UH Random Team Reference

Contents

1. TEMPLATE

1.1. MAIN.

```
#include <bits/stdc++.h>

#define MAX(a, b) (a > b) ? a : b
#define MIN(a, b) (a < b) ? a : b
#define int long long
#define vi vector<int>
#define pii pair<int, int>
#define vii vector<pii>

using namespace std;

void solve()
{
}

int32_t main()
{
   ios_base::sync_with_stdio(0);
   cin.tie(0);

   int t;
   cin >> t;

   for (int i = 0; i < t; i++)
   {
      solve();
   }

   return 0;
}
```

2. MATH

2.1. DISCRETE LOG.

```
int powmod(int a, int b, int m)
{
   int res = 1;
   while (b > 0)
   {
      if (b & 1)
      {
         res = (res * 1ll * a) % m;
      }
      a = (a * 1ll * a) % m;
      b >>= 1;
   }
   return res;
}

int discrete_log(int a, int b, int m)
{
   a %= m, b %= m;
   int n = sqrt(m) + 1;
   map<int, int> vals;
   for (int p = 1; p <= n; ++p)
      vals[powmod(a, p * n, m)] = p;
   for (int q = 0; q <= n; ++q)
   {
      int cur = (powmod(a, q, m) * 1ll * b) % m;
      if (vals.count(cur))
      {
         int ans = vals[cur] * n - q;
         return ans;
      }
   }
   return -1;
}
```

2.2. NTT.

```
using ll = long long;

const ll mod = (119 << 23) + 1, root = 62; // 998244353

ll qp(ll b, ll e)
{
   ll ans = 1;
   for (; e; b = b * b % mod, e /= 2)
      if (e & 1)
         ans = ans * b % mod;
   return ans;
}

void ntt(vector<ll> &a, vector<ll> &rt, vector<ll> &rev, int n)
{
   for (int i = 0; i < n; i++)
      if (i < rev[i])
         swap(a[i], a[rev[i]]);

   for (int k = 1; k < n; k *= 2)
      for (int i = 0; i < n; i += 2 * k)
         for (int j = 0; j < k; j++)
         {
            ll z = rt[j + k] * a[i + j + k] % mod, &ai = a[i + j];
            a[i + j + k] = (z > ai ? ai - z + mod : ai - z);
            ai += (ai + z >= mod ? z - mod : z);
         }
}

vector<ll> convolve(const vector<ll> &a, const vector<ll> &b)
{
   if (a.empty() || b.empty())
      return {};

   int s = a.size() + b.size() - 1, B = 32 - __builtin_clz(s), n = 1 << B;

   vector<ll> L(a), R(b), out(n), rt(n, 1), rev(n);
   L.resize(n), R.resize(n);

   for (int i = 0; i < n; i++)
      rev[i] = (rev[i / 2] | (i & 1) << B) / 2;

   ll curL = mod / 2, inv = qp(n, mod - 2);
   for (int k = 2; k < n; k *= 2)
   {
      ll z[] = {1, qp(root, curL /= 2)};
      for (int i = k; i < 2 * k; i++)
         rt[i] = rt[i / 2] * z[i & 1] % mod;
   }

   ntt(L, rt, rev, n);
   ntt(R, rt, rev, n);

   for (int i = 0; i < n; i++)
      out[-i & (n - 1)] = L[i] * R[i] % mod * inv % mod;

   ntt(out, rt, rev, n);

   return {out.begin(), out.begin() + s};
}
```

2.3. MATRIX POW.

```
const int MAXN = 2;

struct Matrix
{
   ll mat[MAXN][MAXN];
};

Matrix operator*(const Matrix &a, const Matrix &b)
{
   Matrix c;
   for (int i = 0; i < MAXN; ++i)
      for (int j = 0; j < MAXN; ++j)
         c.mat[i][j] = 0;

   for (int i = 0; i < MAXN; i++)
   {
      for (int k = 0; k < MAXN; k++)
      {
         if (a.mat[i][k] == 0)
            continue;
```

```
        for (int j = 0; j < MAXN; j++)
        {
          c.mat[i][j] += a.mat[i][k] * b.mat[k][j];
        }
      }
  }
  return c;
}
Matrix operator^(Matrix &base, ll e)
{
  Matrix c;
  for (int i = 0; i < MAXN; i++)
    for (int j = 0; j < MAXN; j++)
      c.mat[i][j] = (i == j);
  while (e)
  {
    if (e & 1ll)
      c = c * base;
    base = base * base;
    e >>= 1;
  }
  return c;
}
```

2.4. FFT.

```
struct point
{
  double x, y;
  point(double x = 0, double y = 0) : x(x), y(y) {}
};

point operator+(const point &a, const point &b)
{
  return {a.x + b.x, a.y + b.y};
}
point operator-(const point &a, const point &b)
{
  return {a.x - b.x, a.y - b.y};
}
point operator*(const point &a, const point &b)
{
  return {a.x * b.x - a.y * b.y, a.x * b.y + a.y * b.x};
}
point operator/(const point &a, double d) { return {a.x / d, a.y / d}; }

void fft(vector<point> &a, int sign = 1)
{
  int n = a.size(); // n should be a power of two
  double theta = 8 * sign * atan(1.0) / n;
  for (int i = 0, j = 1; j < n - 1; ++j)
  {
    for (int k = n >> 1; k > (i ^= k); k >>= 1)
      ;
    if (j < i)
      swap(a[i], a[j]);
  }
  for (int m, mh = 1; (m = mh << 1) <= n; mh = m)
  {
    int irev = 0;
    for (int i = 0; i < n; i += m)
    {
      point w = point(cos(theta * irev), sin(theta * irev));
      for (int k = n >> 2; k > (irev ^= k); k >>= 1)
        ;
      for (int j = i; j < mh + i; ++j)
      {
        int k = j + mh;
        point x = a[j] - a[k];
        a[j] = a[j] + a[k];
        a[k] = w * x;
      }
    }
  }
  if (sign == -1)
    for (auto &p : a)
      p = p / n;
}

vector<point> convolve(vector<point> &a, vector<point> &b)
{
  int n = a.size();
  int m = b.size();
  int k = n + m;
  while (k != (k & -k))
    k += (k & -k);
  while (a.size() < k)
    a.push_back(point(0, 0));
```

```
   while (b.size() < k)
      b.push_back(point(0, 0));

   fft(a, 1);
   fft(b, 1);

   vector<point> c(k);
   for (int i = 0; i < k; i++)
      c[i] = a[i] * b[i];

   fft(c, -1);

   return c;
}
```

2.5. PRIMITIVE ROOT.

```
int powmod(int a, int b, int p)
{
   int res = 1;
   while (b)
      if (b & 1)
         res = int32_t(res * 1ll * a % p), --b;
      else
         a = int32_t(a * 1ll * a % p), b >>= 1;
   return res;
}

int generator(int p)
{
   vector<int> fact;
   int phi = p - 1, n = phi;
   for (int i = 2; i * i <= n; ++i)
      if (n % i == 0)
      {
         fact.push_back(i);
         while (n % i == 0)
            n /= i;
      }
   if (n > 1)
      fact.push_back(n);

   for (int res = 2; res <= p; ++res)
   {
      bool ok = true;
      for (size_t i = 0; i < fact.size() && ok; ++i)
         ok &= powmod(res, phi / fact[i], p) != 1;
      if (ok)
         return res;
   }
   return -1;
}
```

