

Binary Trees

- an ordered tree w/ following properties:
 - 1.) each node has at most 2 children
 - 2.) each child node is labeled either left or right child
 - 3.) left child precedes a right child in order of children of a node
- the subtree rooted at a left or right child of an internal node v is called a left subtree or right subtree
- a binary tree is proper if each node has 0 or 2 children

Recursive Binary Tree Definition

- node r (root of T which stores an element
- binary tree called left subtree of T
- binary tree called right subtree of T

Binary Tree ADT

- $T.\text{left}(p)$: return position p that represents left child of p
 - $T.\text{right}(p)$: right child of p
 - $T.\text{sibling}(p)$: return position that represents sibling of p
- } returns None if empty

Tree Traversal Algorithms:

- a traversal of T is a systematic way of accessing all positions of T
- specific action performed upon visiting a node is specific to the algorithm

Preorder/Postorder Traversal

- in preorder traversal, the root of T is visited first and then the subtrees at its children are traversed recursively
 - if the tree is ordered, then the subtrees are traversed according to the order of the children

Algorithm preorder(T, p):

perform the "visit" action for position p
 for each child c in $T.\text{children}(p)$
 preorder(T, c)