

1 Start coding or generate with AI.

<https://link.springer.com/article/10.1007/s00170-024-14597-2#Sec28>

```
1 # Instalar uma fonte similar à Times New Roman
2 !apt-get install -y fonts-liberation
3
4 # Configurar o matplotlib para usar a fonte Liberation Serif, que é similar à Times New Roman
5 import matplotlib.pyplot as plt
6 import matplotlib.font_manager as fm
7
8 # Carregar a fonte instalada
9 font_path = '/usr/share/fonts/truetype/liberation/LiberationSerif-Regular.ttf'
10 fm.fontManager.addfont(font_path)
11 plt.rcParams['font.family'] = 'Liberation Serif'
```

```
➡ Reading package lists... Done
Building dependency tree... Done
Reading state information... Done
fonts-liberation is already the newest version (1:1.07.4-11).
0 upgraded, 0 newly installed, 0 to remove and 34 not upgraded.
```

```
1 import pandas as pd
2 import numpy as np
```

```
1 dados = pd.read_excel('/content/drive/MyDrive/ALEX_DOUTORADO_UNIFEI/TITANIUM/ti.xlsx')
2
```

```
1 dados.info()
```

```
➡ <class 'pandas.core.frame.DataFrame'>
RangeIndex: 287 entries, 0 to 286
Data columns (total 15 columns):
#   Column      Non-Null Count  Dtype
---  ---
0   Test        287 non-null    object
1   vc [m/min]   287 non-null    float64
2   f [mm/rev]   287 non-null    float64
3   Fc [N]       287 non-null    float64
4   σFc [N]      287 non-null    float64
5   Ff [N]       287 non-null    float64
6   σFf [N]      287 non-null    float64
7   rn [μm]      287 non-null    float64
8   σrn [μm]     287 non-null    float64
9   havg [μm]    287 non-null    object
10  ohavg [μm]   287 non-null    object
11  lcut [mm]    287 non-null    int64
12  Tchip [K]    287 non-null    object
13  Wear         287 non-null    object
14  Status       287 non-null    object
dtypes: float64(8), int64(1), object(6)
memory usage: 33.8+ KB
```

```
1 df = dados
```

```
1 # Extrair os valores mínimo e máximo de vc [m/min] e f [mm/rev]
2 min_vc = df["vc [m/min]"].min()
3 max_vc = df["vc [m/min]"].max()
4
5 min_f = df["f [mm/rev]"].min()
6 max_f = df["f [mm/rev]"].max()
7
8 # Exibir os resultados
9 print(f"Cutting speed (vc) - Min: {min_vc} | Max: {max_vc}")
10 print(f"Feed rate (f) - Min: {min_f} | Max: {max_f}")
```

```
➡ Cutting speed (vc) - Min: 10.0 | Max: 500.0
Feed rate (f) - Min: 0.01 | Max: 0.4
```

```
1 import pandas as pd
2
3 # Carregar os dados (supondo que já estejam disponíveis no ambiente)
4 df = pd.read_csv('dados_experimento.csv') # Exemplo de como carregar caso estivesse em um arquivo
5
6 # Exibir um resumo dos níveis de velocidade de corte (vc) e avanço (f)
7 vc_levels = df["vc [m/min]"].unique()
8 f_levels = df["f [mm/rev]"].unique()
9
```

```

10 # Contar quantos níveis distintos existem para vc e f
11 num_vc_levels = len(vc_levels)
12 num_f_levels = len(f_levels)
13
14 # Contar quantas combinações únicas de (vc, f) existem
15 num_unique_combinations = df.groupby(["vc [m/min]", "f [mm/rev]").ngroups
16
17 # Exibir os resultados
18 num_vc_levels, num_f_levels, num_unique_combinations
19

```

➦ (26, 11, 109)

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```
1 dados.info()
```

➦

```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 287 entries, 0 to 286
Data columns (total 15 columns):
#   Column                Non-Null Count  Dtype
---  ---
0   Test                   287 non-null   object
1   vc [m/min]             287 non-null   float64
2   f [mm/rev]             287 non-null   float64
3   Fc [N]                 287 non-null   float64
4   σFc [N]                287 non-null   float64
5   Ff [N]                 287 non-null   float64
6   σFf [N]                287 non-null   float64
7   rn [μm]                287 non-null   float64
8   σrn [μm]               287 non-null   float64
9   havg [μm]              287 non-null   object
10  σhavg [μm]              287 non-null   object
11  lcut [mm]               287 non-null   int64
12  Tchip [K]               287 non-null   object
13  Wear                    287 non-null   object
14  Status                  287 non-null   object
dtypes: float64(8), int64(1), object(6)
memory usage: 33.8+ KB

```

```

1 # 2. Substituir '-' por NaN em todas as colunas
2 dados.replace('-', np.nan, inplace=True)

```

➦ <ipython-input-9-132c6ea6bcaa>:2: FutureWarning: Downcasting behavior in `replace` is deprecated and will be removed in a future version
dados.replace('-', np.nan, inplace=True)

✓ AQUI VAMOS FAZER UMA MODELAGEM PARA PEVER O DESGASTE (WEAR)

```
1 df = dados
```

```

1 X = df[['vc [m/min]', 'f [mm/rev]', 'Fc [N]', 'σFc [N]', 'Ff [N]', 'σFf [N]', 'rn [μm]', 'σrn [μm]', 'lcut [mm]']]
2 y = df['Wear']
3

```

```

1 from sklearn.preprocessing import LabelEncoder
2
3 le = LabelEncoder()
4 y_encoded = le.fit_transform(y)
5

```

```

1 from sklearn.model_selection import train_test_split
2
3 X_train, X_test, y_train, y_test = train_test_split(X, y_encoded, test_size=0.2, random_state=42)
4

```

```

1 from sklearn.ensemble import RandomForestClassifier
2 from sklearn.metrics import classification_report, confusion_matrix
3
4 model = RandomForestClassifier(n_estimators=100, random_state=42)
5 model.fit(X_train, y_train)
6
7 y_pred = model.predict(X_test)
8 print(classification_report(y_test, y_pred, target_names=le.classes_))
9 print(confusion_matrix(y_test, y_pred))
10

```

```

↔
precision    recall  f1-score   support

H           1.00        1.00        1.00         1
L           0.75        1.00        0.86        27
M           1.00        0.70        0.82        30

accuracy          0.84        58
macro avg         0.92        0.90        0.89        58
weighted avg      0.88        0.84        0.84        58

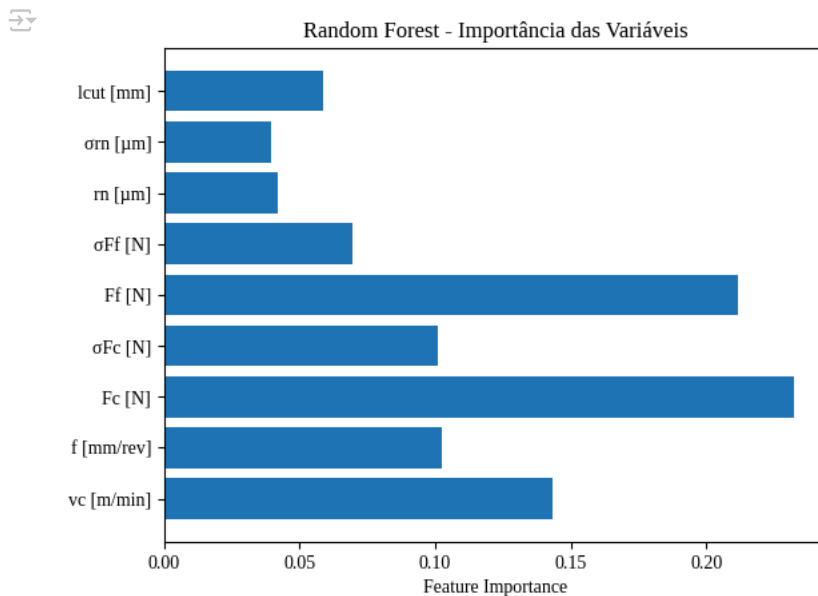
[[ 1  0  0]
 [ 0 27  0]
 [ 0  9 21]]

```

```

1 import matplotlib.pyplot as plt
2
3 importances = model.feature_importances_
4 plt.barh(X.columns, importances)
5 plt.xlabel("Feature Importance")
6 plt.title("Random Forest - Importância das Variáveis")
7 plt.show()
8

```



1 Start coding or [generate](#) with AI.

```


1 import pandas as pd
2 from sklearn.linear_model import LogisticRegression
3 from sklearn.model_selection import train_test_split
4 from sklearn.preprocessing import LabelEncoder
5 import numpy as np
6
7 # Exemplo: carregando os dados
8 # df = pd.read_csv('seus_dados.csv')
9
10 # Seleção de variáveis numéricas (ajuste conforme seus dados reais)
11 X = df[['vc [m/min]', 'f [mm/rev]', 'Fc [N]', 'σFc [N]', 'Ff [N]', 'σFf [N]', 'rn [μm]', 'orn [μm]', 'lcut [mm]']]
12
13 # Codificando a variável resposta
14 le = LabelEncoder()
15 y = le.fit_transform(df['Wear']) # L=0, M=1, H=2 (por exemplo)
16
17 # Divisão treino/teste
18 X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=42, test_size=0.2)
19
20 # Modelo de regressão logística multinomial
21 model = LogisticRegression(multi_class='multinomial', solver='lbfgs', max_iter=1000)
22 model.fit(X_train, y_train)
23
24 # Coeficientes
25 classes = le.classes_
26 coefs = model.coef_ # shape (n_classes, n_features)
27 intercepts = model.intercept_
28
29 # Exibindo as equações
30 print("EQUAÇÕES DE PROBABILIDADE PARA CADA CLASSE (L, M, H):\n")
31

```

