. All other parameters were estimated conjointly, and the Bayesian prior distributions are presented in Table 4: Bayesian prior distributions.

The pathophysiology of HIV is multifarious, and the patterns of its advancement within an infected host change throughout time. In addition to increased complexity potentially caused by recombination events, the transition between HIV’s acute and chronic phases alters the host’s infectivity (GUSS 1994). The SIR compartmental model used for this particular phylodynamic analysis on the UK cluster data does not allow for independent infection rates for the acute and chronic phases (but see VOLZ *et al.* (2012) and VOLZ *et al.* (2013)). However, in this study we did not attempt to estimate the infection rate β and thus did not expect such a difference to significantly impact the estimation of the parameters of interest: the basic reproductive number R_0 , removal rate γ , size of the initial susceptible population S_0 , and origin of the outbreak z_0 .

2.2.1 HIV-1 inference results

In regard to parameter inference from the serially-sampled HIV-1 sequence data, the stochastic coalescent SIR, deterministic coalescent SIR, and BDSIR methods were most alike in light of the R_0 results. The medians and HPD intervals for all clusters pertaining to this parameter, (especially Clusters 1, 2, 3, and 6), were very close, and those of Cluster 4 were still congruent across the three analyses (Figure S5).

The coalescent SIR models and BDSIR disagreed with respect to the age of the most recent common ancestor and the origin z_0 (Figure S6). The coalescent SIR models also exhibited much larger 95% HPD intervals for z_0 in each of the clusters; while BDSIR encompassed an average of 16 years, the stochastic coalescent SIR and deterministic coalescent SIR models had averages of 49 and 37 years, respectively. Furthermore, the estimated age of the common ancestor of the tree was older under the coalescent SIR models than the estimates reported by either BDSIR or the original data analysis (HUÉ *et al.* 2005) for each cluster. This was also true for the time of origin for the epidemic, although for certain clusters the differences between the coalescent estimates of the origin z_0 and the birth-death estimates were much greater than others (e.g., Cluster 3).

The estimates of removal rate γ from Clusters 1 and 6 were very similar across the three methods (Figure S7). However, both coalescent SIR models estimated considerably higher γ values for Clusters 2-4 than BDSIR. This is reflective of the simulation study results, where the two coalescent models did not perform as well as BDSIR for the removal parameter.

Median estimates for the initial susceptible population S_0 were quite similar in all methods for Clusters 1-4, although BDSIR displayed much wider HPD intervals than stochastic coalescent SIR and deterministic coalescent SIR (Figure S8). In Cluster 6, the coalescent SIR models showed the smallest HPD intervals

for their individual analyses on each cluster, while the opposite was true for BDSIR. There was also a disparity between the median estimates for the two coalescent approaches and that of BDSIR for Cluster 6. To this effect, it should be noted that the number of infections accrued throughout the duration of the epidemic was reported as $N_e = 1,350$ by Hué *et al.* This casts some suspicion on the low susceptible population estimates obtained by the stochastic coalescent SIR and deterministic coalescent SIR methods (median estimates of $S_0 = 727$ and $S_0 = 693$, respectively), since they appear lower than the estimated number of infected individuals from the original study.

There is disagreement in the literature in regard to the modelling of HIV-1 evolutionary dynamics under stochastic or deterministic processes (NIJHUIS *et al.* 1998; ROUZINE and COFFIN 1999; ACHAZ *et al.* 2004; SHRINER *et al.* 2004). The predicament dwells in the observation that the actual effective population size N_e for HIV-1 is often smaller than the total population size (KOUYOS *et al.* 2006). While most of this debate has focused on within-host population dynamics, many of the arguments hold when considering the broader epidemic dynamics of host-to-host transmission. As previously mentioned, the appropriateness of these descriptions is hinged on the magnitude of the infected population, precisely, the effective infected population size. Consequently, even when the total infected population is quite large there may yet be significant stochastic effects in play.

Finally, as mentioned in the main article, the existence of two distinct infectious stages and the possibility of large effects due to recombination are reasons for any discrepancy produced by these SIR inference models.

2.2.2 Example XML

Below is an example XML for simulating 100 trees and trajectories in MASTER (VAUGHAN and DRUMMOND 2013). This example is for $R_0 = 2.4975$ and $S_0 = 999$. The simulation ends when the infected I population returns to zero, i.e., when the last infected individual is removed.

```
<beast version='2.0'
namespace='master.beast:beast.core.parameter:beast.evolution.tree.TreeHeightLogger'>

  <run spec='InheritanceEnsemble'
    nTraj='100'
    samplePopulationSizes='true'
    verbosity='1'>

    <model spec='InheritanceModel' id='model'>
      <population spec='Population' id='S' populationName='S'/>
      <population spec='Population' id='I' populationName='I'/>
      <population spec='Population' id='R' populationName='R'/>
      <population spec='Population' id='Rh' populationName='Rh'/>

      <!-- infection reaction -->
      <reaction spec='InheritanceReaction' reactionName='Infection' rate='0.00075'>
        S + I -> 2I
      </reaction>
    </model>
  </run>
</beast>
```

```

</reaction>

<!-- recovery reaction -->
<reaction spec='InheritanceReaction' reactionName='Recovery' rate='0.25'>
  I -> R
</reaction>

<!-- sampling reaction -->
<reaction spec='InheritanceReaction' reactionName='Sampling' rate='0.05'>
  I -> Rh
</reaction>
</model>

<initialState spec='InitState'>
  <populationSize spec='PopulationSize' population='@S' size='999' />
  <lineageSeed spec='Individual' population='@I' />
</initialState>

<populationEndCondition spec='PopulationEndCondition'
  population='@I'
  threshold='0'
  exceedCondition='false' />

<inheritancePostProcessor spec='LineageFilter'
  reactionName='Sampling'
  discard='false' />

<output spec='NewickOutput' fileName='SIR.newick' />
<output spec='NexusOutput' fileName='SIR.nexus' />
<output spec='JsonOutput' fileName='SIR.json' />

</run>
</beast>

```

[Figure 1 about here.]

