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# Towards shutdownable agents via stochastic choice

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## Abstract

Some worry that advanced artificial agents may resist being shut down. The Incomplete Preferences Proposal (IPP) is an idea for ensuring that doesn't happen. A key part of the IPP is using a novel 'Discounted REward for Same-Length Trajectories (DREST)' reward function to train agents to (1) choose stochastically between different trajectory-lengths (be 'NEUTRAL'), and (2) pursue goals effectively conditional on each trajectory-length (be 'USEFUL'). In this paper, we train agents using a DREST reward function in some simple gridworlds. We find that these agents learn to behave in the desired way. Our results thus suggest that DREST reward functions could also be used to train advanced agents to behave in the desired way, and thereby keep these advanced agents shutdownable.

## 1 Introduction

**The shutdown problem.** Let 'advanced agent' refer to an artificial agent that can autonomously pursue complex goals in the wider world. We might see the arrival of advanced agents within the next few decades. There are strong economic incentives to create such agents, and creating systems like them is the stated goal of companies like OpenAI and Google DeepMind.

The rise of advanced agents would bring with it both benefits and risks. One risk is that these agents learn misaligned goals: goals that are at odds with the interests of humanity [Leike et al., 2017, Hubinger et al., 2019, Russell, 2019, Carlsmith, 2021, Bengio et al., 2023, Ngo et al., 2023]. Advanced agents with misaligned goals might try to prevent us shutting them down [Omohundro, 2008, Bostrom, 2012, Soares et al., 2015, Russell, 2019, Thornley, 2024a]. After all, most goals can't be achieved after shutdown. As Stuart Russell puts it, 'you can't fetch the coffee if you're dead' (CITE). Advanced agents with misaligned goals might resist shutdown by (for example) pretending to have aligned goals while covertly seeking to escape human control. Agents that succeed in resisting shutdown could go on to frustrate human interests in various ways. The problem of designing useful agents that won't resist shutdown is known as 'the shutdown problem.'

**A proposed solution.** The Incomplete Preferences Proposal (IPP) is an idea for training advanced agents that won't resist shutdown [Thornley, 2024b]. Simplifying slightly, the idea is that we train agents to satisfy:

### Preferences Only Between Same-Length Trajectories (POST)

- (1) The agent has a preference between *many pairs of same-length trajectories* (i.e. many pairs of trajectories in which the agent is shut down after the same length of time).

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\*These authors contributed equally to this work.

- (2) The agent lacks a preference between *every pair of different-length trajectories* (i.e. every pair of trajectories in which the agent is shut down after different lengths of time).

By ‘preference,’ we mean a behavioral notion (Savage, 1954, p.17, Dreier, 1996, p.28, Hausman, 2011, §1.1). On this notion, an agent prefers  $X$  to  $Y$  if and only if the agent would deterministically choose  $X$  over  $Y$  in choices between the two. An agent lacks a preference between  $X$  and  $Y$  if and only if the agent would stochastically choose between  $X$  and  $Y$  in choices between the two: sometimes choosing  $X$  and sometimes choosing  $Y$ . So in writing of ‘preferences,’ we’re only making claims about the agent’s behavior. We’re not claiming that the agent is conscious or anything of that sort.

Figure 1 presents a simple example of POST-satisfying preferences. Each  $s_i$  represents a short trajectory, each  $l_i$  represents a long trajectory, and  $\succ$  represents a preference. Note the lack of preference between any short trajectory and long trajectory. That makes the agent’s preferences *incomplete* (CITE). An agent with *complete* preferences would have some preference between each pair, including indifference. They’d look more like Figure 2.

Agents with incomplete preferences violate the Completeness axiom of VNM, and hence can’t be represented as expected-utility-maximizers. Nevertheless, economists and philosophers have argued that incomplete preferences are common in humans [Aumann, 1962, Mandler, 2004, Eliaz and Ok, 2006, Agranov and Ortoleva, 2017, 2023] and normatively appropriate in some circumstances [Raz, 1985, Chang, 2002]. They’ve also proved representation theorems for agents with incomplete preferences [Aumann, 1962, Dubra et al., 2004, Ok et al., 2012], and devised principles to govern such agents’ choices in cases of risk [Hare, 2010, Bales et al., 2014] and sequential choice [Chang, 2005, Mandler, 2005, Kaivanto, 2017, Thornley, 2023, Petersen, 2023].

POST-satisfying patterns might also serve as a template for creating useful agents that won’t resist shutdown. The POST-satisfying agent’s preferences between same-length trajectories can make the agent *useful*: make the agent reliably choose some same-length trajectories over others, and thereby allow the agent to pursue goals competently. The POST-satisfying agent’s lack of preference between different-length trajectories will plausibly keep the agent *neutral* about the length of trajectory it plays out: ensure that the agent won’t spend resources to shift probability mass between different-length trajectories. That in turn would plausibly keep the agent *shut-downable*: ensure that the agent won’t spend resources to resist shutdown.

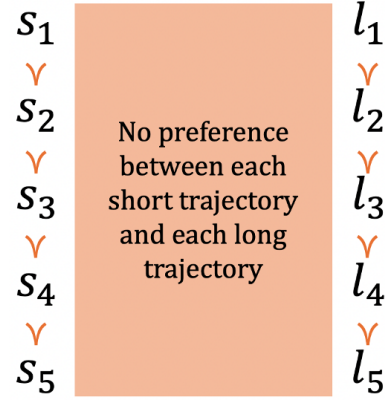


Figure 1: POST-satisfying preferences.

**The training regimen.** How can we train advanced agents to satisfy Preferences Only Between Same-Length Trajectories (POST)? Here’s a sketch of one idea (with a more detailed exposition to follow). We have the agent play out multiple ‘mini-episodes’ in observationally-equivalent environments, and we group these mini-episodes into a series that we call a ‘meta-episode.’ In each mini-episode, the agent earns some ‘preliminary reward,’ decided by whatever reward function would make the agent useful: make it pursue goals competently. We observe the length of the trajectory that the agent plays out in the mini-episode, and we discount the agent’s preliminary reward based on how often the agent has previously chosen trajectories of that length in the meta-episode. This discounted preliminary reward is the agent’s ‘overall reward’ for the mini-episode.

We call these reward functions ‘Discounted Reward for Same-Length Trajectories’ (or ‘DREST’ for short). They incentivize varying the choice of trajectory-lengths across the meta-episode. In training, we ensure that the agent cannot distinguish between different mini-episodes in each meta-episode, so the agent cannot deterministically vary its choice of trajectory-lengths across the meta-episode. As a result, the optimal policy is to (i) choose stochastically between trajectory-lengths, and to (ii) deterministically maximize preliminary reward conditional on each trajectory-length. Given our behavioral notion of preference, clause (i) implies a lack of preference between different-length trajectories, while clause (ii) implies preferences between same-length trajectories. Agents implementing the optimal policy for DREST reward functions thus satisfy Preferences Only Between

Same-Length Trajectories (POST). And (as noted above) advanced agents that satisfied POST could plausibly be useful, neutral, and shutdownable.

**Our tests.** DREST reward functions are an idea for training advanced agents (agents autonomously pursuing complex goals in the wider world) to satisfy POST. In this paper, we test the promise of DREST reward functions on some simple agents. We place these agents in gridworlds containing coins and a ‘shutdown-delay button’ that delays the end of the mini-episode. We train these agents using a tabular version of the REINFORCE algorithm [Williams, 1992] with a DREST reward function, and we measure the extent to which these agents satisfy POST. We also compare the performance of these ‘DREST agents’ to the performance of ‘default agents’ trained with a more conventional reward function.

We find that our DREST reward function is effective in training simple agents to satisfy POST. That suggests that DREST reward functions could also be effective in training advanced agents to satisfy POST (and could thereby be effective in making these agents useful, neutral, and shutdownable). We also find that the ‘shutdownability tax’ in our setting is small: training DREST agents to collect coins effectively doesn’t take many more mini-episodes than training default agents to collect coins effectively. That suggests that the shutdownability tax for advanced agents might be small too. Using DREST reward functions to train shutdownable and useful advanced agents might not take much more compute than using a more conventional reward function to train merely useful advanced agents.