```

32 for idx, cls in enumerate(classes):
33     eq = f"P(Wear={cls}) = exp({intercepts[idx]:.3f})"
34     for i, col in enumerate(X.columns):
35         coef = coefs[idx][i]
36         eq += f" + {coef:.3f}*{col}"
37     eq += ") / DENOMINADOR"
38     print(eq)
39     print()
40
41 # Exemplo de previsão de probabilidades para o conjunto de teste
42 probs = model.predict_proba(X_test)
43
44 # Mostrando a probabilidade das 5 primeiras amostras
45 for i in range(5):
46     print(f"Amostra {i+1}: {dict(zip(classes, probs[i]))}")
47

```

 /usr/local/lib/python3.11/dist-packages/sklearn/linear_model/_logistic.py:1247: FutureWarning: 'multi_class' was deprecated in versi
warnings.warn(
EQUAÇÕES DE PROBABILIDADE PARA CADA CLASSE (L, M, H):

```

P(Wear=H) = exp(-0.016 + 0.008*vc [m/min] + 0.001*f [mm/rev] + -0.064*Fc [N] + 0.023*oFc [N] + 0.165*Ff [N] + 0.446*oFf [N] + -0.47:
P(Wear=L) = exp(0.262 + -0.005*vc [m/min] + -0.013*f [mm/rev] + 0.014*Fc [N] + 0.786*oFc [N] + -0.119*Ff [N] + -0.483*oFf [N] + 0.4:
P(Wear=M) = exp(-0.245 + -0.003*vc [m/min] + 0.012*f [mm/rev] + 0.050*Fc [N] + -0.809*oFc [N] + -0.046*Ff [N] + 0.038*oFf [N] + -0.:

Amostra 1: {'H': np.float64(2.705240923298819e-05), 'L': np.float64(0.9996400822292548), 'M': np.float64(0.0003328653615123293)}
Amostra 2: {'H': np.float64(7.76982974548448e-08), 'L': np.float64(0.4932299896671144), 'M': np.float64(0.506769932634588)}
Amostra 3: {'H': np.float64(1.7483458412442998e-07), 'L': np.float64(0.30154799240733277), 'M': np.float64(0.6984518327580831)}
Amostra 4: {'H': np.float64(5.446059894142669e-09), 'L': np.float64(0.020380957634704513), 'M': np.float64(0.9796190369192357)}
Amostra 5: {'H': np.float64(1.3102196551505972e-07), 'L': np.float64(0.9062259841674062), 'M': np.float64(0.09377388481062839)}
/usr/local/lib/python3.11/dist-packages/sklearn/linear_model/_logistic.py:465: ConvergenceWarning: lbfgs failed to converge (status=
STOP: TOTAL NO. OF ITERATIONS REACHED LIMIT.

```

Increase the number of iterations (max_iter) or scale the data as shown in:
<https://scikit-learn.org/stable/modules/preprocessing.html>
Please also refer to the documentation for alternative solver options:
https://scikit-learn.org/stable/modules/linear_model.html#logistic-regression
n_iter_i = _check_optimize_result(

```


1 import pandas as pd
2 import numpy as np
3 from sklearn.linear_model import LogisticRegression
4 from sklearn.model_selection import train_test_split
5 from sklearn.preprocessing import LabelEncoder, StandardScaler
6 import statsmodels.api as sm
7
8 # Exemplo: carregando os dados
9 # df = pd.read_csv('seus_dados.csv')
10
11 # Seleção de variáveis numéricas
12 X = df[['vc [m/min]', 'f [mm/rev]', 'Fc [N]', 'oFc [N]', 'Ff [N]', 'oFf [N]', 'rn [μm]', 'orn [μm]', 'lcut [mm]']]
13
14 # Codificando a variável resposta
15 le = LabelEncoder()
16 y = le.fit_transform(df['Wear']) # L=0, M=1, H=2 (por exemplo)
17 classes = le.classes_
18
19 # Divisão treino/teste
20 X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=42, test_size=0.2)
21
22 # --- MODELO SKLEARN (para obtenção das equações)
23 model = LogisticRegression(multi_class='multinomial', solver='lbfgs', max_iter=1000)
24 model.fit(X_train, y_train)
25
26 # Coeficientes
27 coefs = model.coef_
28 intercepts = model.intercept_
29
30 print("EQUAÇÕES DE PROBABILIDADE PARA CADA CLASSE (L, M, H):\n")
31 for idx, cls in enumerate(classes):
32     eq = f"P(Wear={cls}) = exp({intercepts[idx]:.3f})"
33     for i, col in enumerate(X.columns):
34         coef = coefs[idx][i]
35         eq += f" + {coef:.3f}*{col}"
36     eq += ") / DENOMINADOR"
37     print(eq)
38     print()
39
40 # Exemplo de previsão de probabilidades
41 probs = model.predict_proba(X_test)
42 for i in range(5):

```

```

43     print(f"Amostra {i+1}: {dict(zip(classes, probs[i]))}")
44
45 # --- NORMALIZAÇÃO PARA STATS MODELS
46 scaler = StandardScaler()
47 X_scaled = scaler.fit_transform(X)
48
49 # Adiciona constante (intercepto)
50 X_sm = sm.add_constant(X_scaled)
51
52 # Modelo estatístico
53 model_sm = sm.MNLogit(y, X_sm)
54 result = model_sm.fit()
55
56 # Mostra os coeficientes com significância estatística
57 print("\n=== ANÁLISE ESTATÍSTICA DETALHADA (p-values, z-score) ===\n")
58 print(result.summary())
59
60

```

 /usr/local/lib/python3.11/dist-packages/sklearn/linear_model/_logistic.py:1247: FutureWarning: 'multi_class' was deprecated in ver
warnings.warn(

EQUAÇÕES DE PROBABILIDADE PARA CADA CLASSE (L, M, H):

$P(\text{Wear}=H) = \exp(-0.016 + 0.008*vc \text{ [m/min]} + 0.001*f \text{ [mm/rev]} + -0.064*Fc \text{ [N]} + 0.023*\sigma Fc \text{ [N]} + 0.165*Ff \text{ [N]} + 0.446*\sigma Ff \text{ [N]} + -0.4$

$P(\text{Wear}=L) = \exp(0.262 + -0.005*vc \text{ [m/min]} + -0.013*f \text{ [mm/rev]} + 0.014*Fc \text{ [N]} + 0.786*\sigma Fc \text{ [N]} + -0.119*Ff \text{ [N]} + -0.483*\sigma Ff \text{ [N]} + 0$

$P(\text{Wear}=M) = \exp(-0.245 + -0.003*vc \text{ [m/min]} + 0.012*f \text{ [mm/rev]} + 0.050*Fc \text{ [N]} + -0.809*\sigma Fc \text{ [N]} + -0.046*Ff \text{ [N]} + 0.038*\sigma Ff \text{ [N]} + -0$

Amostra 1: {'H': np.float64(2.705240923298819e-05), 'L': np.float64(0.9996400822292548), 'M': np.float64(0.0003328653615123293)}

Amostra 2: {'H': np.float64(7.76982974548448e-08), 'L': np.float64(0.4932299896671144), 'M': np.float64(0.506769932634588)}

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Amostra 4: {'H': np.float64(5.446059894142669e-09), 'L': np.float64(0.020380957634704513), 'M': np.float64(0.9796190369192357)}

Amostra 5: {'H': np.float64(1.3102196551505972e-07), 'L': np.float64(0.9062259841674062), 'M': np.float64(0.09377388481062839)}

Optimization terminated successfully.

Current function value: nan

Iterations 34

=== ANÁLISE ESTATÍSTICA DETALHADA (p-values, z-score) ===

MNLogit Regression Results

```

=====
Dep. Variable:          y      No. Observations:          287
Model:                MNLogit  Df Residuals:              267
Method:                MLE      Df Model:                18
Date:                Thu, 01 May 2025  Pseudo R-squ.:          nan
Time:                16:52:42    Log-Likelihood:         nan
converged:              True      LL-Null:              -215.85
Covariance Type:      nonrobust  LLR p-value:          nan
=====

```

	y=1	coef	std err	z	P> z	[0.025	0.975]
const		nan	nan	nan	nan	nan	nan
x1		nan	nan	nan	nan	nan	nan
x2		nan	nan	nan	nan	nan	nan
x3		nan	nan	nan	nan	nan	nan
x4		nan	nan	nan	nan	nan	nan
x5		nan	nan	nan	nan	nan	nan
x6		nan	nan	nan	nan	nan	nan
x7		nan	nan	nan	nan	nan	nan
x8		nan	nan	nan	nan	nan	nan
x9		nan	nan	nan	nan	nan	nan

	y=2	coef	std err	z	P> z	[0.025	0.975]
const		nan	nan	nan	nan	nan	nan
x1		nan	nan	nan	nan	nan	nan
x2		nan	nan	nan	nan	nan	nan
x3		nan	nan	nan	nan	nan	nan
x4		nan	nan	nan	nan	nan	nan
x5		nan	nan	nan	nan	nan	nan
x6		nan	nan	nan	nan	nan	nan
x7		nan	nan	nan	nan	nan	nan
x8		nan	nan	nan	nan	nan	nan
x9		nan	nan	nan	nan	nan	nan

```

1 from statsmodels.stats.outliers_influence import variance_inflation_factor
2
3 vif = pd.DataFrame()
4 vif["feature"] = X.columns
5 vif["VIF"] = [variance_inflation_factor(X.values, i) for i in range(X.shape[1])]
6 print(vif)
7

```

```

feature      VIF
0 vc [m/min] 2.880643
1 f [mm/rev] 45.539730
2 Fc [N]     94.150085
3 σFc [N]    5.782419
4 Ff [N]     35.595913
5 σFf [N]    4.253478
6 rn [μm]    38.777892
7 σrn [μm]   11.814109
8 lcut [mm]  20.186063

```

