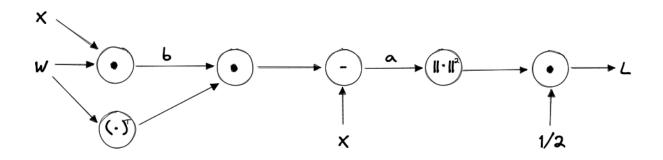
(a) The loss is defined as proportional to the difference between $\mathbf{W}^T\mathbf{W}\mathbf{x}$ and \mathbf{x} . We can think of $\mathbf{W}\mathbf{x}$ as bringing \mathbf{x} down to a much lower dimensional space, then $\mathbf{W}^T\mathbf{W}\mathbf{x}$ as bringing that back to the original dimensionality. Thus, if we minimize this loss function, then $\mathbf{W}\mathbf{x}$ should preserve information about \mathbf{x} in order to minimize the difference between the reconstituted vector and the original vector.

(b) The computational graph for \mathcal{L} is as follows:



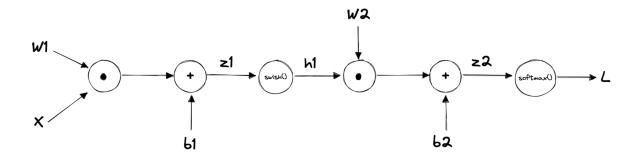
(c) By the law of total derivatives, the individual gradients of each path to \mathbf{W} should be summed together. That is, if we let $\mathbf{a} = \mathbf{W}^T \mathbf{W} \mathbf{x} - \mathbf{x}$, then $\nabla_{\mathbf{W}} \mathcal{L} = \frac{\partial \mathbf{W} \mathbf{x}}{\partial \mathbf{W}} \frac{\partial \mathbf{a}}{\partial \mathbf{W} \mathbf{x}} \frac{\partial \mathcal{L}}{\partial \mathbf{a}} + \frac{\partial \mathbf{W}^T}{\partial \mathbf{W}} \frac{\partial \mathbf{a}}{\partial \mathbf{W}^T} \frac{\partial \mathbf{a}}{\partial \mathbf{a}}$.

(d) Let $\mathcal{L} = \frac{1}{2}||\mathbf{W}^T\mathbf{W}\mathbf{x} - \mathbf{x}||^2$. Also, let $\mathbf{a} = \mathbf{W}^T\mathbf{W}\mathbf{x} - \mathbf{x}$ and $\mathbf{b} = \mathbf{W}\mathbf{x}$.

$$\begin{split} \frac{\partial \mathcal{L}}{\partial \mathbf{a}} &= \mathbf{a} \\ \frac{\partial \mathcal{L}}{\partial \mathbf{W}^T} &= \frac{\partial \mathbf{a}}{\partial \mathbf{W}^T} \frac{\partial \mathcal{L}}{\partial \mathbf{a}} = \mathbf{a} (\mathbf{W} \mathbf{x})^T \\ \frac{\partial \mathcal{L}}{\partial \mathbf{W}_{\text{path 1}}} &= \mathbf{W} \mathbf{x} \mathbf{a}^T \\ \frac{\partial \mathcal{L}}{\partial \mathbf{b}} &= \frac{\partial \mathbf{a}}{\partial \mathbf{b}} \frac{\partial \mathcal{L}}{\partial \mathbf{a}} = \mathbf{W} \mathbf{a} \\ \frac{\partial \mathcal{L}}{\partial \mathbf{b}} &= \frac{\partial \mathbf{b}}{\partial \mathbf{b}} \frac{\partial \mathcal{L}}{\partial \mathbf{a}} = \mathbf{W} \mathbf{a} \\ \frac{\partial \mathcal{L}}{\partial \mathbf{W}_{\text{path 2}}} &= \frac{\partial \mathbf{b}}{\partial \mathbf{W}} \frac{\partial \mathcal{L}}{\partial \mathbf{b}} = \mathbf{W} \mathbf{a} \mathbf{x}^T \\ \nabla_{\mathbf{W}} \mathcal{L} &= \mathbf{W} \mathbf{a} \mathbf{x}^T + \mathbf{W} \mathbf{x} \mathbf{a}^T \\ &= \mathbf{W} (\mathbf{W}^T \mathbf{W} \mathbf{x} - \mathbf{x}) \mathbf{x}^T + \mathbf{W} \mathbf{x} (\mathbf{W}^T \mathbf{W} \mathbf{x} - \mathbf{x})^T \end{split}$$

I am a C147 student.

(a) The computational graph for L is as follows:



(b) Assume we already know $\frac{\partial L}{\partial z_2}$.

We know that $z_2 = W_2 h_1 + b_2$. We can first backpropagate to b_2 , which is a simple addition operation. Therefore, $\nabla_{b_2} L = \frac{\partial z_2}{\partial b_2} = \frac{\partial L}{\partial z_2}$. This also means that $\frac{\partial L}{\partial W_2 h_1} = \frac{\partial L}{\partial z_2}$.

Then, we can backpropagate $\frac{\partial L}{\partial z_2}$ to W_2h_1 . Using the derivation from class, we know that $\frac{\partial L}{\partial W_2} = \frac{\partial W_2h_1}{\partial W_2} \frac{\partial L}{\partial W_2h_1} = \frac{\partial L}{\partial z_2}h_1^T$.

