

# Lecture 2: Basics of Probability Theory

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## Interpretation of probability

# Knowledge-based interpretation



The probability of = how sure I am about the outcome of a coin toss experiments given all the information I have about the initial conditions of the tossing process

# Arguing logical/scientific propositions

- A: a logical sentence
- B: another logical sentence
- I: all the information we know

No other restriction apart that A and B are not contradictions.

# Notation shortcuts

$$\text{not } A \equiv \neg A$$

$$A \text{ and } B \equiv A, B \equiv AB$$

$$A \text{ or } B \equiv A + B$$

# Talking about probabilities

$p(A \mid BI)$  = the probability of A being true given that we know that B and I are true

*or (assuming I is implied)*

= the probability of A being true given that we know that B is true

*or (assuming arguments about truth are implied)*

= the probability of A given B

# Interpretation

$$p(A | B, I) \text{ in } [0,1]$$

quantifying the degree of plausibility that A is true given that B and I are true.

$p(A | B, I) = 1$       we are certain that A is **true** if B is true (and I)

$p(A | B, I) = 0$       we are certain that A is **false** if B is true (and I)

$0 < p(A | B, I) < 1$       we are uncertain about A if B is true (and I)

$p(A | B, I) = \frac{1}{2}$       we are completely ignorant about A if B is true (and I)