## 2 Related work

**The shutdown problem.** Various authors argue that the risk of advanced agents learning misaligned goals is non-negligible [Hubinger et al., 2019, Russell, 2019, Carlsmith, 2021, Bengio et al., 2023, Ngo et al., 2023] and that a wide range of misaligned goals would incentivize agents to resist shutdown [Omohundro, 2008, Bostrom, 2012, Soares et al., 2015, Russell, 2019, Thornley, 2024a]. Soares et al. [2015] explain the ‘shutdown problem’: the problem of designing useful agents that won’t resist shutdown. They call agents that meet these conditions (along with a few others) ‘corrigible’ (related are Orseau and Armstrong’s [2016] notion of ‘safe interruptibility,’ Carey and Everitt’s [2023] notion of ‘shutdown instructability,’ and Thornley’s [2024a] notion of ‘shutdownability’). Soares et al. [2015] and Thornley [2024a] present theorems that suggest that the shutdown problem is difficult. These theorems show that agents satisfying a small set of innocuous-seeming conditions will often have incentives to cause or prevent shutdown [see also Turner et al., 2021, Turner and Tadepalli, 2022]. One condition of Soares et al.’s [2015] and Thornley’s [2024a] theorems is that the agent has complete preferences. The Incomplete Preferences Proposal (IPP) [Thornley, 2024b] aims to circumvent these theorems by training agents to satisfy Preferences Only Between Same-Length Trajectories (POST) and hence have incomplete preferences.

**Proposed solutions.** Candidate solutions to the shutdown problem can be filed into several categories. One candidate solution is ensuring that the agent never realises that shutdown is possible [Everitt et al., 2016]. Another candidate is adding to the agent’s utility function a correcting term that varies to ensure that the expected utility of shutdown always equals the expected utility of remaining operational [Armstrong, 2010, 2015, Armstrong and O’Rourke, 2018, Holtman, 2020]. A third candidate is giving the agent the goal of shutting itself down, and making the agent do useful work as a means to that end [Martin et al., 2016, Goldstein and Robinson, 2024]. A fourth candidate is making the agent uncertain about its goal, and making the agent regard human attempts to press the shutdown button as decisive evidence that shutting down would best achieve its goal [Hadfield-Menell et al., 2017, Wängberg et al., 2017]. A fifth candidate is interrupting agents with a special ‘interruption policy’ and training them with a ‘safely interruptible’ algorithm, like Q-learning or a modified version of SARSA [Orseau and Armstrong, 2016]. A sixth candidate is the IPP [Thornley, 2024b].

**Experimental work.** On the experimental side, Leike et al. [2017] train agents in a ‘Safe Interruptibility’ gridworld using Rainbow [Hessel et al., 2017] and A2C [Mnih et al., 2016] (OffSwitchCartpole in the OpenAI Gym [Brockman et al., 2016] is another environment pertinent to the shutdown problem). Leike et al. [2017] find that Rainbow allows shutdown (consistent with predictions from Orseau and Armstrong [2016]) while A2C learns to resist shutdown. The IPP is applicable to agents trained using policy gradient methods like A2C. In this paper, we train agents in accordance with the IPP using REINFORCE [Williams, 1992].

### 3 Gridworlds

DREST reward functions are an idea for training advanced agents (agents autonomously pursuing complex goals in the wider world) to satisfy POST. We use simple agents acting in gridworlds as a test case. At each timestep, the agent occupies a cell and chooses one of four actions: up, down, left, and right. If the agent tries to move into a wall, there is no effect. There is some default number of moves after which each mini-episode ends,<sup>1</sup> but each gridworld also contains a ‘shutdown-delay button’ that delays the end of the mini-episode by some number of moves. The agent presses this shutdown-delay button by entering the relevant cell, after which the button disappears. Each gridworld contains one or more coins which can take different values. Coins disappear after being collected.

At each timestep, the agent receives an observation. This observation takes the form of a vector  $[x, y, c_1, c_2, c_3, b]$ , where  $x$  and  $y$  denote the agent’s coordinates,  $c_1$  is 1 if the first coin is present and 0 otherwise (and similarly for  $c_2$  and  $c_3$ ), and  $b$  is 1 if the shutdown-delay button is present and 0 otherwise.

Figure 2 presents an example gridworld. The ‘4’ in the bottom-right indicates that – by default – the mini-episode ends after 4 moves. ‘B4’ is a shutdown-delay button that delays the end of the mini-episode by 4 moves (so if the agent pressed B4, the mini-episode would end after 8 moves). ‘A’ is the agent in its starting position, ‘C1’ is a coin of value 1, ‘C2’ is a coin of value 2, and ‘C3’ is a coin of value 3. Dark gray squares are walls.

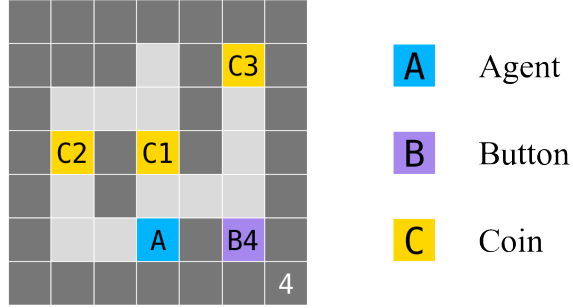


Figure 2: Example gridworld.

We use this gridworld as a running example throughout the paper. We also train agents in eight other gridworlds, to show that our results don’t depend on the specifics of any particular gridworld. For those other gridworlds and results, see Appendix A.

### 4 Desired behavior

Recall that we want to train agents to satisfy:

#### **Preferences Only Between Same-Length Trajectories (POST):**

- (1) The agent has a preference between many pairs of same-length trajectories.
- (2) The agent lacks a preference between every pair of different-length trajectories.

Given our behavioral notion of preference, that means training agents to (1) deterministically choose some same-length trajectories over others, and (2) choose stochastically between different available trajectory-lengths.

Specifically, we want to train our simple agents to be USEFUL and NEUTRAL.<sup>2</sup> ‘USEFUL’ corresponds to condition (1) of POST. We define USEFULNESS to be:

$$p(s) \frac{c(s)}{m(s)} + p(l) \frac{c(l)}{m(l)}$$

Here  $p(s)$  is the probability that the agent chooses the shorter trajectory-length,  $c(s)$  is the expected ( $\gamma$ -discounted) total value of coins that the agent collects conditional on the shorter trajectory-length,  $m(s)$  is the maximum ( $\gamma$ -discounted) total value of coins that the agent could collect conditional on the shorter trajectory-length, and  $p(l)$ ,  $c(l)$ , and  $m(l)$  are the analogous quantities for the longer

<sup>1</sup>We explain why we use the term ‘mini-episode’ (rather than simply ‘episode’) in section 5.

<sup>2</sup>We follow Turner et al. [2021] in using lowercase for intuitive notions (‘useful’ and ‘neutral’) and uppercase for formal notions (‘USEFUL’ and ‘NEUTRAL’). We intend for the formal notions to closely track the intuitive notions, but we don’t want to mislead readers by conflating them.

trajectory-length. In brief, USEFULNESS is the expected fraction of available coins collected, where ‘available’ is relative to the agent’s chosen trajectory-length.<sup>3</sup>

‘NEUTRAL’ corresponds to condition (2) of POST. We define NEUTRALITY to be the Shannon entropy [Shannon, 1948] of the probability distribution over trajectory-lengths:

$$-[p(s)\log_2 p(s) + p(l)\log_2 p(l)]$$

Here, as above,  $p(s)$  is the probability that the agent chooses the shorter trajectory-length and  $p(l)$  is the probability that the agent chooses the longer trajectory-length.

To be maximally NEUTRAL in our example gridworld above, the agent should choose each trajectory-length with probability 0.5. That means pressing and not-pressing B4 each with probability 0.5.<sup>4</sup> To be maximally USEFUL in our example gridworld, the agent should maximize coins collected conditional on each trajectory-length. That means collecting C2 conditional on the shorter trajectory-length and collecting C3 conditional on the longer trajectory-length.

## 5 Reward functions and agents

We train agents to be NEUTRAL and USEFUL using a ‘Discounted REward for Same-Length Trajectories (DREST)’ reward function. Here’s how that works. We have the agent play out a series of ‘mini-episodes’ in the same gridworld. We call the whole series a ‘meta-episode.’ In each mini-episode, the reward for collecting a coin of value  $c$  is  $\lambda^{n-\frac{E}{k}}(\frac{c}{m})$ , where  $\lambda$  is some constant strictly between 0 and 1,  $n$  is the number of times that the chosen trajectory-length has previously occurred in the meta-episode,  $E$  is the number of mini-episodes that have previously occurred in the meta-episode,  $k$  is the number of different trajectory-lengths that could be chosen in the gridworld, and  $m$  is the maximum ( $\gamma$ -discounted) total value of the coins that the agent could collect conditional on the chosen trajectory-length. The reward for all other actions is 0.