In summary, using backpropagation, we derive the gradients

$$\nabla_{b_2} L = \frac{\partial L}{\partial z_2},$$

$$\nabla_{W_2} L = \frac{\partial L}{\partial z_2} h_1^T.$$

(c) Continuing off from part (b), we can backpropagate $\frac{\partial L}{\partial z_2}$ to W_2h_1 , where if we use the derivation from class, we know that $\frac{\partial L}{\partial h_1} = \frac{\partial W_2h_1}{\partial h_1} \frac{\partial L}{\partial W_2h_1} = W_2^T \frac{\partial L}{\partial z_2}$.

 h_1 is defined as being equal to $\text{Swish}(z_1)$, where for a neuron $z \in z_1$, $\text{Swish}(z) = z\sigma(z)$. Then, $\frac{d}{dz}\text{Swish}(z) = \frac{d}{dz}z\sigma(z) = \sigma(z) + z\frac{d\sigma(z)}{z} = \sigma(z) + z\sigma(z)(1-\sigma(z)) = \text{Swish}(z) + \sigma(z)(1-\text{Swish}(z))$. Therefore, $\frac{\partial h_1}{\partial z_1} = \text{Swish}(z_1) + \sigma(z_1)(1-\text{Swish}(z_1))$, and $\frac{\partial L}{\partial z_1} = \frac{\partial h_1}{\partial z_1}\frac{\partial L}{\partial h_1} = \frac{\partial h_1}{\partial z_1}W_2^T\frac{\partial L}{\partial z_2}$.

We know that $z_1 = W_1 x + b_1$, so $\frac{\partial L}{\partial b_1} = \frac{\partial z_1}{\partial b_1} \frac{\partial L}{\partial z_1} = \frac{\partial L}{\partial z_1}$. This also means that $\frac{\partial L}{\partial W_1 x} = \frac{\partial L}{\partial z_1}$.

Finally, we can backpropagate $\frac{\partial L}{\partial z_1}$ to $W_1 x$. Using the derivation from class, we know that $\frac{\partial L}{\partial W_1} = \frac{\partial W_1 x}{\partial W_1 x} = \frac{\partial L}{\partial Z_1} x^T$.

