CSM146: Homework 3

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1.) H = { sgn(ax2+bx+c); a,b,c & R} Grunesian = 3

Proof...



UC = 2:



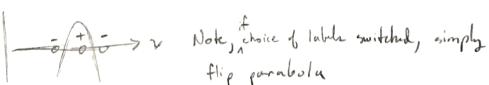






* all 3 some sign obvious extension of above cases

* If 2 of some sign adjournt, simply place 3rd point a x less than or granter than zero of parabala from corresponding example above Final care: some sign points not adjacent ...



flip parabola

in sign switcher 3 times blogs ex)

Such that abjacent points have alternating signs - note sign given to each orbitrary. If 2 abjacent points have alternating signs, they must be separated by aros of the porabola. I = 2 zeros of the porabola, or for any placement of the 4 points of the points of the points. Therefore the given clanifier con't shoutten 4 points => VC Dimension = 3

Hlex Cailbert CSM146: Homework 3 2.) KB(x,2): (1+Bx.2) 1 B>0; x,2 E R2. Find OB(.). Ly K_B(x,z) = φ_B(x) τ φ_B(z) (1+Bx.2) = (1+Bx12)3 = (1+Bx22, +Bx222)3 $= \beta^{3} x_{1}^{3} z_{1}^{3} + \beta^{3} x_{2}^{3} z_{2}^{3} + 3\beta^{3} x_{1}^{2} x_{2}^{2} z_{1}^{2} z_{2}^{2} + 3\beta^{3} x_{1}^{2} z_{1}^{2} z_{1}^{2} z_{1}^{2} + 3\beta^{3} x_{1}^{2} z_{1}^{2} z_{1}^{2}$ + 66 x, x2 2, 22 + 3B x, 2, +3B x22 + $\therefore \phi(x) =$ 516 ×2 53 B x x2 B 1/2 x,3 B 3/2 x2 B adds a constant multiplier equal to B^ (& degree of the term) to each term of the frature vector & the kernal function of K(x,2). This allows you to weight the importance of higher order terms, in limet or indirect proportion to their order.

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$$2 \Rightarrow -1(\omega_1, \omega_2) \cdot (1, 0) = 1$$

$$\omega_1 = -1 \rightarrow \omega_2 = 2$$

$$1 \Rightarrow 1 \left((\omega_1, \omega_2) (1, 1) + b \right) = 1$$

$$w_1 + w_2 + b = 1$$

$$w_2 = 2$$

$$\Rightarrow \omega^* = \begin{bmatrix} 0 \\ 2 \end{bmatrix} \quad b^* = 1$$

4.2.b) Maintaining Class Proportions in K-Fold Cross-Validation

It is important to maintain the proportions of each class across folds in K-fold validation—called stratification—because ideally, one wants each fold to be representative of the entire dataset. This is achieved by distributing the class instances to each fold proportionally to how they occur in the entire sample dataset...which hopefully is a good model for the underlying distribution.

4.2.d) Selecting the Optimal Hyperparameter

The table to the right shows the results of performing K-fold stratified cross validation on the parameter C of linear-kernel SVM classifiers, for three different classifiers - accuracy, F1-score, and area under the receiver operating characteristic curve (AUROC). We see that for judging by accuracy, the optimal C = 10(Accuracy = 0.8300); by F1-score, the optimal C = 10 (F1-Score = 0.8839); by AUROC, the optimal C = 1 (AUROC = 0.8994). Note that for many of all three of the metrics, multiple C's resulted in the same performance score. Accordingly, we chose the smallest such C with the max performance value, to get the largest margin. Typically, it is impossible to say which will improve test results the most, as this depends on the data you encounter during testing, but I found that any of the matching C's actually yielded identical test performance.

$_{10^{-3}}^{C}$	accuracy 0.7102	F1-score	AUROC 0.8542
10^{-2}	0.7245	0.8370	0.8542
10^{-1}	0.5121	0.8782	0.8809
10°	0.8211	0.8779	0.8694
10^1	B.830D	D. 8839	0.8694
10^2	0.5300	0.8839	0.8594
best C			

4.3.c) Test Set Performance

Performance Metric Used	Value of C parameter	Test Performance Score
Accuracy	10	0.7391
F1_Score	10	0.4706
AUROC	1	0.7431