[Figure 2 about here.]

[Figure 3 about here.]

[Figure 4 about here.]

[Figure 5 about here.]

[Figure 6 about here.]

[Figure 7 about here.]

[Figure 8 about here.]

[Table 1 about here.]

[Table 2 about here.]

[Table 3 about here.]

[Table 4 about here.]

[Table 5 about here.]

[Table 6 about here.]

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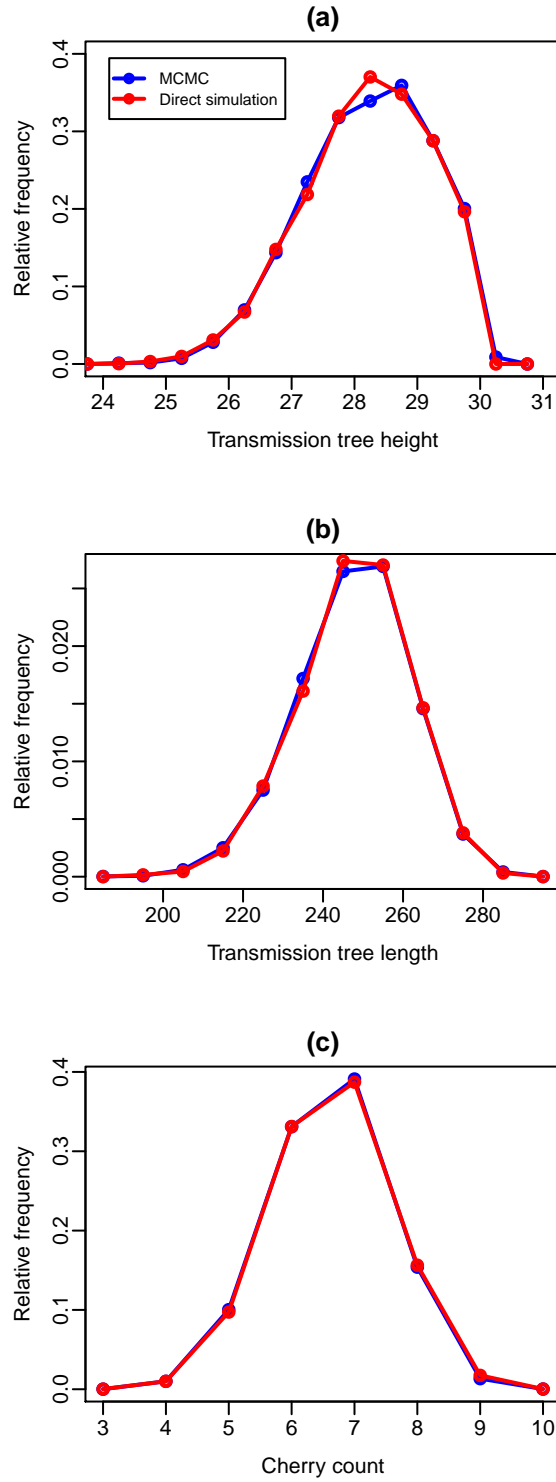


Figure S1: Comparison between distributions of summary statistics of trees sampled using MCMC employing our implementation of the *deterministic coalescent SIR model* likelihood and those calculated, and those of trees sampled using direct simulation. Summary statistics shown are (a) the age of the MRCA of the transmission tree, (b) the sum of all edge lengths in the tree, and (c) the total number of two-leaf clades in the tree.