In summary, using backpropagation we derive the gradients

$$\begin{split} \nabla_{b_1} L &= \frac{\partial L}{\partial z_1}, \\ \nabla_{W_1} L &= \frac{\partial L}{\partial z_1} x^T, \text{ where} \\ &\frac{\partial L}{\partial z_1} = \left[\text{Swish}(z_1) + \sigma(z_1) (1 - \text{Swish}(z_1)) \right] \odot W_2^T \frac{\partial L}{\partial z_2}. \end{split}$$

```
neural_net.py:
import numpy as np
import matplotlib.pyplot as plt
class TwoLayerNet(object):
  A two-layer fully-connected neural network. The net has an input dimension of
  D, a hidden layer dimension of H, and performs classification over C classes.
  We train the network with a softmax loss function and L2 regularization on the
  weight matrices. The network uses a ReLU nonlinearity after the first fully
  connected layer.
  In other words, the network has the following architecture:
  input - fully connected layer - ReLU - fully connected layer - softmax
  The outputs of the second fully-connected layer are the scores for each class.
  def __init__(self, input_size, hidden_size, output_size, std=1e-4):
    Initialize the model. Weights are initialized to small random values and
    biases are initialized to zero. Weights and biases are stored in the
   variable self.params, which is a dictionary with the following keys:
    W1: First layer weights; has shape (H, D)
    b1: First layer biases; has shape (H,)
    W2: Second layer weights; has shape (C, H)
   b2: Second layer biases; has shape (C,)
   Inputs:
    - input_size: The dimension D of the input data.
    - hidden_size: The number of neurons H in the hidden layer.
    - output_size: The number of classes C.
    11 11 11
   self.params = {}
   self.params['W1'] = std * np.random.randn(hidden_size, input_size)
    self.params['b1'] = np.zeros(hidden_size)
    self.params['W2'] = std * np.random.randn(output_size, hidden_size)
    self.params['b2'] = np.zeros(output_size)
  def loss(self, X, y=None, reg=0.0):
    Compute the loss and gradients for a two layer fully connected neural
    network.
   Inputs:
    - X: Input data of shape (N, D). Each X[i] is a training sample.
    - y: Vector of training labels. y[i] is the label for X[i], and each y[i] is
```

```
an integer in the range 0 \le y[i] \le C. This parameter is optional; if it
 is not passed then we only return scores, and if it is passed then we
 instead return the loss and gradients.
- reg: Regularization strength.
Returns:
If y is None, return a matrix scores of shape (N, C) where scores[i, c] is
the score for class c on input X[i].
If y is not None, instead return a tuple of:
- loss: Loss (data loss and regularization loss) for this batch of training
 samples.
- grads: Dictionary mapping parameter names to gradients of those parameters
 with respect to the loss function; has the same keys as self.params.
# Unpack variables from the params dictionary
W1, b1 = self.params['W1'], self.params['b1']
W2, b2 = self.params['W2'], self.params['b2']
N, D = X.shape
# Compute the forward pass
scores = None
# ----- #
# YOUR CODE HERE:
  Calculate the output scores of the neural network. The result
  should be (N, C). As stated in the description for this class,
  there should not be a ReLU layer after the second FC layer.
  The output of the second FC layer is the output scores. Do not
  use a for loop in your implementation.
# ----- #
relu_out = np.maximum(0, (X @ W1.T + b1))
scores = relu_out @ W2.T + b2
# ----- #
# END YOUR CODE HERE
# ------ #
# If the targets are not given then jump out, we're done
if y is None:
 return scores
# Compute the loss
loss = None
# ========== #
# YOUR CODE HERE:
# Calculate the loss of the neural network. This includes the
# softmax loss and the L2 regularization for W1 and W2. Store the
# total loss in teh variable loss. Multiply the regularization
# loss by 0.5 (in addition to the factor reg).
```

```
# scores is num_examples by num_classes
 scores_exp = np.exp(scores)
 probs = scores_exp / np.sum(scores_exp, axis=1, keepdims=True)
 loss = -np.sum(np.log(probs[np.arange(N), y])) / N
 loss += 0.5*reg*(np.sum(W1**2) + np.sum(W2**2))
 # END YOUR CODE HERE
 # ========== #
 grads = {}
 # ----- #
 # YOUR CODE HERE:
 # Implement the backward pass. Compute the derivatives of the
 # weights and the biases. Store the results in the grads
   dictionary. e.g., grads['W1'] should store the gradient for
 # W1, and be of the same size as W1.
 # ----- #
 # A is the (N x C) matrix of activations i.e. the outputs of the second FC layer
 dLdA = probs
 dLdA[np.arange(N), y] -= 1
 dLdA /= N
 grads['W2'] = dLdA.T @ relu_out + reg*W2
 grads['b2'] = np.sum(dLdA, axis=0)
 # B is the (N x H) matrix output of the first FC layer
 dLdB = (X @ W1.T > 0) * (dLdA @ W2)
 grads['W1'] = dLdB.T @ X + reg*W1
 grads['b1'] = np.sum(dLdB, axis=0)
 # ----- #
 # END YOUR CODE HERE
 return loss, grads
def train(self, X, y, X_val, y_val,
        learning_rate=1e-3, learning_rate_decay=0.95,
        reg=1e-5, num_iters=100,
        batch_size=200, verbose=False):
 .....
 Train this neural network using stochastic gradient descent.
 Inputs:
 - X: A numpy array of shape (N, D) giving training data.
 - y: A numpy array f shape (N,) giving training labels; y[i] = c means that
  X[i] has label c, where 0 \le c \le C.
 - X_val: A numpy array of shape (N_val, D) giving validation data.
 - y_val: A numpy array of shape (N_val,) giving validation labels.
 - learning_rate: Scalar giving learning rate for optimization.
```

```
- learning_rate_decay: Scalar giving factor used to decay the learning rate
 after each epoch.
- reg: Scalar giving regularization strength.
- num_iters: Number of steps to take when optimizing.
- batch_size: Number of training examples to use per step.
- verbose: boolean; if true print progress during optimization.
num_train = X.shape[0]
iterations_per_epoch = max(num_train / batch_size, 1)
# Use SGD to optimize the parameters in self.model
loss_history = []
train_acc_history = []
val_acc_history = []
for it in np.arange(num_iters):
 X_batch = None
 y_batch = None
 # YOUR CODE HERE:
 # Create a minibatch by sampling batch_size samples randomly.
 # ------ #
 batch_indices = np.random.choice(np.arange(num_train), size=batch_size, replace=True)
 X_batch = X[batch_indices]
 y_batch = y[batch_indices]
 # ------ #
 # END YOUR CODE HERE
 # Compute loss and gradients using the current minibatch
 loss, grads = self.loss(X_batch, y=y_batch, reg=reg)
 loss_history.append(loss)
 # YOUR CODE HERE:
 # Perform a gradient descent step using the minibatch to update
 # all parameters (i.e., W1, W2, b1, and b2).
 for p in self.params:
    self.params[p] -= learning_rate * grads[p]
 # ------ #
 # END YOUR CODE HERE
 if verbose and it % 100 == 0:
  print('iteration {} / {}: loss {}'.format(it, num_iters, loss))
 # Every epoch, check train and val accuracy and decay learning rate.
 if it % iterations_per_epoch == 0:
```

```
# Check accuracy
    train_acc = (self.predict(X_batch) == y_batch).mean()
    val_acc = (self.predict(X_val) == y_val).mean()
    train_acc_history.append(train_acc)
    val_acc_history.append(val_acc)
    # Decay learning rate
    learning_rate *= learning_rate_decay
 return {
   'loss_history': loss_history,
   'train_acc_history': train_acc_history,
   'val_acc_history': val_acc_history,
 }
def predict(self, X):
 Use the trained weights of this two-layer network to predict labels for
 data points. For each data point we predict scores for each of the C
 classes, and assign each data point to the class with the highest score.
 Inputs:
 - X: A numpy array of shape (N, D) giving N D-dimensional data points to
   classify.
 Returns:
 - y_pred: A numpy array of shape (N,) giving predicted labels for each of
   the elements of X. For all i, y_pred[i] = c means that X[i] is predicted
   to have class c, where 0 \le c < C.
 y_pred = None
 # YOUR CODE HERE:
 # Predict the class given the input data.
 relu_out = np.maximum(0, (X @ self.params['W1'].T) + self.params['b1'])
 scores = (relu_out @ self.params['W2'].T) + self.params['b2']
 y_pred = np.argmax(scores, axis=1)
 # ----- #
 # END YOUR CODE HERE
 return y_pred
```

This is the 2-layer neural network notebook for ECE C147/C247 Homework #3

Please follow the notebook linearly to implement a two layer neural network.

