UH Random Team Reference

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1.1. **MAIN.**

```
#include <bits/stdc++.h>
#define MAX(a, b) (a > b) ? a : b
#define MIN(a, b) (a < b) ? a : b
#define int long long
#define vi vector<int>
#define pii pair<int, int>
#define vii vector<pii>
using namespace std;

void solve()
{
}
```

2.1. DISCRETE LOG.

```
int powmod(int a, int b, int m)
{
   int res = 1;
   while (b > 0)
   {
      if (b & 1)
      {
          res = (res * 111 * a) % m;
      }
      a = (a * 111 * a) % m;
      b >>= 1;
   }
   return res;
}
int discrete_log(int a, int b, int m)
```

1. TEMPLATE

```
int32_t main()
{
    ios_base::sync_with_stdio(0);
    cin.tie(0);

    int t;
    cin >> t;

    for (int i = 0; i < t; i++)
    {
        solve();
    }

    return 0;
}</pre>
```

2. MATH

```
{
    a %= m, b %= m;
    int n = sqrt(m) + 1;
    map<int, int> vals;
    for (int p = 1; p <= n; ++p)
        vals[powmod(a, p * n, m)] = p;
    for (int q = 0; q <= n; ++q)
    {
        int cur = (powmod(a, q, m) * 1ll * b) % m;
        if (vals.count(cur))
        {
            int ans = vals[cur] * n - q;
              return ans;
        }
    }
    return -1;
}</pre>
```

2.2. **NTT.**

```
using 11 = long long;
const 11 mod = (119 << 23) + 1, root = 62; // 998244353
11 qp(11 b, 11 e)
  11 \text{ ans} = 1;
  for (; e; b = b * b % mod, e /= 2)
     if (e & 1)
        ans = ans * b % mod;
  return ans;
void ntt(vector<11> &a, vector<11> &rt, vector<11> &rev, int n)
  for (int i = 0; i < n; i++)</pre>
     if (i < rev[i])
        swap(a[i], a[rev[i]]);
  for (int k = 1; k < n; k *= 2)
     for (int i = 0; i < n; i += 2 * k)
         for (int j = 0; j < k; j++)
            ll z = rt[j + k] * a[i + j + k] % mod, &ai = a[i + j];
            a[i + j + k] = (z > ai ? ai - z + mod : ai - z);
            ai += (ai + z >= mod ? z - mod : z);
vector<11> convolve(const vector<11> &a, const vector<11> &b)
```

2.3. MATRIX POW.

```
const int MAXN = 2;
struct Matrix
{
    l1 mat[MAXN][MAXN];
};

Matrix operator*(const Matrix &a, const Matrix &b)
{
    Matrix c;
```

```
if (a.empty() || b.empty())
   return {};
int s = a.size() + b.size() - 1, B = 32 - __builtin_clz(s), n = 1 << B;</pre>
vector<ll> L(a), R(b), out(n), rt(n, 1), rev(n);
L.resize(n), R.resize(n);
for (int i = 0; i < n; i++)</pre>
  rev[i] = (rev[i / 2] | (i \& 1) << B) / 2;
11 \text{ curL} = \text{mod} / 2, \text{inv} = \text{qp}(n, \text{mod} - 2);
for (int k = 2; k < n; k *= 2)
  11 z[] = \{1, qp(root, curL /= 2)\};
   for (int i = k; i < 2 * k; i++)</pre>
      rt[i] = rt[i / 2] * z[i & 1] % mod;
ntt(L, rt, rev, n);
ntt(R, rt, rev, n);
for (int i = 0; i < n; i++)</pre>
  out [-i \& (n - 1)] = L[i] * R[i] % mod * inv % mod;
ntt(out, rt, rev, n);
return {out.begin(), out.begin() + s};
for (int i = 0; i < MAXN; ++i)</pre>
   for (int j = 0; j < MAXN; ++j)
      c.mat[i][j] = 0;
for (int i = 0; i < MAXN; i++)</pre>
   for (int k = 0; k < MAXN; k++)
      if (a.mat[i][k] == 0)
```

continue;

```
for (int j = 0; j < MAXN; j++)</pre>
           c.mat[i][j] += a.mat[i][k] * b.mat[k][j];
     }
  return c;
Matrix operator (Matrix &base, 11 e)
  Matrix c;
  for (int i = 0; i < MAXN; i++)</pre>
2.4. FFT.
struct point
  double x, y;
  point (double x = 0, double y = 0) : x(x), y(y) {}
};
point operator+(const point &a, const point &b)
  return {a.x + b.x, a.y + b.y};
point operator-(const point &a, const point &b)
  return {a.x - b.x, a.y - b.y};
point operator* (const point &a, const point &b)
  return {a.x * b.x - a.y * b.y, a.x * b.y + a.y * b.x};
point operator/(const point &a, double d) { return {a.x / d, a.y / d}; }
void fft(vector<point> &a, int sign = 1)
  int n = a.size(); // n should be a power of two
   double theta = 8 * sign * atan(1.0) / n;
   for (int i = 0, j = 1; j < n - 1; ++j)
      for (int k = n >> 1; k > (i ^= k); k >>= 1)
     if (j < i)
        swap(a[i], a[j]);
```

```
for (int j = 0; j < MAXN; j++)</pre>
         c.mat[i][j] = (i == j);
   while (e)
      if (e & 111)
        c = c * base;
     base = base * base;
      e >>= 1;
   return c;
   for (int m, mh = 1; (m = mh << 1) <= n; mh = m)</pre>
      int irev = 0;
      for (int i = 0; i < n; i += m)</pre>
        point w = point(cos(theta * irev), sin(theta * irev));
         for (int k = n >> 2; k > (irev ^= k); k >>= 1)
         for (int j = i; j < mh + i; ++j)
            int k = j + mh;
            point x = a[j] - a[k];
            a[j] = a[j] + a[k];
            a[k] = w * x;
      }
   if (sign == -1)
      for (auto &p : a)
        p = p / n;
vector<point> convolve(vector<point> &a, vector<point> &b)
   int n = a.size();
   int m = b.size();
   int k = n + m;
   while (k != (k \& -k))
```

k += (k & -k);

while (a.size() < k)

a.push_back(point(0, 0));

```
while (b.size() < k)
    b.push_back(point(0, 0));

fft(a, 1);
fft(b, 1);

vector<point> c(k);
```

2.5. PRIMITIVE ROOT.

```
int powmod(int a, int b, int p)
{
   int res = 1;
   while (b)
      if (b & 1)
        res = int32_t(res * 111 * a % p), --b;
   else
        a = int32_t(a * 111 * a % p), b >>= 1;
   return res;
}
int generator(int p)
{
   vector<int> fact;
   int phi = p - 1, n = phi;
   for (int i = 2; i * i <= n; ++i)
      if (n % i == 0)
      {
        int phi = p - 1, n = phi;
        for (int i = 2; i * i <= n; ++i)
        if (n % i == 0)
      }
}</pre>
```

