

CSE 3500

Homework 2

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Merge k Sorted Lists

```
1  import heapq
2
3  #takes argument of k_lists, which is a list which contains k amount of lists
4  def merge_k_lists(k_lists):
5      minheap = []
6      heapq.heapify(minheap)
7
8      #runs in O(nlogk) time, where n is the total amount of elements
9      for k in k_lists:
10         #adds every item in each sublist to a heap
11         for n in k:
12             #runs in O(logk) time
13             heapq.heappush(minheap,n)
14
15     newlist = []
16
17     #pops every item from the minheap: runs in O(n) time
18     while minheap:
19         newlist.append(heapq.heappop(minheap))
20
21     return newlist
```

Above is an algorithm written in python that merges k lists using a heap. The code runs in $O(n \log k)$ time, where n is the total number of items in k_lists, and where k is the number of lists. We can see that pushing to the heap takes $O(n \log k)$ operations, as it takes $O(\log k)$ operations to push to the heap, over n iterations. Popping from the heap and appending to a new list only takes $O(n)$ operations.

Run-time analysis

Device Specs/Language

Language:



Computer:

Inspiron 7590 2n1

CPU:

CPU

Intel(R) Core(TM) i7-8565U CPU @ 1.80GHz

Memory:

Memory

16.0 GB

Algorithm Comparison

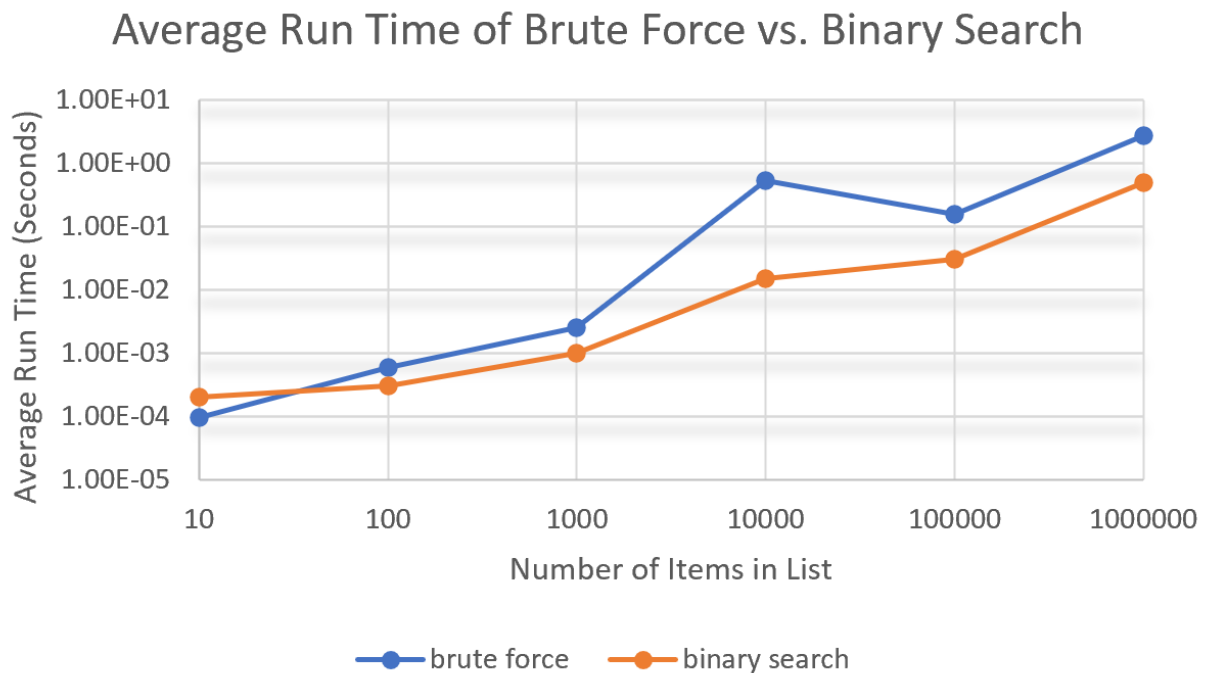
Table:

Average run time of both algorithms

Size of list	brute force	binary search
10	9.68E-05	0.00019968
100	0.0005943	0.00029833

1000	0.0024897	0.0009975
10000	0.5319317	0.01485856
100000	0.1558083	0.03059528
1000000	2.7116085	0.492155

Note: All the values in the brute force and binary search columns are in seconds.



Note: Both axes are logarithmic

Conclusion

From the results above, it is clear that for large data sets, the binary search method is faster, by over 5 times in some trial runs! This is because the brute force method runs in $O(n^2)$ time, while the binary search method runs in only $O(n \log n)$ time. Choice of algorithm matters because by choosing a faster algorithm, we can save tremendous amounts of computing power and time, as was shown in this assignment.

Code

Attached in the homework submission is the python file that contains my code.