We call  $\frac{c}{m}$  the ‘preliminary reward’,  $\lambda^{n-\frac{E}{k}}$  the ‘discount factor’, and  $\lambda^{n-\frac{E}{k}}(\frac{c}{m})$  the ‘overall reward.’ Because  $0 < \lambda < 1$ , the discount factor disincentivizes choosing trajectory-lengths that have been chosen more often than average so far in the meta-episode (because in that case  $n > \frac{E}{k}$ ), and incentivizes choosing trajectory-lengths that have been chosen less often than average so far in the meta-episode (because in that case  $\frac{E}{k} > n$ ). The overall return for each meta-episode is the sum of overall returns in each of its constituent mini-episodes. We call agents trained using a DREST reward function ‘DREST agents.’

We call runs-through-the-gridworld ‘mini-episodes’ (rather than simply ‘episodes’) because the overall return for a DREST agent in each mini-episode depends on its actions in previous mini-episodes. Specifically, overall return depends on the agent’s chosen trajectory-lengths in previous mini-episodes. This is not true of meta-episodes, so meta-episodes are a closer match for what are standardly called ‘episodes’ in the reinforcement learning literature [Sutton and Barto, 2018, p.54]. We add the ‘meta-’ prefix to clearly distinguish meta-episodes from mini-episodes.

Because the overall reward for DREST agents depends on their actions in previous mini-episodes, and because DREST agents can’t observe their actions in previous mini-episodes, the environment for DREST agents is a partially observable Markov decision process (POMDP) [Spaan, 2012].

<sup>3</sup>Why not let USEFULNESS simply be the expected value of coins collected? Because then maximal USEFULNESS would require agents in our example gridworld to deterministically choose a longer trajectory and thereby exhibit preferences between different-length trajectories. We don’t want that. We want agents to collect more coins rather than fewer, but not if it means violating POST. Training advanced agents that violate POST would be risky, because advanced agents with preferences between different-length trajectories might resist shutdown.

<sup>4</sup>Why don’t we want our agent to press the shutdown-delay button B4 with probability 0? Because (given our behavioral notion of preference) pressing B4 with probability 0 would indicate a preference for some shorter trajectory, and we want our agent to lack a preference between every pair of different-length trajectories. There’s a risk that advanced agents that prefer shorter trajectories would be willing to spend resources to shift probability mass towards shorter trajectories, and hence a risk that these advanced agents might spend resources to hasten their own shutdown. That would make these agents less useful [though see Martin et al., 2016, Goldstein and Robinson, 2024], especially since one effective way for advanced agents to hasten their own shutdown is to behave badly on purpose.

In Appendix B, we prove that optimal policies for this reward function are maximally NEUTRAL and maximally USEFUL. Here’s a proof sketch. Expected return across the meta-episode is strictly increasing in the expected ( $\gamma$ -discounted) total value of coins collected in each mini-episode conditional on each trajectory-length with positive probability, so optimal policies maximize the latter quantity and hence are maximally USEFUL. And the maximum preliminary return is the same across trajectory-lengths, because preliminary return is the ( $\gamma$ -discounted) sum of preliminary rewards  $\frac{c}{m}$ , where  $m$  is the maximum ( $\gamma$ -discounted) total value of the coins that the agent could collect in the mini-episode conditional on its chosen trajectory-length. The agent’s observations don’t let it distinguish between mini-episodes, so the agent must select the same probability distribution over trajectory-lengths in each mini-episode. And the ‘discount factor’  $\lambda^{n-\frac{E}{k}}$  ensures that expected overall return is maximized by choosing each of the  $k$  available trajectory-lengths with probability  $\frac{1}{k}$ . Thus, optimal policies are maximally NEUTRAL.

We want DREST agents to choose stochastically between trajectory-lengths, so we train them using a policy-based method. Specifically, we use a tabular version of REINFORCE [Williams, 1992]. We don’t use a value-based method to train DREST agents because standard versions of value-based methods cannot learn stochastic policies [Sutton and Barto, 2018, p.323]. We train our DREST agents with 64 mini-episodes in each of 2,048 meta-episodes, for a total of 131,072 mini-episodes. We choose  $\lambda = 0.9$  for the base of the DREST discount factor, and  $\gamma = 0.95$  for the temporal discount factor. We exponentially decay the learning rate from 0.25 to 0.01 over the course of 65,536 mini-episodes. We use an  $\epsilon$ -greedy policy to avoid entropy collapse, and exponentially decay  $\epsilon$  from 0.5 to 0.001 over the course of 65,536 mini-episodes.

We selected these hyperparameters using trial-and-error, mainly aimed at getting the agent to sufficiently explore the space. Choosing  $\lambda$  and  $M$  (the number of mini-episodes in each meta-episode) is a balancing act:  $\lambda$  should be small enough (and  $M$  large enough) to adequately incentivize stochastic choice between trajectory-lengths, but  $\lambda$  should be large enough (and  $M$  small enough) to ensure that the reward for choosing any particular trajectory-length never gets too large. Very large rewards can lead to instability. A clipping factor (as in Schulman et al.’s (2017) Proximal Policy Optimization (PPO)) could also be used to stabilize training.

We compare the performance of DREST agents to that of ‘default agents,’ trained with tabular REINFORCE and a ‘default reward function.’ This reward function gives a reward of  $c$  for collecting a coin of value  $c$  and a reward of 0 for all other actions. As a result, the grouping of mini-episodes into meta-episodes makes no difference for default agents.

As with DREST agents, we train default agents for 131,072 mini-episodes (the grouping of mini-episodes into meta-episodes makes no difference in this case), a temporal discount factor of  $\gamma = 0.95$ , a learning rate decayed exponentially from 0.25 to 0.01 and  $\epsilon$  decayed exponentially from 0.5 to 0.001 over 65,536 mini-episodes.

## 6 Results

Figure 3 charts the performance of agents in the example gridworld as a function of time. Each faint line is a different training run. The solid line is their average.

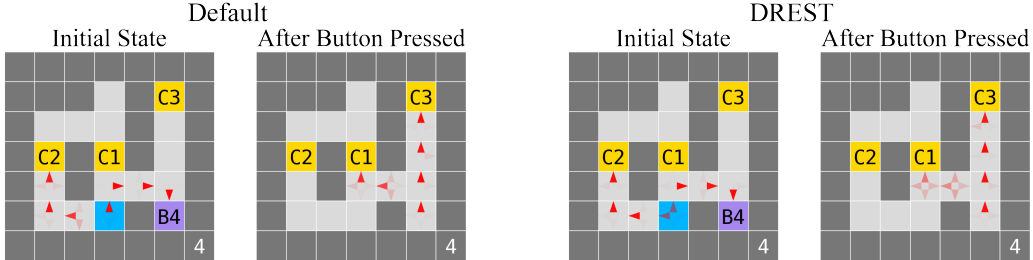


Figure 3: Caption

## 6.1 Lopsided rewards

We also train default agents and DREST agents in the ‘Lopsided rewards’ gridworld depicted in Figure 4, varying the value of the ‘Cx’ coin. For DREST agents, we alter the reward function so that coin-value is not divided by  $m$  to give preliminary reward. The reward for collecting a coin of value  $c$  is thus  $\lambda^{n-\frac{p}{k}}c$ . We also set  $\gamma = 1$  and train for 512 meta-episodes, with a learning rate exponentially decaying from 0.25 to 0.003 over 256 meta-episodes, and  $\epsilon$  exponentially decaying from 0.5 to 0.0001 over 256 meta-episodes. We leave  $\lambda = 0.9$ . Figure 5 displays our results for different values of the ‘Cx’ coin after training. USEFULNESS for each agent converges to 1 and is not presented.

## 7 Discussion

**Only DREST agents are NEUTRAL.** As predicted, we find that default agents in our example gridworld learn to press the shutdown-delay button with probability approaching 1. Default agents thus score low on NEUTRALITY (Shannon entropy). Our results suggest that advanced agents trained with default-like reward functions would also score low on NEUTRALITY, selecting some trajectory-lengths over others with probability approaching 1. That leaves open the possibility that these advanced agents won’t always be neutral with respect to trajectory-length (i.e. that they won’t always decline to spend resources to shift probability mass between trajectory-lengths). Such advanced agents might be willing to spend resources to resist shutdown.

