COMS W4115

Programming Languages and Translators Lecture 9: Predictive Top-Down Parsers February 20, 2013

Lecture Outline

- 1. Review
- 2. FIRST
- 3. FOLLOW
- 4. How to construct a predictive parsing table
- 5. LL(1) grammars
- 6. Transformations on grammars

1. Review

- Top-down parsing consists of constructing or tracing a parse tree for an input string starting from the root and creating the nodes of the parse tree in preorder.
- Recursive-descent parsing is a top-down method of syntax analysis in which a set of recursive procedures is used to process the input string with a procedure
 associated with each nonterminal of the grammar. See Fig. 4.13, p. 219.
- · A nonrecursive predictive parser uses an explicit stack and a parsing table to do deterministic top-down parsing.
- In this class we will develop an algorithm to construct a predictive parsing table for a large class of useful grammars called LL(1) grammars.
- · For this algorithm we need two functions on grammars, FIRST and FOLLOW.

2. FIRST

- FIRST(α) is the set of terminal symbols that begin the strings derivable from a string of terminal and nonterminal symbols α in a grammar.
 If α can derive ε, then ε is also in FIRST(α).
- Algorithm to compute FIRST(X):
- 1. If X is a terminal, then $FIRST(X) = \{X\}$.
- 2. If $X \hat{a}^{\dagger}$ $\hat{l}\mu$ is a production, then add $\hat{l}\mu$ to FIRST(X).
- If X â†' Y₁ Y₂ ... Y_k is a production for k ≥ 1, and for some i ≤ k, Y₁Y₂ ... Y_k derives the empty string, and a is in FIRST(Y_k), then add a to FIRST(X).
 If Y₁Y₂ ... Y_k derives the empty string, then add ε to FIRST(X).
- Example. Consider the grammar G:

```
S â†' ( S ) S | Î\mu
For G, FIRST(S) = {(, Î\mu}.
```

3. FOLLOW

- FOLLOW(A) is the set of terminals that can appear immediately to the right of A in some sentential form in a grammar.

 Let us assume the string to be parsed is terminated by an end-of-string endmarker \$. Then if A can be the rightmost symbol in some sentential form, the right endmarker \$ is also in FOLLOW(A).
- Algorithm to compute FOLLOW(A) for all nonterminals A of a grammar:
- 1. Place \$ in FOLLOW(S) where S is the start symbol of the grammar.
- 2. If $A \hat{a}^{\dagger}$, $\hat{l} \pm B \hat{l}^2$ is a production, then add every terminal symbol a in FIRST(\hat{l}^2) to FOLLOW(B).
- 3. If there is a production A \hat{a} †' $\hat{1}\pm B$, or a production A \hat{a} †' $\hat{1}\pm B\hat{1}^2$, where FIRST($\hat{1}^2$) contains $\hat{1}\mu$, then add every symbol in FOLLOW(A) to FOLLOW(B).
- **Example.** For G above, FOLLOW(S) = $\{ \}$, $\{ \}$.

4. How to Construct a Predictive Parsing Table

- Input: Grammar G.
- Output: Predictive parsing table M.
- · Method:

```
for (each production A \hat{a} \dagger' \hat{1} \pm in G) {
	for (each terminal a in FIRST(\hat{1} \pm i))
	add A \hat{a} \dagger' \hat{1} \pm in M[A, a];
	if (\hat{1}\mu is in FIRST(\hat{1} \pm i))
	for (each symbol b in FOLLOW(A))
```

```
\label{eq:add A at matter} \mbox{ add A at matter} \ \ \mbox{ add A at matter} \ \ \mbox{ at make each undefined entry of M be error;} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \mbox{ add A at matter} \ \mbox{ at matter} \ \
```

• Example 1. Predictive parsing table for the grammar:

• Example 2. Predictive parsing table for the grammar:

• Example 3. Predictive parsing table for the grammar:

5. LL(1) Grammars

- A grammar is LL(1) iff whenever A â†' α | β are two distinct productions, the following three conditions hold:
- 1. For no terminal a do both $\hat{l}\pm$ and \hat{l}^2 derive strings beginning with a.
- 2. At most one of α and β can derive the empty string.
- 3. If β derives the empty string, then α does not derive any string beginning with a terminal in FOLLOW(A). Likewise, if α derives the empty string, then β does not derive any string beginning with a terminal in FOLLOW(A).
- We can use the algorithm above to construct a predictive parsing table with uniquely defined entries for any LL(1) grammar.
- The first "L" in LL(1) means scanning the input from left to right, the second "L" for producing a leftmost derivation, and the "1" for using one symbol of lookahead to make each parsing action decision.

6. Transformations on Grammars

- Two common language-preserving transformations are often applied to grammars to try to make them parsable by top-down methods. These are eliminating
 left recursion and left factoring.
- Eliminating left recursion:
 - Replace

```
expr â†' expr + term
| term
```

```
expr â†' term expr'
expr'â†' + term expr'
| îµ
```

- Left factoring:
- Replace

by

7. Practice Problems

Consider the following grammar G for Boolean expressions:

```
B â†' B or T | T
T â†' T and F | F
F â†' not B | ( B ) | true | false
```

- ullet What precedence and associativity does this grammar give to the operators and , or , not?
- Compute FIRST and FOLLOW for each nonterminal in G.
- Transform G into an equivalent LL(1) grammar G'.
- Construct a predictive parsing table for G'.
- Show how your predictive parser processes the input string

```
true and not false or true
```

Draw the parse tree traced out by your parser.

8. Reading

• ALSU, Section 4.4.