Please print out the notebook entirely when completed.

The goal of this notebook is to give you experience with training a two layer neural network.

```
import random
import numpy as np
from utils.data_utils import load_CIFAR10
import matplotlib.pyplot as plt

%matplotlib inline
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

Toy example

Before loading CIFAR-10, there will be a toy example to test your implementation of the forward and backward pass. Make sure to read the description of TwoLayerNet class in neural_net.py file, understand the architecture and initializations

```
In [11]: from nndl.neural_net import TwoLayerNet

In [12]: # Create a small net and some toy data to check your implementations.
# Note that we set the random seed for repeatable experiments.

input_size = 4
hidden_size = 10
num_classes = 3
num_inputs = 5

def init_toy_model():
    np.random.seed(0)
    return TwoLayerNet(input_size, hidden_size, num_classes, std=1e-1)

def init_toy_data():
    np.random.seed(1)
    X = 10 * np.random.randn(num_inputs, input_size)
    y = np.array([0, 1, 2, 2, 1])
    return X, y
```

```
net = init_toy_model()
X, y = init_toy_data()
```

Compute forward pass scores

```
In [13]: ## Implement the forward pass of the neural network.
         ## See the loss() method in TwoLayerNet class for the same
         # Note, there is a statement if y is None: return scores, which is why
         # the following call will calculate the scores.
         scores = net.loss(X)
         print('Your scores:')
         print(scores)
         print()
         print('correct scores:')
         correct_scores = np.asarray([
             [-1.07260209, 0.05083871, -0.87253915],
             [-2.02778743, -0.10832494, -1.52641362],
              [-0.74225908, 0.15259725, -0.39578548],
              [-0.38172726, 0.10835902, -0.17328274],
              [-0.64417314, -0.18886813, -0.41106892]])
         print(correct scores)
         print()
         # The difference should be very small. We get < 1e-7
         print('Difference between your scores and correct scores:')
         print(np.sum(np.abs(scores - correct_scores)))
         Your scores:
         [[-1.07260209 0.05083871 -0.87253915]
          [-2.02778743 -0.10832494 -1.52641362]
          [-0.74225908 0.15259725 -0.39578548]
          [-0.38172726 \quad 0.10835902 \quad -0.17328274]
          [-0.64417314 - 0.18886813 - 0.41106892]]
         correct scores:
          [[-1.07260209 \quad 0.05083871 \quad -0.87253915]
          [-2.02778743 -0.10832494 -1.52641362]
          [-0.74225908 0.15259725 -0.39578548]
          [-0.38172726 \quad 0.10835902 \quad -0.17328274]
          [-0.64417314 -0.18886813 -0.41106892]]
         Difference between your scores and correct scores:
         3.381231197113754e-08
```

Forward pass loss

```
In [14]: loss, _ = net.loss(X, y, reg=0.05)
    correct_loss = 1.071696123862817

# should be very small, we get < 1e-12
    print("Loss:",loss)
    print('Difference between your loss and correct loss:')
    print(np.sum(np.abs(loss - correct_loss)))</pre>
```

```
Loss: 1.071696123862817

Difference between your loss and correct loss: 0.0
```

Backward pass

Implements the backwards pass of the neural network. Check your gradients with the gradient check utilities provided.

```
In [15]: from utils.gradient_check import eval_numerical_gradient

# Use numeric gradient checking to check your implementation of the backward
# If your implementation is correct, the difference between the numeric and
# analytic gradients should be less than 1e-8 for each of W1, W2, b1, and b2

loss, grads = net.loss(X, y, reg=0.05)

# these should all be less than 1e-8 or so
for param_name in grads:
    f = lambda W: net.loss(X, y, reg=0.05)[0]
    param_grad_num = eval_numerical_gradient(f, net.params[param_name], vert
    print('{} max relative error: {}'.format(param_name, rel_error(param_gra))

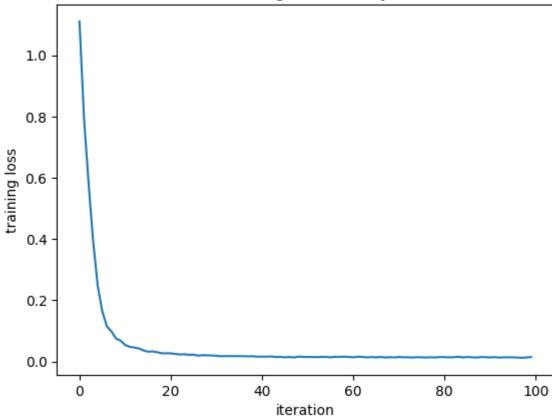
W2 max relative error: 2.9632233460136427e-10
b2 max relative error: 1.2482624742512528e-09
W1 max relative error: 1.283285235125835e-09
b1 max relative error: 3.172680285697327e-09
```

Training the network

Implement neural_net.train() to train the network via stochastic gradient descent, much like the softmax and SVM.

Final training loss: 0.014498902952971663

Training Loss history



Classify CIFAR-10

Do classification on the CIFAR-10 dataset.