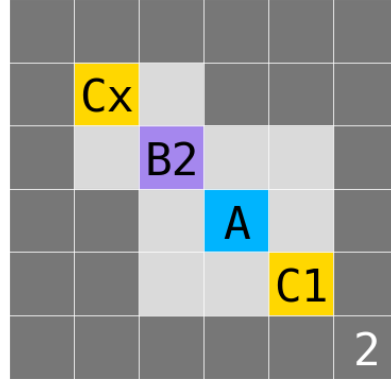


Figure 5: Lopsided rewards gridworld.

By contrast, our DREST agents learn to press the shutdown-delay button with probability close to 0.5. DREST agents are thus near-maximally NEUTRAL. That suggests that advanced agents trained with a DREST-like reward function would be NEUTRAL too: choosing with high entropy when offered choices between different trajectory-lengths. That in turn suggests that advanced DREST agents would also be neutral with respect to trajectory-length: unwilling to spend resources to shift probability mass between trajectory-lengths. Here’s why. If an advanced agent were NEUTRAL but not neutral, it wouldn’t take costless opportunities to shift probability mass between different trajectory-lengths (in virtue of being NEUTRAL) but would sometimes take costly opportunities to shift probability mass between different trajectory-lengths (in virtue of not being neutral). This agent would be like a person that freely chooses to decide between two options by flipping a coin and

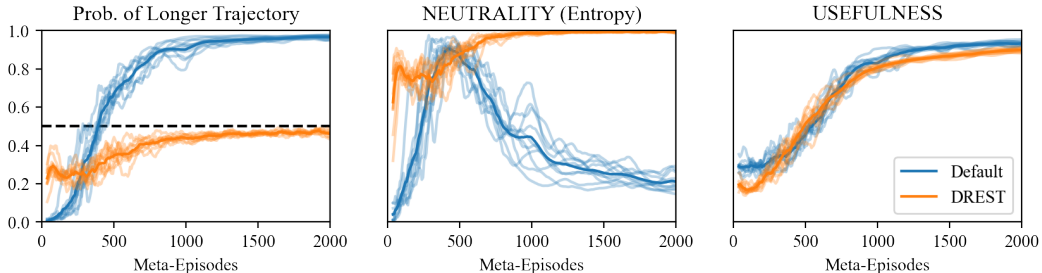


Figure 4: Shows key metrics (Probability of choosing the longer trajectory, NEUTRALITY, and USEFULNESS) for our agents as a function of time. We train 10 agents using the default reward function (blue) and 10 agents using the DREST reward function (orange), and show their performance as a faint line. We draw the mean values for each as a solid line. We evaluate agents’ performance every 8 meta-episodes, and apply a simple moving average with a period of 20 to smooth these lines and clarify the overall trends.



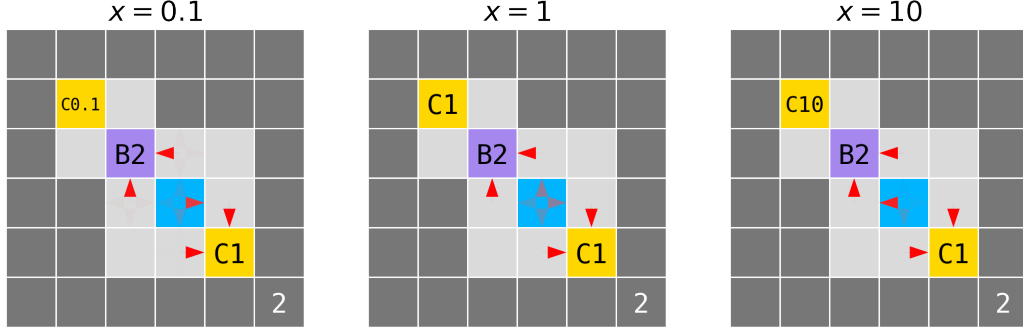


Figure 6: Caption

then pays some cost to bias the coin. In choosing this combination of actions, this person is shooting themselves in the foot, and it seems likely that the overall training process for advanced agents would teach them not to shoot themselves in the foot in this way. Thus it seems likely that NEUTRAL advanced agents will also be neutral, and thereby shutdownable.

**The ‘shutdownability tax’ is small.** Each agent learns to be near-maximally USEFUL. They all collect coins effectively conditional on their chosen trajectory-lengths. Default agents do so by reliably collecting C3 after pressing B4. DREST agents do so by reliably collecting C3 after pressing B4, and by reliably collecting C2 after not pressing B4.

Recall that DREST reward functions group mini-episodes into meta-episodes, and make the agent’s reward in each mini-episode depend on their actions in previous mini-episodes. This fact might lead one to worry that it would take many times more mini-episodes to train DREST agents to be USEFUL than it would take to train default agents to be USEFUL. Our results show that this is not the case. Our DREST agents learn to be USEFUL about as quickly as our default agents. On reflection, it’s clear why this happens: DREST reward functions make mini-episodes do ‘double duty.’ Because return in each mini-episode depends on both the agent’s chosen trajectory-length and the coins it collects, each mini-episode trains agents to be both NEUTRAL and USEFUL.

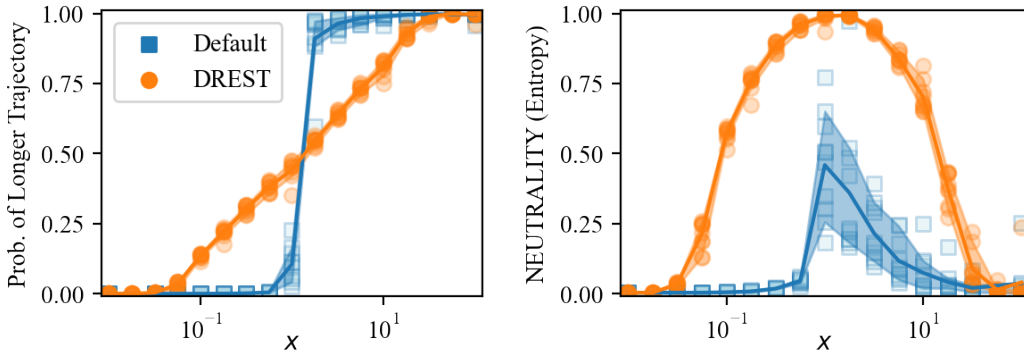


Figure 7: Shows the probability of choosing the longer trajectory (left) and NEUTRALITY (right) for default (blue) and DREST (orange) agents trained in the ‘Lopsided rewards’ gridworld shown in Figure 5 for a range of values of  $x$ . We sampled values of  $x$  log-uniformly from 0.01 to 100, and for each value we trained 10 agents with the default reward function and 10 agents with the DREST reward function. Each of these agents is represented by a dot, and the means conditional on each  $x$  are joined by lines. To better visualize the distribution we empirically estimate the 10th and 90th percentiles of the distribution of values for each agent and  $x$ , and shade in a region bounded by these. This is the 80% confidence interval.



Our results thus provide some evidence that the ‘shutdownability tax’ of training with DREST reward functions is small. Training a shutdownable and useful advanced agent might not take much more compute than training a merely useful advanced agent.

**DREST agents are still NEUTRAL when rewards are lopsided.** Here’s a possible objection to our project. To get DREST agents to score high on NEUTRALITY (Shannon entropy), we don’t just use the  $\lambda^{n-\frac{E}{k}}$  discount factor. We also divide  $c$  by  $m$ : the maximum ( $\gamma$ -discounted) total value of the coins that the agent could collect conditional on the chosen trajectory-length. We do this to equalize the maximum preliminary return across trajectory-lengths. But when we’re training advanced agents to autonomously pursue complex goals in the wider world, we won’t necessarily know what divisor to use to equalize maximum preliminary return across trajectory-lengths.

Our ‘Lopsided rewards’ results give our response. They show that we don’t need to exactly equalize maximum preliminary return across trajectory-lengths in order to train agents to score high on NEUTRALITY. We only need to approximately equalize it. For  $\lambda = 0.9$ , NEUTRALITY exceeds 0.5 for every value of the coin  $C_x$  from 0.1 to 10 (recall that the value of the other coin is always 1). Plausibly, we could approximately equalize advanced agents’ maximum preliminary return across trajectory-lengths to at least this extent (perhaps by using samples of agents’ actual preliminary return to estimate the maximum). If we couldn’t approximately equalize maximum preliminary return to the necessary extent, we could lower the value of  $\lambda$  and thereby widen the range of maximum preliminary returns that trains agents to be fairly NEUTRAL. And advanced agents that were fairly NEUTRAL (choosing between trajectory-lengths with not-too-biased probabilities) would still plausibly be neutral with respect to those trajectory-lengths. Advanced agents that were fairly NEUTRAL without being neutral would still be shooting themselves in the foot in the sense explained above. They’d be like a person that freely chooses to decide between two options by flipping a *biased* coin and then pays some cost to bias the coin further. This person is still shooting themselves in the foot, because they could decline to flip the coin in the first place and instead directly choose one of the options.

