Momentum Turning Points

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TS Momentum Attempts to Exploit Trend, Struggles Around Breaks

Time-series (TS) momentum strategies are based on two premises:

- 1 Expected returns vary over time
- 2 Sign persistence: Expected return positive (neg.) now \Rightarrow likely remain positive (neg.)

TS momentum strategies attempt to exploit such variation, if it exists

► Take long (short) positions in uptrend (downtrend) phases

Momentum turning points

- Unless trend is perennial in one direction, trends break down
- ▶ TS momentum strategies rely on realized returns, which reflect mixture of trend and noise
- ► At/after turning points, TS momentum prone to place bad bets

Nature of Turning Points Difficulty Depends on Speed

The speed of the momentum signal balances the tension between

- Reacting quickly
- Reducing higher-frequency noise

Slow: Relatively long lookback window—e.g., 12 months—reduces influence of noise but *slow* reaction to turning point (Type II error)

Fast: Relatively short lookback window—e.g., 1 month—fast reaction to turning point but more influenced by noise (Type I error)

Main research question:

► Can we react more effectively to momentum turning points?

TS Momentum Strategy Weights

Simple Speeds:

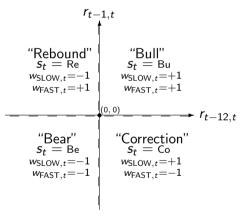
- SLOW: 12-month trailing return—standard horizon: $w_{\text{SLOW},t} = \begin{cases} +1 & \text{if } r_{t-12,t} \geq 0, \\ -1 & \text{if } r_{t-12,t} < 0. \end{cases}$
- FAST: 1-month trailing return: $w_{\mathsf{FAST},t} := \begin{cases} +1 & \text{if } r_{t-1,t} \geq 0, \\ -1 & \text{if } r_{t-1,t} < 0. \end{cases}$

Intermediate Speeds:

- lacksquare Speed parameter $a \in [0,1]$: $w_t(a) = (1-a)w_{\mathsf{SLOW},t} + aw_{\mathsf{FAST},t} \in [-1,+1]$
- ▶ MED ("medium", $a = \frac{1}{2}$): $w_{\text{MED},t} = w_t \left(\frac{1}{2}\right) = \frac{1}{2} w_{\text{SLOW},t} + \frac{1}{2} w_{\text{FAST},t}$ ∈ $\{-1,0,+1\}$

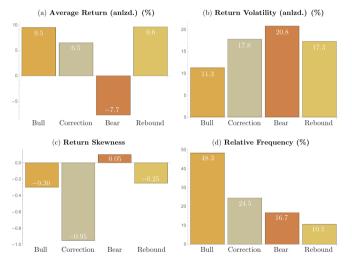
SLOW × FAST Generates Market Cycles

▶ Intersect SLOW (12-month) with FAST (1-month) ⇒ 4 observable market cycles



▶ Strategies of *all* speeds dictated *ex-ante* by these four phases

U.S. Stock Market Cycles: *Predictive* Return Properties



U.S. value-weighted returns, Kenneth French Data Library, 1969-01 to 2018-12

- Bull states followed by high avg. return & low volatility
- Bear states followed by neg. avg. return & high volatility
- Correction states followed by lower avg. returns, increased volatility, & severe downside outcomes—possibly lead up to Bear.
- Rebound states followed by avg. returns & skewness similar to Bull, but higher volatility—possibly lead up to Bull state.
- ► Turning points (Corrections + Rebounds) occur 35% of time

► Economic Linkages

Performance of Market and Momentum of Various Speeds

		Market	a=0 SLOW MOM12	$a=rac{1}{4}$	$a=rac{1}{2}$ MED	$a=\frac{3}{4}$	$a=1 \ {\sf FAST} \ {\sf MOM1}$
1	Average (%) (anlzd.)	5.91	6.46	6.17	5.88	5.59	5.30
	Volatility (%) (anlzd.)	15.64	15.62	12.72	11.60	12.74	15.66
	Sharpe Ratio (anlzd.)	0.38	0.41	0.48	0.51	0.44	0.34
	Skewness	-0.55	-0.43	-0.13	0.02	0.03	0.15
2	Max. Drawdown (%)	-54.36	-43.43	-37.96	-34.43	-34.07	-44.53
2	Avg./ Max. DD	0.11	0.14	0.16	0.17	0.17	0.12
	Average Position	1.00	0.46	0.39	0.32	0.25	0.18
	Market Beta	1.00	0.15	0.05	-0.04	-0.13	-0.23
3	Alpha (%) (anlzd.)	0.00	5.58	5.85	6.12	6.39	6.66
	Alpha \hat{t} -statistic	_	2.54	3.24	3.71	3.57	3.07

U.S. value-weighted excess returns, Kenneth French Data Library, 1969-01 to 2018-12



