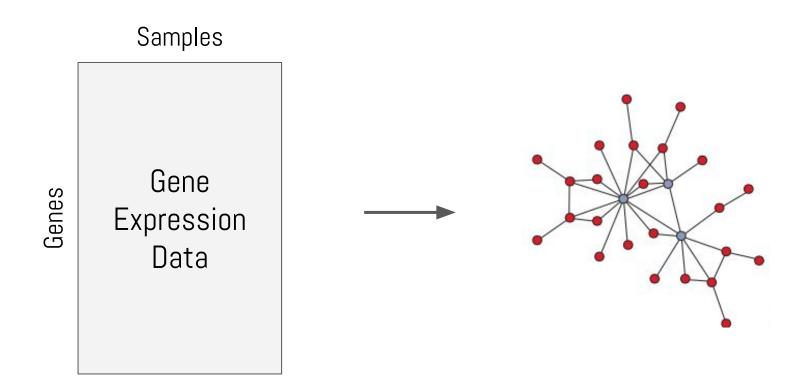
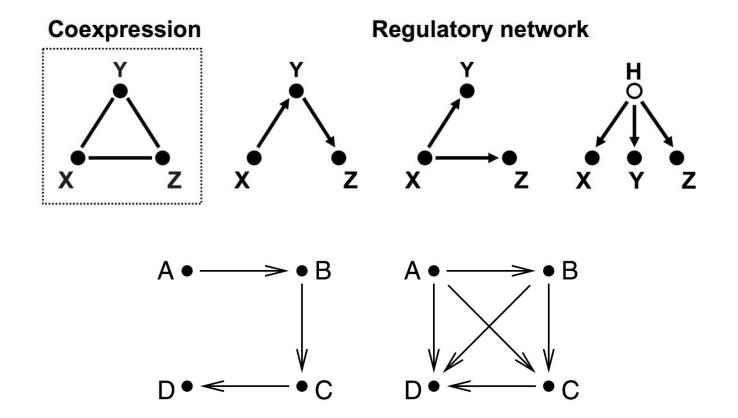
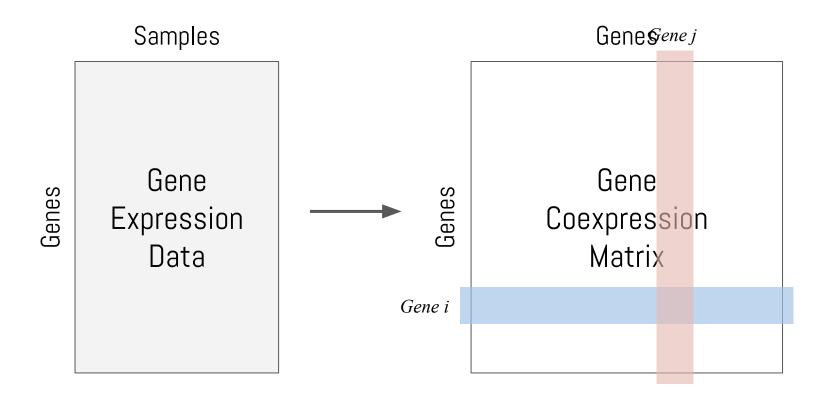
# Week 15: Large-scale biological networks

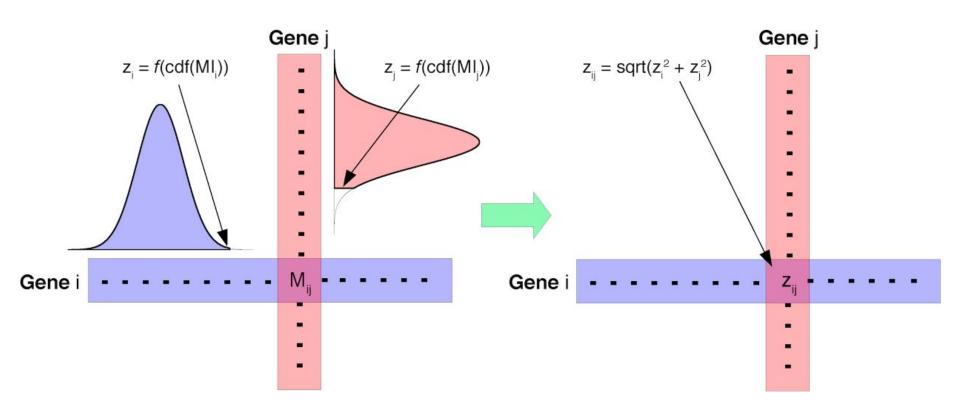
- Network topology
- Network motifs
- Condition-specific networks
- Network reconstruction
- Network propagation