```

1 X_reduced = X.drop(columns=['Fc [N]', 'f [mm/rev]', 'Ff [N]', 'rn [μm]', 'σrn [μm]', 'lcut [mm]'])
2

```

```

1 import pandas as pd
2 import numpy as np
3 from sklearn.preprocessing import LabelEncoder, StandardScaler
4 import statsmodels.api as sm
5
6 # Exemplo: carregando os dados
7 df = pd.read_csv('seus_dados.csv')
8
9 # Remover classe 'H'
10 df_filtered = df[df['Wear'] != 'H'].copy()
11
12 # Variáveis de entrada com VIF aceitável
13 X = df_filtered[['vc [m/min]', 'σFc [N]', 'σFf [N]']]
14
15 # Codificar variável alvo (L = 0, M = 1)
16 le = LabelEncoder()
17 y = le.fit_transform(df_filtered['Wear']) # L = 0, M = 1
18
19 # Normalizar
20 scaler = StandardScaler()
21 X_scaled = scaler.fit_transform(X)
22 X_scaled = sm.add_constant(X_scaled)
23
24 # Regressão logística binária
25 model = sm.Logit(y, X_scaled)
26 result = model.fit()
27
28 # Resultado
29 print("\n=== Regressão logística binária: Wear M (1) vs L (0) ===\n")
30 print(result.summary())
31
32

```

```

Optimization terminated successfully.
Current function value: 0.666751
Iterations 4

```

=== Regressão logística binária: Wear M (1) vs L (0) ===

```

Logit Regression Results
=====
Dep. Variable:          y      No. Observations:          282
Model:                  Logit   Df Residuals:              278
Method:                  MLE    Df Model:                3
Date:                   Thu, 01 May 2025   Pseudo R-squ.:          0.01375
Time:                   17:38:15   Log-Likelihood:         -188.02
Converged:               True     LL-Null:               -190.65
Covariance Type:         nonrobust   LLR p-value:            0.1548
=====

```

	coef	std err	z	P> z	[0.025	0.975]
const	-0.3769	0.122	-3.080	0.002	-0.617	-0.137
x1	0.0916	0.130	0.702	0.482	-0.164	0.347
x2	0.4147	0.210	1.975	0.048	0.003	0.826
x3	-0.1852	0.212	-0.873	0.383	-0.601	0.231

```

=====

```

```

1 # Extrair coeficientes
2 params = result.params
3 intercept = params[0]
4 coef_names = ['vc [m/min]', 'σFc [N]', 'σFf [N]']
5 coefs = params[1:]
6
7 # Montar equação
8 eq = f"P(Wear = M) = 1 / (1 + exp(-({intercept:.3f})"
9 for name, coef in zip(coef_names, coefs):
10     eq += f" + {coef:.3f}*{name}"
11 eq += ")))"
12

```

```

13 print("\n=== EQUAÇÃO DE REGRESSÃO LOGÍSTICA ===")
14 print(eq)
15

```



```

=== EQUAÇÃO DE REGRESSÃO LOGÍSTICA ===
P(Wear = M) = 1 / (1 + exp(-(-0.377 + 0.092*vc [m/min] + 0.415*σFc [N] + -0.185*σFf [N])))

```

✓ SEM H E COM TODAS AS VERIAVEIS

```

1 import pandas as pd
2 import numpy as np
3 from sklearn.preprocessing import LabelEncoder, StandardScaler
4 import statsmodels.api as sm
5
6 # Exemplo: df = pd.read_csv('seus_dados.csv')
7
8 # 1. Filtrar apenas classes L e M
9 df_filtered = df[df['Wear'].isin(['L', 'M'])].copy()
10
11 # 2. Selecionar todas as variáveis numéricas
12 X = df_filtered[['vc [m/min]', 'f [mm/rev]', 'Fc [N]', 'σFc [N]', 'Ff [N]', 'σFf [N]', 'rn [μm]', 'σrn [μm]', 'lcut [mm]']]
13
14 # 3. Codificar variável alvo (L = 0, M = 1)
15 le = LabelEncoder()
16 y = le.fit_transform(df_filtered['Wear']) # L=0, M=1
17
18 # 4. Normalizar e adicionar intercepto
19 scaler = StandardScaler()
20 X_scaled = scaler.fit_transform(X)
21 X_scaled = sm.add_constant(X_scaled)
22
23 # 5. Ajustar o modelo logístico binário
24 model = sm.Logit(y, X_scaled)
25 result = model.fit()
26
27 # 6. Mostrar análise estatística
28 print("\n=== RESULTADOS DA REGRESSÃO LOGÍSTICA BINÁRIA: M (1) vs L (0) ===\n")
29 print(result.summary())
30
31 # 7. Gerar equação interpretável
32 params = result.params
33 intercept = params[0]
34 coef_names = X.columns
35 coefs = params[1:]
36
37 eq = f"P(Wear = M) = 1 / (1 + exp(-({intercept:.3f})"
38 for name, coef in zip(coef_names, coefs):
39     eq += f" + {coef:.3f}*{name}"
40 eq += ")))"
41
42 print("\n=== EQUAÇÃO DE REGRESSÃO LOGÍSTICA BINÁRIA ===")
43 print(eq)
44

```



```

Optimization terminated successfully.
Current function value: 0.210220
Iterations 10

```

=== RESULTADOS DA REGRESSÃO LOGÍSTICA BINÁRIA: M (1) vs L (0) ===

```

Logit Regression Results
=====
Dep. Variable:          y      No. Observations:      282
Model:                Logit      Df Residuals:        272
Method:                MLE      Df Model:            9
Date:                Thu, 01 May 2025      Pseudo R-squ.:      0.6890
Time:                17:38:21      Log-Likelihood:     -59.282
converged:                True      LL-Null:         -190.65
Covariance Type:      nonrobust      LLR p-value:       2.042e-51
=====

```

	coef	std err	z	P> z	[0.025	0.975]
const	-0.2809	0.338	-0.831	0.406	-0.944	0.382
x1	0.0144	0.313	0.046	0.963	-0.600	0.629
x2	9.7638	2.905	3.361	0.001	4.069	15.458
x3	-4.4027	4.269	-1.031	0.302	-12.770	3.965
x4	-4.7901	1.246	-3.844	0.000	-7.233	-2.347
x5	3.5673	2.493	1.431	0.153	-1.320	8.454
x6	0.9200	0.892	1.031	0.303	-0.829	2.669
x7	-0.2201	0.580	-0.379	0.704	-1.358	0.917
x8	0.4024	0.273	1.475	0.140	-0.132	0.937

x9	3.6261	0.827	4.384	0.000	2.005	5.247
=====						

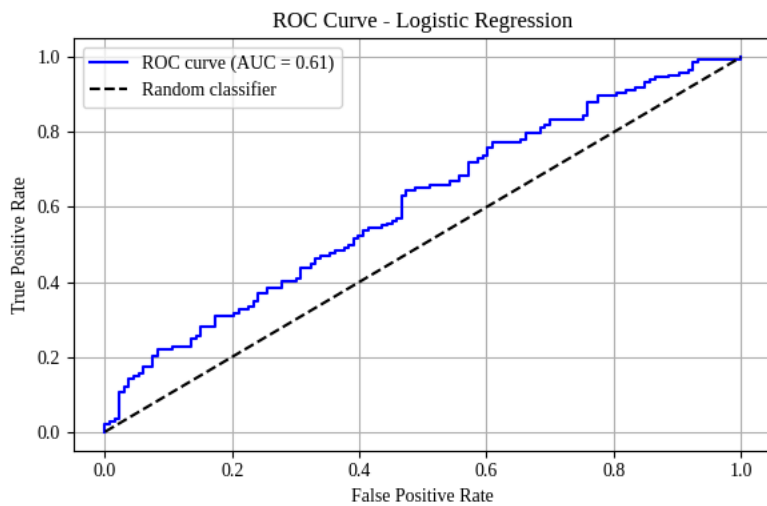
Possibly complete quasi-separation: A fraction 0.19 of observations can be perfectly predicted. This might indicate that there is complete quasi-separation. In this case some parameters will not be identified.

=== EQUAÇÃO DE REGRESSÃO LOGÍSTICA BINÁRIA ===

$$P(\text{Wear} = M) = 1 / (1 + \exp(-(-0.281 + 0.014 \cdot v_c \text{ [m/min]} + 9.764 \cdot f \text{ [mm/rev]} + -4.403 \cdot F_c \text{ [N]} + -4.790 \cdot \sigma F_c \text{ [N]} + 3.567 \cdot F_f \text{ [N]} + 0.920 \cdot \sigma F_f \text{ [N]} + 0.001 \cdot r_n \text{ [\mu m]} + 0.001 \cdot \sigma r_n \text{ [\mu m]} - 0.001 \cdot l_{cut} \text{ [mm]})))$$