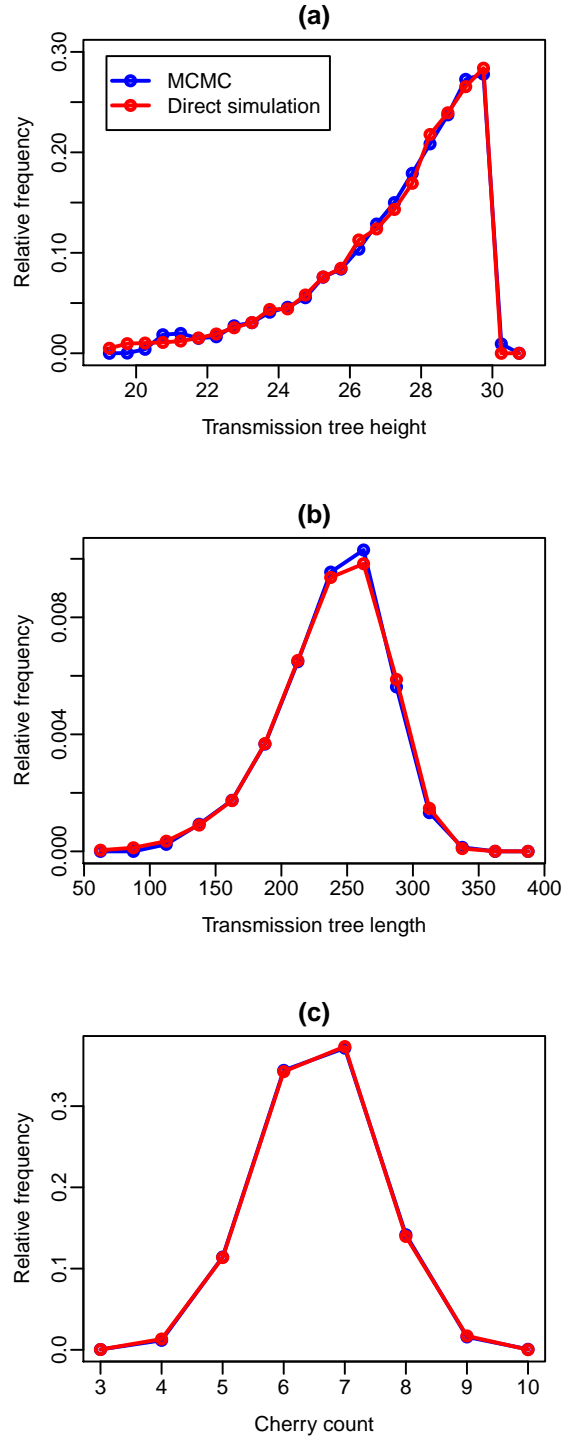


Figure S2: Comparison between distributions of summary statistics of trees sampled using MCMC employing our implementation of the *stochastic coalescent SIR model* likelihood and those calculated, and those of trees sampled using direct simulation. Summary statistics shown are (a) the age of the MRCA of the transmission tree, (b) the sum of all edge lengths in the tree, and (c) the total number of two-leaf clades in the tree.

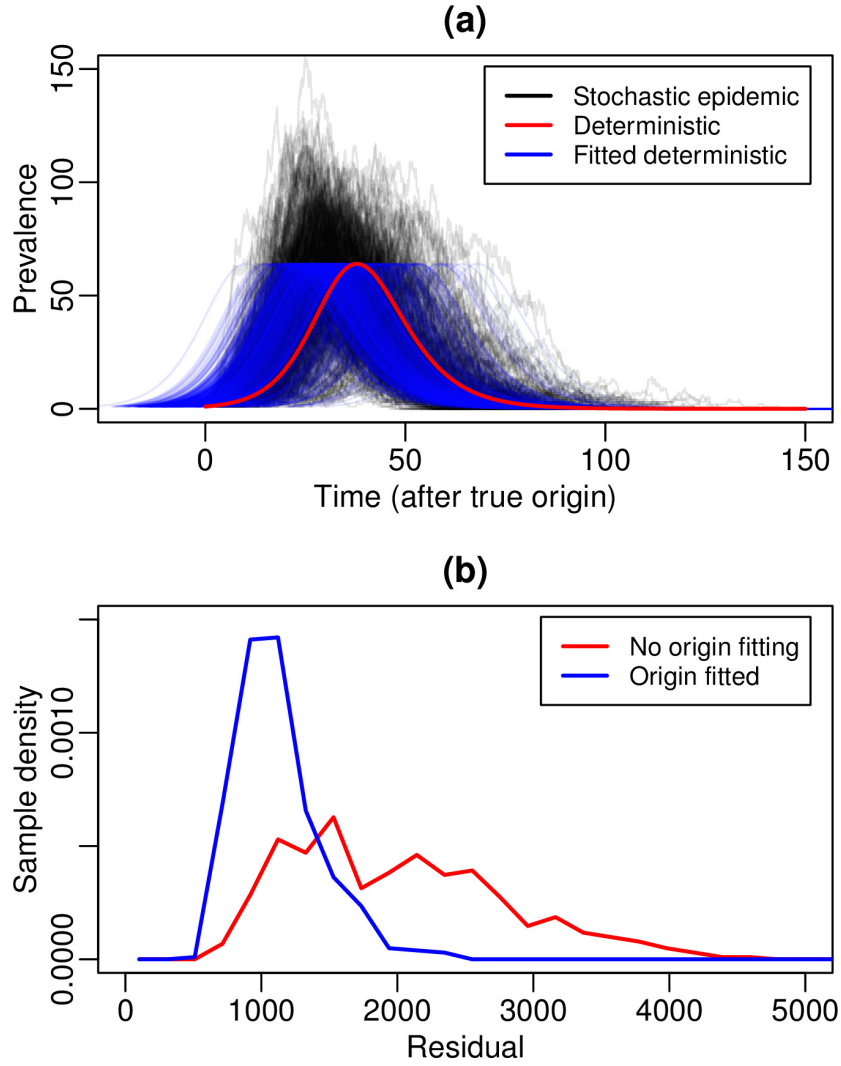


Figure S3: (a) True stochastic SIR trajectories simulated jointly alongside phylogenies, with the corresponding trajectories used by deterministic coalescent SIR. Adjusting deterministic coalescent SIR to fit the underlying stochastic trajectories causes major shifts to the origin z_0 . (b) Deterministic residuals with z_0 either fitted or not.