2.6. FWHT.

```
using ll = long long;

const int mod = 1e9 + 7;

template <const int _mod_>
struct mod_int
{
   static const int mod = _mod_;
   int val;

   mod_int(long long v = 0)
   {
      if (v < 0)
         v = v % mod + mod;
      if (v >= mod)
         v %= mod;
      val = v;
   }

   static int mod_inv(int a, int m = mod)
   {
      int g = m, r = a, x = 0, y = 1;
      while (r != 0)
      {
         int q = g / r;
         g %= r;
         swap(g, r);
```

```cpp
            x -= q * y;
            swap(x, y);
        }
        return x < 0 ? x + m : x;
    }

    explicit operator int() const { return val; }

    mod_int &operator+=(const mod_int &other)
    {
        val += other.val;
        if (val >= mod)
            val -= mod;
        return *this;
    }

    mod_int &operator-=(const mod_int &other)
    {
        val -= other.val;
        if (val < 0)
            val += mod;
        return *this;
    }

    static unsigned fast_mod(uint64_t x, unsigned m = mod)
    {
#if !defined(_WIN32) || defined(_WIN64)
        return x % m;
#endif
        // Optimized mod for Codeforces 32-bit machines.
        // x must be less than 2^32 * m for this to work, so that x / m fits in
        // a 32-bit integer.
        unsigned x_high = x >> 32, x_low = (unsigned)x;
        unsigned quot, rem;
        asm("divl %4\n"
            : "=a"(quot), "=d"(rem)
            : "d"(x_high), "a"(x_low), "r"(m));
        return rem;
    }

    mod_int &operator*=(const mod_int &other)
    {
        val = fast_mod((uint64_t)val * other.val);
        return *this;
    }

    mod_int &operator/=(const mod_int &other) { return *this *= other.inv(); }

    friend mod_int operator+(const mod_int &a, const mod_int &b)
    {
        return mod_int(a) += b;
    }
    friend mod_int operator-(const mod_int &a, const mod_int &b)
    {
        return mod_int(a) -= b;
    }
    friend mod_int operator*(const mod_int &a, const mod_int &b)
    {
        return mod_int(a) *= b;
    }
    friend mod_int operator/(const mod_int &a, const mod_int &b)
    {
        return mod_int(a) /= b;
    }

    mod_int &operator++()
    {
        val = val == mod - 1 ? 0 : val + 1;
        return *this;
    }

    mod_int &operator--()
    {
        val = val == 0 ? mod - 1 : val - 1;
        return *this;
    }

    mod_int operator++(int)
    {
        mod_int a = *this;
        ++*this;
        return a;
    }
    mod_int operator--(int)
    {
        mod_int a = *this;
        --*this;
        return a;
    }
    mod_int operator-() const { return val == 0 ? 0 : mod - val; }
    mod_int inv() const { return mod_inv(val); }

    bool operator==(const mod_int &other) const { return val == other.val; }
    bool operator!=(const mod_int &other) const { return val != other.val; }
```

```cpp
    bool operator<(const mod_int &other) const { return val < other.val; }
    bool operator>(const mod_int &other) const { return val > other.val; }

    template <typename T>
    bool operator<(const T &other) const
    {
        return val < other;
    }

    template <typename T>
    bool operator>(const T &other) const
    {
        return val > other;
    }

    friend string to_string(const mod_int &m) { return to_string(m.val); }
    friend mod_int abs(const mod_int &m) { return mod_int(m.val); }

    friend ostream &operator<<(ostream &stream, const mod_int &m)
    {
        return stream << m.val;
    }
    friend istream &operator>>(istream &stream, mod_int &m)
    {
        return stream >> m.val;
    }
};

// Notar que se uso este tipo de datos entero, que implementa todas las
// operaciones basicos en el sistem residual modulo 10^9+7 para hacer mas
// faciles las implementaciones si se quiere implementarlo, se puede dejar en
// long long, y modificar las operaciones para mantener los resultados teneindo
// en cuenta el modulo a usar.
using T = mod_int<mod>;

void HADAMARD_XOR(vector<T> &a, bool inverse = false)
{
    int n = a.size();
    for (int k = 1; k < n; k <<= 1)
    {
        for (int i = 0; i < n; i += 2 * k)
        {
            for (int j = 0; j < k; j++)
            {
                T x = a[i + j];
                T y = a[i + j + k];
                a[i + j] = x + y;
                a[i + j + k] = x - y;
            }
        }
    }

    if (inverse)
    {
        T q = 1 / static_cast<T>(n);

        for (int i = 0; i < n; i++)
        {
            a[i] *= q;
        }
    }
}

void HADAMARD_AND(vector<T> &a, bool inverse = false)
{
    int n = a.size();
    for (int k = 1; k < n; k <<= 1)
    {
        for (int i = 0; i < n; i += 2 * k)
        {
            for (int j = 0; j < k; j++)
            {
                T x = a[i + j];
                T y = a[i + j + k];
                if (inverse)
                {
                    a[i + j] = -x + y;
                    a[i + j + k] = x;
                }
                else
                {
                    a[i + j] = y;
                    a[i + j + k] = x + y;
                }
            }
        }
    }
}

void HADAMARD_OR(vector<T> &a, bool inverse = false)
{
    int n = a.size();
    for (int k = 1; k < n; k <<= 1)
    {
```

```
      for (int i = 0; i < n; i += 2 * k)
      {
         for (int j = 0; j < k; j++)
         {
            T x = a[i + j];
            T y = a[i + j + k];
            if (inverse)
            {
               a[i + j] = y;
               a[i + j + k] = x - y;
            }
            else
            {
               a[i + j] = x + y;
               a[i + j + k] = x;
            }
         }
      }
   }
}

// Las demas operaciones a nivel de bit tienen una implementacion semejante
template <typename T>
vector<T> FWHT_XOR(vector<T> a, vector<T> b)
{
   bool eq = (a == b);
   int n = 1;

   while (n < (int)max(a.size(), b.size()))
   {
      n <<= 1;
   }

   a.resize(n);
   b.resize(n);

   HADAMARD_XOR(a);

   if (eq)
      b = a;
   else
      HADAMARD_XOR(b);

   for (int i = 0; i < n; i++)
   {
      a[i] *= b[i];
   }

   HADAMARD_XOR(a, true);

   return a;
}
```

2.7. EXTENDED EUCLIDEAN ALGORITHM.

```
int gcd(int a, int b, int &x, int &y)
{
   x = 1, y = 0;
   int x1 = 0, y1 = 1, a1 = a, b1 = b;
   while (b1)
   {
      int q = a1 / b1;
      tie(x, x1) = make_tuple(x1, x - q * x1);
      tie(y, y1) = make_tuple(y1, y - q * y1);
      tie(a1, b1) = make_tuple(b1, a1 - q * b1);
   }
   return a1;
}
```