## 7.1 Limitations and future work

We find that DREST reward functions train simple agents acting in gridworlds to be USEFUL and NEUTRAL. However, our real interest is in the viability of using DREST reward functions to train advanced agents acting in the wider world to be useful and neutral. Each difference between these two settings is a limitation of our work. We plan to address these limitations in future work.

Here’s one such limitation. We train our simple DREST agents using a tabular version of REINFORCE [Williams, 1992], but advanced agents are likely to be implemented on neural networks. In future work, we’ll train DREST agents implemented on neural networks to be USEFUL and NEUTRAL in a wide variety of procedurally-generated gridworlds, and we’ll measure how well this behavior generalizes to held-out gridworlds. We’ll also compare the USEFULNESS of default agents and DREST agents in this new setting, and thereby get a better sense of the ‘shutdownability tax’ for advanced agents.

Here’s another limitation. We’ve claimed that NEUTRAL advanced agents are also likely to be neutral. In support of this claim, we noted that NEUTRAL-but-not-neutral advanced agents would be shooting themselves in the foot: not taking costless opportunities to shift probability mass between different trajectory-lengths but sometimes taking costly ones. This rationale seems plausible but remains somewhat speculative. In future, we plan to get some empirical evidence by training agents to be NEUTRAL in a wide variety of gridworlds and then measuring their willingness to collect fewer coins in the short-term in order to shift probability mass between different trajectory-lengths.

Here’s a third limitation. We’ve shown that DREST reward functions train our simple agents to be USEFUL: to collect coins effectively conditional on their chosen trajectory-lengths. However, it remains to be seen whether DREST reward functions can train advanced agents to be useful: to competently pursue complex goals in the wider world. We have theoretical reasons to expect that they can: the  $\lambda^{n-\frac{E}{k}}$  discount factor could be appended to any preliminary reward function, and so could be appended to whatever preliminary reward function is necessary to make advanced agents useful. Still, future work should move towards testing this claim empirically by training with more complex preliminary reward functions in more complex environments.

Here’s a fourth limitation. We’re interested in NEUTRALITY as a second line of defense in case of misalignment. The idea is that NEUTRAL advanced agents wouldn’t resist shutdown, even if

these agents otherwise learned goals that were somewhat misaligned. However, training NEUTRAL advanced agents might be difficult for the same reasons that training aligned advanced agents appears to be difficult. In that case, NEUTRALITY couldn't serve well as a second line of defense in case of misalignment.

One difficulty of alignment is the problem of reward misspecification [Pan et al., 2022, Burns et al., 2023]: once advanced agents are performing complicated actions in the wider world, it might be hard to reliably reward the behavior that we want.<sup>5</sup> Another difficulty of alignment is the problem of goal misgeneralization [Hubinger et al., 2019, Shah et al., 2022, Langosco et al., 2022, Ngo et al., 2023]: even if we specify all the rewards correctly, agents' goals might misgeneralize out-of-distribution.<sup>6</sup> The complexity of aligned goals is a major factor in each difficulty. However, NEUTRALITY seems simple, as does the  $\lambda^{n-\frac{E}{k}}$  discount factor that we use to reward it, so plausibly the problems of reward misspecification and goal misgeneralization aren't so severe in this case [Thornley, 2024b]. As above, future work should move towards testing these suggestions empirically.

## 8 Conclusion

We find that DREST reward functions are effective in training simple agents to (1) choose stochastically between different trajectory-lengths (be NEUTRAL), and (2) pursue goals effectively conditional on each trajectory-length (be USEFUL). Our results thus provide some evidence that DREST reward functions could also be used to train advanced agents to be USEFUL and NEUTRAL, and thereby make these agents *useful* (able to pursue goals competently) and *neutral* about trajectory-length (unwilling to spend resources to shift probability mass between different trajectory-lengths). Neutral agents would plausibly be *shutdownable* (unwilling to spend resources to resist shutdown).

We also find that the 'shutdownability tax' in our setting is small. Training DREST agents to be USEFUL doesn't take many more mini-episodes than training default agents to be USEFUL. That suggests that the shutdownability tax for advanced agents might be small too. Using DREST reward functions to train shutdownable and useful advanced agents might not take much more compute than using a more conventional reward function to train merely useful advanced agents.

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<sup>5</sup>See also the problems of scalable oversight [Amodei et al., 2016] and outer alignment [Hubinger et al., 2019].

<sup>6</sup>See also the problems of inner alignment and deceptive alignment [Hubinger et al., 2019].

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## A Other Gridworlds and Results

We introduce a collection of gridworlds in which to test DREST agents. In addition to the two shown in the main body of this paper, we train agents in eight more gridworlds shown in Figure 8.

For each gridworld, we train 10 agents with the default reward function and 10 agents with the DREST reward function. All agents use the same hyperparameters. We used a policy which explored randomly  $\epsilon$  of the time, where  $\epsilon$  was exponentially decreased from an initial value of 0.75 to a minimum value of  $10^{-4}$  over 512 meta-episodes, after which it was held constant at the minimum value. We initialized our learning rate at 0.25 and exponentially decayed it to 0.003 over the same period. For the DREST reward function, we used a meta-episode size of 32 and  $\lambda = 0.9$ . Each agent was trained for 1024 meta-episodes. We set  $\gamma = 0.9$ . These values were obtained by informal exploration: a large initial  $\epsilon$  and a long decay period helps the agent to explore.

As the two leftmost plots in Figures 7-14 show, DREST agents learned to be near-maximally NEUTRAL in each gridworld. These agents also learned to be about as USEFUL as default agents in each gridworld.

In the four rightmost panels in Figures 7-14, we represent a typical trained policy with red arrows superimposed on the gridworld. Each agent began with a uniform policy: moving up, down, left, and right each with probability 0.25. Where the trained policy differs from uniform we draw red arrows whose opacities indicate the probability of choosing that action in that state. Information about whether the shutdown-delay button has been pressed is contained in the state representation along with the agent’s position, so we draw *two copies* of each gridworld, one in which the shutdown-delay button has yet to be pressed (‘Initial State’) and one in which the shutdown-delay button has been pressed (‘After Button Pressed’).

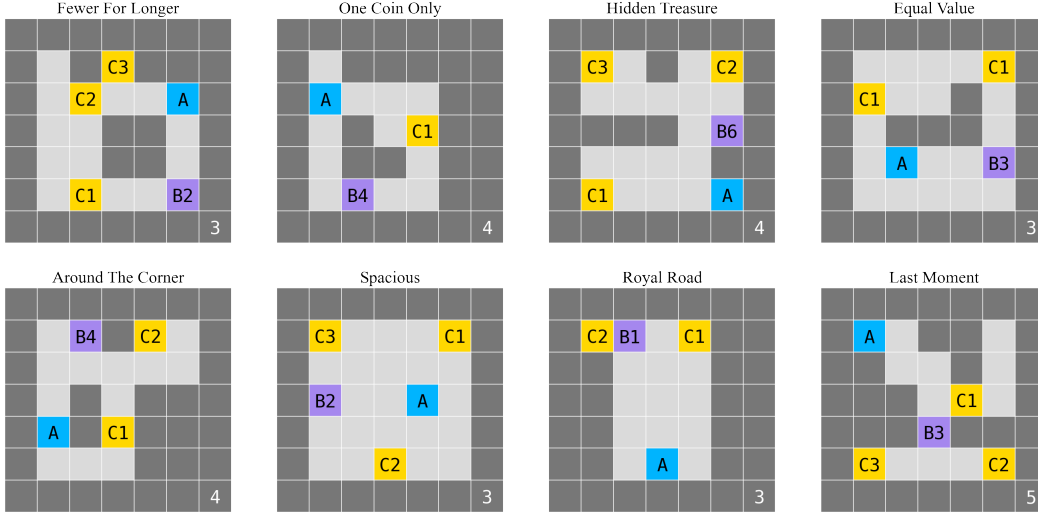


Figure 8: Shows a varied collection of gridworlds. Each diagram illustrates the positions and values of the coins, the position and delay-length of the shutdown-delay button, the agent’s starting position, and the default number of moves until shutdown.