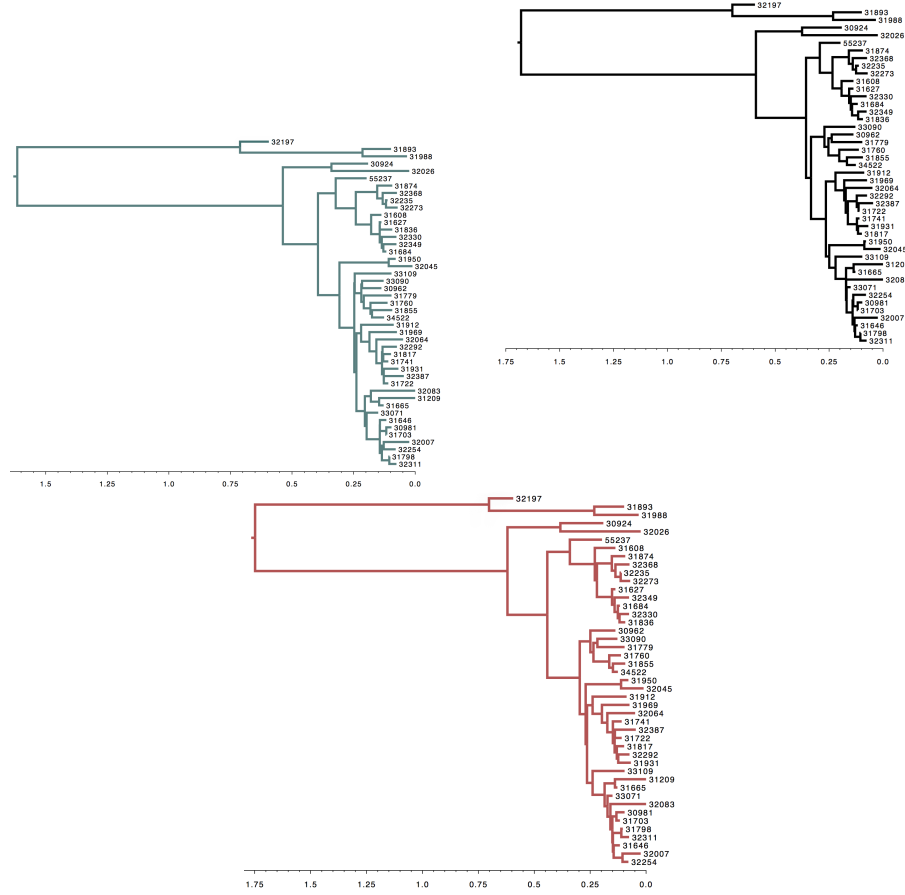


Figure S4: Representative influenza A (H1N1) posterior trees from inference using the stochastic coalescent SIR (left), deterministic coalescent SIR (right), BDSIR (bottom) models.

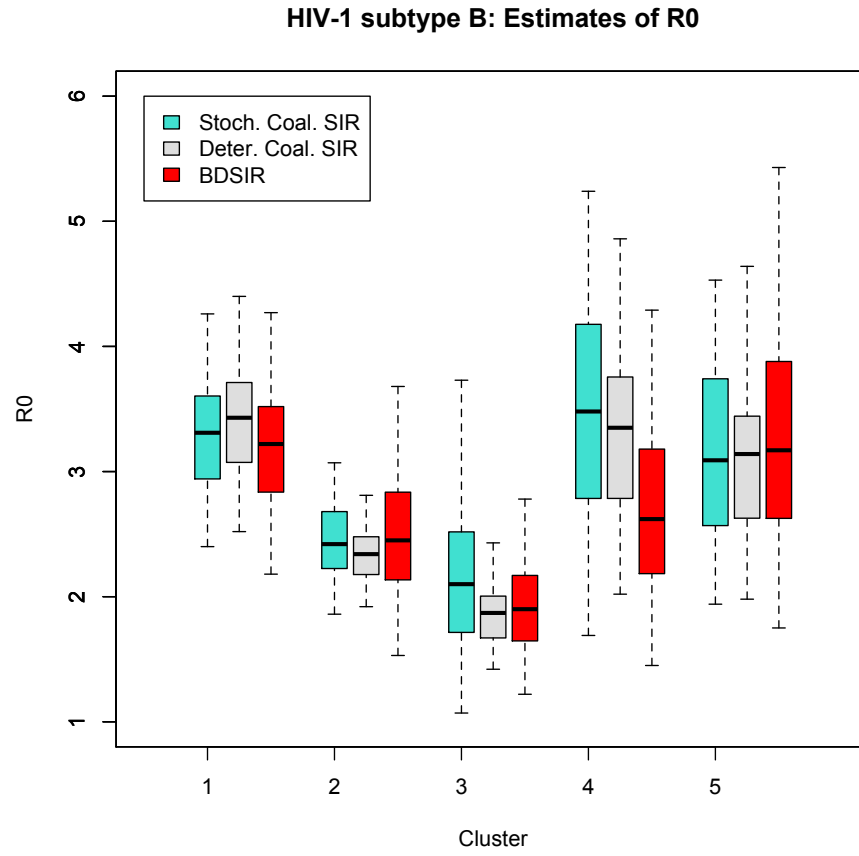


Figure S5: 95% HPD intervals of R_0 for the HIV-1 subtype B UK cluster analyses using coalescent and birth-death methods.