2.6. **FWHT.**

```
using 11 = long long;
const int mod = 1e9 + 7;

template <const int _mod_>
struct mod_int
{
    static const int mod = _mod_;
    int val;

    mod_int(long long v = 0)
    {
        if (v < 0)</pre>
```

```
for (int i = 0; i < k; i++)
    c[i] = a[i] * b[i];

fft(c, -1);

return c;
}</pre>
```

```
fact.push_back(i);
   while (n % i == 0)
        n /= i;
}
if (n > 1)
   fact.push_back(n);

for (int res = 2; res <= p; ++res)
{
   bool ok = true;
   for (size_t i = 0; i < fact.size() && ok; ++i)
        ok &= powmod(res, phi / fact[i], p) != 1;
   if (ok)
        return res;
}
return -1;</pre>
```

```
v = v % mod + mod;
if (v >= mod)
    v %= mod;
val = v;
}

static int mod_inv(int a, int m = mod)
{
  int g = m, r = a, x = 0, y = 1;
  while (r != 0)
  {
    int q = g / r;
    g %= r;
    swap(g, r);
```

```
x -= q * y;
        swap(x, y);
     return x < 0 ? x + m : x;
  explicit operator int() const { return val; }
  mod_int &operator+=(const mod_int &other)
     val += other.val;
     if (val >= mod)
        val -= mod;
     return *this;
  mod_int &operator = (const mod_int &other)
     val -= other.val;
     if (val < 0)
        val += mod;
     return *this;
  static unsigned fast_mod(uint64_t x, unsigned m = mod)
#if !defined(_WIN32) || defined(_WIN64)
     return x % m;
#endif
     // Optimized mod for Codeforces 32-bit machines.
     // x must be less than 2^32 \star m for this to work, so that x / m fits in
     // a 32-bit integer.
     unsigned x_high = x >> 32, x_low = (unsigned) x;
     unsigned quot, rem;
     asm("divl.%4\n"
        : "=a"(quot), "=d"(rem)
        : "d"(x_high), "a"(x_low), "r"(m));
     return rem;
  mod_int &operator*=(const mod_int &other)
     val = fast_mod((uint64_t)val * other.val);
     return *this;
  mod_int &operator/=(const mod_int &other) { return *this *= other.inv(); }
```

```
friend mod_int operator+(const mod_int &a, const mod_int &b)
   return mod_int(a) += b;
friend mod_int operator-(const mod_int &a, const mod_int &b)
  return mod_int(a) -= b;
friend mod_int operator*(const mod_int &a, const mod_int &b)
  return mod_int(a) *= b;
friend mod_int operator/(const mod_int &a, const mod_int &b)
  return mod_int(a) /= b;
mod_int &operator++()
  val = val == mod - 1 ? 0 : val + 1;
  return *this;
mod_int &operator--()
  val = val == 0 ? mod - 1 : val - 1;
  return *this;
mod_int operator++(int)
  mod_int a = *this;
  ++*this;
  return a;
mod_int operator--(int)
  mod_int a = *this;
  --*this;
  return a;
mod_int operator-() const { return val == 0 ? 0 : mod - val; }
mod_int inv() const { return mod_inv(val); }
bool operator==(const mod_int &other) const { return val == other.val; }
bool operator!=(const mod_int &other) const { return val != other.val; }
```

```
bool operator<(const mod_int &other) const { return val < other.val; }</pre>
  bool operator>(const mod_int &other) const { return val > other.val; }
  template <typename T>
  bool operator<(const T &other) const
     return val < other;</pre>
  template <typename T>
  bool operator > (const T &other) const
     return val > other;
  friend string to_string(const mod_int &m) { return to_string(m.val); }
  friend mod_int abs(const mod_int &m) { return mod_int(m.val); }
  friend ostream &operator<<(ostream &stream, const mod_int &m)</pre>
     return stream << m.val;</pre>
  friend istream &operator>>(istream &stream, mod_int &m)
      return stream >> m.val;
};
// Notar que se uso este tipo de datos entero, que implementa todas las
// operaciones basicos en el sistem residual modulo 10^9+7 para hacer mas
// faciles las implementaciones si se quiere implementarlo, se puede dejar en
// long long, y modificar las operaciones para mantener los resultados teneindo
// en cuenta el modulo a usar.
using T = mod_int<mod>;
void HADAMARD_XOR(vector<T> &a, bool inverse = false)
  int n = a.size();
  for (int k = 1; k < n; k <<= 1)</pre>
     for (int i = 0; i < n; i += 2 * k)
         for (int j = 0; j < k; j++)
           T x = a[i + j];
            T y = a[i + j + k];
            a[i + j] = x + y;
```

```
a[i + j + k] = x - y;
   if (inverse)
      T q = 1 / static_cast<T>(n);
      for (int i = 0; i < n; i++)</pre>
         a[i] *= q;
void HADAMARD_AND(vector<T> &a, bool inverse = false)
   int n = a.size();
   for (int k = 1; k < n; k <<= 1)</pre>
      for (int i = 0; i < n; i += 2 * k)
         for (int j = 0; j < k; j++)
            T x = a[i + j];
            T y = a[i + j + k];
            if (inverse)
               a[i + j] = -x + y;
               a[i + j + k] = x;
            else
               a[i + j] = y;
               a[i + j + k] = x + y;
void HADAMARD_OR(vector<T> &a, bool inverse = false)
   int n = a.size();
   for (int k = 1; k < n; k <<= 1)</pre>
```

int n = 1;

n <<= 1;

a.resize(n);

b.resize(n);

if (eq) b = a;

return a;

else

HADAMARD_XOR(a);

HADAMARD_XOR(b);

a[i] *= b[i];

HADAMARD_XOR(a, true);

for (int i = 0; i < n; i++)</pre>

while (n < (int)max(a.size(), b.size()))</pre>

```
for (int i = 0; i < n; i += 2 * k)
{
    for (int j = 0; j < k; j++)
    {
        T x = a[i + j];
        T y = a[i + j + k];
        if (inverse)
        {
            a[i + j] = y;
            a[i + j + k] = x - y;
        }
        else
        {
            a[i + j] = x + y;
            a[i + j + k] = x;
        }
    }
}

// Las demas operaciones a nivel de bit tienen una implementacion semejante
template <typename T>
vector<T> FWHT_XOR(vector<T> a, vector<T> b)
{
    bool eq = (a == b);
```

2.7. EXTENDED EUCLIDEAN ALGORITHM.

```
int gcd(int a, int b, int &x, int &y)
{
    x = 1, y = 0;
    int x1 = 0, y1 = 1, a1 = a, b1 = b;
    while (b1)
    {
        int q = a1 / b1;
    }
}
```

```
tie(y, y1) = make_tuple(y1, y - q * y1);
    tie(a1, b1) = make_tuple(b1, a1 - q * b1);
}
return a1;
}
```

