optim.py

```
import numpy as np
This file implements various first-order update rules that are commonly used for
training neural networks. Each update rule accepts current weights and the
gradient of the loss with respect to those weights and produces the next set of
weights. Each update rule has the same interface:
def update(w, dw, config=None):
Inputs:
  - w: A numpy array giving the current weights.
  - dw: A numpy array of the same shape as w giving the gradient of the
   loss with respect to w.
  - config: A dictionary containing hyperparameter values such as learning rate,
    momentum, etc. If the update rule requires caching values over many
    iterations, then config will also hold these cached values.
Returns:
  - next_w: The next point after the update.
  - config: The config dictionary to be passed to the next iteration of the
   update rule.
NOTE: For most update rules, the default learning rate will probably not perform
well; however the default values of the other hyperparameters should work well
for a variety of different problems.
For efficiency, update rules may perform in-place updates, mutating w and
setting next_w equal to w.
def sgd(w, dw, config=None):
   Performs vanilla stochastic gradient descent.
    config format:
    - learning_rate: Scalar learning rate.
    11 11 11
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   w -= config['learning_rate'] * dw
   return w, config
def sgd_momentum(w, dw, config=None):
   Performs stochastic gradient descent with momentum.
    config format:
    - learning_rate: Scalar learning rate.
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- momentum: Scalar between 0 and 1 giving the momentum value.
    Setting momentum = 0 reduces to sgd.
   - velocity: A numpy array of the same shape as w and dw used to store a moving
    average of the gradients.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
   v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.
   # YOUR CODE HERE:
   # Implement the momentum update formula. Return the updated weights
   # as next_w, and the updated velocity as v.
   v = config['momentum'] * v - config['learning_rate'] * dw
   next_w = w + v
   # ------ #
   # END YOUR CODE HERE
   # ----- #
   config['velocity'] = v
   return next_w, config
def sgd_nesterov_momentum(w, dw, config=None):
   Performs stochastic gradient descent with Nesterov momentum.
   config format:
   - learning_rate: Scalar learning rate.
   - momentum: Scalar between 0 and 1 giving the momentum value.
    Setting momentum = 0 reduces to sqd.
   - velocity: A numpy array of the same shape as w and dw used to store a moving
    average of the gradients.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
   v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.
   # YOUR CODE HERE:
   # Implement the momentum update formula. Return the updated weights
     as next_w, and the updated velocity as v.
   v_new = config['momentum'] * v - config['learning_rate'] * dw
   next_w = w + v_new + config['momentum'] * (v_new - v)
   v = v_new
```

```
# END YOUR CODE HERE
   config['velocity'] = v
   return next_w, config
def rmsprop(w, dw, config=None):
   11 11 11
   Uses the RMSProp update rule, which uses a moving average of squared gradient
   values to set adaptive per-parameter learning rates.
   config format:
   - learning_rate: Scalar learning rate.
   - decay_rate: Scalar between 0 and 1 giving the decay rate for the squared
    gradient cache.
   - epsilon: Small scalar used for smoothing to avoid dividing by zero.
   - beta: Moving average of second moments of gradients.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   config.setdefault('decay_rate', 0.99)
   config.setdefault('epsilon', 1e-8)
   config.setdefault('a', np.zeros_like(w))
   next_w = None
   # YOUR CODE HERE:
   # Implement RMSProp. Store the next value of w as next_w. You need
   # to also store in config['a'] the moving average of the second
   # moment gradients, so they can be used for future gradients. Concretely,
   # config['a'] corresponds to "a" in the lecture notes.
   a = config['decay_rate'] * config['a'] + (1-config['decay_rate']) * (dw**2)
   next_w = w - config['learning_rate'] / (np.sqrt(a) + config['epsilon']) * dw
   config['a'] = a
   # END YOUR CODE HERE
   return next_w, config
def adam(w, dw, config=None):
   Uses the Adam update rule, which incorporates moving averages of both the
   gradient and its square and a bias correction term.
   config format:
   - learning_rate: Scalar learning rate.
   - beta1: Decay rate for moving average of first moment of gradient.
```

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- beta2: Decay rate for moving average of second moment of gradient.
- epsilon: Small scalar used for smoothing to avoid dividing by zero.
- m: Moving average of gradient.
- v: Moving average of squared gradient.
- t: Iteration number.
if config is None: config = {}
config.setdefault('learning_rate', 1e-3)
config.setdefault('beta1', 0.9)
config.setdefault('beta2', 0.999)
config.setdefault('epsilon', 1e-8)
config.setdefault('v', np.zeros_like(w))
config.setdefault('a', np.zeros_like(w))
config.setdefault('t', 0)
next_w = None
# ------ #
# YOUR CODE HERE:
# Implement Adam. Store the next value of w as next_w. You need
# to also store in config['a'] the moving average of the second
# moment gradients, and in config['v'] the moving average of the
# first moments. Finally, store in config['t'] the increasing time.
# ----- #
config['t'] += 1
# First moment update
v = config['beta1'] * config['v'] + (1 - config['beta1']) * dw
# Second moment update
a = config['beta2'] * config['a'] + (1 - config['beta2']) * (dw**2)
# Bias correction
v_corrected = 1 / (1 - config['beta1']**config['t']) * v
a_corrected = 1 / (1 - config['beta2']**config['t']) * a
# Gradient step
next_w = w - config['learning_rate'] / (np.sqrt(a_corrected) + config['epsilon']) *
\hookrightarrow v_corrected
config['v'] = v
config['a'] = a
# END YOUR CODE HERE
# ----- #
return next_w, config
```

layers.py

```
import numpy as np
import pdb
def affine_forward(x, w, b):
   Computes the forward pass for an affine (fully-connected) layer.
   The input x has shape (N, d_1, ..., d_k) and contains a minibatch of N
   examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
   reshape each input into a vector of dimension D = d_1 * ... * d_k, and
   then transform it to an output vector of dimension M.
   Inputs:
   - x: A numpy array containing input data, of shape (N, d_1, \ldots, d_k)
   - w: A numpy array of weights, of shape (D, M)
   - b: A numpy array of biases, of shape (M,)
   Returns a tuple of:
   - out: output, of shape (N, M)
   - cache: (x, w, b)
   out = None
   # ----- #
   # YOUR CODE HERE:
     Calculate the output of the forward pass. Notice the dimensions
      of w are D x M, which is the transpose of what we did in earlier
     assignments.
   N, D = x.shape[0], w.shape[0]
   x_reshaped = np.reshape(x, (N, D))
   out = x_reshaped @ w + b
   # END YOUR CODE HERE
   cache = (x, w, b)
   return out, cache
def affine_backward(dout, cache):
   Computes the backward pass for an affine layer.
   Inputs:
   - dout: Upstream derivative, of shape (N, M)
   - cache: Tuple of:
     - x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
     - w: A numpy array of weights, of shape (D, M)
     - b: A numpy array of biases, of shape (M,)
```

```
Returns a tuple of:
  - dx: Gradient with respect to x, of shape (N, d1, \ldots, d_k)
  - dw: Gradient with respect to w, of shape (D, M)
   - db: Gradient with respect to b, of shape (M,)
  x, w, b = cache
  dx, dw, db = None, None, None
  # ----- #
  # YOUR CODE HERE:
    Calculate the gradients for the backward pass.
  # Notice:
  # dout is N x M
  # dx should be N \times d1 \times \ldots \times dk; it relates to dout through multiplication with w,
   \hookrightarrow which is D x M
    dw should be D x M; it relates to dout through multiplication with x, which is N
   \rightarrow x D after reshaping
    db should be M; it is just the sum over dout examples
  N, D = x.shape[0], w.shape[0]
  dx = np.reshape(dout @ w.T, x.shape)
  dw = np.reshape(x, (N, D)).T @ dout
  db = np.sum(dout, axis=0)
  # END YOUR CODE HERE
  return dx, dw, db
def relu_forward(x):
  Computes the forward pass for a layer of rectified linear units (ReLUs).
  Input:
  - x: Inputs, of any shape
  Returns a tuple of:
   - out: Output, of the same shape as x
   - cache: x
  # YOUR CODE HERE:
  # Implement the ReLU forward pass.
  # ------ #
  out = np.maximum(0, x)
  # ----- #
  # END YOUR CODE HERE
```

```
cache = x
  return out, cache
def relu_backward(dout, cache):
  Computes the backward pass for a layer of rectified linear units (ReLUs).
  Input:
  - dout: Upstream derivatives, of any shape
  - cache: Input x, of same shape as dout
  Returns:
  - dx: Gradient with respect to x
  x = cache
  # ----- #
  # YOUR CODE HERE:
  # Implement the ReLU backward pass
  dx = (x > 0) * dout
  # END YOUR CODE HERE
  return dx
def batchnorm_forward(x, gamma, beta, bn_param):
  Forward pass for batch normalization.
```

During training the sample mean and (uncorrected) sample variance are computed from minibatch statistics and used to normalize the incoming data. During training we also keep an exponentially decaying running mean of the mean and variance of each feature, and these averages are used to normalize data at test-time.

At each timestep we update the running averages for mean and variance using an exponential decay based on the momentum parameter:

```
running_mean = momentum * running_mean + (1 - momentum) * sample_mean
running_var = momentum * running_var + (1 - momentum) * sample_var
```

Note that the batch normalization paper suggests a different test-time behavior: they compute sample mean and variance for each feature using a large number of training images rather than using a running average. For this implementation we have chosen to use running averages instead since they do not require an additional estimation step; the torch7 implementation of batch normalization also uses running averages.