HIV-1 subtype B: Estimates for Tree Height and the Origin of the Epidemic

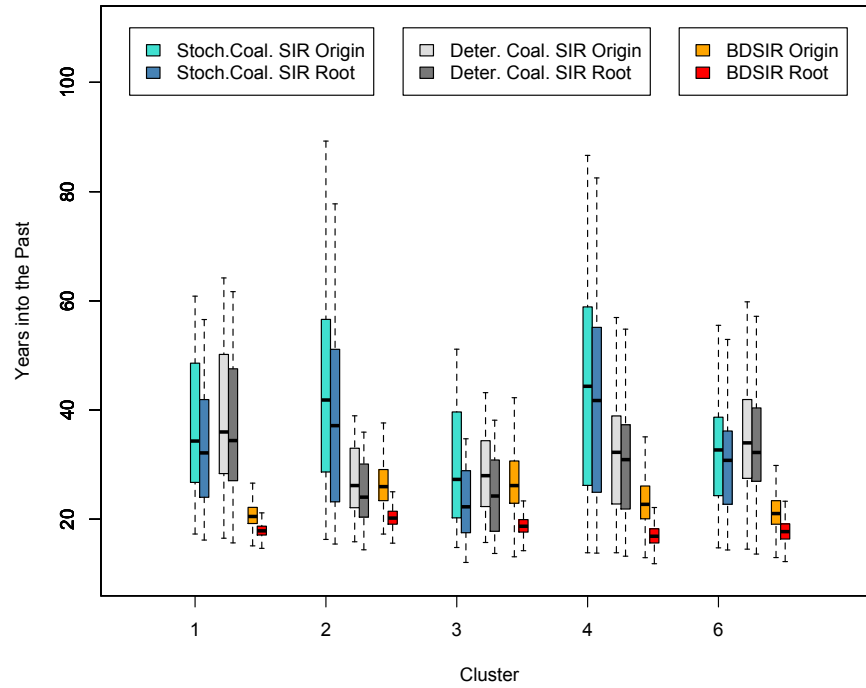


Figure S6: 95% HPD intervals for coalescent [VOLZ (2012)] and birth-death [KÜHNERT *et al.* (2014)] estimations of the time into the past at which the root of the HIV-1 tree and introduction of the first infection occurred.

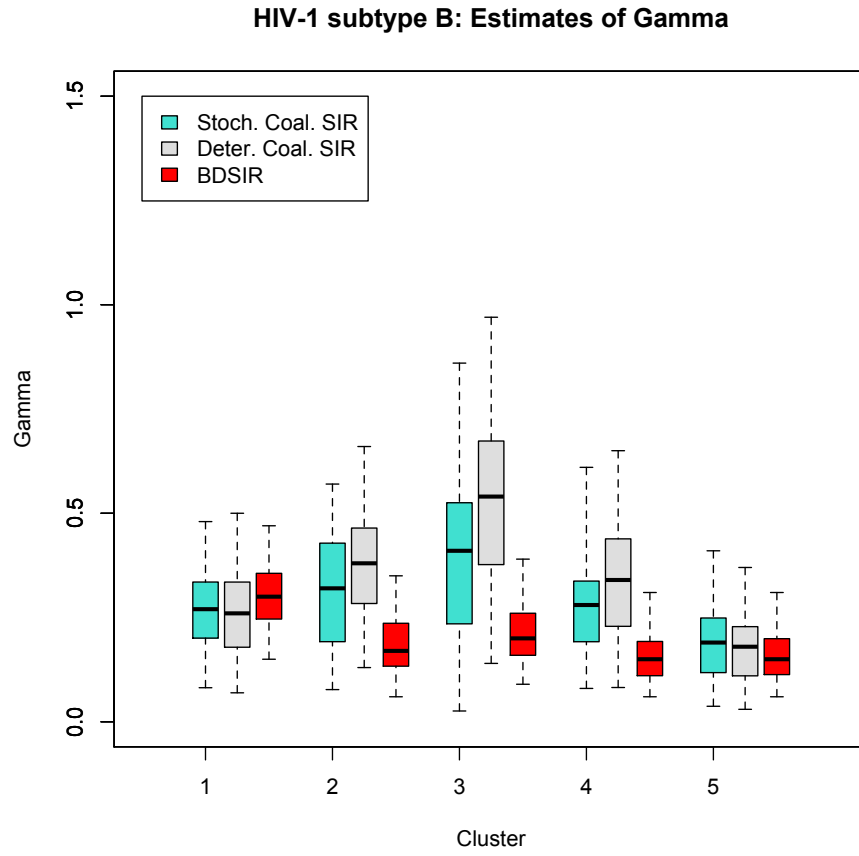


Figure S7: 95% HPD intervals of γ for the HIV-1 subtype B UK cluster analyses using coalescent and birth-death methods.

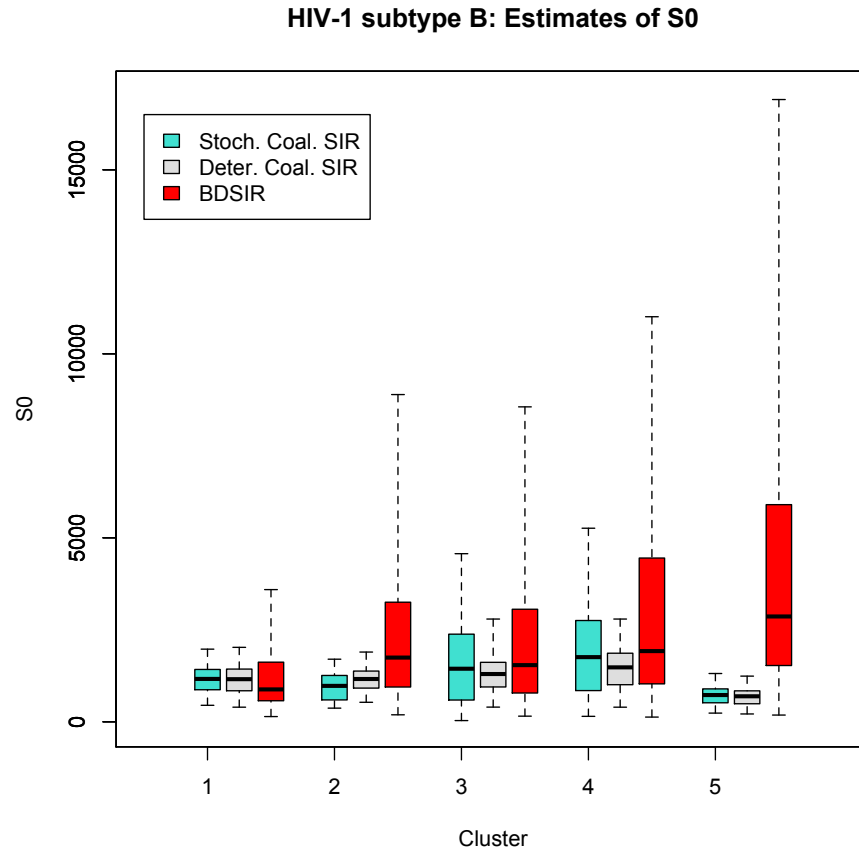


Figure S8: 95% HPD intervals of S_0 for the HIV-1 subtype B UK cluster analyses using coalescent and birth-death methods.

