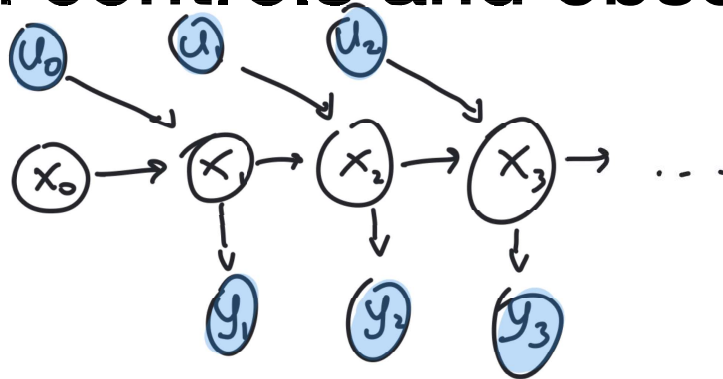


Lecture 20: State-space models - Kalman filters

Professor Ilias Bilonis

Derivation of Kalman filter - Overview

Reminder - Linear dynamical system with controls and observations



Initial Prob. : $x_0 = \mu_0 + z_0, z_0 \sim N(0, \Sigma_0); \underline{p(x_0) = N(x_0 | \mu_0, \Sigma_0)}$

Transition Prob. : $x_{n+1} = Ax_n + Bu_n + z_n, z_n \sim N(0, Q);$
 $\underline{p(x_{n+1} | x_n, u_n) = N(x_{n+1} | Ax_n + Bu_n, Q)}$

Emission Prob. : $y_n = Cx_n + w_n, w_n \sim N(0, R)$
 $\underline{p(y_n | x_n) = N(y_n | Cx_n, R)}$

Filtering Problem : $p(x_{0:n} | y_{1:n}, u_{1:n}) \propto p(x_{0:n}, \underline{y_{1:n}}, \underline{u_{1:n}})$

constants.

$$\underline{p(x_0)} \prod_{t=1}^n \underline{p(x_t | x_{t-1}, u_{t-1})} \underline{p(y_t | x_t)}$$



Derivation of Kalman filter - Overview

$$\underline{p(x_{0:n} | y_{1:n}, u_{1:n})} \propto p(x_0) \prod_{t=1}^n p(x_t | x_{t-1}, u_{t-1}) p(y_t | x_t)$$

$$\underline{KF : p(x_n | y_{1:n}, u_{1:n})}$$