3. GEOMETRY

3.1. BASICS.

```
db DEG_to_RAD(db d) { return d*M_PI / 180.0; }
db RAD_to_DEG(db r) { return r*180.0 / M_PI; }

db EPS = 1e-9;

struct point {
   db x, y;
```

```cpp
   point() { x = y = 0.0; }
   point(db _x, db _y) : x(_x), y(_y) {}

   bool operator < (const point &other) const {
      if (fabs(x-other.x) > EPS)
      return x < other.x;
      return y < other.y;
   }

   bool operator == (const point &other) const {
      return (fabs(x-other.x) < EPS) && (fabs(y-other.y) < EPS);
   }

   db dist(const point &other) {
      return hypot(x-other.x, y-other.y);
   }

   point rotate(db theta) {
      db rad = DEG_to_RAD(theta);
      return point(x*cos(rad) - y*sin(rad), x*sin(rad) + y*cos(rad));
   }
};

struct line {
   db a, b, c;
   line() {}
   line(db _a, db _b, db _c) : a(_a), b(_b), c(_c) {}

   void pointsToLine(const point &p1, const point &p2) {
      if (fabs(p1.x-p2.x) < EPS) {
         a = 1.0;
         b = 0.0;
         c = -p1.x;
      }
      else {
         a = -(db)(p1.y-p2.y) / (p1.x-p2.x);
         b = 1.0;
         c = -(db)(a*p1.x) - p1.y;
      }
   }

   void pointSlopeToLine(point p, db m) {
      a = -m;
      b = 1.0;
      c = -((a * p.x) + (b * p.y));
   }

   bool areParallel(const line &other) {
      return (fabs(a-other.a) < EPS) && (fabs(b-other.b) < EPS);
   }

   bool areSame(const line &other) {
      return areParallel(other) && (fabs(c-other.c) < EPS);
   }

   bool areIntersect(const line &other, point &p) {
      if (areParallel(other)) return false;
      p.x = (other.b*c - b*other.c) / (other.a*b - a*other.b);
      if (fabs(b) > EPS) p.y = -(a*p.x + c);
      else p.y = -(other.a*p.x + other.c);
      return true;
   }
};

struct vec{
   db x, y;
   vec(db _x, db _y) : x(_x), y(_y) {}
   vec(const point &a, const point &b) : x(b.x - a.x), y(b.y - a.y) {}

   vec scale(db s) {
      return vec(x*s, y*s);
   }

   point translate(const point &p) {
      return point(x+p.x, y+p.y);
   }

   db dot(vec a, vec b) { return a.x*b.x + a.y*b.y; }

   db norm_sq(vec v) { return v.x*v.x + v.y*v.y; }

   db angle(const point &a, const point &o, const point &b) {
      vec oa = vec(o, a), ob = vec(o, b);
      return acos(dot(oa, ob) / sqrt(norm_sq(oa) * norm_sq(ob)));
   }

   db cross(vec a, vec b) { return a.x*b.y - a.y*b.x; }

   bool ccw(point p, point q, point r) {
      return cross(vec(p, q), vec(p, r)) > EPS;
   }

   bool collinear(point p, point q, point r) {
      return fabs(cross(vec(p, q), vec(p, r))) < EPS;
```

```
    }

    db distToLine(point p, point a, point b) {
        vec ap = vec(a, p), ab = vec(a, b);
        db u = dot(ap, ab) / norm_sq(ab);
        point c = ab.scale(u).translate(a);
        return c.dist(p);
    }

    db distToLineSegment(point p, point a, point b) {
        vec ap = vec(a, p), ab = vec(a, b);
        db u = dot(ap, ab) / norm_sq(ab);
        if (u < 0.0) {
            point c = point(a.x, a.y);
            return c.dist(p);
        }
        if (u > 1.0) {
            point c = point(b.x, b.y);
            return c.dist(p);
        }
        return distToLine(p, a, b);
    }
};
```

```
struct circle {
    point c;
    db r;
    circle(const point &_c, db _r) : c(_c), r(_r) {}

    int inside(const point &p) {
        db dist = c.dist(p);
        return dist < r ? 1 : (fabs(dist-r) < EPS ? 0 : -1);
    }

    point inCircle(point p1, point p2, point p3) {
        line l1, l2;
        double ratio = p1.dist(p2) / p1.dist(p3);
        point p = vec(p2, p3).scale(ratio / (1+ratio)).translate(p2);
        l1.pointsToLine(p1, p);
        ratio = p2.dist(p1) / p2.dist(p3);
        p = vec(p1, p3).scale(ratio / (1+ratio)).translate(p1);
        l2.pointsToLine(p2, p);
        point c;
        l1.areIntersect(l2, c);
        return c;
    }
};
```

3.2. POLYGON.

```
struct polygon {
    vector<point> P;
    polygon(const vector<point> &_P) : P(_P) {}

    db perimeter() {
        db ans = 0.0;
        for (int i = 0; i < (int)P.size()-1; ++i)
            ans += P[i].dist(P[i+1]);
        return ans;
    }

    db area() {
        db ans = 0.0;
        for (int i = 0; i < (int)P.size()-1; ++i)
            ans += (P[i].x*P[i+1].y - P[i+1].x*P[i].y);
        return fabs(ans) / 2.0;
    }
```

```
    bool isConvex(const vector<point> &P) {
        int n = (int)P.size();
        if (n <= 3) return false;
        bool firstTurn = vec().ccw(P[0], P[1], P[2]);
        for (int i = 1; i < n-1; ++i)
            if (vec().ccw(P[i], P[i+1], P[(i+2) == n ? 1 : i+2]) != firstTurn)
                return false;
        return true;
    }

    int insidePolygon(point pt) {
        int n = (int)P.size();
        if (n <= 3) return -1;
        bool on_polygon = false;
        for (int i = 0; i < n-1; ++i)
            if (fabs(pt.dist(P[i]) + pt.dist(P[i+1]) - P[i].dist(P[i+1])) < EPS)
                on_polygon = true;
        if (on_polygon) return 0;
        double sum = 0.0;
```

```
      for (int i = 0; i < n-1; ++i) {
      if (vec().ccw(pt, P[i], P[i+1]))
         sum += vec().angle(P[i], pt, P[i+1]);
      else
         sum -= vec().angle(P[i], pt, P[i+1]);
      }
      return fabs(sum) > M_PI ? 1 : -1;
   }
};
```

4. DATA STRUCTURE

4.1. SEGMENT TREE.

```
class SegmentTree
{
private:
   vi values;

   vi p_values;
   int n;

   int left(int p) { return p << 1; };

   int right(int p) { return (p << 1) + 1; }

   int simple_node(int index) { return values[index]; }

   int prop(int x, int y) { return x + y; }

   void build(int p, int l, int r)
   {
      if (l == r)
      {
         p_values[p] = simple_node(l);
         return;
      }

      build(left(p), l, (l + r) / 2);
      build(right(p), (l + r) / 2 + 1, r);

      p_values[p] = prop(p_values[left(p)], p_values[right(p)]);
   }

   void set(int p, int l, int r, int i, int v)
   {
      if (l == r)
      {
         values[l] = v;
         p_values[p] = simple_node(l);
         return;
      }

      if (i <= (l + r) / 2)
         set(left(p), l, (l + r) / 2, i, v);
      else
         set(right(p), (l + r) / 2 + 1, r, i, v);

      p_values[p] = prop(p_values[left(p)], p_values[right(p)]);
   }

   int query(int p, int l, int r, int lq, int rq)
   {
      if (lq <= l && r <= rq)
         return p_values[p];

      int l1 = l, r1 = (l + r) / 2;
      int l2 = (l + r) / 2 + 1, r2 = r;

      if (l1 > rq || lq > r1)
         return query(right(p), l2, r2, lq, rq);
      if (l2 > rq || lq > r2)
         return query(left(p), l1, r1, lq, rq);

      int lt = query(left(p), l1, r1, lq, rq);
      int rt = query(right(p), l2, r2, lq, rq);

      return prop(lt, rt);
   }

public:
   SegmentTree(vi &a)
   {
      values = a;
      n = a.size();
      p_values.assign(4 * n, 0);
```

```
      build(1, 0, n - 1);
   }

   int query(int i, int j) { return query(1, 0, n - 1, i, j); }

   void set(int i, int v) { set(1, 0, n - 1, i, v); }

   int get(int i) { return values[i]; }
};
```

4.2. DISJOINT SET UNION.

```
struct dsu {
   vi p;
   void init(int n) {
      p = vi(n, -1);
   }
   int get(int x) {
      if (p[x] < 0)
         return x;
      return p[x] = get(p[x]);
   }
   void unite(int a, int b) {
      a = get(a);
      b = get(b);
      if (a != b) {
         if (p[a] > p[b])
            swap(a, b);
         p[a] += p[b];
         p[b] = a;
      }
   }
};
```

4.3. PBDS.

```
#include <bits/extc++.h> // pbds
using namespace __gnu_pbds;
typedef tree<int, null_type, less<int>, rb_tree_tag,
          tree_order_statistics_node_update>
   ost;

int main()
{
 int n = 9;
 int A[] = {2, 4, 7, 10, 15, 23, 50, 65, 71}; // as in Chapter 2
 ost tree;
 for (int i = 0; i < n; ++i) // O(n log n)
   tree.insert(A[i]);
 // O(log n) select
 cout << *tree.find_by_order(0) << "\n"; // 1-smallest = 2
 cout << *tree.find_by_order(n - 1) << "\n"; // 9-smallest/largest = 71
 cout << *tree.find_by_order(4) << "\n"; // 5-smallest = 15
 // O(log n) rank
 cout << tree.order_of_key(2) << "\n"; // index 0 (rank 1)
 cout << tree.order_of_key(71) << "\n"; // index 8 (rank 9)
 cout << tree.order_of_key(15) << "\n"; // index 4 (rank 5)
 return 0;
}
```