Part

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Part 1: Sharpe Ratio Performance by Speed

	Market	a=0 SLOW MOM12	$a=\frac{1}{4}$	$a = \frac{1}{2}$ MED	$a=\frac{3}{4}$	a=1 FAST MOM1
Average (%) (anlzd.) Variance (%) (anlzd.) Volatility (%) (anlzd.)	5.91 2.45 15.64	6.46 2.44 15.62	6.17 1.62 12.72	5.88 1.35 11.60	5.59 1.62 12.74	5.30 2.45 15.66
Sharpe Ratio (anlzd.)	0.38	0.41	0.48	0.51	0.44	0.34

U.S. value-weighted excess returns, Kenneth French Data Library, 1969-01 to 2018-12

▶ Reducing exposure following Correction/Rebound improves Sharpe ratio:

$$\mathsf{Sharpe}[w_t(a) \cdot r_{t+1}] \approx ((1-a)\,\mathsf{Sharpe}[w_{\mathsf{SLOW},t} \cdot r_{t+1}] + a\,\mathsf{Sharpe}[w_{\mathsf{FAST},t} \cdot r_{t+1}])\,D(a)$$

$$\text{Disagreement Multiplier:} \quad D(a) := \sqrt{\frac{\mathbf{E}[r_{t+1}^2]}{\mathbf{E}[r_{t+1}^2|_{\text{Be}}]\mathbf{P}[_{\text{Be}}^{\text{Bu}}] + (2a-1)^2\mathbf{E}[r_{t+1}^2|_{\text{Re}}]\mathbf{P}[_{\text{Re}}^{\text{Co}}]}} > 1.$$

Part 2a: Cycle-Conditional Market Return Extremes

Cond. Market <i>Monthly</i> Return Percentiles (%)	Bull	Bear	Correction	Rebound
MIN	-9.55	-17.23	-23.24	-10.35
P01	-7.85	-12.79	-14.62	-10.16
P05	-4.64	-10.10	-7.14	-8.41
P10	-3.37	-8.06	-5.64	-5.51
P25	-1.51	-4.83	-2.08	-2.44
P50	1.05	-0.89	1.07	1.15
P75	3.07	3.98	3.82	4.59
P90	4.68	6.82	5.84	7.24
P95	6.13	7.99	7.15	7.98
P99	7.21	13.68	11.79	10.61
MAX	9.59	16.10	12.47	11.30

U.S. value-weighted excess returns, Kenneth French Data Library, 1969-01 to 2018-12

- ► Corrections introduce extreme outcomes and volatility, despite most outcomes being positive
- ▶ 5 of 10 worst months in last 50 years were after Correction phases
- ▶ 4 of 10 best months in last 50 years were after Correction phases





Part 2b: Downside Performance by Speed

	Market	a=0 SLOW MOM12	$a=rac{1}{4}$	$a=rac{1}{2}$ MED	$a=\frac{3}{4}$	a=1 FAST MOM1
Skewness Max. Drawdown (%) Avg./ Max. DD	-0.55 -54.36 0.11	-0.43 -43.43 0.14	-0.13 -37.96 0.16	0.02 -34.43 0.17	0.03 -34.07 0.17	0.15 -44.53 0.12

U.S. value-weighted excess returns, Kenneth French Data Library, 1969-01 to 2018-12

▶ MED's skewness, in general, is scaled/shifted relative to SLOW/FAST:

$$\begin{aligned} \mathbf{Skew}[w_t(\tfrac{1}{2}) \cdot r_{t+1}] &\approx \frac{1}{2} (\mathbf{Skew}[w_{\mathsf{SLOW},t} \cdot r_{t+1}] + \mathbf{Skew}[w_{\mathsf{FAST},t} \cdot r_{t+1}]) \left[D(\tfrac{1}{2}) \right]^3 \\ &+ 3 \, \mathbf{Sharpe}[w_t(\tfrac{1}{2}) \cdot r_{t+1}] \left(\left[D(\tfrac{1}{2}) \right]^2 - 1 \right) \end{aligned}$$

Part 3a: Market Timing and Volatility Timing

Widely-used decomposition of expected returns:

$$\mathsf{E}[w_t(a)\cdot r_{t+1}] = \underbrace{\mathsf{Cov}[w_t(a), r_{t+1}]}_{\text{"market timing"}} + \underbrace{\mathsf{E}[w_t(a)]}_{\text{"static"}} \mathsf{E}[r_{t+1}],$$

New decomposition of covariance between strategy returns and market:

$$\mathsf{Cov}[w_t(a) \cdot r_{t+1}, r_{t+1}] = \mathsf{E}[w_t(a)]\mathsf{Var}[r_{t+1}] + \mathsf{Cov}[w_t(a), r_{t+1}]\mathsf{E}[r_{t+1}] + \mathsf{Cov}[w_t(a), (r_{t+1} - \mathsf{E}[r_{t+1}])^2].$$