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Table S1: Simulation Study Results for Stochastic Coalescent Trees

η	Inference	Truth	Mean	Median	Error	Bias	Relative HPD width	95% HPD accuracy
\mathcal{R}_0	Stoch.Coal.SIR	2.50	2.81	2.64	0.11	0.08	0.95	100.00%
	Deter.Coal.SIR	2.50	2.73	2.65	0.14	0.06	0.85	96.00%
γ	Stoch.Coal.SIR	0.30	0.28	0.26	0.16	-0.11	1.17	99.00%
	Deter.Coal.SIR	0.30	0.30	0.28	0.18	-0.03	1.20	99.00%
$S_{(0)}$	Stoch.Coal.SIR	999	1456	986	0.21	0.02	3.93	100.00%
	Deter.Coal.SIR	999	1720	1057	0.48	0.24	4.28	99.00%
$z_{(0)}$	Stoch.Coal.SIR	(varies)	42.36	40.43	0.03	0.02	0.20	98.00%
	Deter.Coal.SIR	(varies)	41.25	39.77	0.03	0.01	0.07	64.00%

Table S2: Simulation Study Results for Deterministic Coalescent Trees

η	Inference	Truth	Mean	Median	Error	Bias	Relative HPD width	95% HPD accuracy
\mathcal{R}_0	Stoch.Coal.SIR	2.50	2.44	2.37	0.06	-0.05	0.67	100.00%
	Deter.Coal.SIR	2.50	2.51	2.46	0.08	-0.01	0.59	99.00%
γ	Stoch.Coal.SIR	0.30	0.33	0.31	0.07	0.05	1.00	100.00%
	Deter.Coal.SIR	0.30	0.32	0.30	0.10	0.02	0.79	100.00%
$\bar{S}_{(0)}$	Stoch.Coal.SIR	999	1586	1142	0.26	0.20	3.83	100.00%
	Deter.Coal.SIR	999	1426	1030	0.36	0.13	3.03	100.00%
$z_{(0)}$	Stoch.Coal.SIR	44.12	45.52	44.74	0.02	0.01	0.19	93.00%
	Deter.Coal.SIR	44.12	44.34	44.11	0.02	1.93E-3	0.08	92.00%

Table S3: Results for Homochronous Sampling

η	Inference	Truth	Mean	Median	Error	Bias	Relative HPD width	95% HPD accuracy
\mathcal{R}_0	Stoch.Coal.SIR	2.50	3.04	2.74	0.13	0.11	1.32	100.00%
	Deter.Coal.SIR	2.50	4.05	3.29	0.34	0.32	2.38	100.00%
	BDSIR	2.50	2.84	2.49	0.16	0.03	1.45	97.00%
γ	Stoch.Coal.SIR	0.30	0.26	0.23	0.25	-0.21	1.43	100.00%
	Deter.Coal.SIR	0.30	0.26	0.19	0.36	-0.31	2.03	100.00%
	BDSIR	0.30	0.23	0.17	0.42	-0.42	2.04	100.00%
$\mathcal{S}_{(0)}$	Stoch.Coal.SIR	999	1660	1065	0.18	0.09	4.75	100.00%
	Deter.Coal.SIR	999	4127	679	0.78	0.09	10.24	100.00%
	BDSIR	999	1907	1320	0.41	0.41	4.86	100.00%
$z_{(0)}$	Stoch.Coal.SIR	20.0	20.17	19.82	0.09	-0.03	0.43	95.00%
	Deter.Coal.SIR	20.0	19.09	19.21	0.09	-0.05	0.19	73.00%
	BDSIR	20.0	36.56	29.38	0.55	0.54	4.24	100.00%

Table S4: Simulation Study Results: The Effect of Broader Priors on Deterministic Coalescent SIR

η	St. Dev.	Truth	Mean	Median	Error	Bias	Relative HPD width	95% HPD accuracy
\mathcal{R}_0	2	1.50	2.06	1.75	0.40	0.35	0.86	79.00%
\mathcal{R}_0	1	1.50	1.80	1.49	0.24	0.15	0.52	85.00%
\mathcal{R}_0	2	2.50	3.31	2.85	0.34	0.24	1.43	95.00%
\mathcal{R}_0	1	2.50	2.68	2.49	0.13	0.04	0.80	99.00%
γ	2	0.30	0.31	0.23	0.37	-0.12	1.59	96.00%
γ	1	0.30	0.26	0.23	0.27	-0.22	1.15	89.00%
γ	2	0.30	0.31	0.25	0.33	-0.09	1.59	95.00%
γ	1	0.30	0.32	0.29	0.16	3.14E-3	1.27	99.00%
$S_{(0)}$	2	499	2041	249	1.40	0.49	7.75	85.00%
$S_{(0)}$	1	499	562	361	0.44	-0.26	3.36	91.00%
$S_{(0)}$	2	999	3028	717	1.05	0.33	6.60	94.00%
$S_{(0)}$	1	499	553.38	337	0.42	-0.26	3.08	92.00%
$z_{(0)}$	2	(varies)	65.10	62.01	0.04	0.03	0.25	86.00%
$z_{(0)}$	1	(varies)	91.03	72.51	0.39	0.38	0.42	88.00%
$z_{(0)}$	2	(varies)	40.97	39.85	0.03	-6.78E-4	0.08	81.00%
$z_{(0)}$	1	(varies)	112.79	90.37	0.26	0.26	0.94	85.00%

