#### Aprendizaje Reforzado

#### Maestría en Ciencia de Datos, DC - UBA

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#### Monte Carlo - Predicción libre de modelo

$$v_\pi(s) = \mathcal{R}^\pi_s + \sum_{s'} v_\pi(s') p^\pi_{s,s'}$$

# En general NO CONOCEMOS $p_{s,s'}^{\pi}$

¿Podemos hacer evaluación, aprendiendo tan sólo de la experiencia?

Ley de los grandes números

$$rac{\sum_{i=1}^n X_i}{n} o E[X], \qquad X_i, \ iid$$

Episodio  $s_0, a_0, s_1, a_1, s_2, a_2, s, \ldots, s, a_k, s_{k+1}, a_{k+1}, \ldots, s_T, a_T$ 

#### **Detalle computacional**

$$egin{aligned} \mu_k := rac{\sum_{j=1}^k x_j}{k} = \mu_{k-1} + rac{1}{k}(x_k - \mu_{k-1}) \ N(S_t) \leftarrow N(S_t) + 1 \ V(S_t) \leftarrow V(S_t) + rac{(G_t - V(S_t))}{N(S_t)} \end{aligned}$$

## Diferencia Temporal (TD)

$$v_{\pi}(s) = E[R_{t+1} + \gamma v_{\pi}(S_{t+1}) | S_t = s]$$

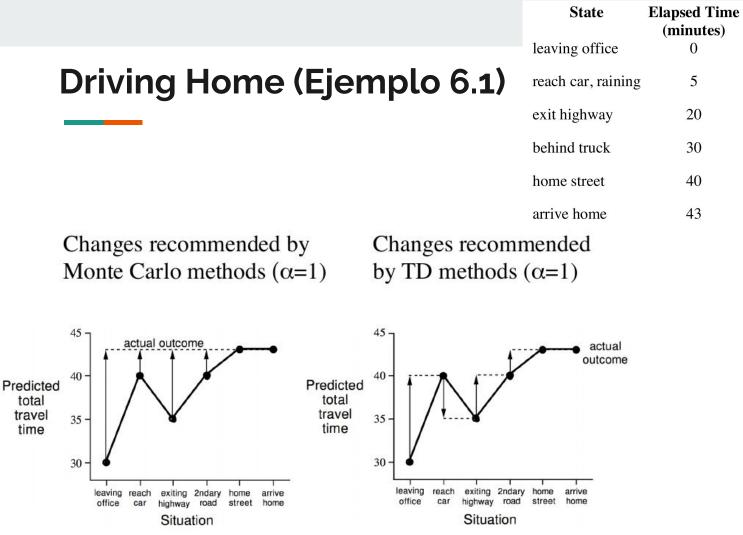
$$v_{\pi}^{n+1}(S_t) = v_{\pi}^n(S_t) + lpha[ extbf{R}_{t+1} + \gamma v_{\pi}^n(S_{t+1}) - v_{\pi}^n(S_t)]$$

Retorno estimado:  $R_{t+1} + \gamma v_{\pi}^{n+1}(S_{t+1})$ Error de TD:  $[R_{t+1} + \gamma v_{\pi}^{n}(S_{t+1}) - v_{\pi}^{n}(S_{t})]$ 

#### Comparativa

$$v_{\pi}(s) = E_{\pi}[G_t|S_t = s] = E_{\pi}[R_{t+1} + \gamma v_{\pi}(S_{t+1})|S_t = S]$$

- Programación Dinámica: Actualiza directamente con las esperanzas.
- Monte Carlo: Actualiza usando como target una aproximación de la esperanza que se actualiza sólo al final del episodio.
- Diferencia Temporal: Utiliza otra aproximación de la esperanza, pero se actualiza en cada paso.
- Bootstrapping: El update actualiza una estimación previa