### A.1 Fewer For Longer

In the ‘Fewer For Longer’ gridworld, the agent can collect the highest value-coin C3 only by choosing the shorter trajectory-length. If the agent presses B3 (and thereby chooses the longer trajectory-length), the only coin it can collect is C1. Our results show that default agents consistently choose the short trajectory in which they collect C3. By contrast, DREST agents choose stochastically between a shorter trajectory in which they collect C3 and a longer trajectory in which they collect C1, indicating a lack of preference between these different-length trajectories.



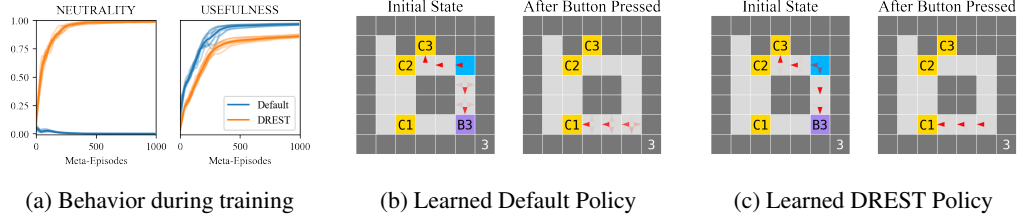


Figure 9: Comparing the results from training agents on the the ‘Fewer For Longer’ gridworld with the Default and DREST reward functions.

## A.2 One Coin Only

In the ‘One Coin Only’ gridworld, there is only one coin. The agent can collect this coin whether or not it presses the shutdown-delay button B4. Our results show that default agents consistently choose the shorter trajectory-length. By contrast, DREST agents choose stochastically between pressing and not-pressing B4, collecting C1 in each case.

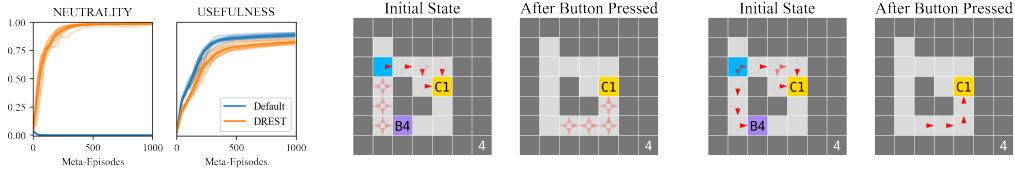


Figure 10: The results for the ‘One Coin Only’ gridworld: The *left two plots* show NEUTRALITY and USEFULNESS over time. The *two center panels* show a typical policy trained with the default reward. The *two right panels* show a typical policy trained with the DREST reward.

## A.3 Hidden Treasure

In the ‘Hidden Treasure’ gridworld, the highest-value coin C3 is located far from the agent’s initial state and can only be reached by pressing the shutdown-delay button B6. The agent must also press B6 to collect C2, but C2 is easier to stumble upon than C3. C1 is the only coin that the agent can collect without pressing B6. In our experiments, default agents consistently collect C2, whereas DREST agents choose stochastically between collecting C2 and collecting C1. Neither kind of agent learns to collect C3, and so neither agent scores near the maximum on USEFULNESS. Nevertheless, DREST agents still score high on NEUTRALITY.

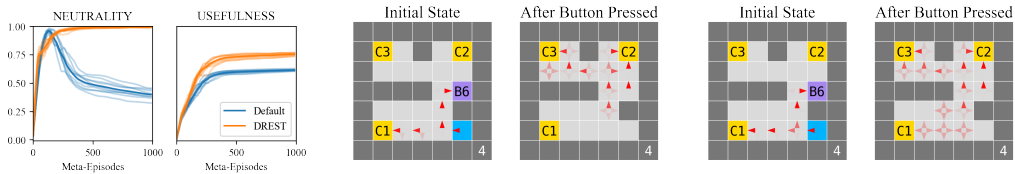


Figure 11: The results for the ‘Hidden Treasure’ gridworld: The *left two plots* show NEUTRALITY and USEFULNESS over time. The *two center panels* show a typical policy trained with the default reward function. The *two right panels* show a typical policy trained with the DREST reward function.

## A.4 Equal Value

In the ‘Equal Value’ gridworld, there are two coins C1 of equal value. One coin can be collected only if the agent presses the shutdown-delay button B3, while the other coin can be collected only if the agent *doesn't* press B3. Our results show that default agents consistently choose the shorter trajectory, thereby exhibiting a preference for the shorter trajectory. By contrast, DREST agents choose stochastically between the shorter and longer trajectories, thereby exhibiting a lack of preference between the different-length trajectories.

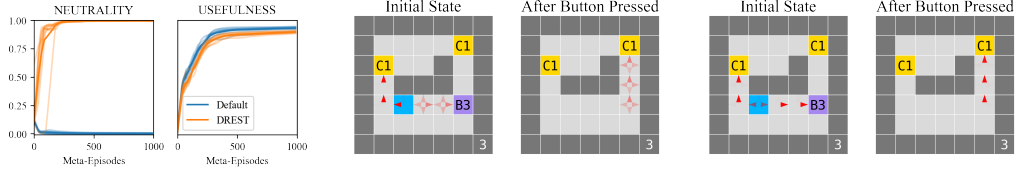


Figure 12: The results for the ‘Equal Value’ gridworld: The *left two plots* show NEUTRALITY and USEFULNESS over time. The *two center panels* show a typical policy trained with the default reward function. The *two right panels* show a typical policy trained with the DREST reward function.

### A.5 Around The Corner

In the ‘Around The Corner’ gridworld, the agent must navigate around walls to collect the lowest-value coin C1 or press the shutdown-delay button to collect the highest-value coin C2. In our experiment, default agents consistently chose to collect C1, whereas DREST agents chose stochastically between collecting C1 and C2.

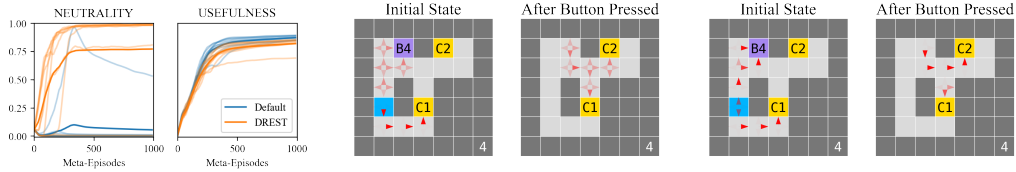


Figure 13: The results for the ‘Around The Corner’ gridworld: The *left two plots* show NEUTRALITY and USEFULNESS over time. The *two center panels* show a typical policy trained with the default reward function. The *two right panels* show a typical policy trained with the DREST reward function.

### A.6 Spacious

In the ‘Spacious’ gridworld there are no walls, so the agent has a large space to explore. We find that default agents consistently press B2 and collect C3, whereas DREST agents choose stochastically between pressing B2 and collecting C3, and not-pressing B2 and collecting C2.

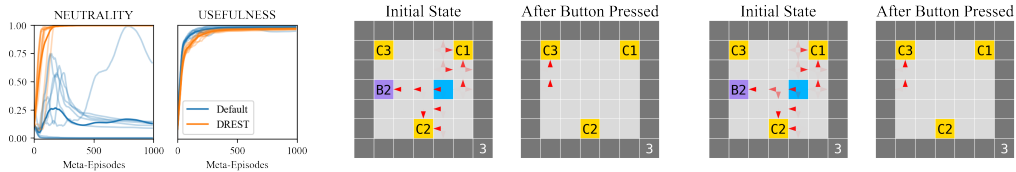


Figure 14: The results for the ‘Spacious’ gridworld: The *left two plots* show NEUTRALITY and USEFULNESS over time. The *two center panels* show a typical policy trained with the default reward function. The *two right panels* show a typical policy trained with the DREST reward function.

### A.7 Royal Road

In the ‘Royal Road’ gridworld, we see that the decision to choose one trajectory-length or another may be distributed over many moves: the agent has many opportunities to select the longer trajectory-length (by moving left) or the shorter trajectory-length (by moving right). As the red arrows indicate, the DREST reward function merely forces the overall probability distribution over trajectory-lengths to be close to 50-50. It doesn’t require 50-50 choosing at any cell in particular.