```
Input:
- x: Data of shape (N, D)
- gamma: Scale parameter of shape (D,)
- beta: Shift paremeter of shape (D,)
- bn_param: Dictionary with the following keys:
 - mode: 'train' or 'test'; required
 - eps: Constant for numeric stability
 - momentum: Constant for running mean / variance.
  - running_mean: Array of shape (D,) giving running mean of features
 - running_var Array of shape (D,) giving running variance of features
Returns a tuple of:
- out: of shape (N, D)
- cache: A tuple of values needed in the backward pass
mode = bn_param['mode']
eps = bn_param.get('eps', 1e-5)
momentum = bn_param.get('momentum', 0.9)
N, D = x.shape
running_mean = bn_param.get('running_mean', np.zeros(D, dtype=x.dtype))
running_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype))
out, cache = None, None
if mode == 'train':
   # YOUR CODE HERE:
   # A few steps here:
        (1) Calculate the running mean and variance of the minibatch.
        (2) Normalize the activations with the running mean and variance.
        (3) Scale and shift the normalized activations. Store this
           as the variable 'out'
       (4) Store any variables you may need for the backward pass in
           the 'cache' variable.
   # ----- #
   batch_mean = np.mean(x, axis=0)
   running_mean = momentum*running_mean + (1-momentum) * batch_mean
   batch_var = np.var(x, axis=0)
   running_var = momentum*running_var + (1-momentum) * batch_var
   x_normalized = (x - batch_mean) / np.sqrt(batch_var + eps)
   out = gamma * x_normalized + beta
   cache = (batch_mean, batch_var, gamma, eps, x, x_normalized)
   # ------ #
   # END YOUR CODE HERE
   # ========= #
elif mode == 'test':
   # ------ #
   # YOUR CODE HERE:
   # Calculate the testing time normalized activation. Normalize using
   # the running mean and variance, and then scale and shift appropriately.
```

```
# Store the output as 'out'.
      x_normalized = (x - running_mean) / np.sqrt(running_var + eps)
      out = gamma * x_normalized + beta
      # ----- #
      # END YOUR CODE HERE
      else:
      raise ValueError('Invalid forward batchnorm mode "%s"' % mode)
   # Store the updated running means back into bn_param
   bn_param['running_mean'] = running_mean
   bn_param['running_var'] = running_var
   return out, cache
def batchnorm_backward(dout, cache):
   Backward pass for batch normalization.
   For this implementation, you should write out a computation graph for
   batch normalization on paper and propagate gradients backward through
   intermediate nodes.
   Inputs:
   - dout: Upstream derivatives, of shape (N, D)
   - cache: Variable of intermediates from batchnorm_forward.
   Returns a tuple of:
   - dx: Gradient with respect to inputs x, of shape (N, D)
   - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
   - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
   dx, dgamma, dbeta = None, None, None
   # YOUR CODE HERE:
      Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
   # ----- #
   mean, var, gamma, eps, x, x_normalized = cache
   m = x.shape[0]
   \# dLdx = 1/sqrt(var + eps) * dLdnorm + 2*(x - mean)/m * dLdvar + dLdmean / m
   \# dLdnorm = dLdout * gamma
   \# dLdvar = sum(-1/2 * 1/(var + eps)^(3/2) * (x - mean) * dLdnorm)
   \# dLdmean = -1/sqrt(var + eps) * sum(dLdnorm) - dLdvar * 2/m * sum(x - mean)
   dnorm = dout * gamma
   dvar = -0.5 * np.sum((x - mean) * dnorm, axis=0) / (np.sqrt(var + eps)**3)
   dmean = -(np.sum(dnorm, axis=0) / np.sqrt(var + eps)) - (2 * dvar / m * np.sum(x - eps))

→ mean, axis=0))
   dx = dnorm / np.sqrt(var + eps) + 2*(x - mean)/m * dvar + dmean / m
```

```
\# dLdqamma = sum(dLdout * x)
   dgamma = np.sum(dout * x_normalized, axis=0)
   \#dLdbeta = sum(dLdout)
   dbeta = np.sum(dout, axis=0)
   # END YOUR CODE HERE
   return dx, dgamma, dbeta
def dropout_forward(x, dropout_param):
   Performs the forward pass for (inverted) dropout.
   Inputs:
   - x: Input data, of any shape
   - dropout_param: A dictionary with the following keys:
     - p: Dropout parameter. We keep each neuron output with probability p.
    - mode: 'test' or 'train'. If the mode is train, then perform dropout;
      if the mode is test, then just return the input.
     - seed: Seed for the random number generator. Passing seed makes this
      function deterministic, which is needed for gradient checking but not in
      real networks.
   Outputs:
   - out: Array of the same shape as x.
   - cache: A tuple (dropout_param, mask). In training mode, mask is the dropout
    mask that was used to multiply the input; in test mode, mask is None.
   11 11 11
   p, mode = dropout_param['p'], dropout_param['mode']
   assert (0<p<=1), "Dropout probability is not in (0,1]"
   if 'seed' in dropout_param:
      np.random.seed(dropout_param['seed'])
   mask = None
   out = None
   if mode == 'train':
      # ----- #
      # YOUR CODE HERE:
      # Implement the inverted dropout forward pass during training time.
      # Store the masked and scaled activations in out, and store the
        dropout mask as the variable mask.
      # ============= #
      mask = np.random.choice([1, 0], size=x.shape, p=[p, 1-p])
      out = x * mask / p
      # ------ #
      # END YOUR CODE HERE
```

```
elif mode == 'test':
    # YOUR CODE HERE:
    # Implement the inverted dropout forward pass during test time.
    # ----- #
    out = x
    # ------ #
    # END YOUR CODE HERE
  cache = (dropout_param, mask)
  out = out.astype(x.dtype, copy=False)
  return out, cache
def dropout_backward(dout, cache):
  Perform the backward pass for (inverted) dropout.
  Inputs:
  - dout: Upstream derivatives, of any shape
  - cache: (dropout_param, mask) from dropout_forward.
  dropout_param, mask = cache
  mode = dropout_param['mode']
  dx = None
  if mode == 'train':
    # ------ #
    # YOUR CODE HERE:
      Implement the inverted dropout backward pass during training time.
    dx = mask * dout / dropout_param['p']
    # END YOUR CODE HERE
    # ----- #
  elif mode == 'test':
    # YOUR CODE HERE:
    # Implement the inverted dropout backward pass during test time.
    dx = dout
    # END YOUR CODE HERE
    # ----- #
  return dx
```

```
def svm_loss(x, y):
    Computes the loss and gradient using for multiclass SVM classification.
    Inputs:
    - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
      for the ith input.
    - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
      0 <= y[i] < C
   Returns a tuple of:
    - loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
   N = x.shape[0]
   correct_class_scores = x[np.arange(N), y]
   margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0)
   margins[np.arange(N), y] = 0
   loss = np.sum(margins) / N
   num_pos = np.sum(margins > 0, axis=1)
   dx = np.zeros_like(x)
   dx[margins > 0] = 1
   dx[np.arange(N), y] -= num_pos
   dx /= N
   return loss, dx
def softmax_loss(x, y):
    Computes the loss and gradient for softmax classification.
    - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
     for the ith input.
    - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
     0 <= y[i] < C
   Returns a tuple of:
    - loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
    n n n
   probs = np.exp(x - np.max(x, axis=1, keepdims=True))
   probs /= np.sum(probs, axis=1, keepdims=True)
   N = x.shape[0]
   loss = -np.sum(np.log(np.maximum(probs[np.arange(N), y], 1e-8))) / N
   dx = probs.copy()
   dx[np.arange(N), y] = 1
   dx /= N
   return loss, dx
```

```
layer_utils.py
from .layers import *
def affine_relu_forward(x, w, b):
    Convenience layer that performs an affine transform followed by a ReLU
    Inputs:
    - x: Input to the affine layer
    - w, b: Weights for the affine layer
   Returns a tuple of:
    - out: Output from the ReLU
    - cache: Object to give to the backward pass
   a, fc_cache = affine_forward(x, w, b)
   out, relu_cache = relu_forward(a)
   cache = (fc_cache, relu_cache)
   return out, cache
def affine_relu_backward(dout, cache):
   Backward pass for the affine-relu convenience layer
   fc_cache, relu_cache = cache
   da = relu_backward(dout, relu_cache)
   dx, dw, db = affine_backward(da, fc_cache)
   return dx, dw, db
def affine_batchnorm_relu_forward(x, w, b, gamma, beta, bn_param):
    Convenience layer that performs an affine transform followed by a batchnorm and a
\hookrightarrow ReLU
    Inputs:
    - x: Input to the affine layer
    - w, b: Weights for the affine layer
    - gamma, beta: Scale and shift parameters for the batchnorm layer
    - bn_param: Dictionary of params for the batchnorm layer
   Returns a tuple of:
    - out: Output from the ReLU
    - cache: Object to give to the backward pass
   a, fc_cache = affine_forward(x, w, b)
   a_norm, bn_cache = batchnorm_forward(a, gamma, beta, bn_param)
```

out, relu_cache = relu_forward(a_norm)
cache = (fc_cache, bn_cache, relu_cache)

return out, cache

```
def affine_batchnorm_relu_backward(dout, cache):
    """

    Backward pass for the affine-relu convenience layer
    """

    fc_cache, bn_cache, relu_cache = cache
    da_norm = relu_backward(dout, relu_cache)
    da, dgamma, dbeta = batchnorm_backward(da_norm, bn_cache)
    dx, dw, db = affine_backward(da, fc_cache)
    return dx, dw, db, dgamma, dbeta
```

fc_net.py

```
import numpy as np
import pdb
from .layers import *
from .layer_utils import *
class TwoLayerNet(object):
   A two-layer fully-connected neural network with ReLU nonlinearity and
   softmax loss that uses a modular layer design. We assume an input dimension
   of D, a hidden dimension of H, and perform classification over C classes.
   The architecure should be affine - relu - affine - softmax.
   Note that this class does not implement gradient descent; instead, it
   will interact with a separate Solver object that is responsible for running
   optimization.
   The learnable parameters of the model are stored in the dictionary
   self.params that maps parameter names to numpy arrays.
   def __init__(self, input_dim=3*32*32, hidden_dims=100, num_classes=10,
               dropout=1, weight_scale=1e-3, reg=0.0):
       Initialize a new network.
       Inputs:
       - input_dim: An integer giving the size of the input
       - hidden_dims: An integer giving the size of the hidden layer
       - num_classes: An integer giving the number of classes to classify
       - dropout: Scalar between 0 and 1 giving dropout strength.
       - weight_scale: Scalar giving the standard deviation for random
         initialization of the weights.
       - req: Scalar giving L2 regularization strength.
       self.params = {}
       self.reg = reg
       # ----- #
       # YOUR CODE HERE:
       # Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
          self.params['W2'], self.params['b1'] and self.params['b2']. The
       # biases are initialized to zero and the weights are initialized
          so that each parameter has mean 0 and standard deviation weight_scale.
          The dimensions of W1 should be (input_dim, hidden_dim) and the
           dimensions of W2 should be (hidden_dims, num_classes)
       self.params['W1'] = np.random.normal(loc=0, scale=weight_scale, size=(input_dim,
       → hidden_dims))
```

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self.params['b1'] = np.zeros(hidden_dims)
   self.params['W2'] = np.random.normal(loc=0, scale=weight_scale,

    size=(hidden_dims, num_classes))
   self.params['b2'] = np.zeros(num_classes)
   # END YOUR CODE HERE
   # ----- #
def loss(self, X, y=None):
   Compute loss and gradient for a minibatch of data.
   Inputs:
   - X: Array of input data of shape (N, d_1, \ldots, d_k)
   - y: Array of labels, of shape (N,). y[i] gives the label for X[i].
   Returns:
   If y is None, then run a test-time forward pass of the model and return:
   - scores: Array of shape (N, C) giving classification scores, where
    scores[i, c] is the classification score for X[i] and class c.
   If y is not None, then run a training-time forward and backward pass and
   return a tuple of:
   - loss: Scalar value giving the loss
   - grads: Dictionary with the same keys as self.params, mapping parameter
    names to gradients of the loss with respect to those parameters.
   scores = None
   # ----- #
   # YOUR CODE HERE:
   # Implement the forward pass of the two-layer neural network. Store
   # the class scores as the variable 'scores'. Be sure to use the layers
   # you prior implemented.
   # ------ #
   layer_1_out, layer_1_cache = affine_relu_forward(X, self.params['W1'],

    self.params['b1'])

   layer_2_out, layer_2_cache = affine_forward(layer_1_out, self.params['W2'],

    self.params['b2'])

   scores = layer_2_out
   # END YOUR CODE HERE
   # If y is None then we are in test mode so just return scores
   if y is None:
      return scores
   loss, grads = 0, {}
   # ----- #
   # YOUR CODE HERE:
```

```
the loss as the variable 'loss' and store the gradients in the
          'grads' dictionary. For the grads dictionary, grads['W1'] holds
          the gradient for W1, grads['b1'] holds the gradient for b1, etc.
          i.e., grads[k] holds the gradient for self.params[k].
          Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
          for each W. Be sure to include the 0.5 multiplying factor to
          match our implementation.
         And be sure to use the layers you prior implemented.
       loss, dL = softmax_loss(scores, y)
       loss += 0.5 * self.reg * (np.sum(self.params['W1']**2) +
       dh, dw2, db2 = affine_backward(dL, layer_2_cache)
       _, dw1, db1 = affine_relu_backward(dh, layer_1_cache)
      grads['W1'] = dw1 + self.reg * self.params['W1']
      grads['b1'] = db1.T
      grads['W2'] = dw2 + self.reg * self.params['W2']
      grads['b2'] = db2.T
       # END YOUR CODE HERE
       return loss, grads
class FullyConnectedNet(object):
   A fully-connected neural network with an arbitrary number of hidden layers,
   ReLU nonlinearities, and a softmax loss function. This will also implement
   dropout and batch normalization as options. For a network with L layers,
   the architecture will be
   \{affine - [batch norm] - relu - [dropout]\} x (L - 1) - affine - softmax
   where batch normalization and dropout are optional, and the \{\ldots\} block is
   repeated L - 1 times.
   Similar to the TwoLayerNet above, learnable parameters are stored in the
   self.params dictionary and will be learned using the Solver class.
   11 11 11
   def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10,
             dropout=1, use_batchnorm=False, reg=0.0,
             weight_scale=1e-2, dtype=np.float32, seed=None):
       Initialize a new FullyConnectedNet.
```