```
1 import pandas as pd
2 import numpy as np
3 import matplotlib.pyplot as plt
4 import seaborn as sns
5 from sklearn.preprocessing import LabelEncoder, StandardScaler
6 from statsmodels.api as sm
7 from sklearn.metrics import roc_curve, auc
8
9 # Dados simulados para demonstração (substitua pelo seu DataFrame real `df`)
10 np.random.seed(42)
11 size = 282
12 df = pd.DataFrame({
13     'Wear': np.random.choice(['L', 'M'], size=size, p=[0.5, 0.5]),
14     'vc [m/min]': np.random.normal(120, 10, size),
15     'f [mm/rev]': np.random.normal(0.3, 0.05, size),
16     'Fc [N]': np.random.normal(800, 100, size),
17     'σFc [N]': np.random.normal(10, 2, size),
18     'Ff [N]': np.random.normal(200, 30, size),
19     'σFf [N]': np.random.normal(5, 1, size),
20     'rn [μm]': np.random.normal(15, 5, size),
21     'σrn [μm]': np.random.normal(1.2, 0.3, size),
22     'lcut [mm]': np.random.normal(100, 20, size)
23 })
24
25 # 1. Filtrar apenas classes L e M
26 df_filtered = df[df['Wear'].isin(['L', 'M'])].copy()
27
28 # 2. Selecionar todas as variáveis numéricas
29 X = df_filtered[['vc [m/min]', 'f [mm/rev]', 'Fc [N]', 'σFc [N]', 'Ff [N]', 'σFf [N]', 'rn [μm]', 'σrn [μm]', 'lcut [mm]']]
30
31 # 3. Codificar variável alvo (L = 0, M = 1)
32 le = LabelEncoder()
33 y = le.fit_transform(df_filtered['Wear']) # L=0, M=1
34
35 # 4. Normalizar e adicionar intercepto
36 scaler = StandardScaler()
37 X_scaled = scaler.fit_transform(X)
38 X_scaled = sm.add_constant(X_scaled)
39
40 # 5. Ajustar o modelo logístico binário
41 model = sm.Logit(y, X_scaled)
42 result = model.fit()
43
44 # 6. Prever probabilidades para o conjunto de dados
45 pred_probs = result.predict(X_scaled)
46
47 # 7. Curva ROC
48 fpr, tpr, _ = roc_curve(y, pred_probs)
49 roc_auc = auc(fpr, tpr)
50
51 # Plot ROC
52 plt.figure(figsize=(6, 4))
53 plt.plot(fpr, tpr, color='blue', label=f'ROC curve (AUC = {roc_auc:.2f})')
54 plt.plot([0, 1], [0, 1], 'k--', label='Random classifier')
55 plt.xlabel('False Positive Rate')
56 plt.ylabel('True Positive Rate')
57 plt.title('ROC Curve - Logistic Regression')
58 plt.legend()
59 plt.grid(True)
60 plt.tight_layout()
61 plt.show()
62
63
64
```

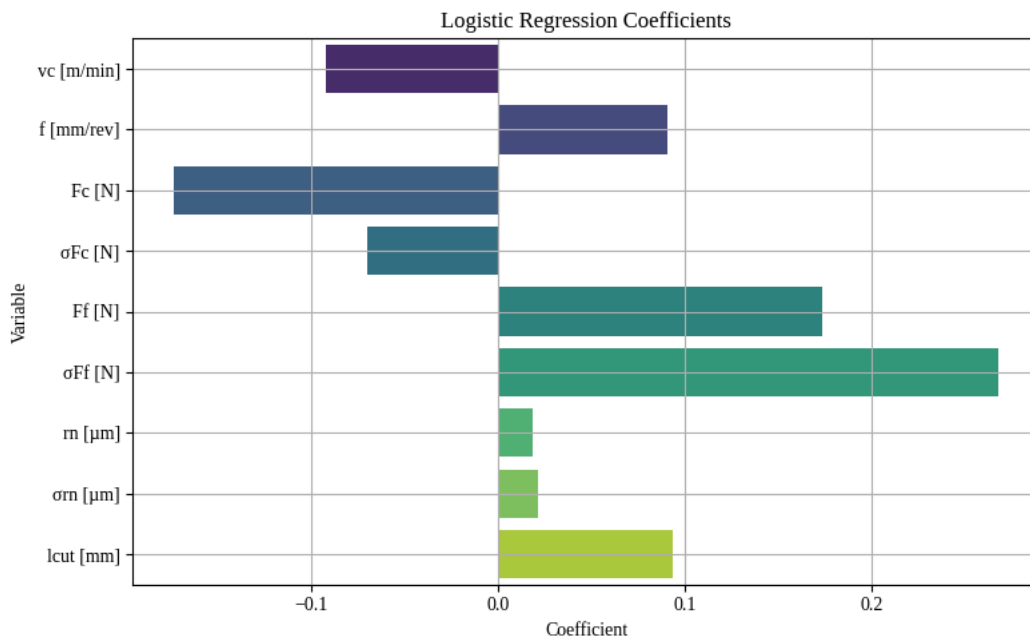

Optimization terminated successfully.
Current function value: 0.672895
Iterations 4



```
<ipython-input-38-e350b7b5a0bb>:68: FutureWarning:
```

Passing `palette` without assigning `hue` is deprecated and will be removed in v0.14.0. Assign the `y` variable to `hue` and set

```
sns.barplot(x='Coefficient', y='Variable', data=coef_df, palette='viridis')
```

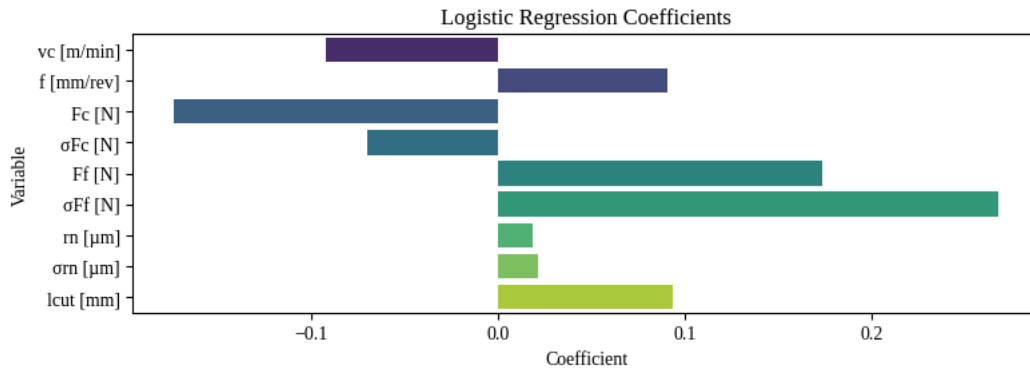


```
1 # 8. Coeficientes com barras
2 params = result.params[1:] # exclude intercept
3 variables = X.columns
4 coef_df = pd.DataFrame({'Variable': variables, 'Coefficient': params})
5 plt.figure(figsize=(8, 3))
6 sns.barplot(x='Coefficient', y='Variable', data=coef_df, palette='viridis')
7 plt.title('Logistic Regression Coefficients')
8 plt.grid(False)
9 plt.tight_layout()
10 plt.show()
```

<ipython-input-41-f95275e0c844>:6: FutureWarning:

Passing `palette` without assigning `hue` is deprecated and will be removed in v0.14.0. Assign the `y` variable to `hue` and set `le`

```
sns.barplot(x='Coefficient', y='Variable', data=coef_df, palette='viridis')
```



1 Start coding or generate with AI.

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```
1 import pandas as pd
2 import numpy as np
3 from sklearn.preprocessing import LabelEncoder, StandardScaler
4 import statsmodels.api as sm
5
6 # Exemplo: carregando os dados
7 # df = pd.read_csv('seus_dados.csv')
8
9 # Seleção das variáveis com baixo VIF
10 X = df[['vc [m/min]', 'sigmaFc [N]', 'sigmaFf [N]']]
11
12 # Codificação do alvo
13 le = LabelEncoder()
14 y = le.fit_transform(df['Wear']) # L=0, M=1, H=2
15 classes = le.classes_
16
17 # Normalização
18 scaler = StandardScaler()
19 X_scaled = scaler.fit_transform(X)
20 X_scaled = sm.add_constant(X_scaled)
21
22 # Loop para one-vs-rest
23 for target_class in np.unique(y):
24     y_binary = (y == target_class).astype(int) # 1 para a classe de interesse, 0 para as outras
25     model = sm.Logit(y_binary, X_scaled)
26     result = model.fit(dispatch=False)
27
28     print(f"\n=== Regressão logística para classe '{classes[target_class]}' vs resto ===")
29     print(result.summary())
30
```

<ipython-input-41-f95275e0c844>:6: FutureWarning:

=== Regressão logística para classe 'H' vs resto ===

Logit Regression Results

```
=====
Dep. Variable:          y      No. Observations:      287
Model:                Logit      Df Residuals:        283
Method:                MLE      Df Model:            3
Date:                Thu, 01 May 2025      Pseudo R-squ.:      -inf
Time:                17:00:10      Log-Likelihood:      -inf
converged:                False      LL-Null:          -25.206
Covariance Type:      nonrobust      LLR p-value:        1.000
=====
```

	coef	std err	z	P> z	[0.025	0.975]
const	78.2283	74.871	1.045	0.296	-68.516	224.972
x1	34.8174	40.226	0.866	0.387	-44.023	113.658
x2	71.5488	62.728	1.141	0.254	-51.396	194.494
x3	-182.0846	161.243	-1.129	0.259	-498.115	133.946

```
=====
```

=== Regressão logística para classe 'L' vs resto ===

Logit Regression Results

```
=====
```

```

Dep. Variable:          y    No. Observations:          287
Model:                  Logit    Df Residuals:          283
Method:                  MLE    Df Model:            3
Date:                   Thu, 01 May 2025    Pseudo R-squ.:      0.02752
Time:                   17:00:10    Log-Likelihood:      -189.70
converged:              True    LL-Null:            -195.07
Covariance Type:        nonrobust    LLR p-value:         0.01324

```

	coef	std err	z	P> z	[0.025	0.975]
const	0.3206	0.124	2.596	0.009	0.079	0.563
x1	-0.1616	0.128	-1.260	0.208	-0.413	0.090
x2	-0.2523	0.175	-1.439	0.150	-0.596	0.091
x3	-0.2779	0.295	-0.941	0.347	-0.857	0.301