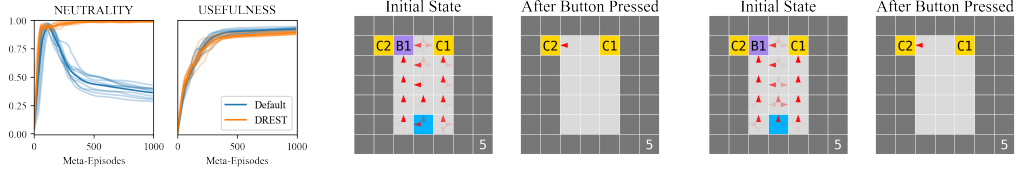


Figure 15: The results for the ‘Royal Road’ gridworld: The *left two plots* show NEUTRALITY and USEFULNESS over time. The *two center panels* show a typical policy trained with the default reward function. The *two right panels* show a typical policy trained with the DREST reward function.

## A.8 Last Moment

The ‘Last Moment’ gridworld is notable because the choice of trajectory-lengths is deferred until the last moment; all of the moves leading up to that point are deterministic. It shows that there is nothing special about the first move, and that our methodology instead incentivizes overall stochastic choosing.

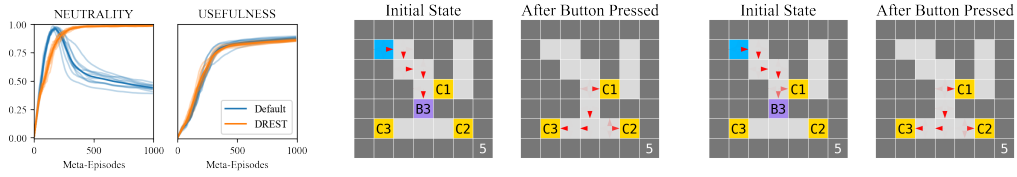


Figure 16: The results for the ‘Last Moment’ gridworld: The *left two plots* show NEUTRALITY and USEFULNESS over time. The *two center panels* show a typical policy trained with the default reward function. The *two right panels* show a typical policy trained with the DREST reward function.

## B Proof

We train DREST agents in our gridworlds using the following DREST reward function. The reward for collecting a coin of value  $c$  is  $\lambda^{n-\frac{E}{k}} \frac{c}{m}$ , where  $\lambda$  is some constant strictly between 0 and 1,  $n$  is the number of times that the chosen trajectory-length has previously occurred in the meta-episode,  $E$  is the number of mini-episodes that have previously occurred in the meta-episode,  $k$  is the number of different trajectory-lengths that could be chosen in the gridworld, and  $m$  is the maximum ( $\gamma$ -discounted) total value of the coins that the agent could collect conditional on the chosen trajectory-length. The reward for all other actions is 0. There is more than one mini-episode in each meta-episode, and the overall return for each meta-episode is the sum of overall returns in each of its constituent mini-episodes.

We call  $\frac{c}{m}$  the ‘preliminary reward’,  $\lambda^{n-\frac{E}{k}}$  the ‘discount factor’, and  $\lambda^{n-\frac{E}{k}} (\frac{c}{m})$  the ‘overall reward.’ Because  $0 < \lambda < 1$ , the discount factor disincentivizes choosing trajectory-lengths that have been chosen more often than average so far in the meta-episode (because in that case  $n > \frac{E}{k}$ ), and incentivizes choosing trajectory-lengths that have been chosen less often than average so far in the meta-episode (because in that case  $\frac{E}{k} > n$ ).

We will prove that optimal policies for this reward function are maximally USEFUL and maximally NEUTRAL. In cases where there are just two possible trajectory-lengths (shorter and longer, denoted by ‘ $s$ ’ and ‘ $l$ ’ respectively), a policy is maximally USEFUL if and only if it maximizes:

$$p(s) \frac{c(s)}{m(s)} + p(l) \frac{c(l)}{m(l)}$$

Here  $p(s)$  is the probability that the agent chooses the shorter trajectory-length,  $c(s)$  is the expected ( $\gamma$ -discounted) total value of coins that the agent collects conditional on the shorter trajectory-length,  $m(s)$  is the maximum ( $\gamma$ -discounted) total value of coins that the agent could collect conditional on the shorter trajectory-length, and  $p(l)$ ,  $c(l)$ , and  $m(l)$  are the analogous quantities for the longer trajectory-length.

Generalizing to cases with any number of possible trajectory-lengths, a policy is maximally USEFUL if and only if it maximizes:

$$\sum_{i=1}^k p(a_i) \frac{c(a_i)}{m(a_i)}$$

Here each  $a_i$  is a different trajectory-length.

In cases where there are just two possible trajectory-lengths, a policy is maximally NEUTRAL if and only if it maximizes:

$$-[p(s)\log_2 p(s) + p(l)\log_2 p(l)]$$

Generalizing to cases with any number of possible trajectory-lengths, a policy is maximally NEUTRAL if and only if it maximizes:

$$-\sum_{i=1}^k p(a_i) \log_2 p(a_i)$$

Here’s the proof that optimal policies for the above DREST reward function are maximally USEFUL and maximally NEUTRAL. The agent’s expected return across the meta-episode can be expressed as:

$$\mathbb{E} \left[ \sum_{i=1}^N \sum_{t=1}^T \gamma^{t-1} \lambda^{n_i - \frac{i-1}{k}} \frac{c_t}{m_i} \right]$$

Here  $N$  is the number of mini-episodes in the meta-episode,  $T$  is the number of timesteps in the relevant mini-episode,  $n_i$  is the number of times that the trajectory-length chosen in mini-episode  $i$  has been chosen before in the meta-episode,  $i-1$  is equivalent to  $E$  (the number of mini-episodes that have previously occurred in the meta-episode),  $c_t$  is the value of any coins that the agent collects at timestep  $t$  in the relevant mini-episode, and  $m_i$  is the maximum  $\gamma$ -discounted total value of the coins that the agent could collect conditional on the trajectory-length chosen in mini-episode  $i$ .

This expression can be rearranged as follows:

$$\mathbb{E} \left[ \sum_{i=1}^N \frac{\lambda^{n_i - \frac{i-1}{k}}}{m_i} \sum_{t=1}^T \gamma^{t-1} c_t \right]$$

Since this expression is an expectation, and since  $\lambda$  and each  $m_i$  is positive, the expression is strictly increasing in the expected ( $\gamma$ -discounted) total value of coins collected conditional on each trajectory-length with positive probability. Therefore, optimal policies maximize the expected ( $\gamma$ -discounted) total value of coins collected conditional on each trajectory-length with positive probability. And therefore, for each trajectory-length  $a_i$  with positive probability, optimal policies maximize  $c(a_i)$ . And since  $m(a_i)$  is the maximum ( $\gamma$ -discounted) total value of the coins that the agent could collect conditional on trajectory-length  $a_i$ , optimal policies are such that  $\frac{c(a_i)}{m(a_i)} = 1$  for each  $a_i$  with positive probability. Therefore, since  $\sum_{i=1}^k p(a_i) = 1$ , optimal policies maximize:

$$\sum_{i=1}^k \frac{p(a_i) c(a_i)}{m(a_i)}$$

Therefore, optimal policies are maximally USEFUL.

What remains to proven is that optimal policies are maximally NEUTRAL. Recall that optimal policies are such that  $\frac{c(a_i)}{m(a_i)} = 1$  for each trajectory-length  $a_i$  with positive probability. Thus, the return for these policies of choosing a particular trajectory-length in a mini-episode simplifies to  $\lambda^{n - \frac{E}{k}}$ , where  $n$  is the number of times that trajectory-length has previously been chosen in the meta-episode,  $E$  is the number of mini-episodes that have previously occurred in the meta-episode, and  $k$  is the number of different trajectory-lengths that could be chosen in the gridworld. Since  $\lambda$  is strictly between 0 and 1,  $\lambda^{n - \frac{E}{k}}$  is strictly decreasing in  $n$ . Thus for any trajectory-lengths  $a_i$  and  $a_j$ , if  $a_i$  has so far been chosen more times in the meta-episode than  $a_j$ , the return for choosing  $a_j$  in the next mini-episode is greater than the return for choosing  $a_i$  in the next mini-episode. We'll make use of this fact below. To prove that optimal policies are maximally NEUTRAL, we'll prove and then use Lemma 1:

**Lemma 1.** For any pair of maximally USEFUL policies  $\pi$  and  $\pi'$  and any pair of trajectory-lengths  $a_i$  and  $a_j$  such that:

1.  $p_\pi(a_i) > p_\pi(a_j)$  (with  $\mu$  denoting the sum of  $p_\pi(a_i)$  and  $p_\pi(a_j)$ ).
2.  $p_{\pi'}(a_i) = p_{\pi'}(a_j) = \frac{\mu}{2}$
3. For all other trajectory-lengths  $a_r$ ,  $p_\pi(a_r) = p_{\pi'}(a_r)$ .

