

Lab Three

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1 CRAFTING A COMPILER

1.1 EXERCISE 4.7

A grammar for infix expressions follows:

```
1 Start → E $
2 E   → T plus E
3     | T
4 T   → T times F
5     | F
6 F   → ( E )
7     | num
```

(a) Show the leftmost derivation of the following string.
num plus num times num plus num \$

```
<Start>
<E> $
<T> plus <E> $
<F> plus <E> $
num plus <E> $
num plus <T> plus <E> $
num plus <T> times <F> plus <E> $
num plus <F> times <F> plus <E> $
num plus num times <F> plus <E> $
num plus num times num plus <E> $
num plus num times num plus <T> $
num plus num times num plus <F> $
num plus num times num plus num $
```

(b) Show the rightmost derivation of the following string.
 num times num plus num times num \$

```

<Start>
<E> $
<T> plus <E> $
<T> plus <T> $
<T> plus <T> times <F> $
<T> plus <T> times num $
<T> plus <F> times num $
<T> plus num times num $
<T> times <F> plus num times num $
<T> times num plus num times num $
<F> times num plus num times num $
num times num plus num times num $

```

(c) Describe how this grammar structures expressions, in terms of the precedence and left- or right- associativity of operators.

This grammar structures expressions with nonterminals on the left hand side and terminals on the right hand side. It uses a right associativity of its operators for <E> as <E> has the potential for the most expansion in the expression <T> plus <E>, but the grammar uses left associativity for <T> as <T> is the most expansive in the expression <T> times <F>.

1.2 EXERCISE 5.2

Consider the following grammar, which is already suitable for LL(1) parsing:

```

1 Start  → Value $
2 Value  → num
3        | lparen Expr rparen
4 Expr   → plus Value Value
5        | prod Values
6 Values → Value Values
7        | λ

```

(c) Construct a recursive-descent parser based on the grammar.

```

parseStart(){
  parseValue()
  match($)
}

parseValue(){
  if(currentToken is num){match(num)}
  else{
    match()
    parseExpr()
    match ()
  }
}

```

```

parseExpr(){
  if(currentToken is plus){
    match(plus)
    parseValue()
    parseValue()
  }
  else{
    match(prod)
    parseValues()
  }
}

parseValues(){
  if(currentToken is number or ( ){
    parseValue()
    parseValues()
  }
  else {
    /* epsilon production */
  }
}

match(expectedToken){
  retVal = false
  if(currentToken in expectedToken){
    retVal = true
  }
  return retVal
}

```

2 THE DRAGON BOOK

2.1 EXERCISE 4.2.1

Consider the context-free grammar:

$S \rightarrow S S + \mid S S * \mid a$

and the string $aa + a^*$.

a) Give a leftmost derivation for the string.

$\langle S \rangle$
 $\langle S \rangle \langle S \rangle *$
 $\langle S \rangle \langle S \rangle + \langle S \rangle *$
 $a \langle S \rangle + \langle S \rangle *$
 $aa + \langle S \rangle *$
 $aa + a^*$

b) Give a rightmost derivation for the string.

$\langle S \rangle$
 $\langle S \rangle \langle S \rangle *$
 $\langle S \rangle a^*$
 $\langle S \rangle \langle S \rangle + a^*$
 $\langle S \rangle a + a^*$
 $aa + a^*$

c) Give a parse tree for the string.