4.4. SEGMENT TREE LAZY.

```
class SegmentTreeLazy
{
private:
   vi values;
   vector<bool> lazy;
   vi l_values;
   vi p_values;
   int n;

   int left(int p) { return p << 1; };

   int right(int p) { return (p << 1) + 1; }
```

```
int simple_node(int index) { return values[index]; }

int prop(int x, int y) { return x + y; }

int prop_lazy(int x, int y) { return x + y; }

int prop_lazy_up(int x, int y, int s) { return x + y * s; }

void update_lazy(int p, int l, int r)
{
   if (l == r)
   {
      values[l] = prop_lazy(values[l], l_values[p]);
   }

   p_values[p] = prop_lazy_up(p_values[p], l_values[p], r - l + 1);
}

void propagate_lazy(int p, int l, int r)
{
   lazy[p] = false;

   if (l == r)
      return;

   l_values[left(p)] = lazy[left(p)]
                     ? prop_lazy(l_values[left(p)], l_values[p])
                     : l_values[p];
   l_values[right(p)] = lazy[right(p)]
                      ? prop_lazy(l_values[right(p)], l_values[p])
                      : l_values[p];

   lazy[left(p)] = true;
   lazy[right(p)] = true;
}

void build(int p, int l, int r)
{
   if (l == r)
   {
      p_values[p] = simple_node(l);
      return;
   }

   build(left(p), l, (l + r) / 2);
   build(right(p), (l + r) / 2 + 1, r);
   p_values[p] = prop(p_values[left(p)], p_values[right(p)]);
}

void set(int p, int l, int r, int i, int v)
{
   if (lazy[p])
   {
      update_lazy(p, l, r);
      propagate_lazy(p, l, r);
   }

   if (l == r)
   {
      values[l] = v;
      p_values[p] = simple_node(l);
      return;
   }

   if (i <= (l + r) / 2)
      set(left(p), l, (l + r) / 2, i, v);
   else
      set(right(p), (l + r) / 2 + 1, r, i, v);

   p_values[p] = prop(p_values[left(p)], p_values[right(p)]);
}

int query(int p, int l, int r, int lq, int rq)
{
   if (lazy[p])
   {
      update_lazy(p, l, r);
      propagate_lazy(p, l, r);
   }

   if (lq <= l && r <= rq)
      return p_values[p];

   int l1 = l, r1 = (l + r) / 2;
   int l2 = (l + r) / 2 + 1, r2 = r;

   if (l1 > rq || lq > r1)
      return query(right(p), l2, r2, lq, rq);
   if (l2 > rq || lq > r2)
      return query(left(p), l1, r1, lq, rq);

   int lt = query(left(p), l1, r1, lq, rq);
```

```
      int rt = query(right(p), l2, r2, lq, rq);

      return prop(lt, rt);
   }

   void set_rank(int p, int l, int r, int lq, int rq, int value)
   {
      if (lazy[p])
      {
         update_lazy(p, l, r);
         propagate_lazy(p, l, r);
      }

      if (l > rq || lq > r)
         return;

      if (lq <= l && r <= rq)
      {
         lazy[p] = true;
         l_values[p] = value;
         update_lazy(p, l, r);
         propagate_lazy(p, l, r);
         return;
      }

      set_rank(left(p), l, (l + r) / 2, lq, rq, value);
      set_rank(right(p), (l + r) / 2 + 1, r, lq, rq, value);

      p_values[p] = prop(p_values[left(p)], p_values[right(p)]);
   }

   int get(int p, int l, int r, int i)
   {
      if (lazy[p])
      {
         update_lazy(p, l, r);
         propagate_lazy(p, l, r);
      }

      if (l == r)
         return values[i];

      if (i <= (l + r) / 2)
         return get(left(p), l, (l + r) / 2, i);

      return get(right(p), (l + r) / 2 + 1, r, i);
   }

public:
   SegmentTreeLazy(vi &a)
   {
      values = a;
      n = a.size();
      p_values.assign(4 * n, 0);
      lazy.assign(4 * n, false);
      l_values.assign(4 * n, 0);
      build(1, 0, n - 1);
   }

   int query(int i, int j) { return query(1, 0, n - 1, i, j); }

   void set(int i, int v) { set(1, 0, n - 1, i, v); }

   void set_rank(int i, int j, int v) { set_rank(1, 0, n - 1, i, j, v); }

   int get(int i) { return get(1, 0, n - 1, i); }
};
```

4.5. AVL.

```
struct avl {
   int key;
   int height;
   int size;
   avl *left;
   avl *right;

   avl(int k) {
      key = k;
      height = 1;
      size = 1;
      left = NULL;
      right = NULL;
   }

   int getBalance() {
      int leftHeight = 0;
```

```
    int rightHeight = 0;

    if (left != NULL)
       leftHeight = left->height;

    if (right != NULL)
       rightHeight = right->height;

    return leftHeight - rightHeight;
 }

 void updateSize() {
    int leftSize = 0;
    int rightSize = 0;

    if (left != NULL)
       leftSize = left->size;

    if (right != NULL)
       rightSize = right->size;

    size = leftSize + rightSize + 1;
 }

 void updateHeight() {
    int leftHeight = 0;
    int rightHeight = 0;

    if (left != NULL)
       leftHeight = left->height;

    if (right != NULL)
       rightHeight = right->height;

    height = max(leftHeight, rightHeight) + 1;
 }

 avl *rotateLeft() {
    avl *newRoot = right;
    right = newRoot->left;
    newRoot->left = this;
    updateHeight();
    newRoot->updateHeight();
    return newRoot;
 }

 avl *rotateRight() {
    avl *newRoot = left;
    left = newRoot->right;
    newRoot->right = this;
    updateHeight();
    newRoot->updateHeight();
    return newRoot;
 }

 avl *balance() {
    updateHeight();
    updateSize();
    int balance = getBalance();

    if (balance == 2) {
       if (left->getBalance() < 0)
          left = left->rotateLeft();
       return rotateRight();
    }

    if (balance == -2) {
       if (right->getBalance() > 0)
          right = right->rotateRight();
       return rotateLeft();
    }

    return this;
 }

 avl *insert(int k) {
    if (k < key) {
       if (left == NULL)
          left = new avl(k);
       else
          left = left->insert(k);
    }
    else {
       if (right == NULL)
          right = new avl(k);
       else
          right = right->insert(k);
    }

    return balance();
 }

 avl *findMin() {
    if (left == NULL)
```

```
         return this;
      else
         return left->findMin();
   }

   avl *removeMin() {
      if (left == NULL)
         return right;
      left = left->removeMin();
      return balance();
   }

   avl *remove(int k) {
      if (k < key)
         left = left->remove(k);
      else if (k > key)
         right = right->remove(k);
      else {
         avl *leftChild = left;
         avl *rightChild = right;

         delete this;

         if (rightChild == NULL)
            return leftChild;

         avl *min = rightChild->findMin();
         min->right = rightChild->removeMin();
         min->left = leftChild;
         return min->balance();
      }

      return balance();
   }

   int getRank(int k) {
      if (k < key) {
         if (left == NULL)
            return 0;
         else
            return left->getRank(k);
      }
      else if (k > key) {
         if (right == NULL)
            return 1 + left->size;
         else
            return 1 + left->size + right->getRank(k);
      }
      else
         return left->size;
   }

   int getKth(int k) {
      if (k < left->size)
         return left->getKth(k);
      else if (k > left->size)
         return right->getKth(k - left->size - 1);
      else
         return key;
   }

   static avl *join(avl *left, avl *right) {
      if (left->height < right->height) {
         right->left = join(left, right->left);
         return right->balance();
      }
      else if (left->height > right->height) {
         left->right = join(left->right, right);
         return left->balance();
      }
      else {
         avl *min = right->findMin();
         min->right = right->removeMin();
         min->left = left;
         return min->balance();
      }
   }

   pair<avl *, avl *> split(int k) {
      if (k < key) {
         pair<avl *, avl *> p = left->split(k);
         left = p.second;
         return {p.first, join(this, left)};
      }
      else {
         pair<avl *, avl *> p = right->split(k);
         right = p.first;
         return {join(this, right), p.second};
      }
   }
};
```

4.6. ABI.

```
class Abi
{

private:
   vi p;
   int _size;

   int ls_one(int i) { return i & (-i); }

public:
   Abi(int n)
   {
      _size = n;
      p.assign(n + 1, 0);
   }

   int rsq(int k)
   {
      int sum = 0;

      for (int i = k; i > 0; i -= ls_one(i))
      {
         sum += p[i];
      }

      return sum;
   }

   int sum(int a, int b) { return rsq(b) - rsq(a - 1); }

   void adjust_sum(int k, int v)
   {
      for (int i = k; i < p.size(); i += ls_one(i))
         p[i] += v;
   }

   int size()
   {
      return _size;
   }
};
```