New market beta and alpha decompositions:

$\mathsf{Beta}[w_t(a) \cdot r_{t+1}] = \underbrace{\mathsf{E}[w_t(a)]}_{} + \mathsf{Cov}[w_t(a), r_{t+1}] \frac{\mathsf{E}[r_{t+1}]}{\mathsf{Var}[r_{t+1}]}_{} +$ $Cov[w_t(a), (r_{t+1} - E[r_{t+1}])^2]$ "market timing" $\mathsf{Alpha}[w_t(a) \cdot r_{t+1}] = \mathsf{Cov}[w_t(a), r_{t+1}] \left(1 - \frac{(\mathsf{E}[r_{t+1}])^2}{\mathsf{Var}[r_{t+1}]}\right)$ "market timing"

Overlooked

"volatility timing" +\left\{ -\frac{\text{Cov}[w_t(a), (r_{t+1} - \text{E}[r_{t+1}])^2]}{\text{Var}[r_{t+1}]} \text{E}[r_{t+1}]^{\text{}}

"volatility timing"

Part 3b: Beta and Alpha Decompositions

Market Beta and Alpha	a = 0 SLOW MOM12	$a=rac{1}{4}$	$a=rac{1}{2}$ MED	$a=\frac{3}{4}$	a=1 FAST MOM1					
Beta	0.15	0.05	-0.04	-0.13	-0.23					
Alpha (%) (anlzd.)	5.58	5.85	6.12	6.39	6.66					
Alpha \hat{t} -stat.	2.54	3.24	3.71	3.57	3.07					
Beta Components										
Static	0.457	0.387	0.317	0.247	0.177					
Market Timing	0.008	0.008	0.008	0.008	0.009					
Volatility Timing	-0.315	-0.339	-0.364	-0.389	-0.414					
Alpha Components (%) (anlzd.)										
Market Timing	3.72	3.84	3.96	4.09	4.21					
Volatility Timing	1.86	2.00	2.15	2.30	2.44					

U.S. value-weighted excess returns, Kenneth French Data Library, 1969-01 to 2018-12



Dynamic Speed Selection

Dynamic speed strategy weight:

$$w_t(a_{s(t)}) = (1 - a_{s(t)})w_{\mathsf{SLOW},t} + a_{s(t)}w_{\mathsf{FAST},t}.$$

Consider choosing state-conditional speeds $a_{s(t)}$ to apply after every occurrence of state s(t) to maximize steady-state Sharpe Ratio:

$$\max_{a_{s(t)}:s(t)\in\{\mathsf{Bu},\mathsf{Co},\mathsf{Be},\mathsf{Re}\}}\mathsf{Sharpe}[w_t(a_{s(t)})\cdot r_{t+1}].$$

Solution:

$$\begin{split} &a_{\text{Bu}} \in [0,1], \quad (w_{\text{SLOW},t} = w_{\text{FAST},t} = 1, \text{ so any } a \text{ results in } +1) \\ &a_{\text{Be}} \in [0,1], \quad (w_{\text{SLOW},t} = w_{\text{FAST},t} = -1, \text{ so any } a \text{ results in } -1) \\ &a_{\text{Co}} = \frac{1}{2} \left(1 - \frac{\mathbf{E}[r_{t+1}^2 | \mathbf{Bu}] \mathbf{P}[\mathbf{Bu}]}{\mathbf{E}[r_{t+1}|\mathbf{Bu}] \mathbf{P}[\mathbf{Bu}]} - \mathbf{E}[r_{t+1}|\mathbf{Be}] \mathbf{P}[\mathbf{Be}]} \frac{\mathbf{E}[r_{t+1}|\mathbf{Co}]}{\mathbf{E}[r_{t+1}^2|\mathbf{Co}]} \right), \\ &a_{\text{Re}} = \frac{1}{2} \left(1 + \frac{\mathbf{E}[r_{t+1}^2 | \mathbf{Bu}] \mathbf{P}[\mathbf{Bu}]}{\mathbf{E}[r_{t+1}^2 | \mathbf{Bu}] \mathbf{P}[\mathbf{Bu}]} \frac{\mathbf{E}[r_{t+1}|\mathbf{Re}]}{\mathbf{E}[r_{t+1}^2 | \mathbf{Re}]} \frac{\mathbf{E}[r_{t+1}|\mathbf{Re}]}{\mathbf{E}[r_{t+1}^2 | \mathbf{Re}]} \right). \end{split}$$