 $tie(x, x1) = make_tuple(x1, x - q * x1);$

3. GEOMETRY

3.1. BASICS.

```
db EPS = 1e-9;
struct point {
   db x, y;
```

```
point() { x = y = 0.0; }
  point(db _x, db _y) : x(_x), y(_y) {}
  bool operator < (const point &other) const {</pre>
     if (fabs(x-other.x) > EPS)
     return x < other.x;</pre>
     return y < other.y;</pre>
  bool operator == (const point &other) const {
     return (fabs(x-other.x) < EPS) && (fabs(y-other.y) < EPS);</pre>
  db dist(const point &other) {
     return hypot(x-other.x, y-other.y);
  point rotate(db theta) {
     db rad = DEG_to_RAD(theta);
     return point(x*cos(rad) - y*sin(rad), x*sin(rad) + y*cos(rad));
};
struct line {
  db a, b, c;
  line() {}
  line(db _a, db _b, db _c) : a(_a), b(_b), c(_c) {}
  void pointsToLine(const point &p1, const point &p2) {
     if (fabs(p1.x-p2.x) < EPS) {
        a = 1.0;
        b = 0.0;
        c = -p1.x;
     else {
        a = -(db)(p1.y-p2.y) / (p1.x-p2.x);
        b = 1.0;
        c = -(db)(a*p1.x) - p1.y;
     }
  void pointSlopeToLine(point p, db m) {
     a = -m;
     b = 1.0;
     c = -((a * p.x) + (b * p.y));
```

```
bool areParallel(const line &other) {
      return (fabs(a-other.a) < EPS) && (fabs(b-other.b) < EPS);
   bool areSame(const line &other) {
      return areParallel(other) && (fabs(c-other.c) < EPS);</pre>
   bool areIntersect(const line &other, point &p) {
      if (areParallel(other)) return false;
      p.x = (other.b*c - b*other.c) / (other.a*b - a*other.b);
      if (fabs(b) > EPS) p.y = -(a*p.x + c);
      else p.y = -(other.a*p.x + other.c);
      return true;
};
struct vec{
   db x, y;
   vec(db _x, db _y) : x(_x), y(_y) {}
   vec(const point &a, const point &b) : x(b.x - a.x), y(b.y - a.y) {}
   vec scale(db s) {
      return vec(x*s, y*s);
   point translate(const point &p) {
      return point(x+p.x, y+p.y);
   db dot(vec a, vec b) { return a.x*b.x + a.y*b.y; }
   db norm_sq(vec v) { return v.x*v.x + v.y*v.y; }
   db angle (const point &a, const point &o, const point &b) {
      vec oa = vec(o, a), ob = vec(o, b);
      return acos(dot(oa, ob) / sqrt(norm_sq(oa) * norm_sq(ob)));
   db cross(vec a, vec b) { return a.x*b.y - a.y*b.x; }
   bool ccw(point p, point q, point r) {
      return cross(vec(p, q), vec(p, r)) > EPS;
   bool collinear(point p, point q, point r) {
      return fabs(cross(vec(p, q), vec(p, r))) < EPS;</pre>
```

```
db distToLine(point p, point a, point b) {
     vec ap = vec(a, p), ab = vec(a, b);
     db u = dot(ap, ab) / norm_sq(ab);
     point c = ab.scale(u).translate(a);
     return c.dist(p);
  db distToLineSegment(point p, point a, point b) {
     vec ap = vec(a, p), ab = vec(a, b);
     db u = dot(ap, ab) / norm_sq(ab);
     if (u < 0.0) {
        point c = point(a.x, a.y);
        return c.dist(p);
     if (u > 1.0) {
        point c = point(b.x, b.y);
        return c.dist(p);
     return distToLine(p, a, b);
};
```

3.2. POLYGON.

```
struct polygon {
    vector<point> P;
    polygon(const vector<point> &_P) : P(_P) {}

    db perimeter() {
        db ans = 0.0;
        for (int i = 0; i < (int)P.size()-1; ++i)
            ans += P[i].dist(P[i+1]);
        return ans;
    }

    db area() {
        db ans = 0.0;
        for (int i = 0; i < (int)P.size()-1; ++i)
            ans += (P[i].x*P[i+1].y - P[i+1].x*P[i].y);
        return fabs(ans) / 2.0;
    }</pre>
```

```
struct circle {
   point c;
   db r;
   circle(const point &_c, db _r) : c(_c), r(_r) {}
   int inside(const point &p) {
     db dist = c.dist(p);
     return dist < r ? 1 : (fabs(dist-r) < EPS ? 0 : -1);
   point inCircle(point p1, point p2, point p3) {
     line 11, 12;
     double ratio = p1.dist(p2) / p1.dist(p3);
     point p = vec(p2, p3).scale(ratio / (1+ratio)).translate(p2);
     11.pointsToLine(p1, p);
     ratio = p2.dist(p1) / p2.dist(p3);
     p = vec(p1, p3).scale(ratio / (1+ratio)).translate(p1);
     12.pointsToLine(p2, p);
     point c;
     11.areIntersect(12, c);
     return c;
};
```

```
bool isConvex(const vector<point> &P) {
  int n = (int)P.size();
  if (n <= 3) return false;</pre>
  bool firstTurn = vec().ccw(P[0], P[1], P[2]);
   for (int i = 1; i < n-1; ++i)
      if (vec().ccw(P[i], P[i+1], P[(i+2) == n ? 1 : i+2]) != firstTurn)
         return false;
  return true;
int insidePolygon(point pt) {
  int n = (int)P.size();
  if (n \le 3) return -1;
  bool on_polygon = false;
   for (int i = 0; i < n-1; ++i)
      if (fabs(pt.dist(P[i]) + pt.dist(P[i+1]) - P[i].dist(P[i+1])) < EPS)
         on_polygon = true;
  if (on_polygon) return 0;
   double sum = 0.0;
```

```
for (int i = 0; i < n-1; ++i) {
    if (vec().ccw(pt, P[i], P[i+1]))
        sum += vec().angle(P[i], pt, P[i+1]);
    else
        sum -= vec().angle(P[i], pt, P[i+1]);
};</pre>
```

4. DATA STRUCTURE

4.1. SEGMENT TREE.

```
class SegmentTree
private:
  vi values;
  vi p_values;
   int n;
   int left(int p) { return p << 1; };</pre>
  int right(int p) { return (p << 1) + 1; }</pre>
   int simple_node(int index) { return values[index]; }
   int prop(int x, int y) { return x + y; }
   void build(int p, int 1, int r)
     if (1 == r)
         p_values[p] = simple_node(1);
         return;
     build(left(p), 1, (1 + r) / 2);
     build(right(p), (1 + r) / 2 + 1, r);
     p_values[p] = prop(p_values[left(p)], p_values[right(p)]);
   void set(int p, int 1, int r, int i, int v)
     if (1 == r)
        values[1] = v;
         p_values[p] = simple_node(1);
```

```
return;
     if (i <= (1 + r) / 2)
         set(left(p), 1, (1 + r) / 2, i, v);
        set(right(p), (l + r) / 2 + 1, r, i, v);
     p_values[p] = prop(p_values[left(p)], p_values[right(p)]);
   int query(int p, int l, int r, int lq, int rq)
     if (lq <= l && r <= rq)
        return p_values[p];
     int 11 = 1, r1 = (1 + r) / 2;
     int 12 = (1 + r) / 2 + 1, r2 = r;
     if (l1 > rq || lq > r1)
        return query(right(p), 12, r2, lq, rq);
     if (12 > rq || lq > r2)
        return query(left(p), 11, r1, lq, rq);
     int lt = query(left(p), l1, r1, lq, rq);
     int rt = query(right(p), 12, r2, lq, rq);
     return prop(lt, rt);
public:
   SegmentTree(vi &a)
     values = a;
     n = a.size();
     p_values.assign(4 * n, 0);
```

return 0;

```
build(1, 0, n - 1);
}
int query(int i, int j) { return query(1, 0, n - 1, i, j); }
```

4.2. DISJOINT SET UNION.

4.3. **PBDS.**

```
int get(int i) { return values[i]; }
};
      return p[x] = get(p[x]);
   bool is_same_set(int a, int b) { return get(a) == get(b); }
   int size_of(int a) { return sz[get(a)]; }
   void unite(int a, int b)
      a = get(a);
      b = get(b);
      if (rank[a] > rank[b])
         swap(a, b);
      p[a] = b;
      if (rank[a] == rank[b])
         rank[b]++;
      sz[b] += sz[a];
      num_sets--;
};
   tree.insert(A[i]);
 // O(log n) select
 cout << *tree.find_by_order(0) << "\n"; // 1-smallest = 2
 cout << *tree.find_by_order(n - 1) << "\n"; // 9-smallest/largest = 71</pre>
 cout << *tree.find_by_order(4) << "\n"; // 5-smallest = 15</pre>
 // O(log n) rank
 cout << tree.order_of_key(2) << "\n"; // index 0 (rank 1)</pre>
 cout << tree.order_of_key(71) << "\n"; // index 8 (rank 9)</pre>
 cout << tree.order_of_key(15) << "\n"; // index 4 (rank 5)</pre>
```