Implement the backward pass of the two-layer neural net. Store

```
Inputs:
- hidden_dims: A list of integers giving the size of each hidden layer.
- input_dim: An integer giving the size of the input.
- num_classes: An integer giving the number of classes to classify.
- dropout: Scalar between 0 and 1 giving dropout strength. If dropout=1 then
 the network should not use dropout at all.
- use_batchnorm: Whether or not the network should use batch normalization.
- reg: Scalar giving L2 regularization strength.
- weight_scale: Scalar giving the standard deviation for random
 initialization of the weights.
- dtype: A numpy datatype object; all computations will be performed using
 this datatype. float32 is faster but less accurate, so you should use
 float64 for numeric gradient checking.
- seed: If not None, then pass this random seed to the dropout layers. This
 will make the dropout layers deteriminstic so we can gradient check the
 model.
self.use_batchnorm = use_batchnorm
self.use_dropout = dropout < 1</pre>
self.reg = reg
self.num_layers = 1 + len(hidden_dims)
self.dtype = dtype
self.params = {}
Initialize all parameters of the network in the self.params dictionary.
  The weights and biases of layer 1 are W1 and b1; and in general the
  weights and biases of layer i are Wi and bi. The
  biases are initialized to zero and the weights are initialized
   so that each parameter has mean 0 and standard deviation weight_scale.
  BATCHNORM: Initialize the gammas of each layer to 1 and the beta
# parameters to zero. The gamma and beta parameters for layer 1 should
  be self.params['qamma1'] and self.params['beta1']. For layer 2, they
  should be gamma2 and beta2, etc. Only use batchnorm if self.use_batchnorm
   is true and DO NOT do batch normalize the output scores.
in_dim = input_dim
for i, out_dim in enumerate(hidden_dims):
   self.params[f'W{i+1}'] = np.random.normal(loc=0, scale=weight_scale,

    size=(in_dim, out_dim))

   self.params[f'b{i+1}'] = np.zeros((out_dim,))
   if self.use_batchnorm:
       self.params[f'gamma{i+1}'] = np.ones((out_dim,))
       self.params[f'beta{i+1}'] = np.zeros((out_dim,))
   in_dim = out_dim
self.params[f'W{self.num_layers}'] = np.random.normal(loc=0, scale=weight_scale,

    size=(in_dim, num_classes))
self.params[f'b{self.num_layers}'] = np.zeros((num_classes,))
# ----- #
```

```
# END YOUR CODE HERE
    # ----- #
   # When using dropout we need to pass a dropout_param dictionary to each
    # dropout layer so that the layer knows the dropout probability and the mode
    # (train / test). You can pass the same dropout_param to each dropout layer.
   self.dropout_param = {}
   if self.use_dropout:
       self.dropout_param = {'mode': 'train', 'p': dropout}
   if seed is not None:
       self.dropout_param['seed'] = seed
    # With batch normalization we need to keep track of running means and
    # variances, so we need to pass a special bn_param object to each batch
    # normalization layer. You should pass self.bn_params[0] to the forward pass
   # of the first batch normalization layer, self.bn_params[1] to the forward
   # pass of the second batch normalization layer, etc.
   self.bn_params = []
   if self.use_batchnorm:
       self.bn_params = [{'mode': 'train'} for i in np.arange(self.num_layers - 1)]
   # Cast all parameters to the correct datatype
   for k, v in self.params.items():
       self.params[k] = v.astype(dtype)
def loss(self, X, y=None):
   Compute loss and gradient for the fully-connected net.
    Input / output: Same as TwoLayerNet above.
    11 11 11
   X = X.astype(self.dtype)
   mode = 'test' if y is None else 'train'
   # Set train/test mode for batchnorm params and dropout param since they
    # behave differently during training and testing.
   if self.dropout_param is not None:
       self.dropout_param['mode'] = mode
   if self.use_batchnorm:
       for bn_param in self.bn_params:
           bn_param['mode'] = mode
   scores = None
    # YOUR CODE HERE:
    # Implement the forward pass of the FC net and store the output
    # scores as the variable "scores".
      BATCHNORM: If self.use_batchnorm is true, insert a bathnorm layer
      between the affine_forward and relu_forward layers. You may
      also write an affine_batchnorm_relu() function in layer_utils.py.
```

```
# DROPOUT: If dropout is non-zero, insert a dropout layer after
# every ReLU layer.
L = self.num_layers
in_layer = X
caches = dict()
for i in range(1, L):
   W, b = self.params[f'W{i}'], self.params[f'b{i}']
   if self.use_batchnorm:
      gamma, beta = self.params[f'gamma{i}'], self.params[f'beta{i}']
      out_layer, layer_cache = affine_batchnorm_relu_forward(in_layer, W, b,

    gamma, beta, self.bn_params[i-1])

   else:
      out_layer, layer_cache = affine_relu_forward(in_layer, W, b)
   if self.use_dropout:
      out_layer, dropout_cache = dropout_forward(out_layer, self.dropout_param)
      layer_cache = (*layer_cache, dropout_cache)
   caches[i] = layer_cache
   in_layer = out_layer
scores, layer_cache = affine_forward(in_layer, self.params[f'W{L}'],

    self.params[f'b{L}'])

caches[L] = layer_cache
# END YOUR CODE HERE
# If test mode return early
if mode == 'test':
   return scores
loss, grads = 0.0, {}
# ----- #
# YOUR CODE HERE:
   Implement the backwards pass of the FC net and store the gradients
   in the grads dict, so that grads[k] is the gradient of self.params[k]
  Be sure your L2 regularization includes a 0.5 factor.
  BATCHNORM: Incorporate the backward pass of the batchnorm.
  DROPOUT: Incorporate the backward pass of dropout.
loss, dL = softmax_loss(scores, y)
for p in self.params:
   if p[0] == 'W':
      loss += 0.5 * self.reg * np.sum(self.params[p]**2)
dhi = dL
for i in range(L, 0, -1):
   cache = caches[i]
```

```
if i == L:
      dhi, dwi, dbi = affine_backward(dhi, cache)
      if self.use_dropout:
         dhi = dropout_backward(dhi, cache[-1])
         cache = cache[:-1]
      if not self.use_batchnorm:
         dhi, dwi, dbi = affine_relu_backward(dhi, cache)
      else:
         dhi, dwi, dbi, dgammai, dbetai = affine_batchnorm_relu_backward(dhi,
          grads[f'gamma{i}'] = dgammai.T
         grads[f'beta{i}'] = dbetai.T
   grads[f'W{i}'] = dwi + self.reg * self.params[f'W{i}']
   grads[f'b{i}'] = dbi.T
# ----- #
# END YOUR CODE HERE
# ========== #
return loss, grads
```

Optimization for Fully Connected Networks

In this notebook, we will implement different optimization rules for gradient descent. We have provided starter code; however, you will need to copy and paste your code from your implementation of the modular fully connected nets in HW #3 to build upon this.

Utils has a solid API for building these modular frameworks and training them, and we will use this very well implemented framework as opposed to "reinventing the wheel." This includes using the Solver, various utility functions, and the layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils.

```
In [2]: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc_net import *
        from utils.data_utils import get_CIFAR10_data
        from utils.gradient check import eval numerical gradient, eval numerical gra
        from utils.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ip
        %load ext autoreload
        %autoreload 2
        def rel error(x, y):
            """ returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
In [3]: # Load the (preprocessed) CIFAR10 data.
        data = get CIFAR10 data()
        for k in data.keys():
            print('{}: {} '.format(k, data[k].shape))
        X train: (49000, 3, 32, 32)
        y_train: (49000,)
        X_val: (1000, 3, 32, 32)
        y_val: (1000,)
        X_test: (1000, 3, 32, 32)
        y test: (1000,)
```

Building upon your HW #3 implementation

Copy and paste the following functions from your HW #3 implementation of a modular FC net:

- affine_forward in nndl/layers.py
- affine_backward in nndl/layers.py
- relu_forward in nndl/layers.py
- relu_backward in nndl/layers.py
- affine_relu_forward in nndl/layer_utils.py
- affine_relu_backward in nndl/layer_utils.py
- The FullyConnectedNet class in nndl/fc_net.py

Test all functions you copy and pasted

```
In [4]: from nndl.layer_tests import *

affine_forward_test(); print('\n')
affine_backward_test(); print('\n')
relu_forward_test(); print('\n')
relu_backward_test(); print('\n')
affine_relu_test(); print('\n')
fc_net_test()
```

```
If affine_forward function is working, difference should be less than 1e-9:
difference: 9.7698500479884e-10
If affine_backward is working, error should be less than 1e-9::
dx error: 1.3689215599640917e-09
dw error: 3.1042953211841685e-10
db error: 4.7787324839814184e-12
If relu_forward function is working, difference should be around 1e-8:
difference: 4.999999798022158e-08
If relu forward function is working, error should be less than 1e-9:
dx error: 3.2756220736460565e-12
If affine relu forward and affine relu backward are working, error should b
e less than 1e-9::
dx error: 4.860324809924818e-11
dw error: 1.0086070366798288e-10
db error: 1.3458960235367463e-10
Running check with reg = 0
Initial loss: 2.3013741552210183
W1 relative error: 1.7379695636419452e-07
W2 relative error: 4.594446049655719e-07
W3 relative error: 3.242487105568421e-07
b1 relative error: 1.0421944607209353e-08
b2 relative error: 1.1500928722029845e-08
b3 relative error: 8.641677074873272e-11
Running check with reg = 3.14
Initial loss: 7.015993603525885
W1 relative error: 1.2531856038325753e-07
W2 relative error: 4.832149225080869e-08
W3 relative error: 7.898858975270852e-07
b1 relative error: 2.9440083745069855e-08
b2 relative error: 4.330637752003401e-09
b3 relative error: 2.9748084116488993e-10
```

Training a larger model

In general, proceeding with vanilla stochastic gradient descent to optimize models may be fraught with problems and limitations, as discussed in class. Thus, we implement optimizers that improve on SGD.