4.7. MOS.

```
void remove(int idx); // TODO: remove value at idx from data structure
void add(int idx); // TODO: add value at idx from data structure
int get_answer(); // TODO: extract the current answer of the data structure

int block_size;

struct Query
{
   int l, r, idx;
   bool operator<(Query other) const
   {
      return make_pair(l / block_size, r) <
           make_pair(other.l / block_size, other.r);
   }
};

vector<int> mo_s_algorithm(vector<Query> queries)
{
   vector<int> answers(queries.size());
   sort(queries.begin(), queries.end());

   // TODO: initialize data structure

   int cur_l = 0;
   int cur_r = -1;
   // invariant: data structure will always reflect the range [cur_l, cur_r]
   for (Query q : queries)
   {
      while (cur_l > q.l)
      {
         cur_l--;
         add(cur_l);
      }
      while (cur_r < q.r)
      {
         cur_r++;
         add(cur_r);
```

```
      }
      while (cur_l < q.l)
      {
         remove(cur_l);
         cur_l++;
      }
      while (cur_r > q.r)
      {
         remove(cur_r);
         cur_r--;
      }
      answers[q.idx] = get_answer();
   }
   return answers;
}
```

4.8. SQRT DECOMPOSITION.

```
struct sqd {
   int n;
   int b;
   vi a;
   vi bsum;
   sqd(vi &a) {
      n = a.size();
      b = sqrt(n);
      this->a = a;
      bsum.assign(b + 1, 0);
      for (int i = 0; i < n; i++)
         bsum[i / b] += a[i];
   }
   void update(int i, int v) {
      bsum[i / b] += v - a[i];
      a[i] = v;
   }
   int query(int l, int r) {
      int sum = 0;
      for (int i = l; i <= r; i++)
         if (i % b == 0 && i + b - 1 <= r) {
            sum += bsum[i / b];
            i += b - 1;
         } else
            sum += a[i];
      return sum;
   }
};
```

5. STRING

5.1. SUFFIX ARRAY.

```
class SuffixArray
{

public:
   SuffixArray(string s)
   {
      n = s.size() + 1;
      s_value = s + "$";

      ra.assign(n, 0);
      sa.assign(n, 0);
      temp_ra.assign(n, 0);
      temp_sa.assign(n, 0);
      construct_sa();
      build_lcp();
   }

   int size() { return n; }

   int get_int(int i) { return sa[i]; }

   int cant_match(string p)
   {
      pii ans = matching(p);

      if (ans.first == -1 && ans.second == -1)
         return 0;
```

```
        return ans.second - ans.first + 1;
    }

    int get_lcp(int i) { return plcp[sa[i]]; }

    int cant_substr() { return v_cant_substr; }

    string get_str(int i) { return s_value.substr(sa[i], n - sa[i] - 1); }

private:
    string s_value;
    int n;
    int v_cant_substr;

    vi ra;
    vi sa;
    vi c;
    vi temp_ra;
    vi temp_sa;
    vi phi;
    vi plcp;

    void counting_sort(int k)
    {
        int sum = 0;
        int maxi = max((int)300, n);

        c.assign(maxi, 0);

        for (int i = 0; i < n; i++)
            c[i + k < n ? ra[i + k] : 0]++;

        for (int i = 0; i < maxi; i++)
        {
            int tx = c[i];
            c[i] = sum;
            sum += tx;
        }

        for (int i = 0; i < n; i++)
            temp_sa[c[sa[i] + k < n ? ra[sa[i] + k] : 0]++] = sa[i];

        for (int i = 0; i < n; i++)
            sa[i] = temp_sa[i];
    }
```

```
    void construct_sa()
    {
        int k, r;

        for (int i = 0; i < n; i++)
        {
            ra[i] = s_value[i];
            sa[i] = i;
        }

        for (k = 1; k < n; k <<= 1)
        {
            counting_sort(k);
            counting_sort(0);

            temp_ra[sa[0]] = r = 0;

            for (int i = 1; i < n; i++)
                temp_ra[sa[i]] = (ra[sa[i]] == ra[sa[i - 1]] && ra[sa[i] + k] == ra[sa

            for (int i = 0; i < n; i++)
                ra[i] = temp_ra[i];

            if (ra[sa[n - 1]] == n - 1)
                break;
        }
    }

    pii matching(string p)
    {
        int l = 0;
        int r = n - 1;
        int p_size = p.size();

        string comp;

        while (l < r)
        {
            int m = (l + r) / 2;

            comp = s_value.substr(sa[m], min(n - sa[m], p_size));

            if (comp >= p)
                r = m;
            else
                l = m + 1;
        }
```

```
        comp = s_value.substr(sa[l], min(n - sa[l], p_size));

        if (comp != p)
            return {-1, -1};

        int ans_l = l;

        l = 0;
        r = n - 1;

        while (l < r)
        {
            int m = (l + r) / 2;

            comp = s_value.substr(sa[m], min(n - sa[m], p_size));

            if (comp > p)
                r = m;
            else
                l = m + 1;
        }

        comp = s_value.substr(sa[r], min(n - sa[r], p_size));

        if (comp != p)
            r--;

        int ans_r = r;

        return {ans_l, ans_r};
    }

    void build_lcp()
    {
        phi.assign(n, 0);
        plcp.assign(n, 0);

        phi[0] = -1;

        for (int i = 1; i < n; i++)
            phi[sa[i]] = sa[i - 1];

        int l = 0;
        int q = 0;
        for (int i = 0; i < n; i++)
        {
            if (phi[i] == -1)
            {
                plcp[i] = 0;
                continue;
            }

            while (s_value[i + l] == s_value[phi[i] + l])
                l++;

            plcp[i] = l;
            q += l;
            l = max(l - 1, (int)0);
        }

        v_cant_substr = n * (n - 1) / 2 - q;
    }
};
```

5.2. Z FUNCTION.

```
// Z[i] is the length of the longest substring
// starting from S[i] which is also a prefix of S.
vi z_function(string s)
{
    int n = (int)s.length();
    vi z(n);

    for (int i = 1, l = 0, r = 0; i < n; ++i)
    {
        if (i <= r)
            z[i] = min(r - i + 1, z[i - l]);
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
            ++z[i];
        if (i + z[i] - 1 > r)
            l = i, r = i + z[i] - 1;
    }
    return z;
}

// suff[i] = length of the longest common suffix of s and s[0..i]
vi suffixes(const string &s)
{
```

```
   int n = s.length();

   vi suff(n, n);

   for (int i = n - 2, g = n - 1, f; i >= 0; --i)
   {
      if (i > g && suff[i + n - 1 - f] != i - g)
         suff[i] = min(suff[i + n - 1 - f], i - g);
      else
      {
         for (g = min(g, f = i); g >= 0 && s[g] == s[g + n - 1 - f]; --g)
            ;
         suff[i] = f - g;
      }
   }

   return suff;
}
```

5.3. HASHING.

```
struct custom_hash
{
   static uint64_t splitmix64(uint64_t x)
   {
      x += 0x9e3779b97f4a7c15;
      x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
      x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
      return x ^ (x >> 31);
   }

   size_t operator()(uint64_t x) const
   {
      static const uint64_t FIXED_RANDOM =
         chrono::steady_clock::now().time_since_epoch().count();
      return splitmix64(x + FIXED_RANDOM);
   }
};

const int MAXN = 5e5 + 5;
const int MOD = 1e9 + 7;
int mod_pow(int b, int e)
{
   int res = 1;
   while (e)
   {
      if (e & 1)
         res = res * b % MOD;
      b = b * b % MOD;
      e >>= 1;
   }
   return res % MOD;
}

typedef unordered_map<ll, ll, custom_hash> safe_map;

int dx[] = {1, 0, -1, 0, 1, -1, -1, 1};
int dy[] = {0, 1, 0, -1, 1, 1, -1, -1};

int dp[MAXN];
vi ady_list[MAXN];

int n, m, t, k;
int f[MAXN];
int comb(int n, int k)
{
   int fk = mod_pow(f[k], MOD - 2);
   int fnk = mod_pow(f[n - k], MOD - 2);
   int x = ((f[n] * fk) % MOD * fnk % MOD);

   return x;
}
```