void set(int i, int v) { set(1, 0, n - 1, i, v); }

4.4. SEGMENT TREE LAZY.

```
class SegmentTreeLazy
private:
  vi values;
  vector<bool> lazy;
  vi l_values;
  vi p_values;
   int n;
  int left(int p) { return p << 1; };</pre>
  int right(int p) { return (p << 1) + 1; }</pre>
   int simple_node(int index) { return values[index]; }
   int prop(int x, int y) { return x + y; }
   int prop_lazy(int x, int y) { return x + y; }
   int prop_lazy_up(int x, int y, int s) { return x + y * s; }
   void update_lazy(int p, int l, int r)
     if (1 == r)
         values[1] = prop_lazy(values[1], l_values[p]);
     p_values[p] = prop_lazy_up(p_values[p], l_values[p], r - 1 + 1);
   void propagate_lazy(int p, int l, int r)
     lazy[p] = false;
     if (1 == r)
        return;
     l_values[left(p)] = lazy[left(p)]
                        ? prop_lazy(l_values[left(p)], l_values[p])
                        : l_values[p];
     l_values[right(p)] = lazy[right(p)]
                         ? prop_lazy(l_values[right(p)], l_values[p])
                         : l_values[p];
```

```
lazy[left(p)] = true;
  lazy[right(p)] = true;
void build(int p, int 1, int r)
  if (1 == r)
     p_values[p] = simple_node(1);
     return;
  build(left(p), 1, (1 + r) / 2);
  build(right(p), (1 + r) / 2 + 1, r);
  p_values[p] = prop(p_values[left(p)], p_values[right(p)]);
void set(int p, int 1, int r, int i, int v)
  if (lazy[p])
     update_lazy(p, l, r);
     propagate_lazy(p, l, r);
  if (1 == r)
     values[1] = v;
     p_values[p] = simple_node(1);
     return;
  if (i <= (1 + r) / 2)
     set(left(p), 1, (1 + r) / 2, i, v);
     set(right(p), (1 + r) / 2 + 1, r, i, v);
  p_values[p] = prop(p_values[left(p)], p_values[right(p)]);
int query(int p, int l, int r, int lq, int rq)
  if (lazy[p])
```

```
update_lazy(p, 1, r);
     propagate_lazy(p, l, r);
  if (lq <= 1 && r <= rq)
     return p_values[p];
  int 11 = 1, r1 = (1 + r) / 2;
  int 12 = (1 + r) / 2 + 1, r2 = r;
  if (l1 > rq || lq > r1)
     return query(right(p), 12, r2, lq, rq);
  if (12 > rq || 1q > r2)
     return query(left(p), 11, r1, lq, rq);
  int lt = query(left(p), l1, r1, lq, rq);
  int rt = query(right(p), 12, r2, lq, rq);
  return prop(lt, rt);
void set_rank(int p, int 1, int r, int lq, int rq, int value)
  if (lazy[p])
     update_lazy(p, 1, r);
     propagate_lazy(p, 1, r);
  if (1 > rq || lq > r)
     return;
  if (lq <= 1 && r <= rq)
     lazy[p] = true;
     l_values[p] = value;
     update_lazy(p, l, r);
     propagate_lazy(p, 1, r);
     return;
  set_rank(left(p), l, (l + r) / 2, lq, rq, value);
```

4.5. **AVL.**

```
set_rank(right(p), (l + r) / 2 + 1, r, lq, rq, value);
     p_values[p] = prop(p_values[left(p)], p_values[right(p)]);
   int get(int p, int 1, int r, int i)
     if (lazy[p])
        update_lazy(p, l, r);
        propagate_lazy(p, 1, r);
      if (1 == r)
         return values[i];
      if (i <= (1 + r) / 2)
         return get(left(p), 1, (1 + r) / 2, i);
      return get(right(p), (1 + r) / 2 + 1, r, i);
public:
   SegmentTreeLazy(vi &a)
     values = a;
     n = a.size();
      p_values.assign(4 * n, 0);
     lazy.assign(4 * n, false);
     l_values.assign(4 * n, 0);
     build(1, 0, n - 1);
   int query(int i, int j) { return query(1, 0, n - 1, i, j); }
   void set(int i, int v) { set(1, 0, n - 1, i, v); }
   void set_rank(int i, int j, int v) { set_rank(1, 0, n - 1, i, j, v); }
   int get(int i) { return get(1, 0, n - 1, i); }
};
```

struct avl {

```
int key;
int height;
int size;
avl *left;
avl *right;
avl(int k) {
  key = k;
  height = 1;
  size = 1;
  left = NULL;
  right = NULL;
int getBalance() {
  int leftHeight = 0;
  int rightHeight = 0;
  if (left != NULL)
     leftHeight = left->height;
  if (right != NULL)
      rightHeight = right->height;
   return leftHeight - rightHeight;
void updateSize() {
   int leftSize = 0;
  int rightSize = 0;
  if (left != NULL)
     leftSize = left->size;
  if (right != NULL)
      rightSize = right->size;
  size = leftSize + rightSize + 1;
void updateHeight() {
  int leftHeight = 0;
  int rightHeight = 0;
  if (left != NULL)
     leftHeight = left->height;
```

```
if (right != NULL)
      rightHeight = right->height;
  height = max(leftHeight, rightHeight) + 1;
avl *rotateLeft() {
  avl *newRoot = right;
   right = newRoot->left;
  newRoot->left = this;
  updateHeight();
  newRoot->updateHeight();
  return newRoot;
avl *rotateRight() {
   avl *newRoot = left;
  left = newRoot->right;
  newRoot->right = this;
  updateHeight();
  newRoot->updateHeight();
  return newRoot;
avl *balance() {
  updateHeight();
   updateSize();
   int balance = getBalance();
  if (balance == 2) {
     if (left->getBalance() < 0)</pre>
        left = left->rotateLeft();
      return rotateRight();
  if (balance == -2) {
     if (right->getBalance() > 0)
         right = right->rotateRight();
      return rotateLeft();
   return this;
avl *insert(int k) {
  if (k < key) {
      if (left == NULL)
```

```
left = new avl(k);
      else
         left = left->insert(k);
   else {
      if (right == NULL)
         right = new avl(k);
      else
         right = right->insert(k);
  return balance();
avl *findMin() {
  if (left == NULL)
      return this;
   else
      return left->findMin();
avl *removeMin() {
  if (left == NULL)
      return right;
  left = left->removeMin();
  return balance();
avl *remove(int k) {
  if (k < key)
     left = left->remove(k);
  else if (k > key)
      right = right->remove(k);
  else {
      avl *leftChild = left;
      avl *rightChild = right;
      delete this;
      if (rightChild == NULL)
         return leftChild;
      avl *min = rightChild->findMin();
      min->right = rightChild->removeMin();
      min->left = leftChild;
      return min->balance();
```

```
return balance();
int getRank(int k) {
  if (k < key) {
     if (left == NULL)
         return 0;
         return left->getRank(k);
  else if (k > key) {
     if (right == NULL)
         return 1 + left->size;
     else
         return 1 + left->size + right->getRank(k);
   else
      return left->size;
int getKth(int k) {
  if (k < left->size)
      return left->getKth(k);
   else if (k > left->size)
      return right->getKth(k - left->size - 1);
   else
      return key;
static avl *join(avl *left, avl *right) {
  if (left->height < right->height) {
      right->left = join(left, right->left);
      return right->balance();
  else if (left->height > right->height) {
     left->right = join(left->right, right);
     return left->balance();
  else {
      avl *min = right->findMin();
     min->right = right->removeMin();
     min->left = left;
      return min->balance();
```

```
pair<avl *, avl *> split(int k) {
     if (k < key) {
        pair<avl *, avl *> p = left->split(k);
        left = p.second;
        return {p.first, join(this, left)};
                                                                                           };
     else {
4.6. ABI.
class Abi
private:
  vi p;
  int _size;
  int ls_one(int i) { return i & (-i); }
public:
   Abi(int n)
     _size = n;
     p.assign(n + 1, 0);
   int rsq(int k)
     int sum = 0;
                                                                                           };
     for (int i = k; i > 0; i -= ls_one(i))
4.7. MOS.
void remove(int idx); // TODO: remove value at idx from data structure
void add(int idx); // TODO: add value at idx from data structure
int get_answer(); // TODO: extract the current answer of the data structure
int block_size;
struct Query
  int 1, r, idx;
  bool operator<(Query other) const</pre>
```

```
pair<avl *, avl *> p = right->split(k);
         right = p.first;
         return {join(this, right), p.second};
         sum += p[i];
      return sum;
   int sum(int a, int b) { return rsq(b) - rsq(a - 1); }
   void adjust_sum(int k, int v)
      for (int i = k; i < p.size(); i += ls_one(i))</pre>
         p[i] += v;
   int size()
      return _size;
      return make_pair(l / block_size, r) <</pre>
           make_pair(other.1 / block_size, other.r);
};
vector<int> mo_s_algorithm(vector<Query> queries)
   vector<int> answers(queries.size());
   sort(queries.begin(), queries.end());
```

```
// TODO: initialize data structure

int cur_1 = 0;
int cur_r = -1;
// invariant: data structure will always reflect the range [cur_1, cur_r]
for (Query q : queries)
{
    while (cur_1 > q.1)
    {
        cur_1--;
        add(cur_1);
    }
    while (cur_r < q.r)
    {
        cur_r++;
        add(cur_r);
}</pre>
```

```
while (cur_l < q.l)
{
    remove(cur_l);
    cur_l++;
}
while (cur_r > q.r)
{
    remove(cur_r);
    cur_r--;
}
answers[q.idx] = get_answer();
}
return answers;
```