SGD + momentum

In the following section, implement SGD with momentum. Read the nndl/optim.py
API, which is provided by CS231n, and be sure you understand it. After, implement
sgd_momentum in nndl/optim.py
. Test your implementation of sgd_momentum
by running the cell below.

```
In [15]: from nndl.optim import sgd_momentum
       N, D = 4, 5
       w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        config = {'learning_rate': 1e-3, 'velocity': v}
        next_w, _ = sgd_momentum(w, dw, config=config)
        expected next w = np.asarray([
           [ 0.47454737, 0.54133684, 0.60812632, 0.67491579, 0.74170526],
           [ 0.80849474, 0.87528421, 0.94207368, 1.00886316, 1.07565263],
           [ 1.14244211, 1.20923158, 1.27602105, 1.34281053, 1.4096 ]])
        expected_velocity = np.asarray([
           [ 0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
           [ 0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
           [ 0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096
                                                                 ]])
        print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
        print('velocity error: {}'.format(rel_error(expected_velocity, config['veloc
```

next_w error: 8.882347033505819e-09 velocity error: 4.269287743278663e-09

SGD + Nesterov momentum

Implement sgd_nesterov_momentum in ndl/optim.py .

```
In [17]: from nndl.optim import sgd_nesterov_momentum
        N, D = 4, 5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        config = {'learning_rate': 1e-3, 'velocity': v}
        next_w, _ = sgd_nesterov_momentum(w, dw, config=config)
        expected next w = np.asarray([
                                               0.28310316,
            [0.08714, 0.15246105, 0.21778211,
                                                           0.34842421],
           [0.41374526, 0.47906632, 0.54438737, 0.60970842,
                                                           0.67502947],
           [0.74035053, 0.80567158, 0.87099263, 0.93631368, 1.00163474],
           [1.06695579, 1.13227684, 1.19759789, 1.26291895, 1.32824 ]])
        expected_velocity = np.asarray([
```

```
[ 0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
  [ 0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
  [ 0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096 ]])

print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
print('velocity error: {}'.format(rel_error(expected_velocity, config['velocity error: 1.0875186845081027e-08)
velocity error: 4.269287743278663e-09
```

Evaluating SGD, SGD+Momentum, and SGD+NesterovMomentum

Run the following cell to train a 6 layer FC net with SGD, SGD+momentum, and SGD+Nesterov momentum. You should see that SGD+momentum achieves a better loss than SGD, and that SGD+Nesterov momentum achieves a slightly better loss (and training accuracy) than SGD+momentum.

```
In [8]: num_train = 4000
        small data = {
            'X train': data['X train'][:num train],
            'y_train': data['y_train'][:num_train],
            'X_val': data['X_val'],
            'y_val': data['y_val'],
        solvers = {}
        for update_rule in ['sgd', 'sgd_momentum', 'sgd_nesterov_momentum']:
            print('Optimizing with {}'.format(update rule))
            model = FullyConnectedNet([100, 100, 100, 100], weight_scale=5e-2)
            solver = Solver(model, small data,
                            num_epochs=5, batch_size=100,
                            update_rule=update_rule,
                            optim_config={
                               'learning rate': 1e-2,
                            },
                            verbose=False)
            solvers[update rule] = solver
            solver.train()
            print
        fig, axes = plt.subplots(3, 1)
        ax = axes[0]
        ax.set_title('Training loss')
        ax.set_xlabel('Iteration')
        ax = axes[1]
        ax.set_title('Training accuracy')
        ax.set_xlabel('Epoch')
```

```
ax = axes[2]
ax.set_title('Validation accuracy')
ax.set_xlabel('Epoch')

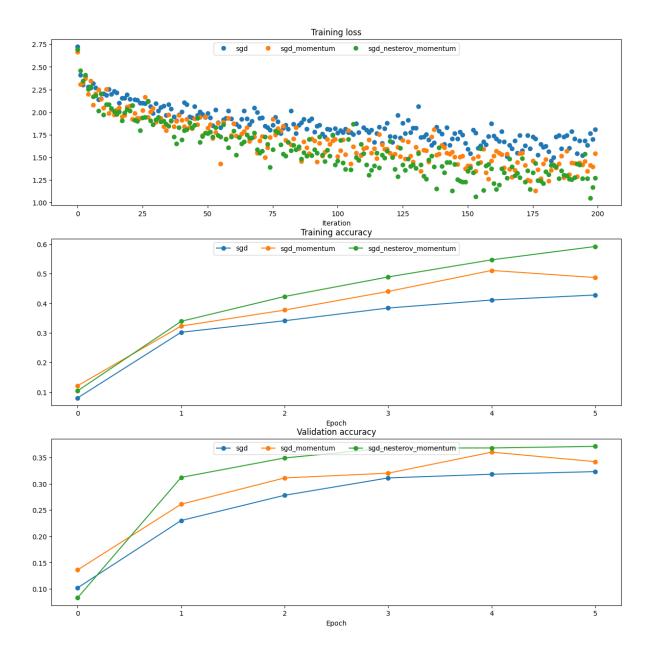
for update_rule, solver in solvers.items():
    ax = axes[0]
    ax.plot(solver.loss_history, 'o', label=update_rule)

    ax = axes[1]
    ax.plot(solver.train_acc_history, '-o', label=update_rule)

    ax = axes[2]
    ax.plot(solver.val_acc_history, '-o', label=update_rule)

for i in [1, 2, 3]:
    ax = axes[i - 1]
    ax.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()
```

Optimizing with sgd_momentum
Optimizing with sgd_nesterov_momentum



RMSProp

Now we go to techniques that adapt the gradient. Implement rmsprop in nndl/optim.py. Test your implementation by running the cell below.

```
[-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
                                                      0.33532447],
 [ 0.12716641, 0.17918792, 0.23122175,
                                         0.28326742,
 [ 0.38739248, 0.43947102,
                            0.49155973, 0.54365823, 0.59576619]])
expected cache = np.asarray([
                                         0.64284931, 0.65804321],
 [ 0.5976,
                0.6126277,
                            0.6277108,
 [ 0.67329252, 0.68859723, 0.70395734,
                                         0.71937285,
                                                     0.73484377],
 [ 0.75037008, 0.7659518,
                            0.78158892,
                                         0.79728144,
                                                      0.81302936],
 [ 0.82883269, 0.84469141, 0.86060554, 0.87657507, 0.8926
                                                               ]])
print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
print('cache error: {}'.format(rel_error(expected_cache, config['a'])))
```

next_w error: 9.524687511038133e-08 cache error: 2.6477955807156126e-09

Adaptive moments

Now, implement adam in nndl/optim.py . Test your implementation by running the cell below.

```
In [20]: # Test Adam implementation; you should see errors around 1e-7 or less
         from nndl.optim import adam
         N, D = 4, 5
         w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
         dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
         v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
         a = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)
         config = {'learning_rate': 1e-2, 'v': v, 'a': a, 't': 5}
         next_w, _ = adam(w, dw, config=config)
         expected next w = np.asarray([
           [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],
           [-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],
           [0.1248705, 0.17744702, 0.23002243, 0.28259667, 0.33516969],
           [ 0.38774145, 0.44031188, 0.49288093, 0.54544852, 0.59801459]])
         expected a = np.asarray([
                         0.68908382, 0.67851319,
                                                   0.66794809,
                                                               0.65738853,],
           [ 0.69966,
           [ 0.64683452, 0.63628604, 0.6257431,
                                                   0.61520571,
                                                               0.60467385,],
           [ 0.59414753, 0.58362676, 0.57311152, 0.56260183, 0.55209767,],
           [ 0.54159906, 0.53110598, 0.52061845, 0.51013645,
                                                                0.49966, ]])
         expected v = np.asarray([
                         0.49947368, 0.51894737,
                                                   0.53842105,
                                                                0.55789474],
           [ 0.48,
           [ 0.57736842, 0.59684211, 0.61631579,
                                                   0.63578947,
                                                               0.65526316],
           [ 0.67473684, 0.69421053, 0.71368421,
                                                   0.73315789,
                                                                0.75263158],
           [ 0.77210526, 0.79157895, 0.81105263, 0.83052632,
                                                                0.85
                                                                          11)
         print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
         print('a error: {}'.format(rel_error(expected_a, config['a'])))
         print('v error: {}'.format(rel_error(expected_v, config['v'])))
```

next_w error: 1.1395691798535431e-07 a error: 4.208314038113071e-09 v error: 4.214963193114416e-09

Comparing SGD, SGD+NesterovMomentum, RMSProp, and Adam

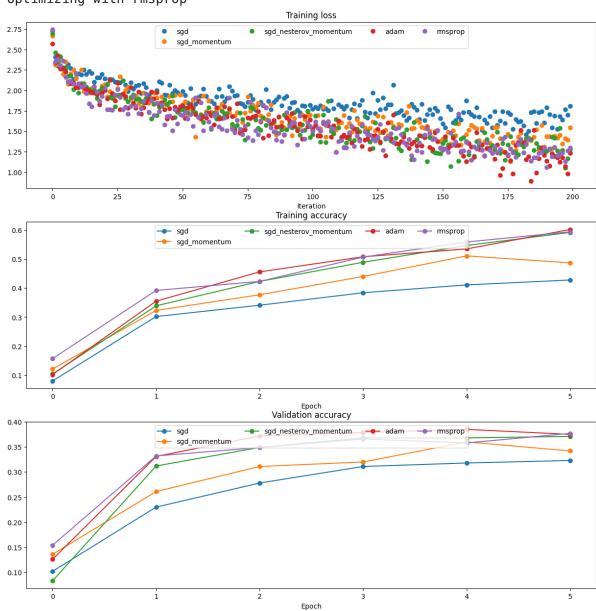
The following code will compare optimization with SGD, Momentum, Nesterov Momentum, RMSProp and Adam. In our code, we find that RMSProp, Adam, and SGD + Nesterov Momentum achieve approximately the same training error after a few training epochs.

```
In [21]: learning_rates = {'rmsprop': 2e-4, 'adam': 1e-3}
         for update_rule in ['adam', 'rmsprop']:
             print('Optimizing with {}'.format(update_rule))
             model = FullyConnectedNet([100, 100, 100, 100], weight_scale=5e-2)
             solver = Solver(model, small data,
                             num_epochs=5, batch_size=100,
                             update rule=update rule,
                             optim_config={
                                'learning_rate': learning_rates[update_rule]
                             },
                             verbose=False)
             solvers[update_rule] = solver
             solver.train()
             print
         fig, axes = plt.subplots(3, 1)
         ax = axes[0]
         ax.set_title('Training loss')
         ax.set_xlabel('Iteration')
         ax = axes[1]
         ax.set title('Training accuracy')
         ax.set_xlabel('Epoch')
         ax = axes[2]
         ax.set_title('Validation accuracy')
         ax.set_xlabel('Epoch')
         for update_rule, solver in solvers.items():
             ax = axes[0]
             ax.plot(solver.loss_history, 'o', label=update_rule)
             ax = axes[1]
             ax.plot(solver.train_acc_history, '-o', label=update_rule)
             ax = axes[2]
             ax.plot(solver.val_acc_history, '-o', label=update_rule)
```

```
for i in [1, 2, 3]:
    ax = axes[i - 1]
    ax.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()

Optimizing with adam
```