DYN Strategy Performance Over the Last 50 Years

DY	N Strate	gy		Evaluation							
Estim	ation Wir	ndow	Evalu	ation Wir	ndow	Sharpe R	Sharpe Ratio (anlzd.)				
From	То	Length	From	То	Length		"Oracle"	Efficiency			
(yr-mo)	(yr-mo)	(yrs)	(yr-mo)	(yr-mo)	(yrs)	$DYN\; (\widehat{a}_{Co}, \widehat{a}_{Re})$	OPT	DYN/OPT			
1926-07	1968-12	42.5	1969-01	2018-12	50.0	0.524 (0.00, 0.58)	0.570	0.920			
1926-07	1973-12	47.5	1974-01	2018-12	45.0	0.547 (0.07, 0.59)	0.572	0.956			
1926-07	1978-12	52.5	1979-01	2018-12	40.0	0.611 (0.08, 0.65)	0.626	0.977			
1926-07	1983-12	57.5	1984-01	2018-12	35.0	0.614 (0.22, 0.67)	0.623	0.985			
1926-07	1988-12	62.5	1989-01	2018-12	30.0	0.688 (0.26, 0.69)	0.721	0.954			
1926-07	1993-12	67.5	1994-01	2018-12	25.0	0.675 (0.11, 0.71)	0.684	0.988			
1926-07	1998-12	72.5	1999-01	2018-12	20.0	0.564 (0.17, 0.69)	0.579	0.975			
1926-07	2003-12	77.5	2004-01	2018-12	15.0	0.611 (0.16, 0.69)	0.621	0.984			

DYN: ex-ante estimated investable strategy; OPT: ex-post estimated "oracle" of best possible speed pair U.S. value-weighted excess returns, Kenneth French Data Library

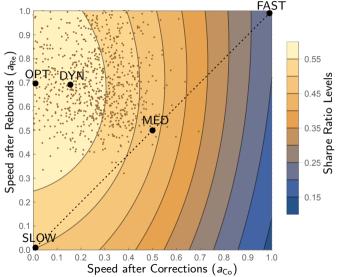
Dynamic vs. Static Speed Performance Per Unit Risk

50-Year	50-Year Evaluation Window, 1969-01 to 2018-12									
						$\widehat{a}_{Co} = 0.00$				
	a = 0.00	0.25	0.50	0.75	1.00	$\widehat{a}_{Re} = 0.58$				
	SLOW		MED		FAST	DYN				
Sharpe Ratio (anlzd.)	0.41	0.48	0.51	0.44	0.34	0.52				
Efficiency (/OPT)	0.73	0.85	0.89	0.77	0.59	0.92				
Avg. (anlzd.)/ Max. DD	0.15	0.16	0.17	0.16	0.12	0.23				
15-Year	Evaluation	Windo	w, 2004-0	01 to 20	018-12					
						$\widehat{a}_{Co} = 0.16$				
	a = 0.00	0.25	0.50	0.75	1.00	$\widehat{a}_{Re} = 0.69$				
	SLOW		MED		FAST	DYN				
Sharpe Ratio (anlzd.)	0.55	0.57	0.51	0.36	0.21	0.61				
Efficiency (/OPT)	0.88	0.91	0.81	0.58	0.34	0.98				
$Avg. \; (anlzd.)/ Max. \; DD $	0.22	0.26	0.23	0.14	0.08	0.28				

U.S. value-weighted excess returns, Kenneth French Data Library



Sharpe Ratios For All Dynamic Speed Pairs—Last 15 Years



- Brown dots correspond to DYN estimated ex-ante from 1,000 block bootstrap historical samples
- Static-speed strategies are on the diagonal
- DYN almost always does better than static speeds
- Upper-left corner relatively efficient: slow after Corrections, fast after Rebounds

Performance in International Equity Markets—Last 15 Years

			Share	e Ratio	(anlzd.)				Sharpe Ratio (anlzd.)										
Country	a = 0.00 SLOW MOM12	0.25	0.50 MED	0.75	1.00 FAST MOM1	$egin{aligned} a_{Co} &= \widehat{a}_{Co} \ a_{Re} &= \widehat{a}_{Re} \ DYN \left(a_{Co}, a_{Re} ight) \end{aligned}$		a_{Re}	= 0.00 = 0.81 DYN										
AU	0.367	0.417	0.420	0.350	0.258	0.526	(0.00, 1.00)		0.528										
CA	0.299	0.417	0.517	0.551	0.527	0.650	(0.56, 1.00)		0.601										
DE	0.458	0.474	0.429	0.316	0.198	0.542	(0.00, 0.66)		0.544										
ES	0.165	0.154	0.120	0.067	0.020	0.238	(0.16, 0.86)		0.256										
FR	0.421	0.487	0.492	0.390	0.269	0.642	(0.28, 0.81)		0.649										
IT	0.329	0.303	0.236	0.140	0.050	0.329	(0.00, 0.00)		0.418										
JP	0.529	0.599	0.618	0.559	0.462	0.554	(0.00, 0.20)		0.547										
NL	0.394	0.343	0.195	0.000	-0.131	0.419	(0.00, 0.81)		0.420										
SE	0.613	0.700	0.687	0.510	0.322	0.820	(0.12, 0.59)		0.803										
UK	0.301	0.211	0.052	-0.115	-0.224	0.475	(0.00, 1.00)		0.472										
US	0.589	0.618	0.565	0.419	0.264	0.669	(0.07, 0.57)		0.659										