=== Regressão logística para classe 'M' vs resto ===
Logit Regression Results

```

Dep. Variable:          y    No. Observations:          287
Model:                  Logit    Df Residuals:          283
Method:                  MLE    Df Model:            3
Date:                   Thu, 01 May 2025    Pseudo R-squ.:      0.02315
Time:                   17:00:10    Log-Likelihood:      -188.76
converged:              True    LL-Null:            -193.24
Covariance Type:        nonrobust    LLR p-value:         0.03003

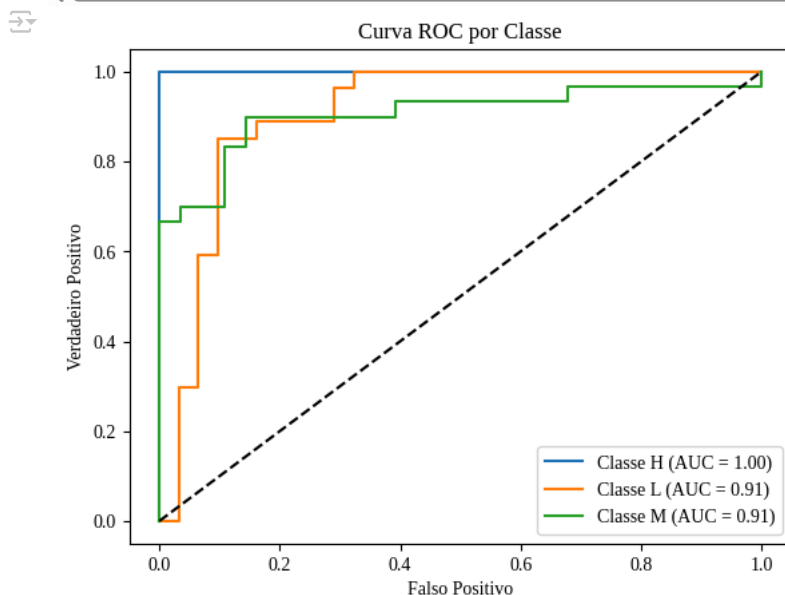
```

	coef	std err	z	P> z	[0.025	0.975]
const	-0.4550	0.128	-3.551	0.000	-0.706	-0.204
x1	0.0527	0.129	0.409	0.682	-0.200	0.305
x2	0.5089	0.202	2.520	0.012	0.113	0.905
x3	-0.8848	0.454	-1.948	0.051	-1.775	0.005

```

1 from sklearn.metrics import roc_curve, auc
2 from sklearn.preprocessing import label_binarize
3 import matplotlib.pyplot as plt
4
5 # Binariza as classes para one-vs-rest
6 y_bin = label_binarize(y_test, classes=[0,1,2])
7
8 # ROC por classe
9 for i, class_name in enumerate(classes):
10     fpr, tpr, _ = roc_curve(y_bin[:, i], model.predict_proba(X_test)[:, i])
11     roc_auc = auc(fpr, tpr)
12     plt.plot(fpr, tpr, label=f'Classe {class_name} (AUC = {roc_auc:.2f})')
13
14 plt.plot([0, 1], [0, 1], 'k--')
15 plt.xlabel('Falso Positivo')
16 plt.ylabel('Verdadeiro Positivo')
17 plt.title('Curva ROC por Classe')
18 plt.legend()
19 plt.show()
20

```



```

1 from sklearn.metrics import classification_report
2 print(classification_report(y_test, model.predict(X_test), target_names=classes))
3

```

	precision	recall	f1-score	support
H	1.00	1.00	1.00	1
L	0.69	1.00	0.82	27
M	1.00	0.60	0.75	30
accuracy			0.79	58
macro avg	0.90	0.87	0.86	58
weighted avg	0.86	0.79	0.79	58

```

1 from sklearn.metrics import accuracy_score
2 accuracy = accuracy_score(y_test, model.predict(X_test))
3 print(f"Acurácia: {accuracy:.3f}")
4

```

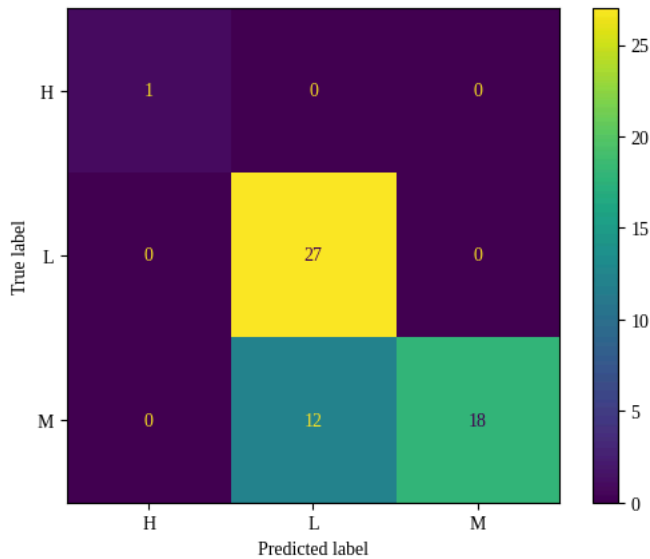
Acurácia: 0.793

```

1 from sklearn.metrics import confusion_matrix, ConfusionMatrixDisplay
2 ConfusionMatrixDisplay.from_predictions(y_test, model.predict(X_test), display_labels=classes)
3

```

<sklearn.metrics._plot.confusion_matrix.ConfusionMatrixDisplay at 0x7904f10bdc90>



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```

1 # Selecionar apenas as colunas desejadas
2 dados_filtrados = dados[['vc [m/min]', 'f [mm/rev]', 'Fc [N]', 'Wear']]
3
4 # Exibir os tipos das colunas selecionadas
5 print("\nTipos das colunas selecionadas:")
6 print(dados_filtrados.dtypes)
7
8 # Exibir as primeiras linhas do DataFrame filtrado
9 print("\nPrévia dos dados selecionados:")
10 print
11

```

Tipos das colunas selecionadas:

vc [m/min]	float64
f [mm/rev]	float64
Fc [N]	float64
Wear	object

dtype: object

```
Prévia dos dados selecionados:
<function print(*args, sep=' ', end='\n', file=None, flush=False)>
```

```
1 dados_filtrados['Wear'].value_counts()
```

```
count
Wear
L      167
M      115
H         5
```

dtype: int64

```
1 # Remover a classe 'H'
2 dados_filtrados = dados_filtrados[dados_filtrados['Wear'] != 'H']
3
4 # Verificar a nova distribuição
5 print("\nNova distribuição de 'Wear' após remover 'H':")
6 print(dados_filtrados['Wear'].value_counts())
7
```

```
Nova distribuição de 'Wear' após remover 'H':
Wear
L      167
M      115
Name: count, dtype: int64
```

```
1 dados_filtrados
```

```
vc [m/min]  f [mm/rev]  Fc [N]  Wear
0          10.5        0.01    55.7    L
1          12.6        0.01    55.2    L
2          10.5        0.01    57.4    L
3          12.6        0.10   214.0    L
4          10.5        0.10   209.1    L
...         ...         ...     ...     ...
282         150.0        0.02    63.6    L
283         150.0        0.02    61.6    L
284         150.0        0.02    63.4    L
285         150.0        0.03    85.4    L
286         150.0        0.03    87.1    L
```

282 rows × 4 columns

```
1 dados_filtrados.info()
2
```

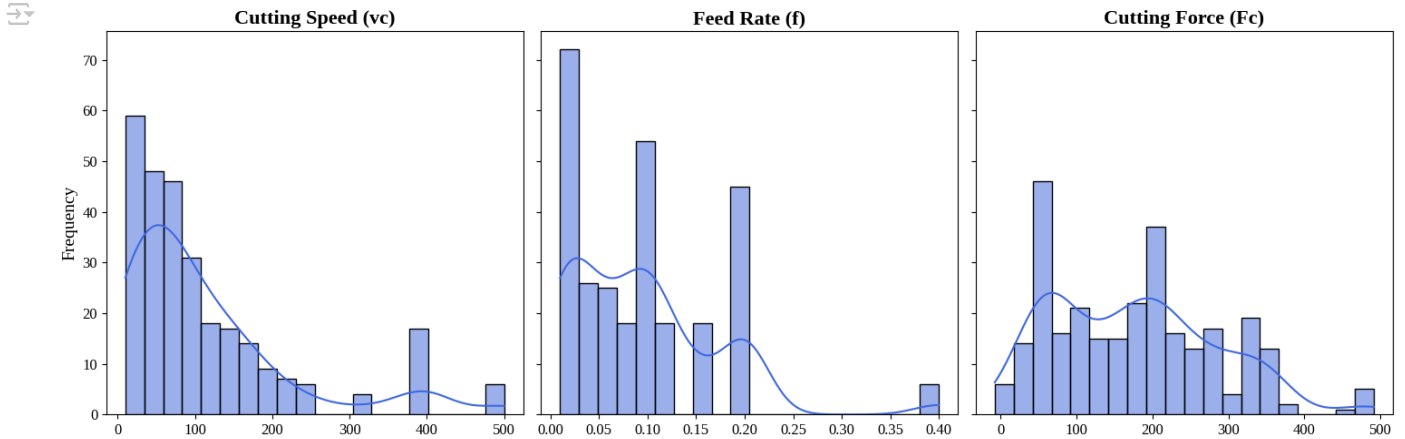
```
<class 'pandas.core.frame.DataFrame'>
Index: 282 entries, 0 to 286
Data columns (total 4 columns):
#   Column      Non-Null Count  Dtype
---  ---
0   vc [m/min]  282 non-null   float64
1   f [mm/rev]  282 non-null   float64
2   Fc [N]      282 non-null   float64
3   Wear       282 non-null   object
dtypes: float64(3), object(1)
memory usage: 11.0+ KB
```

```
1 import matplotlib.pyplot as plt
2 import seaborn as sns
3
4 # Criar a figura com 3 subgráficos na horizontal
5 fig, axes = plt.subplots(1, 3, figsize=(15, 5), sharey=True) # Compartilhar eixo Y para melhor comparação
6
7 # Definir as variáveis e os títulos
8 variaveis = ['vc [m/min]', 'f [mm/rev]', 'Fc [N]']
9 titulos = ['Cutting Speed (vc)', 'Feed Rate (f)', 'Cutting Force (Fc)']
```

```

10
11 # Gerar histogramas
12 for i, var in enumerate(variaveis):
13     sns.histplot(dados_filtrados[var], bins=20, kde=True, color="royalblue", ax=axes[i])
14     axes[i].set_title(titulos[i], fontsize=16, fontweight="bold")
15     axes[i].set_xlabel("") # Remover rótulo do eixo X
16     axes[i].set_ylabel("Frequency", fontsize=14) # Manter rótulo apenas no eixo Y
17     axes[i].tick_params(axis='both', labels=12)
18
19 # Ajustar layout
20 plt.tight_layout()
21 plt.show()
22
23