4.8. SQRT DECOMPOSITION.

```
struct sqd {
   int n;
   int b;
   vi a;
   vi bsum;
   sqd(vi &a) {
      n = a.size();
      b = sqrt(n);
      this->a = a;
      bsum.assign(b + 1, 0);
      for (int i = 0; i < n; i++)
            bsum[i / b] += a[i];
   }
   void update(int i, int v) {</pre>
```

```
bsum[i / b] += v - a[i];
a[i] = v;
}
int query(int 1, int r) {
   int sum = 0;
   for (int i = 1; i <= r; i++)
        if (i % b == 0 && i + b - 1 <= r) {
            sum += bsum[i / b];
            i += b - 1;
        } else
            sum += a[i];
   return sum;
}
</pre>
```

5. STRING

5.1. SUFFIX ARRAY.

```
class SuffixArray
{
public:
    SuffixArray(string s)
```

```
n = s.size() + 1;
s_value = s + "$";

ra.assign(n, 0);
sa.assign(n, 0);
temp_ra.assign(n, 0);
```

```
temp_sa.assign(n, 0);
     construct_sa();
     build_lcp();
  int size() { return n; }
  int get_int(int i) { return sa[i]; }
   int cant_match(string p)
     pii ans = matching(p);
     if (ans.first == -1 \&\& ans.second == -1)
        return 0;
     return ans.second - ans.first + 1;
   int get_lcp(int i) { return plcp[sa[i]]; }
   int cant_substr() { return v_cant_substr; }
   string get_str(int i) { return s_value.substr(sa[i], n - sa[i] - 1); }
private:
   string s_value;
   int n;
   int v_cant_substr;
   vi ra;
   vi sa;
   vi c;
  vi temp_ra;
  vi temp_sa;
   vi phi;
   vi plcp;
   void counting_sort(int k)
     int sum = 0;
     int maxi = max((int)300, n);
     c.assign(maxi, 0);
      for (int i = 0; i < n; i++)</pre>
```

```
c[i + k < n ? ra[i + k] : 0]++;
   for (int i = 0; i < maxi; i++)</pre>
      int tx = c[i];
      c[i] = sum;
      sum += tx;
   for (int i = 0; i < n; i++)</pre>
      temp_sa[c[sa[i] + k < n ? ra[sa[i] + k] : 0]++] = sa[i];
   for (int i = 0; i < n; i++)</pre>
      sa[i] = temp_sa[i];
void construct_sa()
   int k, r;
   for (int i = 0; i < n; i++)</pre>
     ra[i] = s_value[i];
     sa[i] = i;
   for (k = 1; k < n; k <<= 1)
      counting_sort(k);
      counting_sort(0);
      temp_ra[sa[0]] = r = 0;
      for (int i = 1; i < n; i++)</pre>
         temp_ra[sa[i]] = (ra[sa[i]] ==
            ra[sa[i-1]] \&\& ra[sa[i]+k] == ra[sa[i-1]+k]) ? r : ++r;
      for (int i = 0; i < n; i++)</pre>
         ra[i] = temp_ra[i];
      if (ra[sa[n-1]] == n-1)
         break;
pii matching(string p)
```

```
int 1 = 0;
int r = n - 1;
int p_size = p.size();
string comp;
while (1 < r)
   int m = (1 + r) / 2;
   comp = s_value.substr(sa[m], min(n - sa[m], p_size));
   if (comp >= p)
      r = m;
   else
      1 = m + 1;
comp = s_value.substr(sa[1], min(n - sa[1], p_size));
if (comp != p)
   return {-1, -1};
int ans_1 = 1;
1 = 0;
r = n - 1;
while (1 < r)
   int m = (1 + r) / 2;
   comp = s_value.substr(sa[m], min(n - sa[m], p_size));
   if (comp > p)
     r = m;
   else
      1 = m + 1;
comp = s_value.substr(sa[r], min(n - sa[r], p_size));
```

5.2. Z FUNCTION.

```
// Z[i] is the length of the longest substring // starting from S[i] which is also a prefix of S.
```

```
if (comp != p)
         r--;
      int ans_r = r;
      return {ans_l, ans_r};
   void build_lcp()
      phi.assign(n, 0);
      plcp.assign(n, 0);
      phi[0] = -1;
      for (int i = 1; i < n; i++)</pre>
         phi[sa[i]] = sa[i - 1];
      int 1 = 0;
      int q = 0;
      for (int i = 0; i < n; i++)</pre>
         if (phi[i] == -1)
            plcp[i] = 0;
            continue;
         while (s_value[i + 1] == s_value[phi[i] + 1])
           1++;
         plcp[i] = 1;
         q += 1;
         1 = \max(1 - 1, (int)0);
      v_{cant\_substr} = n * (n - 1) / 2 - q;
} ;
```

```
vi z_function(string s)
{
```

```
int n = (int)s.length();
vi z(n);

for (int i = 1, 1 = 0, r = 0; i < n; ++i)
{
    if (i <= r)
        z[i] = min(r - i + 1, z[i - 1]);
    while (i + z[i] < n && s[z[i]] == s[i + z[i]])
        ++z[i];
    if (i + z[i] - 1 > r)
        1 = i, r = i + z[i] - 1;
}
return z;
}

// suff[i] = length of the longest common suffix of s and s[0..i]
vi suffixes(const string &s)
{
```