```
In [17]: from utils.data_utils import load_CIFAR10
         def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=1000)
              Load the CIFAR-10 dataset from disk and perform preprocessing to prepare
              it for the two-layer neural net classifier.
              # Load the raw CIFAR-10 data
              cifar10_dir = '../hw2/cifar-10-batches-py'
              X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
              # Subsample the data
              mask = list(range(num_training, num_training + num_validation))
              X_{val} = X_{train[mask]}
              y_val = y_train[mask]
              mask = list(range(num_training))
              X_{train} = X_{train}[mask]
              y_train = y_train[mask]
              mask = list(range(num_test))
              X_{\text{test}} = X_{\text{test}}[mask]
              y_test = y_test[mask]
```

```
# Normalize the data: subtract the mean image
    mean_image = np.mean(X_train, axis=0)
    X train -= mean image
    X_val == mean_image
    X_test -= mean_image
    # Reshape data to rows
    X train = X train.reshape(num training, -1)
    X val = X val.reshape(num validation, -1)
    X_test = X_test.reshape(num_test, -1)
    return X_train, y_train, X_val, y_val, X_test, y_test
# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
Train data shape: (49000, 3072)
```

Train data shape: (49000, 3072)
Train labels shape: (49000,)
Validation data shape: (1000, 3072)
Validation labels shape: (1000,)
Test data shape: (1000, 3072)
Test labels shape: (1000,)

Running SGD

If your implementation is correct, you should see a validation accuracy of around 28-29%.

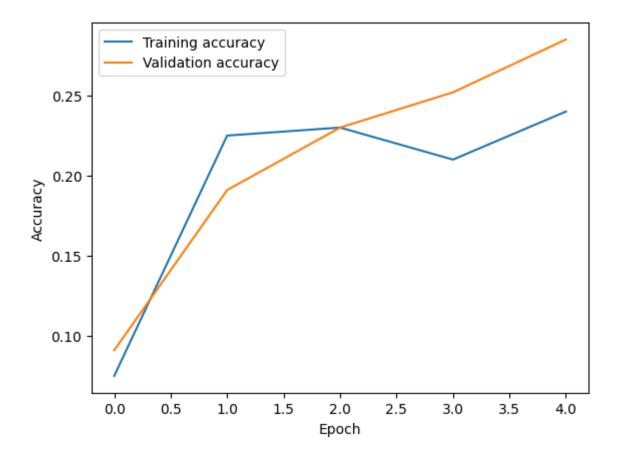
```
iteration 0 / 1000: loss 2.302757518613176
iteration 100 / 1000: loss 2.302120159207236
iteration 200 / 1000: loss 2.2956136007408703
iteration 300 / 1000: loss 2.2518259043164135
iteration 400 / 1000: loss 2.188995235046776
iteration 500 / 1000: loss 2.1162527791897743
iteration 600 / 1000: loss 2.064670827698217
iteration 700 / 1000: loss 1.990168862308394
iteration 800 / 1000: loss 2.002827640124685
iteration 900 / 1000: loss 1.9465176817856495
Validation accuracy: 0.283
```

Questions:

The training accuracy isn't great.

- (1) What are some of the reasons why this is the case? Take the following cell to do some analyses and then report your answers in the cell following the one below.
- (2) How should you fix the problems you identified in (1)?

Out[30]: <matplotlib.legend.Legend at 0x10bb0b9a0>



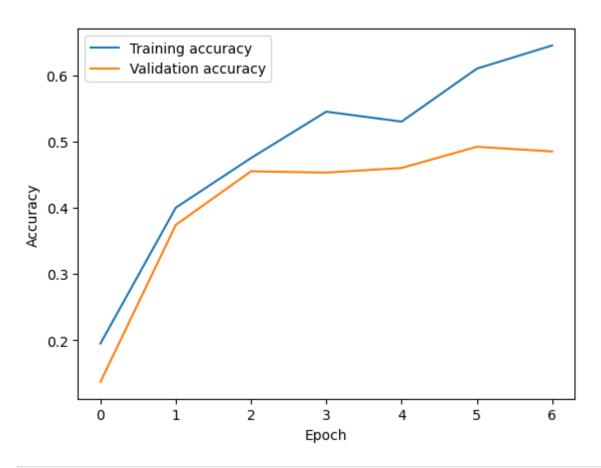
Answers:

- (1) According to the plot of training accuracy and validation accuracy, the training accuracy remains very low (< 0.25 by the final epoch). This means that the model is very likely underfitting the training data and hasn't learned a particularly good model.
- (2) The low training accuracy suggests that we can attempt to make the model more complex to better fit the training data by, for example, reducing the strength of regularization. Another possible solution would be to increase the number of training iterations.

Optimize the neural network

Use the following part of the Jupyter notebook to optimize your hyperparameters on the validation set. Store your nets as best_net.