5.4. KMP PF.

```
vi prefix_function(string p)
{
   vi pf(p.size());
   pf[0] = 0;
   int k = 0;

   for (int i = 1; i < p.size(); i++)
```

```
  {
    while (k > 0 && p[k] != p[i])
      k = pf[k - 1];

    if (p[k] == p[i])
      k++;

    pf[i] = k;
  }

  return pf;
}

vi kmp(string t, string p)
{
  vi result;
  vi pf = prefix_function(p);
  int k = 0;

  for (int i = 0; i < t.size(); i++)
  {
    while (k > 0 && p[k] != t[i])
      k = pf[k - 1];

    if (p[k] == t[i])
      k++;

    if (k == p.size())
    {
      result.push_back(i - (p.size() - 1));
      k = pf[k - 1];
    }
  }

  return result;
}
```

5.5. TRIE.

```
class Trie
{
private:
  int cant_string;
  int cant_string_me;
  int cant_node;
  char value;
  Trie *children[alphabet];

public:
  Trie(char a)
  {
    cant_string = 0;
    cant_node = 1;
    cant_string_me = 0;
    value = a;

    for (int i = 0; i < alphabet; i++)
      children[i] = NULL;
  }

  pair<Trie *, int> search(string s)
  {
    Trie *node = this;
    int i = 0;

    while (i < s.size() && node->children[s[i] - first_char] != NULL)
    {
      node = node->children[s[i] - first_char];

      i++;
    }

    return {node, i};
  }

  void insert(string s)
  {
    int q = s.size() - search(s).second;

    Trie *node = this;

    for (int i = 0; i < s.size(); i++)
    {
      node->cant_node += q;

      if (node->children[s[i] - first_char] == NULL)
      {
        node->children[s[i] - first_char] = new Trie(s[i]);
        q--;
```

```
            }

            node = node->children[s[i] - first_char];
            node->cant_string_me++;
        }

        node->cant_string++;
    }

    void eliminate(string s)
    {
        if (!contains(s))
            return;

        Trie *node = this;
        int q = 0;

        for (int i = 0; i < s.size(); i++)
        {
            if (node->children[s[i] - first_char] == NULL)
            {
                node->children[s[i] - first_char] = new Trie(s[i]);
            }

            if (node->children[s[i] - first_char]->cant_string_me == 1)
            {
                node->children[s[i] - first_char] = NULL;

                q = s.size() - i;
                break;
            }

            node = node->children[s[i] - first_char];
            node->cant_string_me--;

            if (i == s.size() - 1)
                node->cant_string--;
        }

        node = this;

        for (int i = 0; i < s.size() - q + 1; i++)
        {
            node->cant_node -= q;
            node = node->children[s[i] - first_char];
        }
    }

    bool contains(string s)
    {
        auto q = search(s);
        return q.second == s.size() && q.first->cant_string >= 1;
    }

    int cant_words_me() { return cant_string_me; }

    int cant_words() { return cant_string; }

    Trie *get(char a) { return children[a - first_char]; }

    int size() { return cant_node; }
};
```

6. GRAPH

6.1. TOPOLOGICAL SORT.

```
vector<int> topoSort(int V, vector<int> adj[])
{
    vector<int> in(V);
    vector<int> resp;

    for (int i = 0; i < V; i++)
    {
        for (int j = 0; j < adj[i].size(); j++)
        {
            in[adj[i][j]]++;
        }
    }

    queue<int> q;

    for (int i = 0; i < V; i++)
    {
        if (in[i] == 0)
            q.push(i);
    }
```

```
    while (q.size() != 0)
    {
        int n = q.front();
        q.pop();

        for (int i = 0; i < adj[n].size(); i++)
        {
            in[adj[n][i]]--;
            if (in[adj[n][i]] == 0)
                q.push(adj[n][i]);
        }

        resp.push_back(n);
    }

    return resp;
}
```

6.2. DIJSKTRA.

```
int infinite = (int)1e9;

// O(V^2)
vector<int> dijkstra1(int V, vector<vector<int>> adj[], int S)
{
    vector<int> d;

    d.assign(V, infinite);
    d[S] = 0;

    vector<bool> mask;

    mask.assign(V, false);

    for (int i = 0; i < V; i++)
    {
        int m = infinite;
        int act = -1;

        for (int j = 0; j < V; j++)
        {
            if (mask[j])
                continue;

            if (m > d[j])
            {
                m = d[j];
                act = j;
            }
        }

        for (int j = 0; j < adj[act].size(); j++)
        {
            if (d[act] + adj[act][j][1] < d[adj[act][j][0]])
            {
                d[adj[act][j][0]] = d[act] + adj[act][j][1];
            }
        }

        mask[act] = true;
    }

    return d;
}

// O((V+E)log(E))
vi dijkstra2(int V, vii adj[], int S)
{
    vector<int> d;

    d.assign(V, infinite);
    d[S] = 0;

    priority_queue<pair<int, int>> q;
    q.push({d[S], S});

    while (!q.empty())
    {
        int act = q.top().second;
        int m = abs(q.top().first);
        q.pop();

        if (m > d[act])
            continue;

        for (int j = 0; j < adj[act].size(); j++)
```

```
      {
         if (d[act] + adj[act][j].second < d[adj[act][j].first])
         {
            d[adj[act][j].first] = d[act] + adj[act][j].second;
            q.push({-d[adj[act][j].first], adj[act][j].first});
         }
      }
   }

   return d;
}
```

6.3. BRIDGE EDGES.

```
vector<bool> visited;
vector<int> t;
vector<int> low;
set<pair<int, int>> bridges;

void dfs_bridges(vector<int> adj[], int n, int p, int q)
{
   t[n] = q;
   low[n] = q++;
   visited[n] = true;

   int j = 0;

   for (int i = 0; i < adj[n].size(); i++)
   {
      if (!visited[adj[n][i]])
      {
         dfs_bridges(adj, adj[n][i], n, q);
         low[n] = min(low[adj[n][i]], low[n]);
         j++;
      }
      else if (adj[n][i] != p)
      {
         low[n] = min(t[adj[n][i]], low[n]);
      }
   }

   if (t[n] == low[n] && p != -1)
   {
      bridges.insert({min(n, p), max(n, p)});
   }
}

set<pair<int, int>> bridge_edges(int V, vector<int> adj[])
{
   visited.assign(V, false);
   t.assign(V, -1);
   low.assign(V, -1);
   bridges = set<pair<int, int>>();

   for (int i = 0; i < V; i++)
   {
      if (!visited[i])
      {
         dfs_bridges(adj, i, -1, 1);
      }
   }

   return bridges;
}
```

6.4. PRIM.

```
int spanningTreePrim(int V, vector<vector<int>> adj[])
{

   priority_queue<pair<int, int>> q;

   vector<bool> mask;
   mask.assign(V, false);
   mask[0] = true;

   int cost = 0;

   for (int i = 0; i < adj[0].size(); i++)
   {
      q.push({-adj[0][i][1], adj[0][i][0]});
   }
```

```
   while (q.size() != 0)
   {
      auto aux = q.top();
      q.pop();

      int k = aux.second;
      if (mask[k])
         continue;

      mask[k] = true;
      cost += abs(aux.first);
      for (int i = 0; i < adj[k].size(); i++)
      {
         if (!mask[adj[k][i][0]])
         {
            q.push({-adj[k][i][1], adj[k][i][0]});
         }
      }
   }

   return cost;
}
```