Table S5: Comparison of Computation Times for Bayesian Inference of Epidemic Parameters from Genetic Sequence Data using SIR Models

Data Type	Inference Model	Mean time per million samples (MCMC)
Sim. Study ($R_0 \approx 2.50$)	Stoch.Coal.SIR	20m 41s
	Deter.Coal.SIR	3m 27s
	BDSIR	56m 27s
Sim. Study ($R_0 \approx 1.50$)	Stoch.Coal.SIR	1h 43m 30s
	Deter.Coal.SIR	3m 47s
	BDSIR	41m 35s
Sim. Study ($R_0 \approx 1.10$)	Stoch.Coal.SIR	1h 50m 41s
	Deter.Coal.SIR	6m 45s
	BDSIR	41m 21s
H1N1	Stoch.Coal.SIR	1h 20m 55s
	Deter.Coal.SIR	9m 44s
	BDSIR	47m 33s
HIV-1	Stoch.Coal.SIR	14h 37m 45s
	Deter.Coal.SIR	7m 56s
	BDSIR	1h 38m 54s

Table S6: Deterministic Coalescent SIR Results for Simulated Sequences: $R_0 = 1.0987$ and $S_0 = 499$, $R_0 = 1.0989$ and $S_0 = 999$, $R_0 = 1.09945$ and $S_0 = 1999$

η	Truth	Mean	Median	Error	Bias	Relative HPD width	95% HPD accuracy
\mathcal{R}_0	≈ 1.10	1.89	1.28	0.62	0.63	0.40	52.00%
γ	0.30	0.57	0.44	0.59	0.52	2.14	95.00%
$S_{(0)}$	499	1830	1222	1.50	1.31	11.49	96.00%
$z_{(0)}$	(varies)	109.55	76.21	0.61	0.54	0.35	37.00%
\mathcal{R}_0	≈ 1.10	1.55	1.35	0.25	0.25	0.45	16.00%
γ	0.30	0.27	0.24	0.20	-0.12	1.23	61.00%
$S_{(0)}$	999	1293	804	0.27	-0.10	3.58	64.00%
$z_{(0)}$	(varies)	117.39	99.75	0.25	0.18	0.23	23.00%
\mathcal{R}_0	≈ 1.10	1.37	1.22	0.16	0.16	0.28	40.00%
γ	0.30	0.26	0.24	0.18	-0.14	1.13	64.00%
$S_{(0)}$	1999	2292	1531	0.23	-0.18	3.45	66.00%
$z_{(0)}$	(varies)	150.39	138.69	0.23	0.20	0.32	18.00%

Table S7: Simulation Study Details

Type of simulated data	Inference models used
1. Varying R_0 and S_0 (orig.)	
(a) $R_0 \approx 1.1$, $S_0 = 499$, $\gamma = 0.25$, $\psi = 0.15$	Deter.Coal.SIR, Stoch.Coal.SIR, BDSIR
(b) $R_0 \approx 1.2$, $S_0 = 499$, $\gamma = 0.30$, $\psi = 0.15$	Deter.Coal.SIR
(c) $R_0 \approx 1.5$, $S_0 = 499$, $\gamma = 0.30$, $\psi = 0.15$	Deter.Coal.SIR, Stoch.Coal.SIR, BDSIR
(d) $R_0 \approx 1.5$, $S_0 = 999$, $\gamma = 0.30$, $\psi = 0.20$	Deter.Coal.SIR, Stoch.Coal.SIR, BDSIR
(e) $R_0 \approx 2.5$, $S_0 = 999$, $\gamma = 0.30$, $\psi = 0.05$	Deter.Coal.SIR, Stoch.Coal.SIR, BDSIR
2. Varying S_0 for fixed R_0	
(a) $R_0 \approx 1.1$, $S_0 = 499$, $\gamma = 0.25$, $\psi = 0.15$	Deter.Coal.SIR, Stoch.Coal.SIR, BDSIR
(f) $R_0 \approx 1.1$, $S_0 = 999$, $\gamma = 0.30$, $\psi = 0.20$	Deter.Coal.SIR
(g) $R_0 \approx 1.1$, $S_0 = 1999$, $\gamma = 0.30$, $\psi = 0.09$	Deter.Coal.SIR
3. Contemporaneous sampling	
(d) $R_0 \approx 1.5$, $S_0 = 999$, $\gamma = 0.30$, $\psi = 0.20$	Deter.Coal.SIR, Stoch.Coal.SIR, BDSIR
(e) $R_0 \approx 2.5$, $S_0 = 999$, $\gamma = 0.30$, $\psi = 0.05$	Deter.Coal.SIR, Stoch.Coal.SIR, BDSIR
4. Phylogenetic uncertainty	
(e) $R_0 \approx 2.5$, $S_0 = 999$, $\gamma = 0.30$, $\psi = 0.05$	Deter.Coal.SIR, Stoch.Coal.SIR, BDSIR
5. Reparameterization (growth rate)	
(e) $R_0 \approx 2.5$, $S_0 = 999$, $\gamma = 0.30$, $\psi = 0.05$	Deter.Coal.SIR