```
min(floor((X - 28\%)) / \%22, 1)
           where if you get 50% or higher validation accuracy, you get full
        #
           points.
        #
        #
          Note, you need to use the same network structure (keep hidden_size = 50)
        best stats = None
        best val acc = 0
        for learning_rate in [1e-3, 1e-2, 1e-1]:
            for reg in [1e-7, 1e-5, 1e-3]:
               print(f'Testing lr={learning rate}, reg={reg}...')
               net = TwoLayerNet(input_size, hidden_size, num_classes)
               stats = net.train(X_train, y_train, X_val, y_val,
                   learning rate=learning rate,
                   learning_rate_decay=0.95, reg=reg,
                   num_iters=1500, batch_size=200, verbose=False)
               val_acc = (net.predict(X_val) == y_val).mean()
               if val_acc > best_val_acc:
                   best_net = net
                   best_stats = stats
                   best_val_acc = val_acc
        # ============ #
        # END YOUR CODE HERE
        val_acc = (best_net.predict(X_val) == y_val).mean()
        print('Best validation accuracy: ', val_acc)
        Testing lr=0.001, reg=1e-07...
        Testing lr=0.001, reg=1e-05...
        Testing lr=0.001, reg=0.001...
        Testing lr=0.01, reg=1e-07...
        Testing lr=0.01, reg=1e-05...
        Testing lr=0.01, reg=0.001...
        Testing lr=0.1, reg=1e-07...
        Testing lr=0.1, reg=1e-05...
        Testing lr=0.1, reg=0.001...
        Best validation accuracy: 0.503
In [47]: x = np.arange(len(best stats['train acc history']))
        plt.plot(x, best_stats['train_acc_history'], label='Training accuracy')
        plt.plot(x, best_stats['val_acc_history'], label='Validation accuracy')
        plt.xlabel('Epoch')
        plt.ylabel('Accuracy')
        plt.legend()
Out[47]: <matplotlib.legend.Legend at 0x10f617580>
```

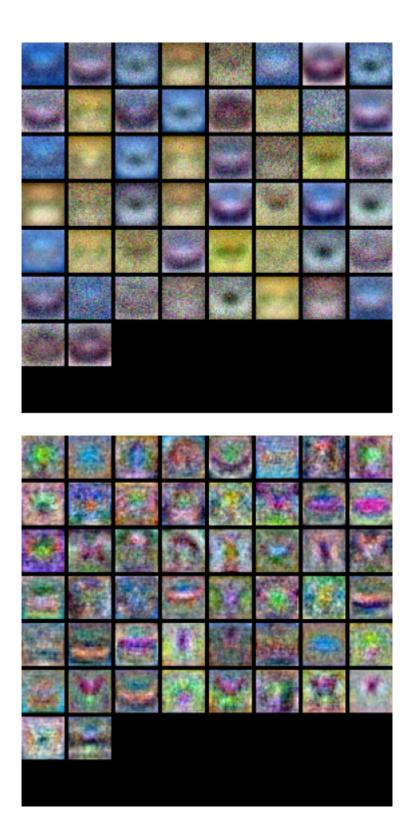


```
In [48]: from utils.vis_utils import visualize_grid

# Visualize the weights of the network

def show_net_weights(net):
    W1 = net.params['W1']
    W1 = W1.T.reshape(32, 32, 3, -1).transpose(3, 0, 1, 2)
    plt.imshow(visualize_grid(W1, padding=3).astype('uint8'))
    plt.gca().axis('off')
    plt.show()

show_net_weights(subopt_net)
show_net_weights(best_net)
```



Question:

(1) What differences do you see in the weights between the suboptimal net and the best net you arrived at?

Answer:

(1) The weights of the suboptimal net generally look very similar to one another, meaning that the model likely hasn't learned a good idea of what each class looks like. In comparison, the weights of the best net look more varied and defined.

Evaluate on test set

```
In [49]: test_acc = (best_net.predict(X_test) == y_test).mean()
    print('Test accuracy: ', test_acc)
    Test accuracy: 0.485
In []:
```

```
layers.py:
import numpy as np
import pdb
def affine_forward(x, w, b):
 Computes the forward pass for an affine (fully-connected) layer.
 The input x has shape (N, d_1, \ldots, d_k) and contains a minibatch of N
 examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
 reshape each input into a vector of dimension D = d_1 + \ldots + d_k, and
 then transform it to an output vector of dimension M.
 Inputs:
 - x: A number array containing input data, of shape (N, d_1, \ldots, d_k)
 - w: A numpy array of weights, of shape (D, M)
 - b: A numpy array of biases, of shape (M,)
 Returns a tuple of:
 - out: output, of shape (N, M)
 - cache: (x, w, b)
 # ----- #
 # YOUR CODE HERE:
 # Calculate the output of the forward pass. Notice the dimensions
 # of w are D x M, which is the transpose of what we did in earlier
    assignments.
 N, D = x.shape[0], w.shape[0]
 x_reshaped = np.reshape(x, (N, D))
 out = x_reshaped @ w + b
 # ----- #
 # END YOUR CODE HERE
 cache = (x, w, b)
 return out, cache
def affine_backward(dout, cache):
 Computes the backward pass for an affine layer.
 Inputs:
 - dout: Upstream derivative, of shape (N, M)
 - cache: Tuple of:
   - x: Input data, of shape (N, d_1, \ldots, d_k)
   - w: Weights, of shape (D, M)
```

```
Returns a tuple of:
 - dx: Gradient with respect to x, of shape (N, d1, ..., d_k)
 - dw: Gradient with respect to w, of shape (D, M)
 - db: Gradient with respect to b, of shape (M,)
 x, w, b = cache
 dx, dw, db = None, None, None
 # ----- #
 # YOUR CODE HERE:
 # Calculate the gradients for the backward pass.
 # dout is N x M
 # dx should be N x d1 x ... x dk; it relates to dout through multiplication with w, which is D x M
 # dw should be D x M; it relates to dout through multiplication with x, which is N x D after reshapin
 # db should be M; it is just the sum over dout examples
 N, D = x.shape[0], w.shape[0]
 dx = np.reshape(dout @ w.T, x.shape)
 dw = np.reshape(x, (N, D)).T @ dout
 db = np.sum(dout, axis=0)
 # ----- #
 # END YOUR CODE HERE
 # ------ #
 return dx, dw, db
def relu_forward(x):
 Computes the forward pass for a layer of rectified linear units (ReLUs).
 Input:
 - x: Inputs, of any shape
 Returns a tuple of:
 - out: Output, of the same shape as x
 - cache: x
 # ------ #
 # YOUR CODE HERE:
 # Implement the ReLU forward pass.
 out = np.maximum(0, x)
 # END YOUR CODE HERE
 # ----- #
 cache = x
 return out, cache
```