5.3. HASHING.

```
struct custom hash
  static uint64_t splitmix64(uint64_t x)
     x += 0x9e3779b97f4a7c15;
     x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
     x = (x ^(x >> 27)) * 0x94d049bb133111eb;
     return x ^ (x >> 31);
  size_t operator()(uint64_t x) const
     static const uint64_t FIXED_RANDOM =
        chrono::steady_clock::now().time_since_epoch().count();
     return splitmix64(x + FIXED_RANDOM);
};
const int MAXN = 5e5 + 5;
const int MOD = 1e9 + 7;
int mod_pow(int b, int e)
  int res = 1;
  while (e)
     if (e & 1)
```

```
int n = s.length();
   vi suff(n, n);
   for (int i = n - 2, g = n - 1, f; i >= 0; --i)
     if (i > q && suff[i + n - 1 - f] != i - q)
        suff[i] = min(suff[i + n - 1 - f], i - q);
        for (q = min(q, f = i); q >= 0 && s[q] == s[q + n - 1 - f]; --q)
        suff[i] = f - q;
   return suff;
        res = res * b % MOD;
     b = b * b % MOD;
      e >>= 1;
   return res % MOD;
typedef unordered_map<11, 11, custom_hash> safe_map;
int dx[] = \{1, 0, -1, 0, 1, -1, -1, 1\};
int dy[] = \{0, 1, 0, -1, 1, 1, -1, -1\};
int dp[MAXN];
vi ady_list[MAXN];
int n, m, t, k;
int f[MAXN];
int comb(int n, int k)
   int fk = mod_pow(f[k], MOD - 2);
   int fnk = mod_pow(f[n - k], MOD - 2);
   int x = ((f[n] * fk) % MOD * fnk % MOD);
   return x;
```

5.4. **KMP PF.**

```
vi prefix_function(string p)
  vi pf(p.size());
  pf[0] = 0;
  int k = 0;
   for (int i = 1; i < p.size(); i++)</pre>
      while (k > 0 && p[k] != p[i])
        k = pf[k - 1];
     if (p[k] == p[i])
        k++;
     pf[i] = k;
   return pf;
vi kmp(string t, string p)
5.5. TRIE.
class Trie
private:
   int cant_string;
   int cant_string_me;
  int cant_node;
   char value;
  Trie *children[alphabet];
public:
   Trie (char a)
     cant_string = 0;
     cant_node = 1;
     cant_string_me = 0;
     value = a;
      for (int i = 0; i < alphabet; i++)</pre>
```

```
vi result;
vi pf = prefix_function(p);
int k = 0;
for (int i = 0; i < t.size(); i++)</pre>
   while (k > 0 \&\& p[k] != t[i])
     k = pf[k - 1];
  if (p[k] == t[i])
     k++;
   if (k == p.size())
     result.push_back(i - (p.size() - 1));
     k = pf[k - 1];
return result;
      children[i] = NULL;
pair<Trie *, int> search(string s)
  Trie *node = this;
  int i = 0;
   while (i < s.size() && node->children[s[i] - first_char] != NULL)
     node = node->children[s[i] - first_char];
     i++;
   return {node, i};
```

```
void insert(string s)
  int q = s.size() - search(s).second;
  Trie *node = this;
  for (int i = 0; i < s.size(); i++)</pre>
      node->cant_node += q;
      if (node->children[s[i] - first_char] == NULL)
         node->children[s[i] - first_char] = new Trie(s[i]);
      node = node->children[s[i] - first_char];
     node->cant_string_me++;
  node->cant string++;
void eliminate(string s)
  if (!contains(s))
     return;
  Trie *node = this;
  int q = 0;
  for (int i = 0; i < s.size(); i++)</pre>
      if (node->children[s[i] - first_char] == NULL)
         node->children[s[i] - first_char] = new Trie(s[i]);
```

```
if (node->children[s[i] - first_char]->cant_string_me == 1)
        node->children[s[i] - first_char] = NULL;
        q = s.size() - i;
         break;
      node = node->children[s[i] - first_char];
     node->cant_string_me--;
     if (i == s.size() - 1)
        node->cant_string--;
  node = this;
   for (int i = 0; i < s.size() - q + 1; i++)</pre>
     node->cant_node -= q;
     node = node->children[s[i] - first_char];
bool contains(string s)
   auto q = search(s);
   return q.second == s.size() && q.first->cant_string >= 1;
int cant_words_me() { return cant_string_me; }
int cant_words() { return cant_string; }
Trie *get(char a) { return children[a - first_char]; }
int size() { return cant_node; }
```

6. GRAPH

6.1. TOPOLOGICAL SORT.

```
vector<int> topoSort(int V, vector<int> adj[])
{
    vector<int> in(V);
```

```
vector<int> resp;
for (int i = 0; i < V; i++)</pre>
```

```
for (int j = 0; j < adj[i].size(); j++)
{
    in[adj[i][j]]++;
}

queue<int> q;

for (int i = 0; i < V; i++)
{
    if (in[i] == 0)
        q.push(i);
}

while (q.size() != 0)
{</pre>
```

6.2. DIJSKTRA.

```
int n = q.front();
    q.pop();

for (int i = 0; i < adj[n].size(); i++)
{
       in[adj[n][i]]--;
       if (in[adj[n][i]] == 0)
            q.push(adj[n][i]);
    }

    resp.push_back(n);
}

return resp;
}</pre>
```

```
q.emplace(0, S);
while (!q.empty())
{
    auto [d, u] = q.top();
    q.pop();
    if (d > dist[u])
        continue;

    for (auto &[v, w] : adj[u])
        {
        if (dist[u] + w >= dist[v])
            continue;

        dist[v] = dist[u] + w;
        q.emplace(dist[v], v);
    }
}
return dist;
```

6.3. BRIDGE EDGES.

```
vector<bool> visited;
vector<int> t;
vector<int> low;
set<pair<int, int>> bridges;

void dfs_bridges(vector<int> adj[], int n, int p, int q)
{
    t[n] = q;
    low[n] = q++;
    visited[n] = true;

    int j = 0;

    for (int i = 0; i < adj[n].size(); i++)
    {
        if (!visited[adj[n][i]])
        {
            dfs_bridges(adj, adj[n][i], n, q);
            low[n] = min(low[adj[n][i]], low[n]);
            j++;
        }
        else if (adj[n][i] != p)</pre>
```

```
void solve()
{
}

int main()
{
    ios_base::sync_with_stdio(0);
    cin.tie(0);

    int t;
    cin >> t;

    for (int i = 0; i < t; i++)
    {
        solve();
    }

    return 0;
}
</pre>
```

```
dfs_bridges(adj, i, -1, 1);
}
}
```

6.4. **PRIM.**

```
int spanningTreePrim(int V, vector<vector<int>> adj[])
{
    priority_queue<pair<int, int>> q;

    vector<bool> mask;
    mask.assign(V, false);
    mask[0] = true;

    int cost = 0;

    for (int i = 0; i < adj[0].size(); i++)
    {
        q.push({-adj[0][i][1], adj[0][i][0]});
    }

    while (q.size() != 0)
    {
        auto aux = q.top();
        q.pop();
    }
}</pre>
```