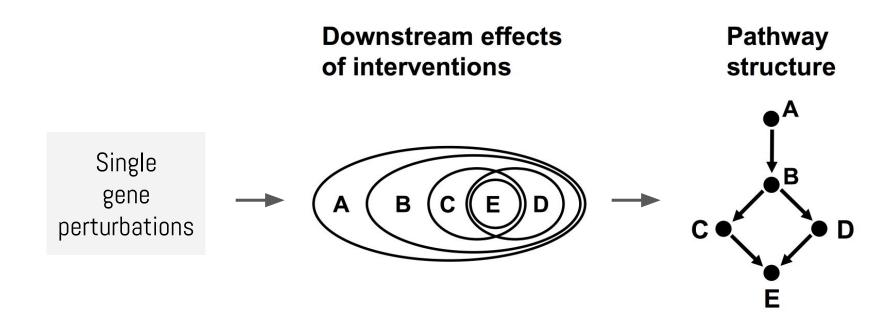




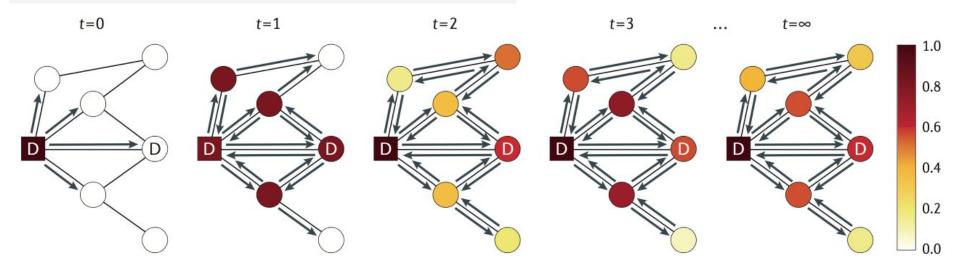


Context likelihood relatedness





Tracing the flow of information through a network over time.

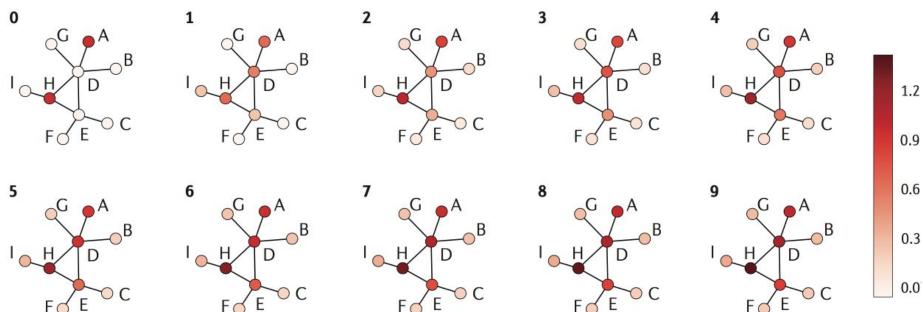


#### Random walk

A mathematical formalization of the paths resulting from successive random steps a 'walker' takes from **one node to another** with a probability that is **proportional to the weight of the edge** connecting the nodes.

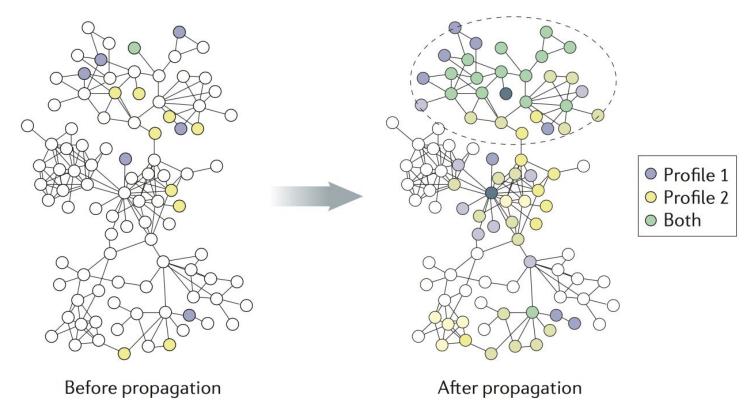
Tracing the flow of information through a network over time.

Initial node scores... (e.g. expression in a condition or association with a disease)



Convergence...

Tracing the flow of information through a network over time.



Random Walk

 $p_{n}(v)$ : Vector of initial node scores representing experimental measurements or our prior knowledge (e.g. expression in a condition or association with a disease)

 $p_0(v)$ 

 $p_{\nu}(v)$ : node scores at time-step k.

 $p_k(v) = \sum_{k=1}^{n} p_{k-1}(u) w(u, v)$ 

 $u \in N(v)$ 

w(u,v): (normalized) weight or the confidence of the interaction between u and v.

 $p_k = Wp_{k-1}$ 

 $p_{\nu} = W^{k} p_{0}$ 

**W**: normalized adjacency matrix (stochastic).

Cowen (2017) Nat. Rev. Genet.

Random Walk with Restart (RWR)

p<sub>0</sub>(v): Vector of initial node scores representing
experimental measurements or our prior knowledge (e.g. expression in a condition or association with a disease)

$$p_0(v)$$

$$\mathbf{p_k(v)}$$
: node scores at time-step k.

$$p_{k} = \alpha p_{0} + (1 - \alpha) W p_{k-1}$$

**W**: normalized adjacency matrix (stochastic).

 $\pmb{\alpha} :$  user-defined parameter that specifies the trade-off between prior information and network smoothing

Random Walk & RWR

**p**: steady-state distribution of node scores.

**S**: Can be interpreted as a similarity matrix.

S<sub>ij</sub>: the amount of information propagated to node i, given that the initial ranking  $\mathbf{p_0}$  is an elementary vector with 1 at entry j and 0 elsewhere.

$$p = Sp_0$$