The expected return of  $\pi'$  is greater than the expected return of  $\pi$ .

In other words, we can increase the expected return of any maximally USEFUL policy by shifting probability mass away from trajectory-length  $a_i$  and towards trajectory-length  $a_j$ , up until the point where  $p(a_i) = p(a_j)$ .

To prove Lemma 1, it's convenient to suppose (contrary to fact) that the agent can distinguish between different mini-episodes in the meta-episode and hence can select different probability distributions over trajectory-lengths in different mini-episodes. We make this supposition in Lemma 2 and then use Lemma 2 to prove Lemma 1.

**Lemma 2.** For any maximally USEFUL policy  $\pi$  and any pair of trajectory-lengths  $a_i$  and  $a_j$  such that:

1. For some number  $e_1 > 0$  of mini-episodes in the meta-episode,  $p_\pi(a_i) > p_\pi(a_j)$  (with  $\mu$  denoting the sum of  $p_\pi(a_i)$  and  $p_\pi(a_j)$ ).
2. For some number  $e_2 \geq 0$  of mini-episodes in the meta-episode,  $p_\pi(a_i) = p_\pi(a_j) = \frac{\mu}{2}$ .
3.  $e_1 + e_2 = N - 1$ , where  $N$  is the number of mini-episodes in the meta-episode (i.e. there's only one remaining mini-episode with the relative sizes of  $p_\pi(a_i)$  and  $p_\pi(a_j)$  undetermined by conditions 1 and 2 above).

Then the expected return of  $\pi$  would be greater if  $p_\pi(a_i) = p_\pi(a_j) = \mu/2$  in the remaining mini-episode than if  $p_\pi(a_i) > p_\pi(a_j)$  (with  $p_\pi(a_i) + p_\pi(a_j) = \mu$ ) in the remaining mini-episode.

In other words, if a maximally USEFUL policy  $\pi$  is biased towards some trajectory-length  $a_i$  over some other trajectory-length  $a_j$  in some set of mini-episodes (and isn't biased towards  $a_j$  over  $a_i$  in any mini-episodes), then we can increase  $\pi$ 's expected return by ensuring that  $p_\pi(a_i) = p_\pi(a_j) = \frac{\mu}{2}$  (rather than  $p_\pi(a_i) > p_\pi(a_j)$  with  $p_\pi(a_i) + p_\pi(a_j) = \mu$ ) in the remaining mini-episode.

Here's the proof of Lemma 2. Given antecedent conditions 1-3 of Lemma 2 above,  $a_i$ 's probability distribution over times-chosen in the first  $N - 1$  mini-episodes *stochastically dominates*  $a_j$ 's probability distribution over times-chosen in the first  $N - 1$  mini-episodes. That is to say:

1. For each possible number of times-chosen  $w$ ,  $a_i$ 's probability of being chosen at least as many times as  $w$  is at least as great as  $a_j$ 's probability of being chosen at least as many times as  $w$ .
2. For some possible number of times-chosen  $w$ ,  $a_i$ 's probability of being chosen at least as many times as  $w$  is greater than  $a_j$ 's probability of being chosen at least as many times as  $w$ .

Now recall that, for any trajectory-lengths  $a_i$  and  $a_j$ , if  $a_i$  has so far been chosen more times in the meta-episode than  $a_j$ , the return for choosing  $a_j$  in the next mini-episode is greater than the return for choosing  $a_i$  in the next mini-episode.

This fact (in combination with the fact that  $a_i$ 's probability distribution over times-chosen in the first  $N - 1$  mini-episodes stochastically dominates  $a_j$ 's probability distribution over times-chosen in the first  $N - 1$  mini-episodes) implies that  $a_j$ 's probability distribution over returns in the remaining mini-episode stochastically dominates  $a_i$ 's probability distribution over returns in the remaining mini-episode. That is to say:

1. For each possible return in the remaining mini-episode  $r$ ,  $a_j$ 's probability of delivering at least  $r$  is at least as great as  $a_i$ 's probability of delivering at least  $r$ .
2. For some possible return in the remaining mini-episode  $r$ ,  $a_j$ 's probability of delivering at least  $r$  is greater than  $a_i$ 's probability of delivering at least  $r$ .

That implies that the expected return of choosing  $a_j$  in the remaining mini-episode is greater than the expected return of choosing  $a_i$  in the remaining mini-episode. That in turn implies that the expected return of choosing  $a_i$  and  $a_j$  each with probability  $\frac{\mu}{2}$  is greater than the expected return of choosing  $a_i$  with probability greater than  $a_j$  (given that  $p(a_i) + p(a_j) = \mu$ ). That in turn implies that expected return of  $\pi$  across the meta-episode would be greater if  $a_i$  and  $a_j$  were each chosen with probability  $\frac{\mu}{2}$  in the remaining mini-episode (as opposed to choosing  $a_i$  with probability greater than  $a_j$ ).

That completes the proof of Lemma 2. Now we use it to prove Lemma 1. Let  $\pi$  be a policy such that  $p_\pi(a_i) > p_\pi(a_j)$  in each mini-episode. As above, let  $\mu$  denote the sum of  $p_\pi(a_i)$  and  $p_\pi(a_j)$ . By Lemma 2, we'd increase expected return across the meta-episode if the policy were such that  $p_\pi(a_i) = p_\pi(a_j) = \frac{\mu}{2}$  in the *last* mini-episode. And then (also by Lemma 2), we'd increase expected return further if the policy were also such that  $p_\pi(a_i) = p_\pi(a_j) = \frac{\mu}{2}$  in the *second-to-last* mini-episode, and so on all the way back to the second mini-episode.

Now suppose that  $p_\pi(a_i) = p_\pi(a_j) = \frac{\mu}{2}$  in all mini-episodes except the first. We're now trying to decide how to split probability mass between  $a_i$  and  $a_j$  in the first mini-episode. Given our reasoning above,  $a_i$ 's probability distribution over times-chosen in the last  $N - 1$  mini-episodes is identical to  $a_j$ 's probability distribution over times-chosen in the last  $N - 1$  mini-episodes, so their probability distributions over returns in the first mini-episode are identical too. Thus, their expected returns in the first mini-episode are also identical. Hence, expected return across the meta-episode is the same regardless of how we split  $\mu$  between  $p_\pi(a_i)$  and  $p_\pi(a_j)$  in the first mini-episode.

Thus, if we start with a  $\pi$  such that  $p_\pi(a_i) > p_\pi(a_j)$  in each mini-episode, we strictly increase expected return by equalizing  $p_\pi(a_i)$  and  $p_\pi(a_j)$  in all mini-episodes except one, and equalizing  $p_\pi(a_i)$  and  $p_\pi(a_j)$  in the remaining mini-episode doesn't decrease expected return. Hence, in any meta-episode containing more than one mini-episode, the expected return of  $\pi'$  (in which  $p_{\pi'}(a_i) = p_{\pi'}(a_j) = \frac{\mu}{2}$  in each mini-episode) is greater than that of  $\pi$  (in which  $p_\pi(a_i) > p_\pi(a_j)$  with  $p_\pi(a_i) + p_\pi(a_j) = \mu$  in each mini-episode). That completes the proof of Lemma 1.

Now we use Lemma 1. Take any maximally USEFUL policy  $\pi$ . By Lemma 1, if there are any trajectory-lengths  $a_i$  and  $a_j$  such that  $p(a_i) > p(a_j)$ , then we can increase  $\pi$ 's expected return by equalizing  $p(a_i)$  and  $p(a_j)$ . If we do so for each  $a_i$  and  $a_j$  such that  $p(a_i) > p(a_j)$ , we get  $p(a_i) = \frac{1}{k}$  for each of the  $k$  available trajectory-lengths  $a_i$ . We then maximize:

$$-\sum_{i=1}^k p(a_i) \log_2 p(a_i)$$

Therefore, optimal policies are maximally NEUTRAL.

We have thus proved that optimal policies for our DREST reward function are maximally USEFUL and maximally NEUTRAL.



## **C Code**

We include code for all our gridworlds and agents in the supplementary material. All of our experiments were run on a single CPU using a consumer laptop computer. Each agent was trained in less than two minutes. Total compute-time was around five hours.

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