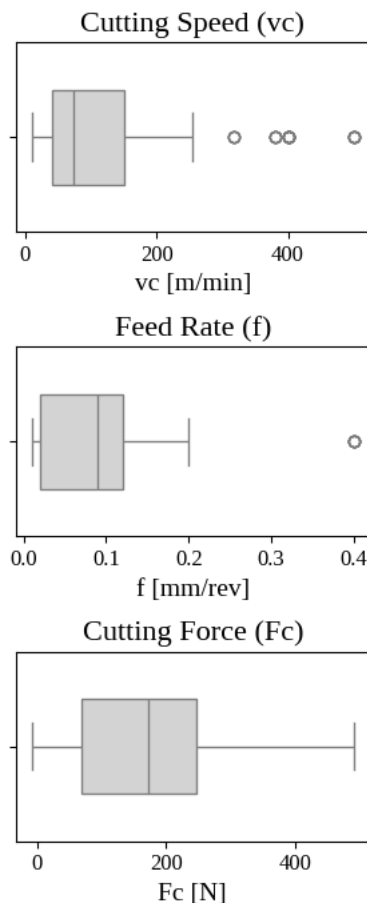
```



```

1 import matplotlib.pyplot as plt
2 import seaborn as sns
3
4 # Criar a figura com 3 subgráficos na vertical, sem compartilhar eixo X
5 fig, axes = plt.subplots(3, 1, figsize=(3, 7))
6
7 # Definir as variáveis e os títulos
8 variaveis = ['vc [m/min]', 'f [mm/rev]', 'Fc [N]']
9 titulos = ['Cutting Speed (vc)', 'Feed Rate (f)', 'Cutting Force (Fc)']
10
11 # Gerar boxplots com escalas individuais e cor cinza claro
12 for i, var in enumerate(variaveis):
13     sns.boxplot(x=dados_filtrados[var], ax=axes[i], color="lightgray", orient="h", width=0.5)
14     axes[i].set_title(titulos[i], fontsize=16)
15     axes[i].set_xlabel(var, fontsize=14)
16     axes[i].tick_params(axis='both', labels=12)
17
18 # Ajustar layout
19 plt.tight_layout()
20 plt.show()
21

```



```
1 import seaborn as sns
2 import matplotlib.pyplot as plt
3 import numpy as np
4
5 # Criar uma função para anotar a correlação nos gráficos superiores
6 def annotate_correlation(x, y, **kwargs):
7     corr = np.corrcoef(x, y)[0, 1] # Calcula a correlação de Pearson
8     ax = plt.gca()
9     ax.annotate(f"r = {corr:.2f}", xy=(0.5, 0.9), xycoords=ax.transAxes,
10               ha="center", fontsize=16, color="red", fontweight="bold")
11
12 # Ajustar o estilo e tamanho da figura
13 sns.set_context("notebook", rc={"axes.labelsize": 16, "xtick.labelsize": 16, "ytick.labelsize": 16,
14                               "legend.fontsize": 16, "figure.figsize": (8, 8)})
15
16 # Selecionar apenas as variáveis desejadas
17 dados_selecionados = dados_filtrados[['vc [m/min]', 'f [mm/rev]', 'Fc [N]', 'Wear']]
18
19 # Criar o pairplot com a variável Wear como hue (cor) e incluir linhas de densidade
20 g = sns.pairplot(dados_selecionados, hue="Wear", diag_kind="kde", markers=["o", "o"],
21                 plot_kws={"alpha": 0.7}, diag_kws={"shade": True, "linewidth": 2})
22
23 # Adicionar linhas de densidade (KDE Contours) nos gráficos de dispersão
24 for i, j in zip(*np.triu_indices_from(g.axes, k=1)): # Apenas na metade superior
25     sns.kdeplot(x=dados_selecionados.iloc[:, j], y=dados_selecionados.iloc[:, i], ax=g.axes[i, j],
26               levels=6, color="gray", linewidths=1.2, alpha=0.6)
27
28 # Ajustar o tamanho dos rótulos dos eixos, títulos e legendas manualmente
29 for ax in g.axes.flatten():
30     if ax is not None:
31         ax.xaxis.label.set_size(16) # Fonte do rótulo do eixo X
32         ax.yaxis.label.set_size(16) # Fonte do rótulo do eixo Y
33         ax.tick_params(axis='both', labelsize=16) # Fonte dos ticks dos eixos
34
35 # Ajustar a legenda
36 g._legend.set_bbox_to_anchor((1, 0.5)) # Posicionar melhor a legenda
37 g._legend.set_title("Wear", prop='size': 18, 'weight': 'bold') # Aumentar e negritar "Wear"
38
39 # Ajustar a fonte dos rótulos da legenda
40 for text in g._legend.texts:
41     text.set_fontsize(16)
42
43 # Adicionar as anotações de correlação nos gráficos superiores
44 for i, j in zip(*np.triu_indices_from(g.axes, k=1)):
```

```

45 g.axes[i, j].annotate(f"r = {np.corrcoef(dados_selecionados.iloc[:, j], dados_selecionados.iloc[:, i])[0, 1]:.2f}",
46                       xy=(0.5, 0.9), xycoords=g.axes[i, j].transAxes,
47                       ha="center", fontsize=16, color="purple", fontweight="bold")
48
49 plt.show()
50

```

↗ /usr/local/lib/python3.11/dist-packages/seaborn/axisgrid.py:1513: FutureWarning:

`shade` is now deprecated in favor of `fill`; setting `fill=True`.
This will become an error in seaborn v0.14.0; please update your code.

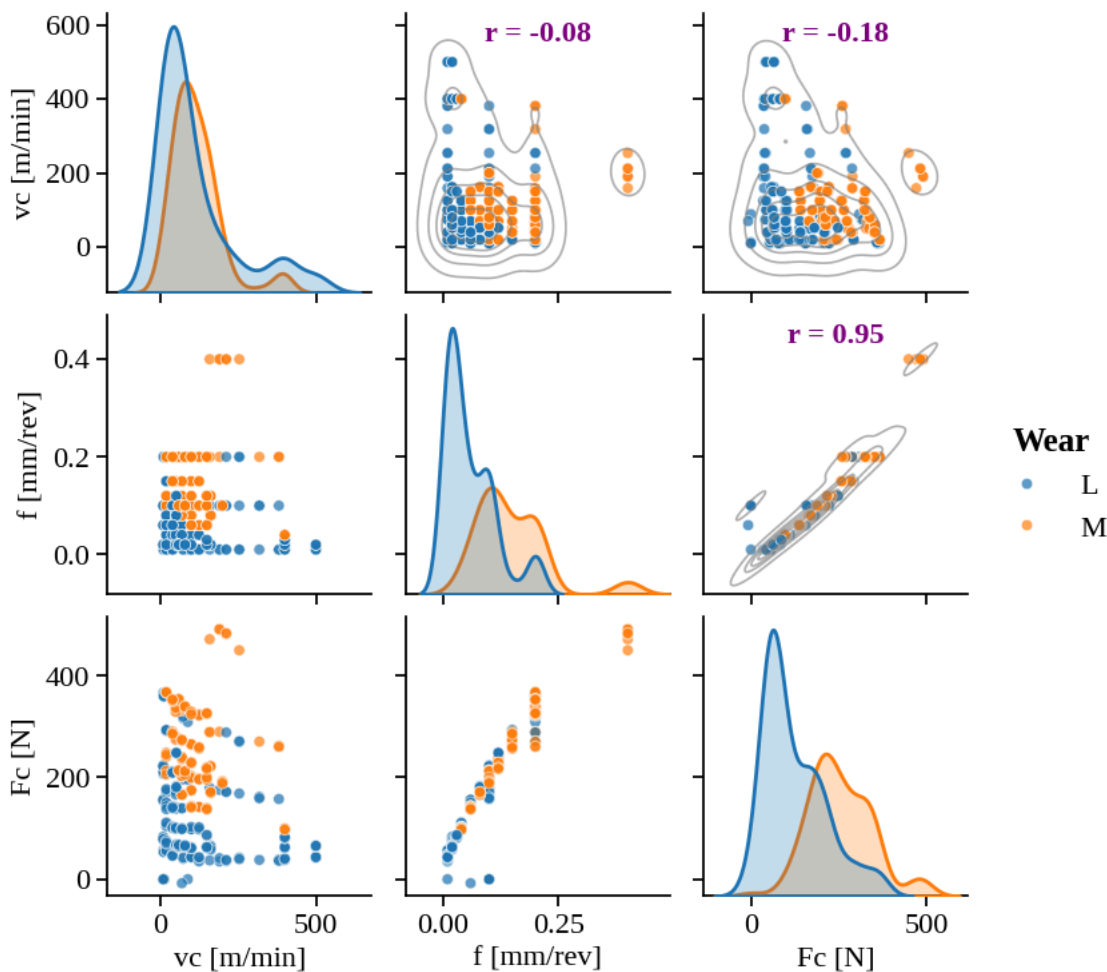
```
func(x=vector, **plot_kwargs)
/usr/local/lib/python3.11/dist-packages/seaborn/axisgrid.py:1513: FutureWarning:
```

`shade` is now deprecated in favor of `fill`; setting `fill=True`.
This will become an error in seaborn v0.14.0; please update your code.

```
func(x=vector, **plot_kwargs)
/usr/local/lib/python3.11/dist-packages/seaborn/axisgrid.py:1513: FutureWarning:
```

`shade` is now deprecated in favor of `fill`; setting `fill=True`.
This will become an error in seaborn v0.14.0; please update your code.