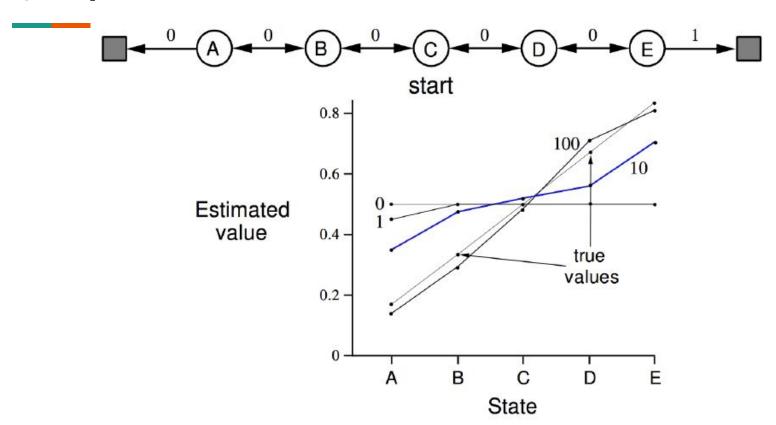
**Predicted** 

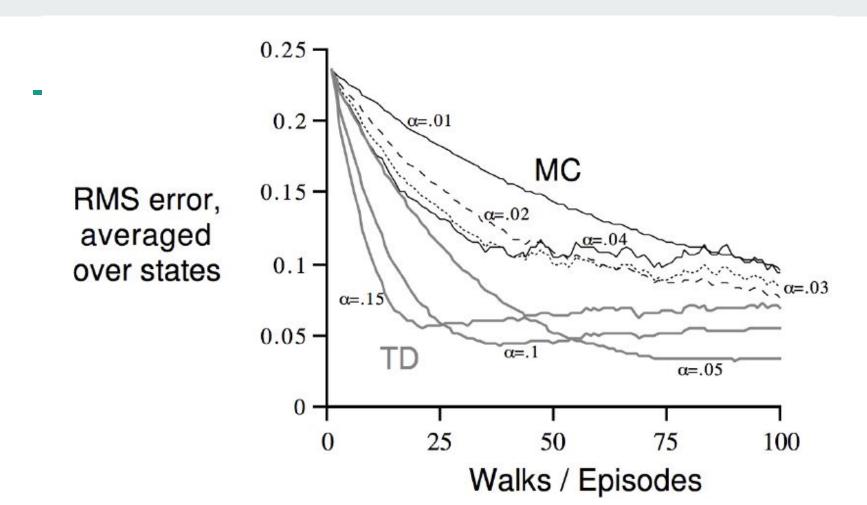
Time to Go

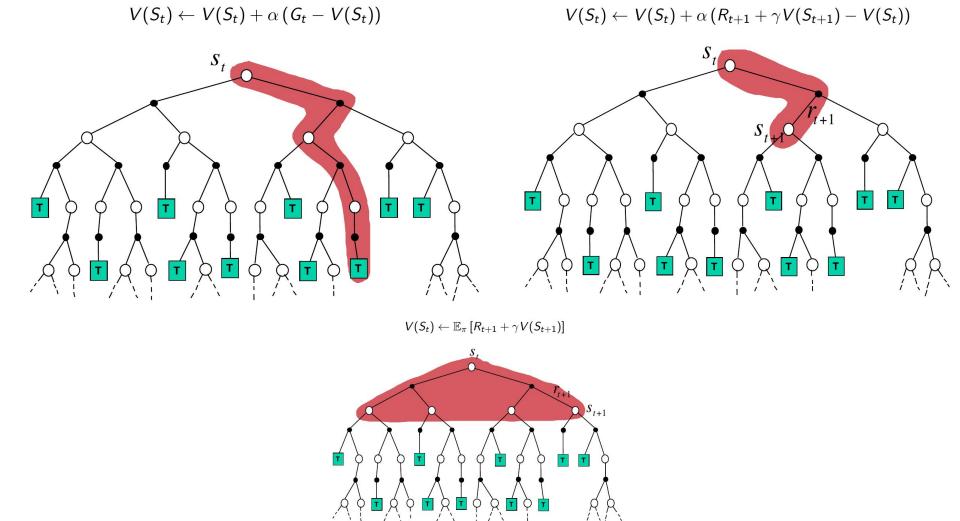
**Predicted** 

**Total Time** 

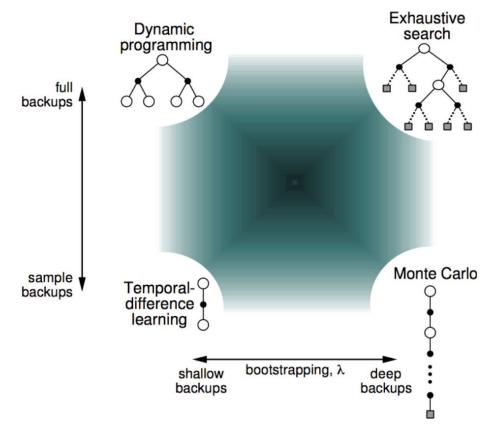
#### Ejemplo 6.2: Caminata aleatoria



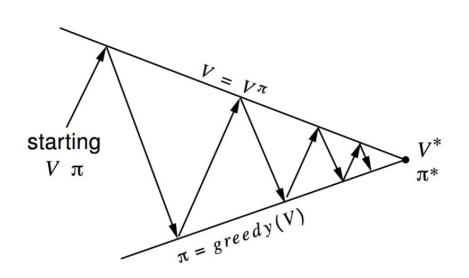




## Comparativa de los métodos vistos

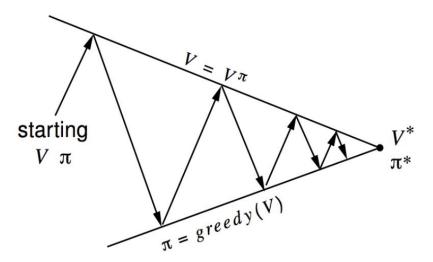


## Control (Improvement) - Monte Carlo



$$egin{aligned} q_{\pi_k}(s,a) &= \mathcal{R}^a_s + \gamma \sum_{s'} v_{\pi_k(s')} p^a_{s,s'} \ \pi_{k+1}(s) &= arg \max_a q_{\pi_k}(s,a) \end{aligned}$$