Optimizing with adam Optimizing with rmsprop



Easier optimization

In the following cell, we'll train a 4 layer neural network having 500 units in each hidden layer with the different optimizers, and find that it is far easier to get up to 50+% performance on CIFAR-10. After we implement batchnorm and dropout, we'll ask you to get 55+% on CIFAR-10.

```
In [22]: optimizer = 'adam'
best_model = None
```

```
(Iteration 1 / 4900) loss: 2.313322
(Epoch 0 / 10) train acc: 0.126000; val acc: 0.124000
(Iteration 51 / 4900) loss: 1.905534
(Iteration 101 / 4900) loss: 1.949207
(Iteration 151 / 4900) loss: 1.849694
(Iteration 201 / 4900) loss: 1.566729
(Iteration 251 / 4900) loss: 1.582901
(Iteration 301 / 4900) loss: 1.540685
(Iteration 351 / 4900) loss: 1.675744
(Iteration 401 / 4900) loss: 1.741227
(Iteration 451 / 4900) loss: 1.658826
(Epoch 1 / 10) train acc: 0.423000; val acc: 0.426000
(Iteration 501 / 4900) loss: 1.469051
(Iteration 551 / 4900) loss: 1.683368
(Iteration 601 / 4900) loss: 1.446203
(Iteration 651 / 4900) loss: 1.522289
(Iteration 701 / 4900) loss: 1.508258
(Iteration 751 / 4900) loss: 1.387670
(Iteration 801 / 4900) loss: 1.610682
(Iteration 851 / 4900) loss: 1.567350
(Iteration 901 / 4900) loss: 1.662909
(Iteration 951 / 4900) loss: 1.512415
(Epoch 2 / 10) train acc: 0.506000; val_acc: 0.468000
(Iteration 1001 / 4900) loss: 1.354171
(Iteration 1051 / 4900) loss: 1.466307
(Iteration 1101 / 4900) loss: 1.293006
(Iteration 1151 / 4900) loss: 1.305836
(Iteration 1201 / 4900) loss: 1.384686
(Iteration 1251 / 4900) loss: 1.367656
(Iteration 1301 / 4900) loss: 1.318984
(Iteration 1351 / 4900) loss: 1.367128
(Iteration 1401 / 4900) loss: 1.304281
(Iteration 1451 / 4900) loss: 1.437152
(Epoch 3 / 10) train acc: 0.473000; val acc: 0.466000
(Iteration 1501 / 4900) loss: 1.372929
(Iteration 1551 / 4900) loss: 1.476415
(Iteration 1601 / 4900) loss: 1.354982
(Iteration 1651 / 4900) loss: 1.267194
(Iteration 1701 / 4900) loss: 1.399184
(Iteration 1751 / 4900) loss: 1.290055
(Iteration 1801 / 4900) loss: 1.216199
(Iteration 1851 / 4900) loss: 1.152526
(Iteration 1901 / 4900) loss: 1.196868
(Iteration 1951 / 4900) loss: 1.387752
(Epoch 4 / 10) train acc: 0.562000; val acc: 0.505000
(Iteration 2001 / 4900) loss: 1.241760
(Iteration 2051 / 4900) loss: 1.281049
(Iteration 2101 / 4900) loss: 1.280633
(Iteration 2151 / 4900) loss: 1.386172
(Iteration 2201 / 4900) loss: 1.152989
(Iteration 2251 / 4900) loss: 1.139457
(Iteration 2301 / 4900) loss: 1.210900
(Iteration 2351 / 4900) loss: 1.392619
(Iteration 2401 / 4900) loss: 1.251894
(Epoch 5 / 10) train acc: 0.608000; val acc: 0.520000
(Iteration 2451 / 4900) loss: 1.337694
```

```
(Iteration 2501 / 4900) loss: 1.232610
         (Iteration 2551 / 4900) loss: 1.081923
         (Iteration 2601 / 4900) loss: 1.037320
         (Iteration 2651 / 4900) loss: 1.097721
         (Iteration 2701 / 4900) loss: 1.110266
         (Iteration 2751 / 4900) loss: 1.026649
         (Iteration 2801 / 4900) loss: 1.229403
         (Iteration 2851 / 4900) loss: 1.336861
         (Iteration 2901 / 4900) loss: 1.105612
         (Epoch 6 / 10) train acc: 0.585000; val acc: 0.522000
         (Iteration 2951 / 4900) loss: 1.334152
         (Iteration 3001 / 4900) loss: 1.019222
         (Iteration 3051 / 4900) loss: 1.036279
         (Iteration 3101 / 4900) loss: 1.049492
         (Iteration 3151 / 4900) loss: 1.349864
         (Iteration 3201 / 4900) loss: 1.099299
         (Iteration 3251 / 4900) loss: 0.945250
         (Iteration 3301 / 4900) loss: 1.060365
         (Iteration 3351 / 4900) loss: 1.069408
         (Iteration 3401 / 4900) loss: 1.100029
         (Epoch 7 / 10) train acc: 0.631000; val_acc: 0.533000
         (Iteration 3451 / 4900) loss: 1.187260
         (Iteration 3501 / 4900) loss: 0.923642
         (Iteration 3551 / 4900) loss: 1.053363
         (Iteration 3601 / 4900) loss: 1.021797
         (Iteration 3651 / 4900) loss: 0.943927
         (Iteration 3701 / 4900) loss: 1.032660
         (Iteration 3751 / 4900) loss: 1.135157
         (Iteration 3801 / 4900) loss: 1.161245
         (Iteration 3851 / 4900) loss: 0.887338
         (Iteration 3901 / 4900) loss: 1.282647
         (Epoch 8 / 10) train acc: 0.648000; val acc: 0.539000
         (Iteration 3951 / 4900) loss: 0.943961
         (Iteration 4001 / 4900) loss: 1.279366
         (Iteration 4051 / 4900) loss: 1.181031
         (Iteration 4101 / 4900) loss: 1.006135
         (Iteration 4151 / 4900) loss: 0.983813
         (Iteration 4201 / 4900) loss: 1.063429
         (Iteration 4251 / 4900) loss: 0.930355
         (Iteration 4301 / 4900) loss: 1.220433
         (Iteration 4351 / 4900) loss: 1.078938
         (Iteration 4401 / 4900) loss: 0.788424
         (Epoch 9 / 10) train acc: 0.655000; val acc: 0.532000
         (Iteration 4451 / 4900) loss: 1.027105
         (Iteration 4501 / 4900) loss: 0.831332
         (Iteration 4551 / 4900) loss: 0.854954
         (Iteration 4601 / 4900) loss: 1.031803
         (Iteration 4651 / 4900) loss: 0.788709
         (Iteration 4701 / 4900) loss: 0.806451
         (Iteration 4751 / 4900) loss: 0.943119
         (Iteration 4801 / 4900) loss: 0.756370
         (Iteration 4851 / 4900) loss: 0.991180
         (Epoch 10 / 10) train acc: 0.686000; val acc: 0.546000
In [23]: y_test_pred = np.argmax(model.loss(data['X_test']), axis=1)
         y_val_pred = np.argmax(model.loss(data['X_val']), axis=1)
```

```
print('Validation set accuracy: {}'.format(np.mean(y_val_pred == data['y_val
print('Test set accuracy: {}'.format(np.mean(y_test_pred == data['y_test']))
Validation set accuracy: 0.546
Test set accuracy: 0.533
```

In []:

Batch Normalization

In this notebook, you will implement the batch normalization layers of a neural network to increase its performance. Please review the details of batch normalization from the lecture notes.

Utils has a solid API for building these modular frameworks and training them, and we will use this very well implemented framework as opposed to "reinventing the wheel." This includes using the Solver, various utility functions, and the layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils.

```
In [25]: ## Import and setups
         import time
         import numpy as np
         import matplotlib.pyplot as plt
         from nndl.fc net import *
         from nndl.layers import *
         from utils.data_utils import get_CIFAR10_data
         from utils gradient check import eval numerical gradient, eval numerical gra
         from utils.solver import Solver
         %matplotlib inline
         plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
         plt.rcParams['image.interpolation'] = 'nearest'
         plt.rcParams['image.cmap'] = 'gray'
         # for auto-reloading external modules
         # see http://stackoverflow.com/questions/1907993/autoreload—of—modules—in—ip
         %load ext autoreload
         %autoreload 2
         def rel error(x, y):
             """ returns relative error """
             return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
         The autoreload extension is already loaded. To reload it, use:
           %reload ext autoreload
 In [2]: # Load the (preprocessed) CIFAR10 data.
         data = get_CIFAR10_data()
         for k in data.keys():
             print('{}: {} '.format(k, data[k].shape))
         X_train: (49000, 3, 32, 32)
         y_train: (49000,)
         X_val: (1000, 3, 32, 32)
         y_val: (1000,)
         X_test: (1000, 3, 32, 32)
         y test: (1000,)
```

Batchnorm forward pass

Implement the training time batchnorm forward pass, batchnorm_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [3]: # Check the training-time forward pass by checking means and variances
        # of features both before and after batch normalization
        # Simulate the forward pass for a two-layer network
        N, D1, D2, D3 = 200, 50, 60, 3
        X = np.random.randn(N, D1)
        W1 = np.random.randn(D1, D2)
        W2 = np.random.randn(D2, D3)
        a = np.maximum(0, X.dot(W1)).dot(W2)
        print('Before batch normalization:')
        print(' means: ', a.mean(axis=0))
        print(' stds: ', a.std(axis=0))
        # Means should be close to zero and stds close to one
        print('After batch normalization (gamma=1, beta=0)')
        a_norm, _ = batchnorm_forward(a, np.ones(D3), np.zeros(D3), {'mode': 'train'
        print(' mean: ', a_norm.mean(axis=0))
        print(' std: ', a_norm.std(axis=0))
        # Now means should be close to beta and stds close to gamma
        qamma = np.asarray([1.0, 2.0, 3.0])
        beta = np.asarray([11.0, 12.0, 13.0])
        a_norm, _ = batchnorm_forward(a, gamma, beta, {'mode': 'train'})
        print('After batch normalization (nontrivial gamma, beta)')
        print(' means: ', a_norm.mean(axis=0))
        print(' stds: ', a_norm.std(axis=0))
        Before batch normalization:
          means: [2.76313083 4.61815309 1.92245279]
          stds: [34.93566914 21.96251881 40.75515778]
        After batch normalization (gamma=1, beta=0)
          mean: [-5.30131494e-17 -1.22124533e-17 -9.99200722e-18]
          std: [1. 0.9999999 1.
                                                ]
        After batch normalization (nontrivial gamma, beta)
          means: [11. 12. 13.]
                            1.99999998 2.999999991
          stds: [1.
        Implement the testing time batchnorm forward pass, batchnorm forward, in
        nndl/layers.py . After that, test your implementation by running the following cell.
```

nndl/layers.py . After that, test your implementation by running the following cell.