Datastream 1980-2018, Exceeds all static speeds ;

Below best static speed

Conclusion

- Intermediate static speeds strategies: many advantages over SLOW and FAST
 - ▶ Higher Sharpe ratios, less severe drawdowns, more positive (less negative) skewness, higher significance of alphas, stronger predictability of all moments of future returns
 - Market cycles (bull, correction, bear, and rebound) useful for explaining phenomena
 - New understanding of Sharpe ratios and skewness
- ▶ Volatility timing plays important (overlooked) role:
 - We provide formal decomposition of what drives beta and alpha
 - Momentum weights are strong negative predictors of return volatility
 - Betas are lower than static tilts might imply
- Dynamic speed strategies
 - ► Can dynamically time optimal speed blends
 - Slow down after Corrections, speed up after Rebounds
- ▶ Insights apply to international equity markets

Appendix



Market Cycle Patterns

Takeaway from U.S. stock market: Slow down after Corrections; speed up after Rebounds

Cycle patterns reinforce this takeaway

_	Unconditional Frequency (%)									
	Bull	Correction	Bear	Rebound						
	48.3	24.3	16.8	10.5						

		Monthly Transition Probability (%)								
	Bull Correction Bear Rebound Up D									
Bull	62.8	34.8	2.1	0.3	63.3	36.7				
Correction	61.2	29.9	8.8	0.0	61.2	38.8				
Bear	9.0	0.0	55.0	36.0	45.0	55.0				
Rebound	14.3	1.6	42.9	41.3	55.6	44.4				

U.S. value-weighted excess returns, Kenneth French Data Library, 1969-01 to 2018-12

More Stats

- Corrections tend to revert to Bulls—FAST takes short position, which is a bad bet
- Market likely to go up after Rebounds—FAST takes long position, which is a good bet

Does this takeaway apply in international markets?



MOM6 vs. MED

		a = 0	$a=rac{1}{4}$	$a=rac{1}{2}$	$a=\frac{3}{4}$	a = 1
		SLOW		MED		FAST
	MOM6	MOM12				MOM1
Average (%) (anlzd.)	4.75	6.46	6.17	5.88	5.59	5.30
Volatility (%) (anlzd.)	15.67	15.62	12.72	11.60	12.74	15.66
Sharpe Ratio (anlzd.)	0.30	0.41	0.48	0.51	0.44	0.34
Skewness	-0.61	-0.43	-0.13	0.02	0.03	0.15
Max. Drawdown (%)	-64.56	-43.43	-37.96	-34.43	-34.07	-44.53
Avg. (anlzd.)/ Max. DD	0.07	0.14	0.16	0.17	0.17	0.12
Average Position	0.33	0.46	0.39	0.32	0.25	0.18
Market Beta	-0.01	0.15	0.05	-0.04	-0.13	-0.23
Alpha (%) (anlzd.)	4.79	5.58	5.85	6.12	6.39	6.66
Alpha <i>t</i> -statistic	2.15	2.54	3.24	3.71	3.57	3.07

Sample: 1969-01 to 2018-12

- ▶ MOM6 is relatively slow-moving: 5 of 6 (83%) months overlap in consecutive month signals
- ► MOM6 does not lever down at/after turning points



Economic Linkages: Macro Innovations by Cycle (t-Stats)

		Econom	y (Surprises)							
Phase	Production	Consumption	Employment	Sales	MP Shock					
Bull Correction Bear Rebound	1.53 1.46 -3.15 -1.41	2.25 -0.29 -3.24 -0.23	2.30 1.06 -4.06 -1.30	$ \begin{array}{r} 2.63 \\ -0.13 \\ -3.73 \\ -0.65 \end{array} $	0.41 1.72 0.58 -3.96					
Risk (Surprises)										
Phase	NFCI*	PS Liquidity	TED*	Noise*	Vol Spread					
Bull Correction Bear Rebound	$1.72 \\ -1.21 \\ -3.41 \\ 2.32$	4.63 -1.67 -6.22 0.43	$1.67 \\ -1.67 \\ -3.03 \\ 2.00$	1.53 -0.52 -4.29 2.15	3.80 -1.02 -4.19 -0.86					
		Surveys	(Surprises)							
Phase	News Uncertainty*	Consumer Sentiment	PMI	SPF Recession*	SPF Corporate Profits					
Bull Correction Bear Rebound	2.09 0.06 -4.04 -0.28	$1.64 \\ -0.10 \\ -3.30 \\ 0.09$	3.48 -0.77 -3.21 -2.39	$2.30 \\ -1.21 \\ -3.00 \\ 0.84$	$1.80 \\ -0.61 \\ -2.83 \\ 0.76$					



Economic Linkages: Data

The macro series all ends on March 2019 unless specified otherwise. The starting dates vary and are subject to availability from the original sources.