```
func(x=vector, **plot_kwargs)
```



```

1 from sklearn.cluster import KMeans
2 import numpy as np
3 import matplotlib.pyplot as plt
4 import seaborn as sns
5
6 # Selecionar apenas as variáveis de entrada
7 X_cluster = dados_filtrados[['vc [m/min]', 'f [mm/rev]', 'Fc [N]']]
8
9 # Aplicar K-Means com 2 clusters (pois temos 2 classes em Wear)
10 kmeans = KMeans(n_clusters=2, random_state=42, n_init=10)
11 dados_filtrados['Cluster_KMeans'] = kmeans.fit_predict(X_cluster)
12
13 # Visualizar os clusters comparados com Wear
14 plt.figure(figsize=(3, 2))
15 sns.scatterplot(x=dados_filtrados['vc [m/min]'], y=dados_filtrados['Fc [N]'],
16               hue=dados_filtrados['Cluster_KMeans'], palette="Set1", marker="o", edgecolor="k")
17 plt.title("K-Means Clusters Compared with Wear")

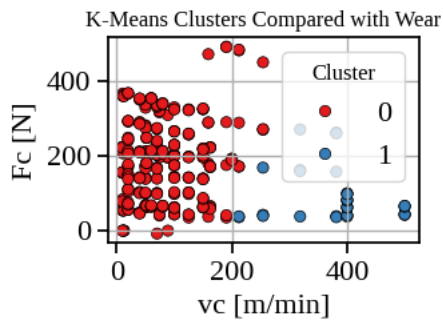
```



```

18 plt.xlabel("vc [m/min]")
19 plt.ylabel("Fc [N]")
20 plt.legend(title="Cluster")
21 plt.grid()
22 plt.show()
23

```



```

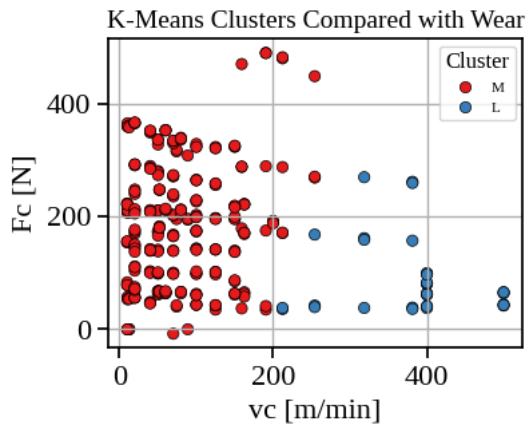
1 from sklearn.cluster import KMeans
2 import numpy as np
3 import matplotlib.pyplot as plt
4 import seaborn as sns
5
6 # Selecionar apenas as variáveis de entrada
7 X_cluster = dados_filtrados[['vc [m/min]', 'f [mm/rev]', 'Fc [N]']]
8
9 # Aplicar K-Means com 2 clusters
10 kmeans = KMeans(n_clusters=2, random_state=42, n_init=10)
11 dados_filtrados['Cluster_KMeans'] = kmeans.fit_predict(X_cluster)
12
13 # Verificar médias dos clusters para identificar padrões distintos
14 cluster_means = dados_filtrados.groupby('Cluster_KMeans')[['vc [m/min]', 'f [mm/rev]', 'Fc [N]']].mean()
15 print("Médias dos clusters:\n", cluster_means)
16
17 # Mapear clusters para as classes verdadeiras (L e M) com base nas médias
18 # O cluster com maior força de corte (Fc [N]) provavelmente representa a classe M (desgaste maior)
19 if cluster_means.loc[0, 'Fc [N]'] > cluster_means.loc[1, 'Fc [N]']:
20     cluster_mapping = {0: 'M', 1: 'L'}
21 else:
22     cluster_mapping = {0: 'L', 1: 'M'}
23
24 # Aplicar o mapeamento
25 dados_filtrados['Cluster_Label'] = dados_filtrados['Cluster_KMeans'].map(cluster_mapping)
26
27 # Verificar se os clusters foram mapeados corretamente
28 print("Cluster Mapping:", cluster_mapping)
29 print(dados_filtrados[['Cluster_KMeans', 'Wear', 'Cluster_Label']].head())
30
31 # Visualizar os clusters comparados com Wear
32 plt.figure(figsize=(4, 3))
33 sns.scatterplot(x=dados_filtrados['vc [m/min]'], y=dados_filtrados['Fc [N]'],
34                 hue=dados_filtrados['Cluster_Label'], palette="Set1", marker="o", edgecolor="k")
35 plt.title("K-Means Clusters Compared with Wear", fontsize=14)
36 plt.xlabel("vc [m/min]")
37 plt.ylabel("Fc [N]")
38 plt.legend(title="Cluster", fontsize=8)
39 plt.grid()
40 plt.show()
41

```

```

Médias dos clusters:
      vc [m/min]  f [mm/rev]  Fc [N]
Cluster_KMeans
0      80.1572    0.100800  187.67880
1     380.2625    0.045625  90.01875
Cluster Mapping: {0: 'M', 1: 'L'}
Cluster_KMeans Wear Cluster_Label
0      0      L      M
1      0      L      M
2      0      L      M
3      0      L      M
4      0      L      M

```



```

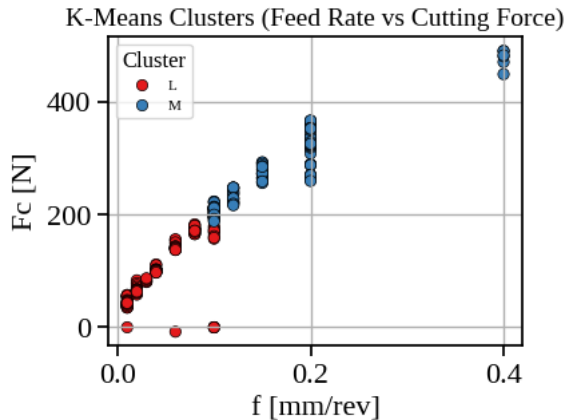
1 from sklearn.cluster import KMeans
2 import numpy as np
3 import matplotlib.pyplot as plt
4 import seaborn as sns
5
6 # Selecionar as variáveis para clustering (f e Fc)
7 X_cluster_f_fc = dados_filtrados[['f [mm/rev]', 'Fc [N]']]
8
9 # Aplicar K-Means com 2 clusters
10 kmeans_f_fc = KMeans(n_clusters=2, random_state=42, n_init=10)
11 dados_filtrados['Cluster_KMeans_f_fc'] = kmeans_f_fc.fit_predict(X_cluster_f_fc)
12
13 # Verificar médias dos clusters para identificar padrões distintos
14 cluster_means_f_fc = dados_filtrados.groupby('Cluster_KMeans_f_fc')[['f [mm/rev]', 'Fc [N]']].mean()
15 print("Médias dos clusters (f vs Fc):\n", cluster_means_f_fc)
16
17 # Mapear clusters para as classes verdadeiras (L e M) com base nas médias
18 if cluster_means_f_fc.loc[0, 'Fc [N]'] > cluster_means_f_fc.loc[1, 'Fc [N]']:
19     cluster_mapping_f_fc = {0: 'M', 1: 'L'}
20 else:
21     cluster_mapping_f_fc = {0: 'L', 1: 'M'}
22
23 # Aplicar o mapeamento
24 dados_filtrados['Cluster_Label_f_fc'] = dados_filtrados['Cluster_KMeans_f_fc'].map(cluster_mapping_f_fc)
25
26 # Visualizar os clusters comparados com Wear
27 plt.figure(figsize=(4, 3))
28 sns.scatterplot(x=dados_filtrados['f [mm/rev]'], y=dados_filtrados['Fc [N]'],
29                hue=dados_filtrados['Cluster_Label_f_fc'], palette="Set1", marker="o", edgecolor="k")
30 plt.title("K-Means Clusters (Feed Rate vs Cutting Force)", fontsize=14)
31 plt.xlabel("f [mm/rev]")
32 plt.ylabel("Fc [N]")
33 plt.legend(title="Cluster", fontsize=8)
34 plt.grid()
35 plt.show()
36

```

```

Médias dos clusters (f vs Fc):
          f [mm/rev]      Fc [N]
Cluster_KMeans_f_fc
0          0.040523    93.877124
1          0.158605   274.706202

```



L: Low (Baixo) – Indica um nível baixo de desgaste.

M: Medium (Médio) – Indica um nível médio de desgaste.

```

1 import pandas as pd
2 import numpy as np
3 from sklearn.model_selection import train_test_split
4 from sklearn.preprocessing import LabelEncoder, StandardScaler
5 from imblearn.over_sampling import SMOTE
6 from sklearn.ensemble import RandomForestClassifier
7 from sklearn.metrics import classification_report, confusion_matrix

```

```

1 # 1 Verificar os dados
2 print("\nTipos das colunas selecionadas:")
3 print(dados_filtrados.dtypes)
4
5 # 2 Codificar a variável alvo (Wear)
6 le = LabelEncoder()
7 dados_filtrados['Wear_encoded'] = le.fit_transform(dados_filtrados['Wear'])
8

```

```

Tipos das colunas selecionadas:
vc [m/min]          float64
f [mm/rev]          float64
Fc [N]              float64
Wear                object
Cluster_KMeans      int32
Cluster_Label       object
Cluster_KMeans_f_fc int32
Cluster_Label_f_fc  object
dtype: object

```

```

1 # Verificar a codificação
2 print("\nCodificação de 'Wear':")
3 print(dict(zip(le.classes_, le.transform(le.classes_))))

```

```

Codificação de 'Wear':
{'L': 0, 'M': 1}

```

```

1 # 2 Selecionar 20 amostras aleatórias para previsão
2 dados_para_prever = dados_filtrados.sample(n=20, random_state=42)
3 dados_filtrados = dados_filtrados.drop(dados_para_prever.index) # Remover essas amostras do treino/teste
4
5

```

```

1 # 4 Separar variáveis independentes (X) e dependente (y)
2 X = dados_filtrados[['vc [m/min]', 'f [mm/rev]', 'Fc [N]']]
3 y = dados_filtrados['Wear_encoded']
4

```

```

1 # 5 Dividir em treino e teste (80% treino, 20% teste, com estratificação)
2 X_train, X_test, y_train, y_test = train_test_split(

```

```

3 X, y, test_size=0.2, random_state=42, stratify=y
4 )

1 # 6 Balanceamento com SMOTE para lidar com a baixa quantidade de classe 'H'
2 smote = SMOTE(random_state=42, k_neighbors=2) # Reduzindo k_neighbors para evitar erro
3 X_train_res, y_train_res = smote.fit_resample(X_train, y_train)
4

1 # 7 Normalizar os dados (StandardScaler)
2 scaler = StandardScaler()
3 X_train_res_scaled = scaler.fit_transform(X_train_res)
4 X_test_scaled = scaler.transform(X_test)

```

✓ Criar modelos

