# Lecture 7: Basic Sampling

**Professor Ilias Bilionis** 

#### Pseudo-random number generators



### Pseudo-random number generators

- Computers are deterministic machines and therefore they cannot generate completely random numbers?
- Idea: Are there deterministic sequences of numbers that look random?
- Pseudo-random number generators do exactly that.
- We use statistical tests to see how good they are.

## Pseudo-random number generators

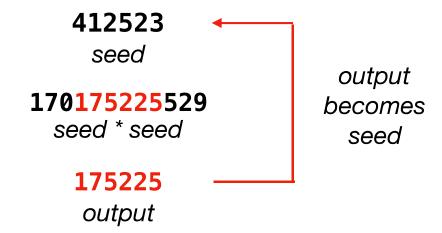
How do you generate a uniform random number?



John von Neumann. (Los Alamos)

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The middle-square method



The first, but it doesn't pass all statistical tests.

## Linear congruential generators

Seed  $x_0$ 

$$x_{i+1} = (ax_i + b) \mod m$$

#### Mersenne Twister PRNG

- This is what is inside numpy.random.
- Details beyond the scope of this class.