From the FRED database of the St. Louis Federal Reserve:

- Chicago Fed National Activity Index: Personal Consumption and Housing
- Chicago Fed National Activity Index: Production and Income
- Chicago Fed National Activity Index: Sales, Orders and Inventories
- Chicago Fed National Activity Index: Employment, Unemployment and Hours
- Chicago Fed National Financial Conditions Index
- Effective Federal Funds Rate
- ► TED Spread
- University of Michigan: Consumer Sentiment

From Gertler and Karadi (2015) we obtain:

► Monetary policy shocks (end date: June 2012)



Economic Linkages: Data (cont'd...)

From Pastor and Stambaugh (2003):

- Aggregate liquidity measure (end date: December 2018)
- ► Liquidity innovation measure (end date: December 2018)

Bond illiquidity metric from Hu et al. (2013):

▶ Noise (end date: December 2016)

High vol/low vol valuation spread from Pflueger et al. (2018):

PVS indicator (end date: Q2 2016)

From Bloom et al. (2016):

U.S. News uncertainty

From Bloomberg:

► PMI

From the Survey of Professional Forecasters

- ▶ Recession probabilities (QTR1, median response)
 - Corporate profits after tax (DCPROF2, % change of median response)



Cycle-Conditional Market Return Extremes

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P10	-3.37	-8.06	-5.64	-5.51
P25	-1.51	-4.83	-2.08	-2.44
P50	1.05	-0.89	1.07	1.15
P75	3.07	3.98	3.82	4.59
P90	4.68	6.82	5.84	7.24
P95	6.13	7.99	7.15	7.98
P99	7.21	13.68	11.79	10.61
MAX	9.59	16.10	12.47	11.30

Sample: 1969-01 to 2018-12

- Corrections introduce extreme outcomes and volatility, despite most outcomes being positive
- ▶ 5 of 10 worst months in last 50 years were after Correction phases: -23.24 (1987-10); -16.08(1998-08); -12.90 (1980-03); -11.91 (1978-10); -10.72 (2000-11)
- ▶ 4 of 10 best months in last 50 years were after Correction phases: 12.47 (1987-01); 12.16 (1976-01); 11.35 (2011-10); 10.84 (1991-12)



Performance of Market and Momentum of Various Speeds—Last 15 yrs

	Market	a = 0 SLOW MOM12	$a=rac{1}{4}$	$a=rac{1}{2}$ MED	$a=\frac{3}{4}$	a = 1 FAST MOM1
Average (%) (anlzd.)	7.58	7.60	6.45	5.30	4.15	3.00
Volatility (%) (anlzd.)	13.91	13.91	11.41	10.48	11.50	14.06
Sharpe Ratio (anIzd.)	0.54	0.55	0.57	0.51	0.36	0.21
Skewness	-0.77	0.12	0.27	0.49	0.35	0.00
Max. Drawdown (%)	-51.51	-33.96	-24.67	-23.32	-29.34	-38.36
Avg./ Max. DD	0.15	0.22	0.26	0.23	0.14	0.08
Average Position	1.00	0.72	0.62	0.52	0.41	0.31
Market Beta	1.00	0.20	0.14	0.08	0.01	-0.05
Alpha (%) (anlzd.)	0.00	6.08	5.40	4.72	4.04	3.37
Alpha <i>t</i> -statistic	_	1.70	1.83	1.73	1.34	0.91



Beta and Alpha Decompositions—Last 15 yrs

Market Beta and Alpha	a = 0 SLOW MOM12	$a=rac{1}{4}$	$a=rac{1}{2}$ MED	$a=rac{3}{4}$	a = 1 FAST MOM1
Beta Alpha (%) (anlzd.) Alpha <i>t</i> -stat.	0.20 6.08 1.70	0.14 5.40 1.83	0.08 4.72 1.73	0.01 4.04 1.34	-0.05 3.37 0.91
Beta Components					
Static Market Timing Volatility Timing	0.722 0.007 -0.528	$0.619 \\ 0.006 \\ -0.487$	0.517 0.005 -0.445	0.414 0.003 -0.403	0.311 0.002 -0.362
Alpha Components (%) (an	lzd.)				
Market Timing Volatility Timing	2.09 4.00	1.72 3.69	1.36 3.37	0.99 3.06	0.63 2.74