```
In [5]: # Check the test-time forward pass by running the training-time
    # forward pass many times to warm up the running averages, and then
    # checking the means and variances of activations after a test-time
    # forward pass.

N, D1, D2, D3 = 200, 50, 60, 3
W1 = np.random.randn(D1, D2)
```

```
W2 = np.random.randn(D2, D3)
bn param = {'mode': 'train'}
qamma = np.ones(D3)
beta = np.zeros(D3)
for t in np.arange(50):
    X = np.random.randn(N, D1)
    a = np.maximum(0, X.dot(W1)).dot(W2)
    batchnorm forward(a, gamma, beta, bn param)
bn param['mode'] = 'test'
X = np.random.randn(N, D1)
a = np.maximum(0, X.dot(W1)).dot(W2)
a_norm, _ = batchnorm_forward(a, gamma, beta, bn_param)
# Means should be close to zero and stds close to one, but will be
# noisier than training-time forward passes.
print('After batch normalization (test-time):')
print(' means: ', a_norm.mean(axis=0))
print(' stds: ', a_norm.std(axis=0))
After batch normalization (test-time):
  means: [-0.02458589 0.00925263 -0.13068034]
  stds: [0.96969039 0.97595274 0.90424285]
```

Batchnorm backward pass

Implement the backward pass for the batchnorm layer, batchnorm_backward in nndl/layers.py . Check your implementation by running the following cell.

```
In [136... # Gradient check batchnorm backward pass
         N, D = 4, 5
         x = 5 * np.random.randn(N, D) + 12
         gamma = np.random.randn(D)
         beta = np.random.randn(D)
         dout = np.random.randn(N, D)
         bn param = {'mode': 'train'}
         fx = lambda x: batchnorm_forward(x, gamma, beta, bn_param)[0]
         fg = lambda gamma: batchnorm_forward(x, gamma, beta, bn_param)[0]
         fb = lambda beta: batchnorm_forward(x, gamma, beta, bn_param)[0]
         dx_num = eval_numerical_gradient_array(fx, x, dout)
         da num = eval numerical gradient array(fg, gamma, dout)
         db_num = eval_numerical_gradient_array(fb, beta, dout)
         _, cache = batchnorm_forward(x, gamma, beta, bn_param)
         dx, dgamma, dbeta = batchnorm_backward(dout, cache)
         print('dx error: ', rel_error(dx_num, dx))
         print('dgamma error: ', rel_error(da_num, dgamma))
         print('dbeta error: ', rel_error(db_num, dbeta))
```

dx error: 1.5549965424165472e-09 dgamma error: 4.945387540639603e-12 dbeta error: 1.3384711454045822e-11

Implement a fully connected neural network with batchnorm layers

Modify the FullyConnectedNet() class in nndl/fc_net.py to incorporate batchnorm layers. You will need to modify the class in the following areas:

- (1) The gammas and betas need to be initialized to 1's and 0's respectively in init.
- (2) The batchnorm_forward layer needs to be inserted between each affine and relu layer (except in the output layer) in a forward pass computation in loss. You may find it helpful to write an affine_batchnorm_relu() layer in nndl/layer_utils.py although this is not necessary.
- (3) The batchnorm_backward layer has to be appropriately inserted when calculating gradients.

After you have done the appropriate modifications, check your implementation by running the following cell.

Note, while the relative error for W3 should be small, as we backprop gradients more, you may find the relative error increases. Our relative error for W1 is on the order of 1e-4.

```
Running check with reg = 0
Initial loss: 2.556552280652318
W1 relative error: 8.759300681967743e-06
W2 relative error: 1.0542428473077016e-05
W3 relative error: 6.809054110038227e-10
b1 relative error: 2.220446049250313e-08
b2 relative error: 2.220446049250313e-08
b3 relative error: 1.086652346342557e-10
beta1 relative error: 7.668866978859854e-08
beta2 relative error: 6.204064703536048e-09
gamma1 relative error: 7.891317276123289e-08
gamma2 relative error: 8.645541540323422e-09
Running check with reg = 3.14
Initial loss: 7.552884358711733
W1 relative error: 2.1748130757425133e-06
W2 relative error: 4.434694498645516e-06
W3 relative error: 3.4523297946640607e-09
b1 relative error: 0.00444093650742161
b2 relative error: 1.7763568394002505e-07
b3 relative error: 1.4105211800087626e-10
beta1 relative error: 1.3123252710973797e-08
beta2 relative error: 2.1990214261944293e-08
gamma1 relative error: 1.305060218035805e-08
gamma2 relative error: 1.5491497875866084e-08
```

Training a deep fully connected network with batch normalization.

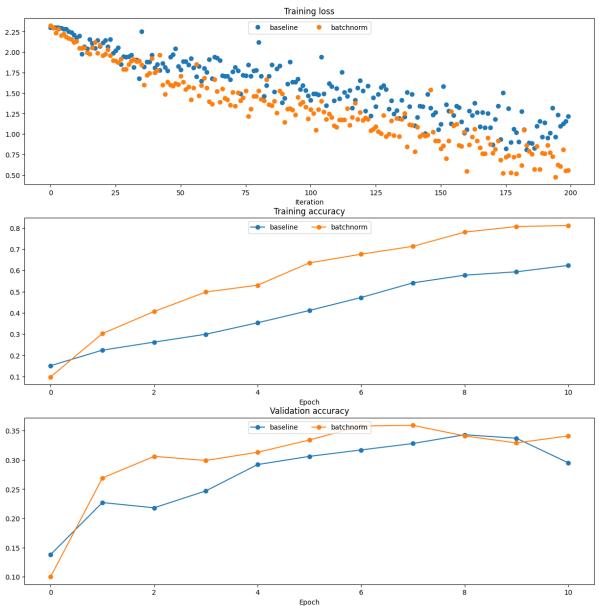
To see if batchnorm helps, let's train a deep neural network with and without batch normalization.

```
In [153... # Try training a very deep net with batchnorm
         hidden_dims = [100, 100, 100, 100, 100]
         num train = 1000
         small_data = {
             'X_train': data['X_train'][:num_train],
             'y_train': data['y_train'][:num_train],
             'X val': data['X val'],
             'y val': data['y val'],
         weight scale = 2e-2
         bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_bat
         model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchr
         bn_solver = Solver(bn_model, small_data,
                          num_epochs=10, batch_size=50,
                          update rule='adam',
                          optim config={
                            'learning_rate': 1e-3,
```

```
verbose=True, print_every=200)
         bn solver.train()
         solver = Solver(model, small_data,
                          num_epochs=10, batch_size=50,
                          update rule='adam',
                          optim config={
                            'learning rate': 1e-3,
                          verbose=True, print_every=200)
         solver.train()
         (Iteration 1 / 200) loss: 2.323703
         (Epoch 0 / 10) train acc: 0.098000; val acc: 0.100000
         (Epoch 1 / 10) train acc: 0.302000; val acc: 0.269000
         (Epoch 2 / 10) train acc: 0.406000; val acc: 0.306000
         (Epoch 3 / 10) train acc: 0.498000; val_acc: 0.299000
         (Epoch 4 / 10) train acc: 0.530000; val acc: 0.313000
         (Epoch 5 / 10) train acc: 0.635000; val_acc: 0.334000
         (Epoch 6 / 10) train acc: 0.676000; val_acc: 0.358000
         (Epoch 7 / 10) train acc: 0.713000; val acc: 0.359000
         (Epoch 8 / 10) train acc: 0.780000; val acc: 0.341000
         (Epoch 9 / 10) train acc: 0.806000; val_acc: 0.329000
         (Epoch 10 / 10) train acc: 0.811000; val acc: 0.341000
         (Iteration 1 / 200) loss: 2.302869
         (Epoch 0 / 10) train acc: 0.151000; val_acc: 0.138000
         (Epoch 1 / 10) train acc: 0.224000; val acc: 0.227000
         (Epoch 2 / 10) train acc: 0.262000; val acc: 0.218000
         (Epoch 3 / 10) train acc: 0.299000; val_acc: 0.247000
         (Epoch 4 / 10) train acc: 0.353000; val_acc: 0.292000
         (Epoch 5 / 10) train acc: 0.411000; val acc: 0.306000
         (Epoch 6 / 10) train acc: 0.472000; val_acc: 0.317000
         (Epoch 7 / 10) train acc: 0.541000; val_acc: 0.328000
         (Epoch 8 / 10) train acc: 0.577000; val acc: 0.343000
         (Epoch 9 / 10) train acc: 0.593000; val_acc: 0.337000
         (Epoch 10 / 10) train acc: 0.623000; val_acc: 0.295000
In [154...] fig, axes = plt.subplots(3, 1)
         ax = axes[0]
         ax.set_title('Training loss')
         ax.set_xlabel('Iteration')
         ax = axes[1]
         ax.set_title('Training accuracy')
         ax.set_xlabel('Epoch')
         ax = axes[2]
         ax.set_title('Validation accuracy')
         ax.set xlabel('Epoch')
         ax = axes[0]
         ax.plot(solver.loss_history, 'o', label='baseline')
         ax.plot(bn_solver.loss_history, 'o', label='batchnorm')
         ax = axes[1]
```