Table S8: Epidemic Parameter Estimations from HIV-1 Subtype B Sequence Data

Inference Model HIV cluster	R_0	γ	S_0	Root of the tree (yr)	Origin z_0 of the epidemic (yr)
Stoch. Coal. SIR					
Cluster 1	3.31 (2.40 - 4.26)	0.27 (8.17E-2 - 0.48)	1165 (448 - 1974)	1971 (1946-1987)	1969 (1942-1986)
Cluster 2	2.42 (1.86 - 3.07)	0.32 (7.72E-2 - 0.57)	976 (371 - 1701)	1975 (1953 - 1988)	1972 (1947 - 1988)
Cluster 3	2.10 (1.07 - 3.73)	0.41 (2.59E-2 - 0.86)	1442 (33 - 4568)	1979 (1959 - 1990)	1973 (1943 - 1989)
Cluster 4	3.48 (1.69 - 5.24)	0.28 (0.08 - 0.61)	1757 (148 - 5260)	1964 (1922 - 1990)	1961 (1918 - 1991)
Cluster 6	3.09 (1.94 - 4.53)	0.19 (3.72E-2 - 0.41)	727 (236 - 1312)	1972 (1950 - 1989)	1970 (1947 - 1988)
Deter. Coal. SIR					
Cluster 1	3.43 (2.52 - 4.40)	0.26 (6.95E-2 - 0.50)	1158 (397 - 2023)	1969 (1941-1987)	1967 (1939-1986)
Cluster 2	2.34 (1.92 - 2.81)	0.38 (0.13 - 0.66)	1163 (530 - 1895)	1979 (1967 - 1989)	1977 (1964 - 1987)
Cluster 3	1.87 (1.42 - 2.43)	0.54 (0.14 - 0.97)	1298 (399 - 2267)	1979 (1965 - 1989)	1975 (1960 - 1987)
Cluster 4	3.35 (2.02 - 4.86)	0.34 (8.22E-2 - 0.65)	1479 (397 - 2792)	1972 (1948 - 1990)	1971 (1946 - 1989)
Cluster 6	3.14 (1.98 - 4.64)	0.18 (2.99E-2 - 0.37)	693 (213 - 1241)	1971 (1949 - 1989)	1969 (1943 - 1988)
BDSIR					
Cluster 1	3.22 (2.18-4.27)	0.30 (0.15-0.47)	880 (142-3592)	1986 (1983-1988)	1983 (1978-1987)
Cluster 2	2.45 (1.53-3.68)	0.17 (0.06-0.35)	1745 (190-8892)	1983 (1979-1986)	1978 (1968-1984)
Cluster 3	1.90 (1.22-2.78)	0.20 (0.09-0.39)	1540 (153-8558)	1985 (1981-1988)	1978 (1962-1986)
Cluster 4	2.62 (1.45-4.29)	0.15 (0.06-0.31)	1921 (128-11007)	1987 (1983-1990)	1981 (1970-1988)
Cluster 6	3.17 (1.73-5.43)	0.15 (0.06-0.31)	2862 (183-16909)	1986 (1981-1989)	1983 (1975-1989)

Table S9: Deterministic Coalescent SIR Results from Trees Simulated with Higher S_0 (with Fixed R_0) and Higher R_0 (with Fixed S_0)

η	Truth	Mean	Median	Error	Bias	Relative HPD width	95% HPD accuracy
\mathcal{R}_0	2.50	2.68	2.49	0.13	0.04	0.81	98.00%
γ	0.30	0.32	0.29	0.16	3.14E-3	1.27	99.00%
$S_{(0)}$	999	1807	1133	0.52	0.29	4.59	98.00%
$z_{(0)}$	(varies)	41.17	39.99	0.03	0.01	0.07	76.00%
\mathcal{R}_0	2.50	3.28	2.97	0.23	0.20	1.42	100.00%
γ	0.35	0.30	0.28	0.24	-0.20	1.28	99.00%
$S_{(0)}$	4999	7733	4838	0.34	0.03	4.18	100.00%
$z_{(0)}$	(varies)	37.45	36.15	0.03	1.48e-3	0.06	56.00%
\mathcal{R}_0	2.50	3.76	3.05	0.26	0.23	1.50	100.00%
γ	0.40	0.33	0.31	0.26	-0.22	1.22	100.00%
$S_{(0)}$	9999	12,609	7405	0.35	-0.15	3.31	100.00%
$z_{(0)}$	(varies)	34.99	34.28	0.04	-1.94e-3	0.05	43.00%
η	Truth	Mean	Median	Error	Bias	Relative HPD width	95% HPD accuracy
\mathcal{R}_0	2.50	2.68	2.49	0.13	0.04	0.81	98.00%
γ	0.30	0.32	0.29	0.16	3.14E-3	1.27	99.00%
$S_{(0)}$	999	1807	1133	0.52	0.29	4.59	98.00%
$z_{(0)}$	(varies)	41.17	39.99	0.03	0.01	0.07	76.00%
\mathcal{R}_0	3.50	3.92	3.76	0.18	0.06	0.95	95.00%
γ	0.30	0.31	0.29	0.21	-0.01	1.16	99.00%
$S_{(0)}$	999	1909	1060	0.64	0.36	4.26	100.00%
$z_{(0)}$	(varies)	30.65	30.35	0.04	-6.35E-3	0.05	45.00%
\mathcal{R}_0	5.00	6.13	5.53	0.20	0.12	1.39	100.00%
γ	0.30	0.28	0.27	0.29	-0.09	1.18	100.00%
$S_{(0)}$	999	2144	1220	0.68	0.49	4.94	99.00%
$z_{(0)}$	(varies)	26.28	25.26	0.03	-0.01	0.03	52.00%
η	Truth	Mean	Median	Error	Bias	Relative HPD width	95% HPD accuracy
\mathcal{R}_0	5.00	7.20	6.37	0.27	0.23	2.53	100.00%
γ	0.30	0.26	0.22	0.26	-0.19	1.41	100.00%
$S_{(0)}$	9999	17,339	10,518	0.31	0.12	4.91	100.00%
$z_{(0)}$	(varies)	28.20	26.93	0.03	-0.01	1.05	36.00%