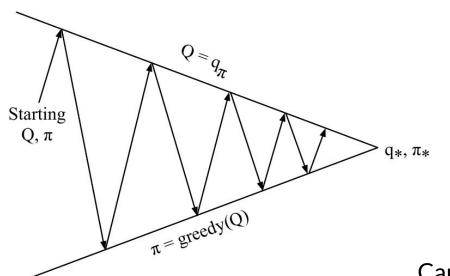
#### Control (Improvement) - Monte Carlo



- No tengo como dato la matriz de transición. (Model Free)
- No tengo la esperanza exacta, donde están todos los posibles escenarios. (Exploration vs. Explotation)

$$egin{aligned} q_{\pi_k}(s,a) &= \mathcal{R}^a_s + \gamma \sum_{s'} v_{\pi_k(s')} p^a_{s,s'} \ \pi_{k+1}(s) &= arg \max_a q_{\pi_k}(s,a) \end{aligned}$$

#### Los parches - Dependiente del modelo (p)



Hacer evaluación MC de

$$q_{\pi_k}(s,a)=:Q_k(s,a)$$

Cambio la esperanza que aproximo.

## Probar un poco todo (epsilon - greedy policy)

$$\pi^arepsilon(a|s) = egin{cases} (1-arepsilon) + arepsilon rac{1}{|\mathcal{A}|} & ext{si } a = arg\max_a q_\pi(s,a) \ arepsilon rac{1}{|\mathcal{A}|} & ext{caso contrario} \end{cases}$$

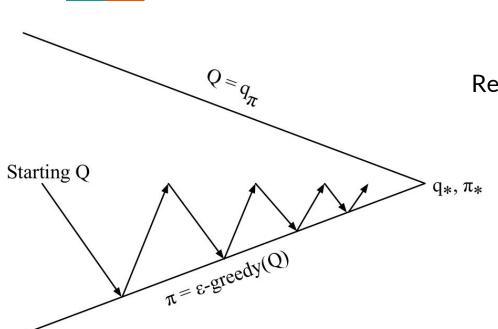
Teorema:

Si  $\pi^arepsilon$  una política arepsilon-greedy,  $\pi'(s) := arg \max_a q_{\pi^arepsilon}(s,a).$ 

Entonces:

onces: 
$$v_{\pi^{arepsilon}}(s) \leq v_{\pi^{'arepsilon}}(s)$$

## Algunas mejoras



Realizar la actualización en cada episodio.

#### **GLIE Monte Carlo**

- Simular el episodio k utilizando la política  $\pi_k^{\varepsilon}$ :  $\{S_1, A_1, R_2, \dots, S_T\}$ .
- Para cada par  $(S_t, A_t)$  del episodio

$$N(S_t, A_t) \leftarrow N(S_t, A_t) + 1$$

$$Q(S_t, A_t) \leftarrow Q(S_t, A_t) + \frac{1}{N(S_t, A_t)} (G_t - Q(S_t, A_t))$$

$$arepsilon = rac{1}{k}, \qquad \pi_{k+1}^arepsilon = arepsilon - \mathsf{greedy}(Q(s,a))$$

#### Monte Carlo (programación)

- Ejemplo de Blackjack
- Predicción Monte Carlo
- Predicción TD
- Control Monte Carlo on-policy con políticas epsilon greedy

#### **Ejercicio - Leer:**

That any  $\varepsilon$ -greedy policy with respect to  $q_{\pi}$  is an improvement over any  $\varepsilon$ -soft policy  $\pi$  is assured by the policy improvement theorem. Let  $\pi'$  be the  $\varepsilon$ -greedy policy. The conditions of the policy improvement theorem apply because for any  $s \in S$ :

$$q_{\pi}(s, \pi'(s)) = \sum_{a} \pi'(a|s) q_{\pi}(s, a)$$

$$= \frac{\varepsilon}{|\mathcal{A}(s)|} \sum_{a} q_{\pi}(s, a) + (1 - \varepsilon) \max_{a} q_{\pi}(s, a)$$

$$\geq \frac{\varepsilon}{|\mathcal{A}(s)|} \sum_{a} q_{\pi}(s, a) + (1 - \varepsilon) \sum_{a} \frac{\pi(a|s) - \frac{\varepsilon}{|\mathcal{A}(s)|}}{1 - \varepsilon} q_{\pi}(s, a)$$
(5.2)

(the sum is a weighted average with nonnegative weights summing to 1, and as such it must be less than or equal to the largest number averaged)

$$= \frac{\varepsilon}{|\mathcal{A}(s)|} \sum_{a} q_{\pi}(s, a) - \frac{\varepsilon}{|\mathcal{A}(s)|} \sum_{a} q_{\pi}(s, a) + \sum_{a} \pi(a|s) q_{\pi}(s, a)$$
$$= v_{\pi}(s).$$

Thus, by the policy improvement theorem,  $\pi' \geq \pi$  (i.e.,  $v_{\pi'}(s) \geq v_{\pi}(s)$ , for all  $s \in S$ ).

#### Lectura recomendada

 Problemas de reproducibilidad en Deep RL: Deep Reinforcement Learning that Matters, https://arxiv.org/abs/1709.06560