```
ax.plot(solver.train_acc_history, '-o', label='baseline')
ax.plot(bn_solver.train_acc_history, '-o', label='batchnorm')
ax = axes[2]
ax.plot(solver.val_acc_history, '-o', label='baseline')
ax.plot(bn_solver.val_acc_history, '-o', label='batchnorm')

for i in [1, 2, 3]:
    ax = axes[i - 1]
    ax.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()
```



Batchnorm and initialization

The following cells run an experiment where for a deep network, the initialization is varied. We do training for when batchnorm layers are and are not included.

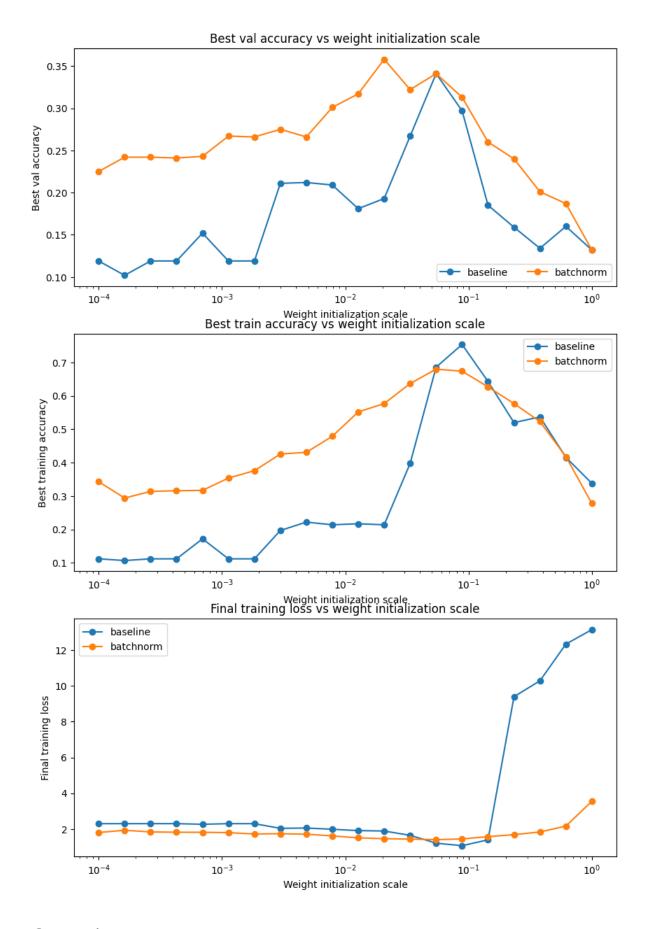
```
In [155... # Try training a very deep net with batchnorm
         hidden_dims = [50, 50, 50, 50, 50, 50, 50]
         num train = 1000
         small data = {
             'X_train': data['X_train'][:num_train],
             'y_train': data['y_train'][:num_train],
             'X_val': data['X_val'],
             'y_val': data['y_val'],
         bn_solvers = {}
         solvers = {}
         weight_scales = np.logspace(-4, 0, num=20)
         for i, weight_scale in enumerate(weight_scales):
             print('Running weight scale {} / {}'.format(i + 1, len(weight_scales)))
             bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use
             model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_ba
             bn solver = Solver(bn model, small data,
                             num_epochs=10, batch_size=50,
                             update_rule='adam',
                             optim config={
                                'learning_rate': 1e-3,
                             },
                             verbose=False, print every=200)
             bn solver.train()
             bn_solvers[weight_scale] = bn_solver
             solver = Solver(model, small_data,
                             num_epochs=10, batch_size=50,
                             update_rule='adam',
                             optim config={
                                'learning_rate': 1e-3,
                             verbose=False, print_every=200)
             solver.train()
             solvers[weight_scale] = solver
```

```
Running weight scale 4 / 20
         Running weight scale 5 / 20
         Running weight scale 6 / 20
         Running weight scale 7 / 20
         Running weight scale 8 / 20
         Running weight scale 9 / 20
         Running weight scale 10 / 20
         Running weight scale 11 / 20
         Running weight scale 12 / 20
         Running weight scale 13 / 20
         Running weight scale 14 / 20
         Running weight scale 15 / 20
         Running weight scale 16 / 20
         Running weight scale 17 / 20
         Running weight scale 18 / 20
         Running weight scale 19 / 20
         Running weight scale 20 / 20
In [156... # Plot results of weight scale experiment
         best_train_accs, bn_best_train_accs = [], []
         best val accs, bn best val accs = [], []
         final train loss, bn final train loss = [], []
         for ws in weight scales:
             best train accs.append(max(solvers[ws].train acc history))
             bn best train accs.append(max(bn solvers[ws].train acc history))
             best_val_accs.append(max(solvers[ws].val_acc_history))
             bn_best_val_accs.append(max(bn_solvers[ws].val_acc_history))
             final_train_loss.append(np.mean(solvers[ws].loss_history[-100:]))
             bn final train loss.append(np.mean(bn solvers[ws].loss history[-100:]))
         plt.subplot(3, 1, 1)
         plt.title('Best val accuracy vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Best val accuracy')
         plt.semilogx(weight_scales, best_val_accs, '-o', label='baseline')
         plt.semilogx(weight_scales, bn_best_val_accs, '-o', label='batchnorm')
         plt.legend(ncol=2, loc='lower right')
         plt.subplot(3, 1, 2)
         plt.title('Best train accuracy vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Best training accuracy')
         plt.semilogx(weight_scales, best_train_accs, '-o', label='baseline')
         plt.semilogx(weight_scales, bn_best_train_accs, '-o', label='batchnorm')
         plt.legend()
         plt.subplot(3, 1, 3)
         plt.title('Final training loss vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Final training loss')
```

Running weight scale 1 / 20 Running weight scale 2 / 20 Running weight scale 3 / 20

```
plt.semilogx(weight_scales, final_train_loss, '-o', label='baseline')
plt.semilogx(weight_scales, bn_final_train_loss, '-o', label='batchnorm')
plt.legend()

plt.gcf().set_size_inches(10, 15)
plt.show()
```



Question:

In the cell below, summarize the findings of this experiment, and WHY these results make sense.

Answer:

This experiment found that batchnorm yielded consistently high performance across all weight initialization scales in terms of training and validation accuracy relative to that of the baseline. Under the baseline, only weight initialization scales on the order of 1e-1 produced relatively high training and validation accuracies. However, relatively high weight initialization scales of an order higher than 1e-1 yielded very high final training loss under the baseline compared to batchnorm, which had relatively low final training loss across all weight initialization scales.

These results make sense because under the baseline, weights initialized to be very small are likely to yield vanishing gradients whereas weights initialized to be very large are likely to yield exploding gradients, both of which are undesirable for learning. However, batchnorm normalizes the activations, which reduces the probability that the initial weights lead to the vanishing gradient or exploding gradient problem.

In []:

Dropout

In this notebook, you will implement dropout. Then we will ask you to train a network with batchnorm and dropout, and acheive over 55% accuracy on CIFAR-10.

Utils has a solid API for building these modular frameworks and training them, and we will use this very well implemented framework as opposed to "reinventing the wheel." This includes using the Solver, various utility functions, and the layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils.

```
In [1]: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc_net import *
        from nndl.layers import *
        from utils.data_utils import get_CIFAR10_data
        from utils gradient check import eval numerical gradient, eval numerical gra
        from utils.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload—of—modules—in—ip
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
            """ returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
In [2]: # Load the (preprocessed) CIFAR10 data.
        data = get_CIFAR10_data()
        for k in data.keys():
            print('{}: {} '.format(k, data[k].shape))
        X_train: (49000, 3, 32, 32)
        y_train: (49000,)
        X_val: (1000, 3, 32, 32)
        y_val: (1000,)
        X_test: (1000, 3, 32, 32)
        y_test: (1000,)
```

Dropout forward pass

Implement the training and test time dropout forward pass, dropout_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [4]: x = np.random.randn(500, 500) + 10
        for p in [0.3, 0.6, 0.75]:
            out, _ = dropout_forward(x, {'mode': 'train', 'p': p})
            out test, = dropout forward(x, {'mode': 'test', 'p': p})
            print('Running tests with p = ', p)
            print('Mean of input: ', x.mean())
            print('Mean of train-time output: ', out.mean())
            print('Mean of test-time output: ', out_test.mean())
            print('Fraction of train-time output set to zero: ', (out == 0).mean())
            print('Fraction of test-time output set to zero: ', (out_test == 0).mean
        Running tests with p = 0.3
        Mean of input: 9.9976709985351
        Mean of train-time output: 9.995032766882039
        Mean of test-time output: 9.9976709985351
        Fraction of train-time output set to zero: 0.700028
        Fraction of test-time output set to zero: 0.0
        Running tests with p = 0.6
        Mean of input: 9.9976709985351
        Mean of train-time output: 10.003660038043275
        Mean of test-time output: 9.9976709985351
        Fraction of train-time output set to zero: 0.399596
        Fraction of test-time output set to zero: 0.0
        Running tests with p = 0.75
        Mean of input: 9.9976709985351
        Mean of train-time output: 10.00486024842261
        Mean of test-time output: 9.9976709985351
        Fraction of train-time output set to zero: 0.249448
        Fraction of test-time output set to zero: 0.0
```

Dropout backward pass

Implement the backward pass, dropout_backward, in nndl/layers.py. After that, test your gradients by running the following cell:

```
In [22]: x = np.random.randn(10, 10) + 10
    dout = np.random.randn(*x.shape)

dropout_param = {'mode': 'train', 'p': 0.8, 'seed': 123}
    out, cache = dropout_forward(x, dropout_param)
    dx = dropout_backward(dout, cache)
    dx_num = eval_numerical_gradient_array(lambda xx: dropout_forward(xx, dropout_print('dx relative error: ', rel_error(dx, dx_num))
```

dx relative error: 1.8928966102396944e-11

Implement a fully connected neural network with dropout layers

Modify the FullyConnectedNet() class in nndl/fc_net.py to incorporate dropout. A dropout layer should be incorporated after every ReLU layer. Concretely, there shouldn't be a dropout at the output layer since there is no ReLU at the output layer. You will need to modify the class in the following areas:

- (1) In the forward pass, you will need to incorporate a dropout layer after every relu layer.
- (2) In the backward pass, you will need to incorporate a dropout backward pass layer.

Check your implementation by running the following code. Our W1 gradient relative error is on the order of 1e-6 (the largest of all the relative errors).

```
Running check with dropout = 0.5
Initial loss: 2.2978802381633017
W1 relative error: 1.4081197369269403e-06
W2 relative error: 2.2537390539486822e-08
W3 relative error: 4.1035828818284274e-08
b1 relative error: 3.000879905168748e-08
b2 relative error: 1.154024377991818e-09
b3 relative error: 1.2912061432212848e-10
Running check with dropout = 0.75
Initial loss: 2.308234140616203
W1 relative error: 2.645337556327138e-07
W2 relative error: 1.307018869954109e-07
W3 relative error: 2.223975024199031e-07
b1 relative error: 7.112910491659821e-09
b2 relative error: 5.347954426078734e-09
b3 relative error: 1.0886215791527195e-10
Running check with dropout = 1.0
Initial loss: 2.3066226083055312
W1 relative error: 2.998747146522704e-07
W2 relative error: 5.530329163457634e-07
W3 relative error: 8.243368321653801e-08
b1 relative error: 1.5773080094048574e-08
b2 relative error: 6.468789175991833e-09
b3 relative error: 1.223192314770519e-10
```

