# Lecture 10: Quantifying uncertainties in Monte Carlo estimates

**Professor Ilias Bilionis** 

Visualizing Monte Carlo uncertainty



## Example: 1D

(This is Example 3.4 of Robert & Casella (2004))

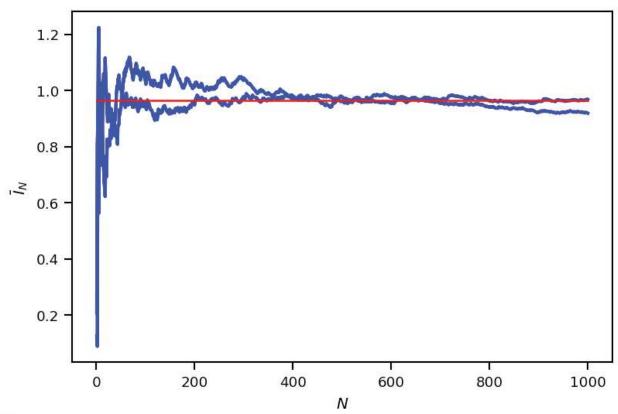
$$X \sim \mathcal{U}([0,1])$$

$$g(x) = \left(\cos(50x) + \sin(20x)\right)^2$$

The correct value for the integral is:

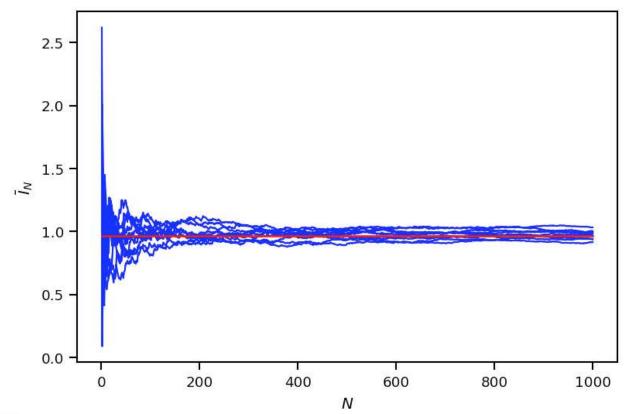
$$\mathbb{E}[g(X)] = 0.965$$

### Two different estimates





### Ten different estimates





#### 100 different estimates