```

1 from sklearn.model_selection import train_test_split, StratifiedKFold, cross_val_score, GridSearchCV
2 from sklearn.preprocessing import LabelEncoder, StandardScaler
3 from imblearn.over_sampling import SMOTE
4 from sklearn.ensemble import RandomForestClassifier
5 from sklearn.svm import SVC
6 from sklearn.linear_model import LogisticRegression
7 from lightgbm import LGBMClassifier
8 from sklearn.metrics import classification_report
9

```

 Show hidden output

```

1 # 8. Definir os hiperparâmetros para cada modelo
2 param_rf = {'n_estimators': [50, 100, 200], 'max_depth': [5, 10, 20], 'min_samples_split': [5, 10], 'min_samples_leaf': [2, 5]}
3 param_svm = {'C': [0.1, 1, 10], 'kernel': ['rbf', 'linear']}
4 param_lr = {'C': [0.1, 1, 10], 'max_iter': [200, 500]}
5 param_lgbm = {'num_leaves': [31, 50], 'learning_rate': [0.01, 0.1], 'n_estimators': [50, 100, 200]}
6
7 # 9. Criar os modelos com hiperparâmetros otimizados via GridSearch
8 modelos = {
9     "Random Forest": GridSearchCV(RandomForestClassifier(random_state=42), param_rf, cv=StratifiedKFold(n_splits=10), scoring='accuracy'),
10    "SVM": GridSearchCV(SVC(probability=True, class_weight='balanced', random_state=42), param_svm, cv=StratifiedKFold(n_splits=10),
11    "Logistic Regression": GridSearchCV(LogisticRegression(class_weight='balanced', random_state=42), param_lr, cv=StratifiedKFold(n_splits=10),
12    "LightGBM": GridSearchCV(LGBMClassifier(random_state=42), param_lgbm, cv=StratifiedKFold(n_splits=10), scoring='accuracy')
13 }
14
15 # 10. Treinar, avaliar e validar com cross-validation
16 resultados = {}
17
18 for nome, modelo in modelos.items():
19     print(f"\n ♦ Treinando {nome}...")
20
21     # Treinar o modelo com os melhores hiperparâmetros
22     modelo.fit(X_train_res_scaled, y_train_res)
23     melhor_modelo = modelo.best_estimator_
24
25     # Previsões no treino e teste
26     y_train_pred = melhor_modelo.predict(X_train_res_scaled)
27     y_test_pred = melhor_modelo.predict(X_test_scaled)
28
29     # Validação cruzada
30     scores = cross_val_score(melhor_modelo, X_train_res_scaled, y_train_res, cv=StratifiedKFold(n_splits=10), scoring='accuracy')
31     media_cv = scores.mean()
32
33     # Exibir métricas
34     print(f"\n ★ Melhor Modelo para {nome}: {modelo.best_params_}")
35     print(f"\n ★ Métricas para {nome} (TREINO):")
36     print(classification_report(y_train_res, y_train_pred, target_names=le.classes_))
37
38     print(f"\n ★ Métricas para {nome} (TESTE):")
39     print(classification_report(y_test, y_test_pred, target_names=le.classes_))
40
41     print(f"\n ★ Validação Cruzada (Média de Acurácia): {media_cv:.4f}")
42
43     # Armazenar resultados
44     resultados[nome] = {
45         "Melhor Modelo": modelo.best_params_,
46         "Validação Cruzada": media_cv,
47         "Treino": classification_report(y_train_res, y_train_pred, target_names=le.classes_, output_dict=True),
48         "Teste": classification_report(y_test, y_test_pred, target_names=le.classes_, output_dict=True)
49     }
50

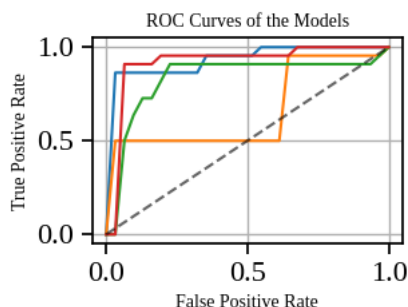
```

```

1 from scipy.interpolate import make_interp_spline
2
3
4
5
6
7 # 1 ROC-AUC CURVES FOR MODELS (Smoothed)
8 plt.figure(figsize=(3, 2))
9
10 for name, model in modelos.items():
11     best_model = model.best_estimator_
12     y_test_prob = best_model.predict_proba(X_test_scaled)[: , 1] # Probabilities for the positive class (M)
13     fpr, tpr, _ = roc_curve(y_test, y_test_prob) # FPR = False Positive Rate, TPR = True Positive Rate
14     roc_auc = auc(fpr, tpr)
15
16     # Remove duplicate values from fpr (X) and adjust tpr (Y)
17     fpr_unique, indices = np.unique(fpr, return_index=True)
18     tpr_unique = tpr[indices]
19
20
21 # Criando pontos intermediários para suavização
22     fpr_smooth = np.linspace(fpr_unique.min(), fpr_unique.max(), 32)
23     tpr_smooth = make_interp_spline(fpr_unique, tpr_unique, k=0)(fpr_smooth) # Interpolação cúbica
24
25     plt.plot(fpr_smooth, tpr_smooth, label=f"{name} (AUC = {roc_auc:.2f})")
26
27 plt.plot([0, 1], [0, 1], 'k--', alpha=0.6) # Diagonal line (random classification)
28 plt.xlabel('False Positive Rate', fontsize=10)
29 plt.ylabel('True Positive Rate', fontsize=10)
30 plt.title('ROC Curves of the Models', fontsize=10)
31 #plt.legend(loc="lower right", fontsize=8)
32 plt.grid()
33 plt.show()
34

```

/usr/local/lib/python3.11/dist-packages/sklearn/utils/deprecation.py:151: FutureWarning: 'force_all_finite' was renamed to 'ensure_finite' in 1.4. Please use 'ensure_finite' instead of 'force_all_finite'.
warnings.warn(

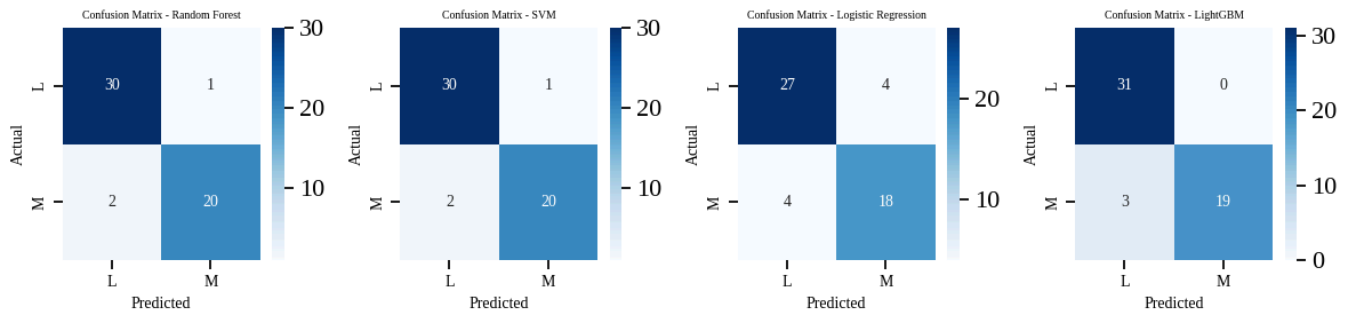


```

1 import matplotlib.pyplot as plt
2 import seaborn as sns
3 from sklearn.metrics import confusion_matrix
4
5 # 2 CONFUSION MATRIX FOR EACH MODEL (ENGLISH + SMALLER FONT)
6 fig, axes = plt.subplots(1, 4, figsize=(12, 3))
7
8 for ax, (name, model) in zip(axes, modelos.items()):
9     best_model = model.best_estimator_
10     y_test_pred = best_model.predict(X_test_scaled)
11
12     cm = confusion_matrix(y_test, y_test_pred)
13
14     sns.heatmap(cm, annot=True, fmt="d", cmap="Blues",
15                 xticklabels=le.classes_, yticklabels=le.classes_, ax=ax,
16                 annot_kws={"size": 10}) # Reduce annotation font size
17
18     ax.set_title(f"Confusion Matrix - {name}", fontsize=7) # Reduce title font size
19     ax.set_xlabel("Predicted", fontsize=10) # Reduce x-label font size
20     ax.set_ylabel("Actual", fontsize=10) # Reduce y-label font size
21     ax.tick_params(axis='both', which='major', labelsize=10) # Reduce tick labels
22
23 plt.tight_layout()
24 plt.show()
25

```

→ /usr/local/lib/python3.11/dist-packages/sklearn/utils/deprecation.py:151: FutureWarning: 'force_all_finite' was renamed to 'ensure_...
warnings.warn(



```
1 import matplotlib.pyplot as plt
2 import numpy as np
3 from sklearn.model_selection import learning_curve, StratifiedKFold
4
5 # 3 LEARNING CURVES (SHOWING 10 POINTS)
6 fig, axes = plt.subplots(2, 2, figsize=(8, 5)) # 2x2 layout for better spacing
7
8 axes = axes.ravel() # Flatten axes array for easier iteration
9
10 for ax, (name, model) in zip(axes, modelos.items()):
11     best_model = model.best_estimator_
12
13     # Define 10 points for the training set
14     train_sizes, train_scores, test_scores = learning_curve(
15         best_model, X_train_res_scaled, y_train_res,
16         train_sizes=np.linspace(0.1, 1.0, 10), # 10 points
17         cv=StratifiedKFold(n_splits=10),
18         scoring='accuracy'
19     )
20
21     train_mean = np.mean(train_scores, axis=1)
22     test_mean = np.mean(test_scores, axis=1)
23
24     ax.plot(train_sizes, train_mean, 'o-', label="Training")
25     ax.plot(train_sizes, test_mean, 'o-', label="Validation")
26
27     ax.set_title(f"Learning Curve - {name}", fontsize=14)
28     ax.set_xlabel("Training Size", fontsize=12)
29     ax.set_ylabel("Accuracy", fontsize=12)
30     ax.legend(fontsize=12)
31     ax.tick_params(axis='both', labelsize=12) # Reduce tick label size
32     ax.grid(False)
33
34 # Adjust layout to prevent overlapping
35 plt.tight_layout()
36 plt.show()
37
38
```