6.5. KRUSKAL.

```
class ufds
{
private:
   vector<int> p, rank, sizeSet;
   int disjoinSet;

public:
   ufds(int n)
   {
      p.assign(n, 0);
      rank.assign(n, 0);
      sizeSet.assign(n, 1);
      disjoinSet = n;
      for (int i = 0; i < n; i++)
      {
         p[i] = i;
      }
   }

   int find(int n)
   {
      if (n == p[n])
         return n;
      p[n] = find(p[n]);
      return p[n];
   }

   bool isSameSet(int i, int j) { return find(i) == find(j); }

   void unionSet(int i, int j)
   {
      if (!isSameSet(i, j))
      {
         disjoinSet--;
         int x = find(i);
         int y = find(j);
         if (rank[x] > rank[y])
         {
            p[y] = x;
            sizeSet[x] += sizeSet[y];
         }
         else
         {
            p[x] = y;
            sizeSet[y] += sizeSet[x];
            if (rank[x] == rank[y])
               rank[y]++;
         }
      }
   }

   int numDisjoinset() { return disjoinSet; }

   int sizeofSet(int i) { return sizeSet[find(i)]; }
};

// Function to find sum of weights of edges of the Minimum Spanning Tree.
int spanningTreeKruskal(int V, vector<vector<int>> adj[])
{
   ufds dsu(V);

   vector<pair<int, pair<int, int>>> a;
```

```
   for (int i = 0; i < V; i++)
   {
      for (int j = 0; j < adj[i].size(); j++)
      {
         a.push_back({adj[i][j][1], {i, adj[i][j][0]}});
      }
   }

   sort(a.begin(), a.end());

   int cost = 0;

   for (int i = 0; i < a.size(); i++)
   {
      if (!dsu.isSameSet(a[i].second.first, a[i].second.second))
      {
         cost += a[i].first;

         dsu.unionSet(a[i].second.first, a[i].second.second);
      }
   }

   return cost;
}
```

6.6. BELLMAN FORD.

```
int infinite = (int)1e9;

vector<int> bellman_ford(int V, vector<vector<int>> &edges, int S)
{
   vector<int> d;
   d.assign(V, infinite);
   d[S] = 0;

   for (int i = 0; i < V - 1; i++)
   {
      for (int j = 0; j < edges.size(); j++)
      {
         if (d[edges[j][0]] + edges[j][2] < d[edges[j][1]])
         {
            d[edges[j][1]] = d[edges[j][0]] + edges[j][2];
         }
      }
   }

   for (int j = 0; j < edges.size(); j++)
   {
      if (d[edges[j][0]] + edges[j][2] < d[edges[j][1]])
      {
         vector<int> resp(1);
         resp[0] = -1;

         return resp;
      }
   }

   return d;
}
```

6.7. DINIC.

```
template <typename flow_type>
struct dinic
{
   struct edge
   {
      size_t src, dst, rev;
      flow_type flow, cap;
   };

   int n;

   vector<vector<edge>> adj;

   dinic(int n) : n(n), adj(n), level(n), q(n), it(n) {}

   void add_edge(size_t src, size_t dst, flow_type cap, flow_type rcap = 0)
   {
      adj[src].push_back({src, dst, adj[dst].size(), 0, cap});
      if (src == dst)
         adj[src].back().rev++;
      adj[dst].push_back({dst, src, adj[src].size() - 1, 0, rcap});
```

```
    }

    vector<int> level, q, it;

    bool bfs(int source, int sink)
    {
        fill(level.begin(), level.end(), -1);
        for (int qf = level[q[0] = sink] = 0, qb = 1; qf < qb; ++qf)
        {
            sink = q[qf];
            for (edge &e : adj[sink])
            {
                edge &r = adj[e.dst][e.rev];
                if (r.flow < r.cap && level[e.dst] == -1)
                    level[q[qb++] = e.dst] = 1 + level[sink];
            }
        }
        return level[source] != -1;
    }

    flow_type augment(int source, int sink, flow_type flow)
    {
        if (source == sink)
            return flow;
        for (; it[source] != adj[source].size(); ++it[source])
        {
            edge &e = adj[source][it[source]];
            if (e.flow < e.cap && level[e.dst] + 1 == level[source])
            {
                flow_type delta = augment(e.dst, sink, min(flow, e.cap - e.flow));
                if (delta > 0)
                {
                    e.flow += delta;
                    adj[e.dst][e.rev].flow -= delta;
                    return delta;
                }
            }
        }
        return 0;
    }

    flow_type max_flow(int source, int sink)
    {
        for (int u = 0; u < n; ++u)
            for (edge &e : adj[u])
                e.flow = 0;
        flow_type flow = 0;
        flow_type oo = numeric_limits<flow_type>::max();

        while (bfs(source, sink))
        {
            fill(it.begin(), it.end(), 0);
            for (flow_type f; (f = augment(source, sink, oo)) > 0;)
                flow += f;

        } // level[u] = -1 => source side of min cut
        return flow;
    }
};
```

6.8. CENTROID DESCOMPOSITION.

```
const int MAXN = 2e5 + 5;

vi ady[MAXN];

bitset<MAXN> is_centroid;

int sz[MAXN], ct_par[MAXN];
void centroid_dfs(int node, int parent)
{
    sz[node] = 1;
    for (int &nxt : ady[node])
    {
        if (is_centroid[nxt] || nxt == parent)
            continue;
        centroid_dfs(nxt, node);
        sz[node] += sz[nxt];
    }
}
int get_centroid(int node, int parent, int tree_sz)
{
    for (int nxt : ady[node])
    {
        if (is_centroid[nxt] || nxt == parent)
            continue;
        if (sz[nxt] * 2 > tree_sz)
            return get_centroid(nxt, node, tree_sz);
```

```
    }
    return node;
}
void centroid_decomp(int node, int parent = -1)
{
    centroid_dfs(node, -1);
    int tree_sz = sz[node];
    int centroid = get_centroid(node, -1, tree_sz);
    is_centroid[centroid] = 1;
    ct_par[centroid] = parent;

    for (int &child : ady[centroid])
    {
        if (is_centroid[child])
            continue;
        centroid_decomp(child, centroid);
    }
}
```

```
void solve()
{
}

int32_t main()
{
    ios_base::sync_with_stdio(0);
    cin.tie(0);

    int t;
    cin >> t;

    for (int i = 0; i < t; i++)
    {
        solve();
    }

    return 0;
}
```

6.9. LOWER BOUND FLOW.

```
template <typename T>
struct dinic
{
    struct edge
    {
        int src, dst;
        T low, cap, flow;
        int rev;
    };

    int n;
    vector<vector<edge>> adj;

    dinic(int n) : n(n), adj(n + 2) {}

    void add_edge(int src, int dst, T low, T cap)
    {
        adj[src].push_back({src, dst, low, cap, 0, (int)adj[dst].size()});
        if (src == dst)
            adj[src].back().rev++;
        adj[dst].push_back({dst, src, 0, 0, 0, (int)adj[src].size() - 1});
    }
```

```
    vector<int> level, iter;

    T augment(int u, int t, T cur)
    {
        if (u == t)
            return cur;
        for (int &i = iter[u]; i < (int)adj[u].size(); ++i)
        {
            edge &e = adj[u][i];
            if (e.cap - e.flow > 0 && level[u] > level[e.dst])
            {
                T f = augment(e.dst, t, min(cur, e.cap - e.flow));
                if (f > 0)
                {
                    e.flow += f;
                    adj[e.dst][e.rev].flow -= f;
                    return f;
                }
            }
        }
        return 0;
    }

    int bfs(int s, int t)
```

```
    {
        level.assign(n + 2, n + 2);
        level[t] = 0;
        queue<int> Q;
        for (Q.push(t); !Q.empty(); Q.pop())
        {
            int u = Q.front();
            if (u == s)
                break;
            for (edge &e : adj[u])
            {
                edge &erev = adj[e.dst][e.rev];
                if (erev.cap - erev.flow > 0 && level[e.dst] > level[u] + 1)
                {
                    Q.push(e.dst);
                    level[e.dst] = level[u] + 1;
                }
            }
        }
        return level[s];
    }

    const T oo = numeric_limits<T>::max();

    T max_flow(int source, int sink)
    {
        vector<T> delta(n + 2);

        for (int u = 0; u < n; ++u) // initialize
            for (auto &e : adj[u])
            {
                delta[e.src] -= e.low;
                delta[e.dst] += e.low;
                e.cap -= e.low;
                e.flow = 0;
            }

        T sum = 0;
        int s = n, t = n + 1;

        for (int u = 0; u < n; ++u)
        {
            if (delta[u] > 0)
            {
                add_edge(s, u, 0, delta[u]);
                sum += delta[u];
            }
            else if (delta[u] < 0)
                add_edge(u, t, 0, -delta[u]);
        }

        add_edge(sink, source, 0, oo);
        T flow = 0;

        while (bfs(s, t) < n + 2)
        {
            iter.assign(n + 2, 0);
            for (T f; (f = augment(s, t, oo)) > 0;)
                flow += f;
        }

        if (flow != sum)
            return -1; // no solution

        for (int u = 0; u < n; ++u)
            for (auto &e : adj[u])
            {
                e.cap += e.low;
                e.flow += e.low;
                edge &erev = adj[e.dst][e.rev];
                erev.cap -= e.low;
                erev.flow -= e.low;
            }

        adj[sink].pop_back();
        adj[source].pop_back();

        while (bfs(source, sink) < n + 2)
        {
            iter.assign(n + 2, 0);
            for (T f; (f = augment(source, sink, oo)) > 0;)
                flow += f;
        } // level[u] == n + 2 ==> s-side

        return flow;
    }
};
```