6.5. KRUSKAL.

```
class ufds
{
private:
    vector<int> p, rank, sizeSet;
    int disjoinSet;

public:
    ufds(int n)
    {
        p.assign(n, 0);
        rank.assign(n, 0);
        sizeSet.assign(n, 1);
        disjoinSet = n;
        for (int i = 0; i < n; i++)
        {
            p[i] = i;
        }
}</pre>
```

```
return bridges;
}
```

```
int k = aux.second;
if (mask[k])
    continue;

mask[k] = true;
    cost += abs(aux.first);

for (int i = 0; i < adj[k].size(); i++)
{
    if (!mask[adj[k][i][0]])
    {
        q.push({-adj[k][i][1], adj[k][i][0]});
    }
}
return cost;
}</pre>
```

```
int find(int n)
{
    if (n == p[n])
        return n;
    p[n] = find(p[n]);
    return p[n];
}

bool isSameSet(int i, int j) { return find(i) == find(j); }

void unionSet(int i, int j)
{
    if (!isSameSet(i, j))
```

```
disjoinSet--;
        int x = find(i);
        int y = find(j);
        if (rank[x] > rank[y])
           p[y] = x;
           sizeSet[x] += sizeSet[y];
        else
           p[x] = y;
           sizeSet[y] += sizeSet[x];
           if (rank[x] == rank[y])
              rank[y]++;
     }
  int numDisjoinset() { return disjoinSet; }
  int sizeofSet(int i) { return sizeSet[find(i)]; }
};
// Function to find sum of weights of edges of the Minimum Spanning Tree.
int spanningTreeKruskal(int V, vector<vector<int>> adj[])
  ufds dsu(V);
```

6.6. BELLMAN FORD.

```
int infinite = (int)1e9;

vector<int> bellman_ford(int V, vector<vector<int>> &edges, int S)
{
   vector<int> d;
   d.assign(V, infinite);
   d[S] = 0;

   for (int i = 0; i < V - 1; i++)
   {
      for (int j = 0; j < edges.size(); j++)
      {
       if (d[edges[j][0]] + edges[j][2] < d[edges[j][1]])
            {
            d[edges[j][1]] = d[edges[j][0]] + edges[j][2];
            }
}</pre>
```

```
vector<pair<int, pair<int, int>>> a;
for (int i = 0; i < V; i++)</pre>
   for (int j = 0; j < adj[i].size(); j++)</pre>
      a.push_back({adj[i][j][1], {i, adj[i][j][0]}});
sort(a.begin(), a.end());
int cost = 0;
for (int i = 0; i < a.size(); i++)</pre>
   if (!dsu.isSameSet(a[i].second.first, a[i].second.second))
      cost += a[i].first;
      dsu.unionSet(a[i].second.first, a[i].second.second);
return cost;
for (int j = 0; j < edges.size(); j++)</pre>
   if (d[edges[j][0]] + edges[j][2] < d[edges[j][1]])</pre>
      vector<int> resp(1);
     resp[0] = -1;
```

return resp;

return d;

6.7. **DINIC.**

```
template <typename flow_type>
struct dinic
  struct edge
     size_t src, dst, rev;
     flow_type flow, cap;
  int n;
  vector<vector<edge>> adj;
  dinic(int n) : n(n), adj(n), level(n), q(n), it(n) {}
  void add_edge(size_t src, size_t dst, flow_type cap, flow_type rcap = 0)
     adj[src].push_back({src, dst, adj[dst].size(), 0, cap});
     if (src == dst)
        adj[src].back().rev++;
     adj[dst].push_back({dst, src, adj[src].size() - 1, 0, rcap});
  vector<int> level, q, it;
  bool bfs(int source, int sink)
     fill(level.begin(), level.end(), -1);
     for (int qf = level[q[0] = sink] = 0, qb = 1; qf < qb; ++qf)
        sink = q[qf];
        for (edge &e : adj[sink])
            edge &r = adj[e.dst][e.rev];
            if (r.flow < r.cap && level[e.dst] == -1)</pre>
              level[q[qb++] = e.dst] = 1 + level[sink];
     return level[source] != -1;
```

```
flow_type augment(int source, int sink, flow_type flow)
      if (source == sink)
         return flow;
      for (; it[source] != adj[source].size(); ++it[source])
         edge &e = adj[source][it[source]];
         if (e.flow < e.cap && level[e.dst] + 1 == level[source])</pre>
            flow_type delta = augment(e.dst, sink, min(flow, e.cap - e.flow));
            if (delta > 0)
               e.flow += delta;
               adj[e.dst][e.rev].flow -= delta;
               return delta;
      return 0;
   flow_type max_flow(int source, int sink)
      for (int u = 0; u < n; ++u)
         for (edge &e : adj[u])
            e.flow = 0;
      flow_type flow = 0;
      flow_type oo = numeric_limits<flow_type>::max();
      while (bfs(source, sink))
         fill(it.begin(), it.end(), 0);
         for (flow_type f; (f = augment(source, sink, oo)) > 0;)
            flow += f;
      } // level[u] = -1 => source side of min cut
      return flow;
};
```

6.8. CENTROID DESCOMPOSITION.

```
const int MAXN = 2e5 + 5;
vi ady[MAXN];
bitset<MAXN> is_centroid;
int sz[MAXN], ct_par[MAXN];
void centroid_dfs(int node, int parent)
   sz[node] = 1;
   for (int &nxt : ady[node])
     if (is_centroid[nxt] || nxt == parent)
         continue;
     centroid_dfs(nxt, node);
     sz[node] += sz[nxt];
int get_centroid(int node, int parent, int tree_sz)
   for (int nxt : ady[node])
     if (is_centroid[nxt] || nxt == parent)
         continue;
     if (sz[nxt] * 2 > tree_sz)
         return get_centroid(nxt, node, tree_sz);
  return node;
void centroid_decomp(int node, int parent = -1)
   centroid_dfs(node, -1);
```

6.9. LOWER BOUND FLOW.

```
template <typename T>
struct dinic
{
    struct edge
    {
        int src, dst;
        T low, cap, flow;
```

```
int tree_sz = sz[node];
   int centroid = get_centroid(node, -1, tree_sz);
   is_centroid[centroid] = 1;
   ct_par[centroid] = parent;
   for (int &child : ady[centroid])
      if (is_centroid[child])
         continue;
      centroid_decomp(child, centroid);
void solve()
int32_t main()
   ios_base::sync_with_stdio(0);
   cin.tie(0);
   int t;
   cin >> t;
   for (int i = 0; i < t; i++)</pre>
      solve();
   return 0;
```

```
int rev;
};
int n;
vector<vector<edge>> adj;
dinic(int n) : n(n), adj(n + 2) {}
```

```
void add_edge(int src, int dst, T low, T cap)
  adj[src].push_back({src, dst, low, cap, 0, (int)adj[dst].size()});
  if (src == dst)
     adj[src].back().rev++;
  adj[dst].push_back({dst, src, 0, 0, 0, (int)adj[src].size() - 1});
vector<int> level, iter;
T augment (int u, int t, T cur)
  if (u == t)
      return cur;
  for (int &i = iter[u]; i < (int)adj[u].size(); ++i)</pre>
      edge &e = adj[u][i];
      if (e.cap - e.flow > 0 && level[u] > level[e.dst])
        T f = augment(e.dst, t, min(cur, e.cap - e.flow));
        if (f > 0)
            e.flow += f;
            adj[e.dst][e.rev].flow -= f;
            return f;
     }
  return 0;
int bfs(int s, int t)
  level.assign(n + 2, n + 2);
  level[t] = 0;
  queue<int> Q;
  for (Q.push(t); !Q.empty(); Q.pop())
      int u = Q.front();
      if (u == s)
        break;
      for (edge &e : adj[u])
         edge &erev = adj[e.dst][e.rev];
         if (erev.cap - erev.flow > 0 && level[e.dst] > level[u] + 1)
            Q.push(e.dst);
```

```
level[e.dst] = level[u] + 1;
   return level[s];
const T oo = numeric_limits<T>::max();
T max_flow(int source, int sink)
  vector<T> delta(n + 2);
   for (int u = 0; u < n; ++u) // initialize
      for (auto &e : adj[u])
        delta[e.src] -= e.low;
        delta[e.dst] += e.low;
        e.cap -= e.low;
        e.flow = 0;
  T sum = 0;
   int s = n, t = n + 1;
   for (int u = 0; u < n; ++u)
      if (delta[u] > 0)
        add_edge(s, u, 0, delta[u]);
        sum += delta[u];
     else if (delta[u] < 0)</pre>
         add_edge(u, t, 0, -delta[u]);
  add_edge(sink, source, 0, oo);
  T flow = 0;
  while (bfs(s, t) < n + 2)
     iter.assign(n + 2, 0);
     for (T f; (f = augment(s, t, oo)) > 0;)
        flow += f;
  if (flow != sum)
```

```
return -1; // no solution

for (int u = 0; u < n; ++u)
    for (auto &e : adj[u])
    {
        e.cap += e.low;
        e.flow += e.low;
        edge &erev = adj[e.dst][e.rev];
        erev.cap -= e.low;
        erev.flow -= e.low;
    }

adj[sink].pop_back();</pre>
```