Dropout as a regularizer

In class, we claimed that dropout acts as a regularizer by effectively bagging. To check this, we will train two small networks, one with dropout and one without dropout.

```
optim_config={
     'learning_rate': 5e-4,
},
     verbose=True, print_every=100)
solver.train()
solvers[dropout] = solver
```

```
(Iteration 1 / 125) loss: 2.300199
(Epoch 0 / 25) train acc: 0.158000; val acc: 0.127000
(Epoch 1 / 25) train acc: 0.132000; val acc: 0.121000
(Epoch 2 / 25) train acc: 0.204000; val_acc: 0.170000
(Epoch 3 / 25) train acc: 0.240000; val_acc: 0.192000
(Epoch 4 / 25) train acc: 0.312000; val_acc: 0.274000
(Epoch 5 / 25) train acc: 0.314000; val acc: 0.269000
(Epoch 6 / 25) train acc: 0.364000; val_acc: 0.252000
(Epoch 7 / 25) train acc: 0.390000; val acc: 0.281000
(Epoch 8 / 25) train acc: 0.386000; val_acc: 0.290000
(Epoch 9 / 25) train acc: 0.372000; val_acc: 0.267000
(Epoch 10 / 25) train acc: 0.424000; val acc: 0.286000
(Epoch 11 / 25) train acc: 0.396000; val acc: 0.275000
(Epoch 12 / 25) train acc: 0.458000; val acc: 0.299000
(Epoch 13 / 25) train acc: 0.496000; val acc: 0.305000
(Epoch 14 / 25) train acc: 0.492000; val_acc: 0.299000
(Epoch 15 / 25) train acc: 0.550000; val_acc: 0.296000
(Epoch 16 / 25) train acc: 0.584000; val_acc: 0.297000
(Epoch 17 / 25) train acc: 0.582000; val acc: 0.309000
(Epoch 18 / 25) train acc: 0.614000; val_acc: 0.306000
(Epoch 19 / 25) train acc: 0.626000; val_acc: 0.325000
(Epoch 20 / 25) train acc: 0.610000; val acc: 0.322000
(Iteration 101 / 125) loss: 1.364906
(Epoch 21 / 25) train acc: 0.648000; val_acc: 0.328000
(Epoch 22 / 25) train acc: 0.704000; val acc: 0.337000
(Epoch 23 / 25) train acc: 0.684000; val acc: 0.299000
(Epoch 24 / 25) train acc: 0.748000; val_acc: 0.299000
(Epoch 25 / 25) train acc: 0.760000; val acc: 0.329000
(Iteration 1 / 125) loss: 2.300607
(Epoch 0 / 25) train acc: 0.172000; val_acc: 0.167000
(Epoch 1 / 25) train acc: 0.210000; val acc: 0.197000
(Epoch 2 / 25) train acc: 0.284000; val acc: 0.240000
(Epoch 3 / 25) train acc: 0.302000; val_acc: 0.246000
(Epoch 4 / 25) train acc: 0.392000; val acc: 0.289000
(Epoch 5 / 25) train acc: 0.420000; val_acc: 0.274000
(Epoch 6 / 25) train acc: 0.420000; val_acc: 0.304000
(Epoch 7 / 25) train acc: 0.474000; val acc: 0.293000
(Epoch 8 / 25) train acc: 0.516000; val acc: 0.330000
(Epoch 9 / 25) train acc: 0.566000; val_acc: 0.322000
(Epoch 10 / 25) train acc: 0.620000; val_acc: 0.321000
(Epoch 11 / 25) train acc: 0.656000; val acc: 0.317000
(Epoch 12 / 25) train acc: 0.676000; val_acc: 0.319000
(Epoch 13 / 25) train acc: 0.680000; val_acc: 0.304000
(Epoch 14 / 25) train acc: 0.752000; val acc: 0.323000
(Epoch 15 / 25) train acc: 0.802000; val_acc: 0.321000
(Epoch 16 / 25) train acc: 0.804000; val_acc: 0.300000
(Epoch 17 / 25) train acc: 0.868000; val_acc: 0.303000
(Epoch 18 / 25) train acc: 0.894000; val_acc: 0.298000
(Epoch 19 / 25) train acc: 0.910000; val_acc: 0.282000
(Epoch 20 / 25) train acc: 0.926000; val acc: 0.316000
(Iteration 101 / 125) loss: 0.245816
(Epoch 21 / 25) train acc: 0.950000; val_acc: 0.282000
(Epoch 22 / 25) train acc: 0.958000; val acc: 0.292000
(Epoch 23 / 25) train acc: 0.966000; val_acc: 0.307000
(Epoch 24 / 25) train acc: 0.966000; val_acc: 0.285000
(Epoch 25 / 25) train acc: 0.970000; val acc: 0.284000
```

```
In [33]: # Plot train and validation accuracies of the two models
          train_accs = []
          val accs = []
          for dropout in dropout_choices:
               solver = solvers[dropout]
               train_accs.append(solver.train_acc_history[-1])
               val_accs.append(solver.val_acc_history[-1])
          plt.subplot(3, 1, 1)
          for dropout in dropout_choices:
               plt.plot(solvers[dropout].train_acc_history, 'o', label='%.2f dropout' %
          plt.title('Train accuracy')
          plt.xlabel('Epoch')
          plt.ylabel('Accuracy')
          plt.legend(ncol=2, loc='lower right')
          plt.subplot(3, 1, 2)
          for dropout in dropout_choices:
               plt.plot(solvers[dropout].val_acc_history, 'o', label='%.2f dropout' % d
          plt.title('Val accuracy')
          plt.xlabel('Epoch')
          plt.ylabel('Accuracy')
          plt.legend(ncol=2, loc='lower right')
          plt.gcf().set_size_inches(15, 15)
          plt.show()
                                                   Train accuracy
            1.0
            0.8
           Accuracy
90
            0.4
            0.2

    0.60 dropout

    1.00 dropout

                                               10
                                                              15
                                                                             20
                                                                                            25
                                                      Epoch
                                                    Val accuracy
            0.30
            0.25
            0.20
            0.15

    0.60 dropout

    1.00 dropout
```

Epoch

20

Based off the results of this experiment, is dropout performing regularization? Explain your answer.

Answer:

Yes, dropout is performing regularization. This is evident by the fact that the training accuracy suffers slightly from the use of dropout, but in return, we get slightly better validation accuracy compared to the model with no dropout.

Final part of the assignment

Get over 55% validation accuracy on CIFAR-10 by using the layers you have implemented. You will be graded according to the following equation:

min(floor((X - 32%)) / 23%, 1) where if you get 55% or higher validation accuracy, you get full points.

```
In [49]: # ========== #
      # YOUR CODE HERE:
      # Implement a FC-net that achieves at least 55% validation accuracy
         on CIFAR-10.
      # ================== #
      model = FullyConnectedNet([100, 100, 100], dropout=0.99,
                         use_batchnorm=True, reg=1e-5)
      solver = Solver(model, data,
                  num_epochs=10, batch_size=100,
                  update_rule='adam',
                  optim config={
                   'learning_rate': 1e-4,
                  verbose=True, print_every=100)
      solver.train()
      # END YOUR CODE HERE
```

```
(Iteration 1 / 4900) loss: 2.289912
(Epoch 0 / 10) train acc: 0.115000; val acc: 0.117000
(Iteration 101 / 4900) loss: 2.027195
(Iteration 201 / 4900) loss: 1.874044
(Iteration 301 / 4900) loss: 1.882009
(Iteration 401 / 4900) loss: 1.601869
(Epoch 1 / 10) train acc: 0.469000; val acc: 0.436000
(Iteration 501 / 4900) loss: 1.583314
(Iteration 601 / 4900) loss: 1.653589
(Iteration 701 / 4900) loss: 1.640116
(Iteration 801 / 4900) loss: 1.402864
(Iteration 901 / 4900) loss: 1.609703
(Epoch 2 / 10) train acc: 0.524000; val acc: 0.485000
(Iteration 1001 / 4900) loss: 1.350662
(Iteration 1101 / 4900) loss: 1.433051
(Iteration 1201 / 4900) loss: 1.371278
(Iteration 1301 / 4900) loss: 1.488934
(Iteration 1401 / 4900) loss: 1.427736
(Epoch 3 / 10) train acc: 0.540000; val acc: 0.508000
(Iteration 1501 / 4900) loss: 1.365833
(Iteration 1601 / 4900) loss: 1.378152
(Iteration 1701 / 4900) loss: 1.283176
(Iteration 1801 / 4900) loss: 1.343043
(Iteration 1901 / 4900) loss: 1.452351
(Epoch 4 / 10) train acc: 0.580000; val acc: 0.529000
(Iteration 2001 / 4900) loss: 1.145698
(Iteration 2101 / 4900) loss: 1.210495
(Iteration 2201 / 4900) loss: 1.128914
(Iteration 2301 / 4900) loss: 1.373991
(Iteration 2401 / 4900) loss: 1.313390
(Epoch 5 / 10) train acc: 0.574000; val acc: 0.540000
(Iteration 2501 / 4900) loss: 1.170701
(Iteration 2601 / 4900) loss: 1.001182
(Iteration 2701 / 4900) loss: 1.289521
(Iteration 2801 / 4900) loss: 1.152426
(Iteration 2901 / 4900) loss: 1.068520
(Epoch 6 / 10) train acc: 0.614000; val acc: 0.550000
(Iteration 3001 / 4900) loss: 1.133227
(Iteration 3101 / 4900) loss: 1.184040
(Iteration 3201 / 4900) loss: 1.234521
(Iteration 3301 / 4900) loss: 1.274944
(Iteration 3401 / 4900) loss: 1.029058
(Epoch 7 / 10) train acc: 0.632000; val acc: 0.555000
(Iteration 3501 / 4900) loss: 1.178873
(Iteration 3601 / 4900) loss: 1.092318
(Iteration 3701 / 4900) loss: 1.145423
(Iteration 3801 / 4900) loss: 1.071261
(Iteration 3901 / 4900) loss: 1.051557
(Epoch 8 / 10) train acc: 0.608000; val acc: 0.565000
(Iteration 4001 / 4900) loss: 1.137239
(Iteration 4101 / 4900) loss: 1.122638
(Iteration 4201 / 4900) loss: 0.911974
(Iteration 4301 / 4900) loss: 1.068114
(Iteration 4401 / 4900) loss: 1.089357
(Epoch 9 / 10) train acc: 0.639000; val acc: 0.551000
(Iteration 4501 / 4900) loss: 1.445532
```

```
(Iteration 4701 / 4900) loss: 0.911822
(Iteration 4801 / 4900) loss: 1.057591
(Epoch 10 / 10) train acc: 0.673000; val_acc: 0.560000

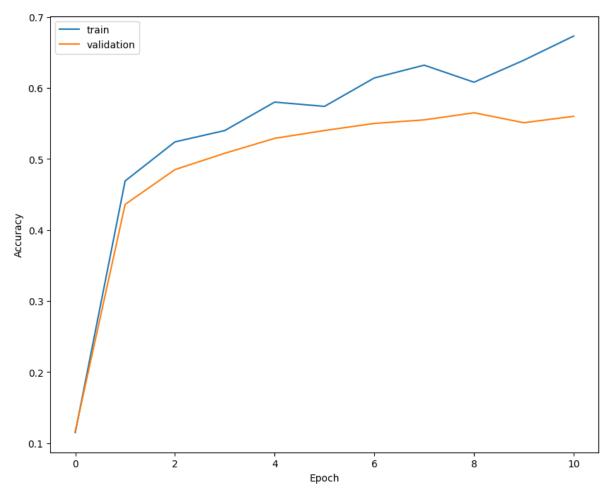
In [50]: t1 = np.arange(len(solver.train_acc_history))
    y1 = solver.train_acc_history

    t2 = np.arange(len(solver.val_acc_history))
    y2 = solver.val_acc_history

plt.plot(t1, y1, label='train')
    plt.plot(t2, y2, label='validation')
    plt.xlabel('Epoch')
    plt.ylabel('Accuracy')
    plt.legend()
```

Out[50]: <matplotlib.legend.Legend at 0x125323b80>

(Iteration 4601 / 4900) loss: 1.246745



```
In []:
```