6.10. FLOYD WARSHALL.

```
int infinite = (int)1e8;

void shortest_distance(vector<vector<int>> &matrix)
{
   for (int k = 0; k < matrix.size(); k++)
   {
      for (int i = 0; i < matrix.size(); i++)
      {
         for (int j = 0; j < matrix[0].size(); j++)
         {
            matrix[i][j] = min(matrix[i][j], matrix[i][k] + matrix[k][j]);
         }
      }
   }
}

void find_path_k(vector<vector<bool>> &matrix, int k)
{
   for (int x = 0; x < k; x++)
   {
      for (int i = 0; i < matrix.size(); i++)
      {
         for (int j = 0; j < matrix[0].size(); j++)
         {
            matrix[i][j] = matrix[i][j] || (matrix[i][x] && matrix[x][j]);
         }
      }
   }
}
```

6.11. DFS BFS.

```
void dfs_g(int n, int c, vi adj[], vector<bool> &visited, vi &cc)
{
   visited[n] = true;
   cc[n] = c;

   for (int i = 0; i < adj[n].size(); i++)
   {
      if (!visited[adj[n][i]])
         dfs_g(adj[n][i], c, adj, visited, cc);
   }
}

void dfs_t(int n, int p, int d, vi adj[], vi &deep)
{
   deep[n] = d;

   for (int i = 0; i < adj[n].size(); i++)
   {
      if (p != adj[n][i])
         dfs_t(adj[n][i], n, d + 1, adj, deep);
   }
}

vi bfs(int node, int n, vi adj[])
{
   vi result(n);
   vector<bool> visited;
   visited.assign(n, false);

   queue<int> q;
   visited[node] = true;

   q.push(node);

   while (q.size() != 0)
   {
      int w = q.front();
      q.pop();

      for (int i = 0; i < adj[w].size(); i++)
      {
         if (!visited[adj[w][i]])
         {
            q.push(adj[w][i]);
            result[adj[w][i]] = result[w] + 1;
            visited[adj[w][i]] = true;
         }
      }
   }

   return result;
}
```

6.12. SCC TARJANS.

```
stack<int> q;
vector<bool> mask;
vector<int> cc_list;

void g_transp(int V, vector<int> adj[], vector<int> new_adj[])
{
   for (int i = 0; i < V; i++)
   {
      for (int j = 0; j < adj[i].size(); j++)
      {
         new_adj[adj[i][j]].push_back(i);
      }
   }
}

void dfs_visit(int n, vector<int> adj[], int cc)
{
   mask[n] = true;

   for (int i = 0; i < adj[n].size(); i++)
   {
      if (!mask[adj[n][i]])
         dfs_visit(adj[n][i], adj, cc);
   }

   if (cc == -1)
      q.push(n);
   else
   {
      cc_list[n] = cc;
   }
}

void tarjans(int V, vector<int> adj[])
{
   vector<int> new_adj[V];
   g_transp(V, adj, new_adj);

   mask.assign(V, false);
   cc_list.assign(V, -1);

   for (int i = 0; i < V; i++)
   {
      if (mask[i])
         continue;

      dfs_visit(i, adj, -1);
   }

   for (int i = 0; i < V; i++)
      mask[i] = false;

   int ind = 0;

   while (q.size() != 0)
   {
      int act = q.top();

      q.pop();

      if (!mask[act])
      {
         dfs_visit(act, new_adj, ind);
         ind++;
      }
   }
}
```

6.13. MIN COST MAX FLOW.

```
template <typename flow_type, typename cost_type> struct min_cost_max_flow {
      struct edge {
            size_t src, dst, rev;
            flow_type flow, cap;
            cost_type cost;
      };

      int n;
      vector<vector<edge>> adj;

      min_cost_max_flow(int n) : n(n), adj(n), potential(n), dist(n), back(n) {}
```

```
	void add_edge(size_t src, size_t dst, flow_type cap, cost_type cost) {
		adj[src].push_back({src, dst, adj[dst].size(), 0, cap, cost});
		if (src == dst)
			adj[src].back().rev++;
		adj[dst].push_back({dst, src, adj[src].size() - 1, 0, 0, -cost});
	}

	vector<cost_type> potential;

	inline cost_type rcost(const edge &e) {
		return e.cost + potential[e.src] - potential[e.dst];
	}

	void bellman_ford(int source) {
		for (int k = 0; k < n; ++k)
			for (int u = 0; u < n; ++u)
				for (edge &e : adj[u])
					if (e.cap > 0 && rcost(e) < 0)
						potential[e.dst] += rcost(e);
	}

	const cost_type oo = numeric_limits<cost_type>::max();

	vector<cost_type> dist;
	vector<edge *> back;

	cost_type dijkstra(int source, int sink) {
		fill(dist.begin(), dist.end(), oo);

		typedef pair<cost_type, int> node;
		priority_queue<node, vector<node>, greater<node>> pq;

		for (pq.push({dist[source] = 0, source}); !pq.empty();) {
			node p = pq.top();
			pq.pop();

			if (dist[p.second] < p.first)
				continue;
			if (p.second == sink)
				break;

			for (edge &e : adj[p.second])
				if (e.flow < e.cap && dist[e.dst] > dist[e.src] + rcost(e)
					back[e.dst] = &e;
					pq.push({dist[e.dst] = dist[e.src] + rcost(e), e.dst
				}
		}

		return dist[sink];
	}

	pair<flow_type, cost_type> max_flow(int source, int sink) {
		flow_type flow = 0;
		cost_type cost = 0;

		for (int u = 0; u < n; ++u)
			for (edge &e : adj[u])
				e.flow = 0;

		potential.assign(n, 0);
		dist.assign(n, 0);
		back.assign(n, nullptr);

		bellman_ford(source); // remove negative costs

		while (dijkstra(source, sink) < oo) {
			for (int u = 0; u < n; ++u)
				if (dist[u] < dist[sink])
					potential[u] += dist[u] - dist[sink];

			flow_type f = numeric_limits<flow_type>::max();

			for (edge *e = back[sink]; e; e = back[e->src])
				f = min(f, e->cap - e->flow);
			for (edge *e = back[sink]; e; e = back[e->src])
				e->flow += f, adj[e->dst][e->rev].flow -= f;

			flow += f;
			cost += f * (potential[sink] - potential[source]);
		}
		return {flow, cost};
	}
};
```

6.14. ARTICULATION POINT.

```
vector<bool> visited;
vi t;
```

```
vi low;
vector<bool> art;

void dfs_art(vi adj[], int n, int p, int q)
{
   t[n] = q;
   low[n] = q++;
   visited[n] = true;

   int j = 0;

   for (int i = 0; i < adj[n].size(); i++)
   {
      if (!visited[adj[n][i]])
      {
         dfs_art(adj, adj[n][i], n, q);
         low[n] = min(low[adj[n][i]], low[n]);
         j++;

         if (low[adj[n][i]] >= t[n] && p != -1)
         {
            art[n] = true;
         }
      }
      else if (adj[n][i] != p)
      {
         low[n] = min(t[adj[n][i]], low[n]);
      }
   }

   if (p == -1)
   {
      art[n] = j >= 2;
   }
}

void articulationPoints(int V, vi adj[])
{
   visited.assign(V, false);
   t.assign(V, -1);
   low.assign(V, -1);
   art.assign(V, false);

   for (int i = 0; i < V; i++)
   {
      if (!visited[i])
      {
         dfs_art(adj, i, -1, 1);
      }
   }
}
```