6.10. FLOYD WARSHALL.

6.11. **DFS BFS.**

```
void dfs_g(int n, int c, vi adj[], vector<bool> &visited, vi &cc)
{
    visited[n] = true;
    cc[n] = c;

    for (int i = 0; i < adj[n].size(); i++)
    {
        if (!visited[adj[n][i]])
            dfs_g(adj[n][i], c, adj, visited, cc);
    }
}</pre>
```

```
adj[source].pop_back();

while (bfs(source, sink) < n + 2)
{
    iter.assign(n + 2, 0);
    for (T f; (f = augment(source, sink, oo)) > 0;)
        flow += f;
    } // level[u] == n + 2 ==> s-side
    return flow;
}
```

```
void find_path_k(vector<vector<bool>>> &matrix, int k)
{
    for (int x = 0; x < k; x++)
    {
        for (int i = 0; i < matrix.size(); i++)
        {
            for (int j = 0; j < matrix[0].size(); j++)
              {
                 matrix[i][j] = matrix[i][j] || (matrix[i][x] && matrix[x][j]);
              }
        }
    }
}</pre>
```

```
vi bfs(int node, int n, vi adj[])
{
    vi result(n);
    vector<bool> visited;
    visited.assign(n, false);

    queue<int> q;
    visited[node] = true;

    q.push(node);

    while (q.size() != 0)
    {
        int w = q.front();
    }
}
```

6.12. SCC TARJANS.

```
q.pop();
      for (int i = 0; i < adj[w].size(); i++)</pre>
         if (!visited[adj[w][i]])
            q.push(adj[w][i]);
            result[adj[w][i]] = result[w] + 1;
            visited[adj[w][i]] = true;
   return result;
      cc_list[n] = cc;
void tarjans(int V, vector<int> adj[])
   vector<int> new_adj[V];
   g_transp(V, adj, new_adj);
   mask.assign(V, false);
   cc_list.assign(V, -1);
   for (int i = 0; i < V; i++)</pre>
      if (mask[i])
         continue;
      dfs_visit(i, adj, -1);
   for (int i = 0; i < V; i++)</pre>
      mask[i] = false;
   int ind = 0;
   while (q.size() != 0)
```

```
int act = q.top();
q.pop();
if (!mask[act])
{
```

6.13. MIN COST MAX FLOW.

```
template <typename flow_type, typename cost_type>
struct min_cost_max_flow
     struct edge
            size_t src, dst, rev;
            flow_type flow, cap;
            cost_type cost;
     };
     int n;
     vector<vector<edge>> adj;
     min_cost_max_flow(int n) : n(n), adj(n), potential(n), dist(n), back(n) {}
     void add_edge(size_t src, size_t dst, flow_type cap, cost_type cost)
            adj[src].push_back({src, dst, adj[dst].size(), 0, cap, cost});
            if (src == dst)
                  adj[src].back().rev++;
            adj[dst].push_back({dst, src, adj[src].size() - 1, 0, 0, -cost});
     vector<cost_type> potential;
     inline cost_type rcost(const edge &e)
            return e.cost + potential[e.src] - potential[e.dst];
     void bellman_ford(int source)
            for (int k = 0; k < n; ++k)
                  for (int u = 0; u < n; ++u)
                        for (edge &e : adj[u])
                              if (e.cap > 0 && rcost(e) < 0)</pre>
```

```
potential[e.dst] += rcost(e);
}
const cost_type oo = numeric_limits<cost_type>::max();
vector<cost_type> dist;
vector<edge *> back;
cost_type dijkstra(int source, int sink)
      fill(dist.begin(), dist.end(), oo);
      typedef pair<cost_type, int> node;
      priority_queue<node, vector<node>, greater<node>> pq;
      for (pq.push({dist[source] = 0, source}); !pq.empty();)
            node p = pq.top();
            pq.pop();
            if (dist[p.second] < p.first)</pre>
                  continue;
            if (p.second == sink)
                  break;
            for (edge &e : adj[p.second])
                  if (e.flow < e.cap && dist[e.dst] >
                              dist[e.src] + rcost(e))
                        back[e.dst] = &e;
                        pq.push({dist[e.dst] =
                              dist[e.src] + rcost(e), e.dst});
                  }
      return dist[sink];
```

dfs_visit(act, new_adj, ind);

ind++;

6.14. ARTICULATION POINT.

```
vector<bool> visited;
vi t;
vi low;
vector<bool> art;
void dfs_art(vi adj[], int n, int p, int q)
   t[n] = q;
   low[n] = q++;
   visited[n] = true;
   int \dot{j} = 0;
   for (int i = 0; i < adj[n].size(); i++)</pre>
      if (!visited[adj[n][i]])
         dfs_art(adj, adj[n][i], n, q);
         low[n] = min(low[adj[n][i]], low[n]);
         j++;
         if (low[adj[n][i]] >= t[n] && p != -1)
            art[n] = true;
```

}

6.15. **KUHN.**

```
const int MAXN = 2 * 1e5 + 5;
int n, m;
vi mt;
vi ady[MAXN];
vector<bool> used;
vector<bool> visitedx;
vector<bool> visitedy;
vector<bool> coverx;
vector<bool> covery;
bool try_kuhn(int v)
   if (used[v])
     return false;
   used[v] = true;
   for (int to : ady[v])
     if (mt[to] == -1 || try_kuhn(mt[to]))
        mt[to] = v;
        return true;
   return false;
void augm_path(int n, bool isX)
  if (isX)
     visitedx[n] = true;
   else
     visitedy[n] = true;
  if (!isX)
     if (!visitedx[mt[n]])
        augm_path(mt[n], true);
```

}

```
return;
   for (auto i : ady[n])
      if (!visitedy[i])
         augm_path(i, false);
int32_t main()
   ios_base::sync_with_stdio(0);
   cin.tie(0);
   cin >> n >> m;
   forl(i, 1, m)
     int a, b;
      cin >> a >> b;
     ady[a].pb(b);
   int max_matching = 0;
   mt.assign(m + 1, -1);
   int ans = 0;
   for (int v = 1; v <= n; v++)</pre>
     used.assign(n + 1, false);
     if (try_kuhn(v))
        max_matching++;
   // vertex cover
   visitedx.assign(n + 1, false);
   visitedy.assign(m + 1, false);
   used.assign(n + 1, false);
   for (int v = 1; v \le m; v++)
     if (mt[v] != −1)
        used[mt[v]] = true;
```

```
for (int v = 1; v <= n; v++)
   if (!used[v] && !visitedx[v])
        augm_path(v, true);

coverx.assign(n + 1, false);
covery.assign(m + 1, false);

for (int v = 1; v <= n; v++)
   if (!visitedx[v])</pre>
```

```
coverx[v] = true;

for (int v = 1; v <= m; v++)
   if (visitedy[v])
      covery[v] = true;

cout << max_matching << '\n';
   return 0;
}</pre>
```