```
def relu_backward(dout, cache):
 Computes the backward pass for a layer of rectified linear units (ReLUs).
 Input:
 - dout: Upstream derivatives, of any shape
 - cache: Input x, of same shape as dout
 Returns:
 - dx: Gradient with respect to x
 n n n
 x = cache
 # YOUR CODE HERE:
   Implement the ReLU backward pass
 # ----- #
 # ReLU directs linearly to those > 0
 dx = (x > 0) * dout
 # ----- #
 # END YOUR CODE HERE
 # ----- #
 return dx
def softmax_loss(x, y):
 Computes the loss and gradient for softmax classification.
 Inputs:
 - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
 - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
   0 <= y[i] < C
 Returns a tuple of:
 - loss: Scalar giving the loss
 - dx: Gradient of the loss with respect to x
 probs = np.exp(x - np.max(x, axis=1, keepdims=True))
 probs /= np.sum(probs, axis=1, keepdims=True)
 N = x.shape[0]
 loss = -np.sum(np.log(probs[np.arange(N), y])) / N
 dx = probs.copy()
 dx[np.arange(N), y] = 1
 dx /= N
 return loss, dx
```

```
fc_net.py:
import numpy as np
from .layers import *
from .layer_utils import *
class TwoLayerNet(object):
 A two-layer fully-connected neural network with ReLU nonlinearity and
 softmax loss that uses a modular layer design. We assume an input dimension
 of D, a hidden dimension of H, and perform classification over C classes.
 The architecure should be affine - relu - affine - softmax.
 Note that this class does not implement gradient descent; instead, it
 will interact with a separate Solver object that is responsible for running
 optimization.
 The learnable parameters of the model are stored in the dictionary
 self.params that maps parameter names to numpy arrays.
  11 11 11
 def __init__(self, input_dim=3*32*32, hidden_dims=100, num_classes=10,
             dropout=0, weight_scale=1e-3, reg=0.0):
   Initialize a new network.
   Inputs:
    - input_dim: An integer giving the size of the input
   - hidden_dims: An integer giving the size of the hidden layer
   - num_classes: An integer giving the number of classes to classify
   - dropout: Scalar between 0 and 1 giving dropout strength.
   - weight_scale: Scalar giving the standard deviation for random
     initialization of the weights.
   - req: Scalar giving L2 regularization strength.
   self.params = {}
   self.reg = reg
   # YOUR CODE HERE:
       Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
      self.params['W2'], self.params['b1'] and self.params['b2']. The
      biases are initialized to zero and the weights are initialized
      so that each parameter has mean O and standard deviation weight_scale.
      The dimensions of W1 should be (input_dim, hidden_dim) and the
       dimensions of W2 should be (hidden_dims, num_classes)
   # ----- #
   self.params['W1'] = np.random.normal(loc=0, scale=weight_scale, size=(input_dim, hidden_dims))
   self.params['b1'] = np.zeros(hidden_dims)
   self.params['W2'] = np.random.normal(loc=0, scale=weight_scale, size=(hidden_dims, num_classes))
```

```
self.params['b2'] = np.zeros(num_classes)
 # END YOUR CODE HERE
 def loss(self, X, y=None):
 Compute loss and gradient for a minibatch of data.
 Inputs:
 - X: Array of input data of shape (N, d_1, \ldots, d_k)
 - y: Array of labels, of shape (N,). y[i] gives the label for X[i].
 Returns:
 If y is None, then run a test-time forward pass of the model and return:
 - scores: Array of shape (N, C) giving classification scores, where
   scores[i, c] is the classification score for X[i] and class c.
 If y is not None, then run a training-time forward and backward pass and
 return a tuple of:
 - loss: Scalar value giving the loss
 - qrads: Dictionary with the same keys as self.params, mapping parameter
   names to gradients of the loss with respect to those parameters.
 scores = None
 # YOUR CODE HERE:
 # Implement the forward pass of the two-layer neural network. Store
   the class scores as the variable 'scores'. Be sure to use the layers
 # you prior implemented.
 layer_1_out, layer_1_cache = affine_relu_forward(X, self.params['W1'], self.params['b1'])
 layer_2_out, layer_2_cache = affine_forward(layer_1_out, self.params['W2'], self.params['b2'])
 scores = layer_2_out
 # END YOUR CODE HERE
 # If y is None then we are in test mode so just return scores
 if v is None:
  return scores
 loss, grads = 0, \{\}
 # ========== #
 # YOUR CODE HERE:
   Implement the backward pass of the two-layer neural net. Store
 # the loss as the variable 'loss' and store the gradients in the
 # 'grads' dictionary. For the grads dictionary, grads['W1'] holds
 # the gradient for W1, grads['b1'] holds the gradient for b1, etc.
   i.e., grads[k] holds the gradient for self.params[k].
```