DYN vs. Static: Performance Summary—Last 15 yrs

		a = 0 SLOW	$a=\frac{1}{4}$	$a=rac{1}{2}$ MED	$a=\frac{3}{4}$	a=1 FAST	
	Market	MOM12				MOM1	DYN
Average (%) (anlzd.)	7.58	7.60	6.45	5.30	4.15	3.00	7.20
Volatility (%) (anlzd.)	13.91	13.91	11.41	10.48	11.50	14.06	11.78
Sharpe Ratio (anlzd.)	0.54	0.55	0.57	0.51	0.36	0.21	0.61
Skewness	-0.77	0.12	0.27	0.49	0.35	0.00	0.21
Max. Drawdown (%)	-51.51	-33.96	-24.67	-23.32	-29.34	-38.36	-25.74
Avg./ Max. DD	0.15	0.22	0.26	0.23	0.14	0.08	0.28
Average Position	1.00	0.72	0.62	0.52	0.41	0.31	0.72
Market Beta	1.00	0.20	0.14	0.08	0.01	-0.05	0.33
Alpha (%) (anlzd.)	0.00	6.08	5.40	4.72	4.04	3.37	4.71
Alpha <i>t</i> -statistic	_	1.70	1.83	1.73	1.34	0.91	1.65

DYN vs. Static: Beta and Alpha Decompositions—Last 15 yrs

a=0 SLOW MOM12	$a=rac{1}{4}$	$a=rac{1}{2}$ MED	$a=\frac{3}{4}$	$a=1 \ {\sf FAST} \ {\sf MOM1}$	DYN
0.20	0.14	0.08	0.01	-0.05	0.33
6.08	5.40	4.72	4.04	3.37	4.71
1.70	1.83	1.73	1.34	0.91	1.65
0.722	0.619	0.517	0.414	0.311	0.724
0.007	0.006	0.005	0.003	0.002	0.006
-0.528	-0.487	-0.445	-0.403	-0.362	-0.400
inlzd.)					
2.09	1.72	1.36	0.99	0.63	1.69
4.00	3.69	3.37	3.06	2.74	3.03
	SLOW MOM12 0.20 6.08 1.70 0.722 0.007 -0.528 anlzd.)	SLOW MOM12 0.20 0.14 6.08 5.40 1.70 1.83 0.722 0.619 0.007 0.006 -0.528 -0.487 anlzd.) 2.09 1.72	SLOW MED MOM12 0.20 0.14 0.08 6.08 5.40 4.72 1.70 1.83 1.73 0.722 0.619 0.517 0.007 0.006 0.005 -0.528 -0.487 -0.445 anlzd.) 2.09 1.72 1.36	SLOW MED MED 0.20 0.14 0.08 0.01 6.08 5.40 4.72 4.04 1.70 1.83 1.73 1.34 0.007 0.006 0.005 0.003 -0.528 -0.487 -0.445 -0.403 anlzd.)	SLOW MOM12 MED FAST MOM1 0.20 0.14 0.08 0.01 -0.05 0.01 -0.05 6.08 5.40 4.72 4.04 3.37 1.70 1.83 1.73 1.34 0.91 0.722 0.619 0.517 0.414 0.311 0.007 0.006 0.005 0.003 0.002 -0.528 -0.487 -0.445 -0.403 -0.362 anlzd.) 2.09 1.72 1.36 0.99 0.63



Drawdowns in International Equity Markets—Last 15 Years

	Average Return (anlzd.)/ Max. DD (in %)											
Country	a=0.00 SLOW MOM12	0.25	0.50 MED	0.75	1.00 FAST MOM1	$a_{\rm R}$	$egin{aligned} a_{Co} &= \widehat{a}_{Co} \ a_{Re} &= \widehat{a}_{Re} \ DYN \; ig(a_{Co}, a_{Re} ig) \end{aligned}$		= 0.00 = 0.81 DYN			
AU	0.099	0.128	0.127	0.092	0.063		(0.56, 1.00)		0.223			
CA	0.107	0.162	0.188	0.214	0.209	0.261	(0.00, 0.66)		0.256			
DE	0.160	0.177	0.191	0.169	0.094	0.202	(0.00, 0.66)		0.205			
ES	0.047	0.043	0.032	0.019	0.006	0.083	(0.16, 0.86)		0.095			
FR	0.126	0.148	0.194	0.137	0.089	0.304	(0.28, 0.81)		0.269			
ΙΤ	0.094	0.088	0.078	0.042	0.015	0.094	(0.00, 0.00)		0.212			
JP	0.224	0.279	0.347	0.305	0.231	0.264	(0.00, 0.20)		0.240			
NL	0.138	0.148	0.080	0.000	-0.038	0.167	(0.00, 0.81)		0.168			
SE	0.255	0.394	0.360	0.281	0.175	0.491	(0.12, 0.59)		0.442			
UK	0.097	0.073	0.018	-0.031	-0.056	0.219	(0.00, 1.00)		0.243			
US	0.241	0.279	0.249	0.190	0.118	0.302	(0.07, 0.57)		0.312			

Datastream 1980-2018, Exceeds all static speeds;

Below best static speed



Market Cycle Patterns: More Statistics

Und	conditional I	ncy (%)	Aı	erage Dura	tion (n	nonths)	
Bull	Correction	Bear	Rebound	Bull	Correction	Bear	Rebound
48.3	24.3	16.8	10.5	2.70	1.43	2.22	1.70

		Monthly Transition Probability (%)						litional on L	eaving	the State (%)
	Bull	Correction	Bear	Rebound	Up	Down	Bull	Correction	Bear	Rebound
Bull	62.8	34.8	2.1	0.3	63.3	36.7	_	94.4	4.7	0.9
Correction	61.2	29.9	8.8	0.0	61.2	38.8	87.4	_	12.6	0.0
Bear	9.0	0.0	55.0	36.0	45.0	55.0	20.0	0.0		80.0
Rebound	14.3	1.6	42.9	41.3	55.6	44.4	24.3	2.7	73.0	

Sample: 1969-01 to 2018-12

- ▶ Rebounds twice as likely as Corrections to signal turning point
- ► Though Rebounds ultimately tend to be false alarms about turning points (down-to-up), they still indicate good bets before transitioning: 41.3% chance of remaining in Rebound, 55.6% success rate



Predictability: Why Do Intermediate Speeds Have Higher Alpha t-Stats?

$Corr(w_t(a), f(r_{t+1}))$	a = 0 SLOW MOM12	$a=rac{1}{4}$	$a=rac{1}{2}$ MED	$a=\frac{3}{4}$	a = 1 FAST MOM1
Return: $f(r_{t+1}) = r_{t+1}$ Volatility:	0.078	0.094	0.100	0.093	0.080
$f(r_{t+1}) = r_{t+1} - \mathbf{E}[r_{t+1}] $	-0.235	-0.279	-0.294	-0.270	-0.230
$f(r_{t+1}) = (r_{t+1} - \mathbf{E}[r_{t+1}])^2$ Lower Tail:	-0.181	-0.226	-0.251	-0.241	-0.214
$f(r_{t+1}) = r_{t+1} \mathbb{1}_{\{r_{t+1} \leq 10 \text{th pctl.}\}}$ Upper Tail:	0.184	0.224	0.242	0.227	0.197
$f(r_{t+1}) = r_{t+1} 1_{\{r_{t+1} \ge 90 \text{th pctl.}\}}$	-0.100	-0.113	-0.114	-0.100	-0.081

Sample: 1969-01 to 2018-12

▶ Intermediate speeds have stronger predictability than average of SLOW/FAST

$$\mathsf{Corr}[w_t(a), f(r_{t+1})] \approx \left((1-a)\mathsf{Corr}[w_{\mathsf{SLOW},t}, f(r_{t+1})] + a\mathsf{Corr}[w_{\mathsf{FAST},t}, f(r_{t+1})]\right) D_1(a)$$

$$\textit{D}_{1}(\textit{a}) := \sqrt{\frac{1}{\textbf{P}[\frac{\text{Bu}}{\text{Be}}] + (2\textit{a}-1)^{2}\textbf{P}[\frac{\text{Co}}{\text{Re}}]}} > 1$$



Predictability & Alpha: DYN vs. static speeds—over last 50 years

	a=0 SLOW	$a=rac{1}{4}$	$a=rac{1}{2}$ MED	$a=\frac{3}{4}$	a=1 FAST	
$Corr(w_t(a), f(r_{t+1}))$	MOM12				MOM1	DYN
Return: $f(r_{t+1}) = r_{t+1}$ Volatility:	0.078	0.094	0.100	0.093	0.080	0.104
$f(r_{t+1}) = r_{t+1} - \mathbf{E}[r_{t+1}] $	-0.235	-0.279	-0.294	-0.270	-0.230	-0.244
$f(r_{t+1}) = (r_{t+1} - \mathbf{E}[r_{t+1}])^2$ Lower Tail:	-0.181	-0.226	-0.251	-0.241	-0.214	-0.197
$f(r_{t+1}) = r_{t+1} \mathbb{1}_{\{r_{t+1} \leq 10 ext{th pctl.}\}}$ Upper Tail:	0.184	0.224	0.242	0.227	0.197	0.213
$f(r_{t+1}) = r_{t+1} 1_{\{r_{t+1} \ge 90 \text{th pctl.}\}}$	-0.100	-0.113	-0.114	-0.100	-0.081	-0.086
Alpha T-Stat	2.54	3.24	3.71	3.57	3.07	2.99

- ▶ DYN is slightly better at predicting returns and not as bad at giving up high returns (90th pctl.)
- ▶ DYN is somewhat worse at predicting volatility and turning lower tail events into positive outcomes