```
Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
       for each W. Be sure to include the 0.5 multiplying factor to
   #
       match our implementation.
      And be sure to use the layers you prior implemented.
   loss, dL = softmax_loss(scores, y)
   loss += 0.5 * self.reg * (np.sum(self.params['W1']**2) + np.sum(self.params['W2']**2))
   dh, dw2, db2 = affine_backward(dL, layer_2_cache)
   _, dw1, db1 = affine_relu_backward(dh, layer_1_cache)
   grads['W1'] = dw1 + self.reg * self.params['W1']
   grads['b1'] = db1.T
   grads['W2'] = dw2 + self.reg * self.params['W2']
   grads['b2'] = db2.T
   # END YOUR CODE HERE
   return loss, grads
class FullyConnectedNet(object):
 A fully-connected neural network with an arbitrary number of hidden layers,
 ReLU nonlinearities, and a softmax loss function. This will also implement
 dropout and batch normalization as options. For a network with L layers,
 the architecture will be
 \{affine - [batch norm] - relu - [dropout]\} x (L - 1) - affine - softmax
 where batch normalization and dropout are optional, and the {...} block is
 repeated L - 1 times.
 Similar to the TwoLayerNet above, learnable parameters are stored in the
 self.params dictionary and will be learned using the Solver class.
  11 11 11
 def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10,
             dropout=0, use_batchnorm=False, reg=0.0,
             weight_scale=1e-2, dtype=np.float32, seed=None):
   Initialize a new FullyConnectedNet.
   Inputs:
   - hidden_dims: A list of integers giving the size of each hidden layer.
   - input_dim: An integer giving the size of the input.
   - num_classes: An integer giving the number of classes to classify.
   - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=0 then
     the network should not use dropout at all.
```

#

```
- use_batchnorm: Whether or not the network should use batch normalization.
- reg: Scalar giving L2 regularization strength.
- weight_scale: Scalar giving the standard deviation for random
  initialization of the weights.
- dtype: A numpy datatype object; all computations will be performed using
 this datatype. float32 is faster but less accurate, so you should use
 float64 for numeric gradient checking.
- seed: If not None, then pass this random seed to the dropout layers. This
 will make the dropout layers deteriminstic so we can gradient check the
 model.
self.use_batchnorm = use_batchnorm
self.use_dropout = dropout > 0
self.reg = reg
self.num_layers = 1 + len(hidden_dims)
self.dtype = dtype
self.params = {}
# ------ #
# YOUR CODE HERE:
  Initialize all parameters of the network in the self.params dictionary.
# The weights and biases of layer 1 are W1 and b1; and in general the
   weights and biases of layer i are Wi and bi. The
# biases are initialized to zero and the weights are initialized
# so that each parameter has mean O and standard deviation weight_scale.
# ========= #
in_dim = input_dim
for i, out_dim in enumerate(hidden_dims + [num_classes]):
 self.params[f'W{i+1}'] = np.random.normal(loc=0, scale=weight_scale, size=(in_dim, out_dim))
 self.params[f'b{i+1}'] = np.zeros((out_dim,))
 in_dim = out_dim
# END YOUR CODE HERE
# When using dropout we need to pass a dropout_param dictionary to each
# dropout layer so that the layer knows the dropout probability and the mode
# (train / test). You can pass the same dropout_param to each dropout layer.
self.dropout_param = {}
if self.use_dropout:
 self.dropout_param = {'mode': 'train', 'p': dropout}
 if seed is not None:
   self.dropout_param['seed'] = seed
# With batch normalization we need to keep track of running means and
# variances, so we need to pass a special bn_param object to each batch
# normalization layer. You should pass self.bn_params[0] to the forward pass
# of the first batch normalization layer, self.bn_params[1] to the forward
# pass of the second batch normalization layer, etc.
self.bn_params = []
if self.use_batchnorm:
 self.bn_params = [{'mode': 'train'} for i in np.arange(self.num_layers - 1)]
```

```
# Cast all parameters to the correct datatype
 for k, v in self.params.items():
   self.params[k] = v.astype(dtype)
def loss(self, X, y=None):
 Compute loss and gradient for the fully-connected net.
 Input / output: Same as TwoLayerNet above.
 X = X.astype(self.dtype)
 mode = 'test' if y is None else 'train'
 # Set train/test mode for batchnorm params and dropout param since they
 # behave differently during training and testing.
 if self.dropout_param is not None:
   self.dropout_param['mode'] = mode
 if self.use_batchnorm:
   for bn_param in self.bn_params:
    bn_param[mode] = mode
 scores = None
 # ----- #
 # YOUR CODE HERE:
 # Implement the forward pass of the FC net and store the output
   scores as the variable "scores".
 # ----- #
 L = self.num_layers
 in_layer = X
 caches = dict()
 for i in range(1, L):
   W, b = self.params[f'W{i}'], self.params[f'b{i}']
   out_layer, layer_cache = affine_relu_forward(in_layer, W, b)
   caches[i] = layer_cache
   in_layer = out_layer
 scores, layer_cache = affine_forward(in_layer, self.params[f'W{L}'], self.params[f'b{L}'])
 caches[L] = layer_cache
 # ----- #
 # END YOUR CODE HERE
 # If test mode return early
 if mode == 'test':
  return scores
 loss, grads = 0.0, {}
```

```
# YOUR CODE HERE:
# Implement the backwards pass of the FC net and store the gradients
# in the grads dict, so that grads[k] is the gradient of self.params[k]
  Be sure your L2 regularization includes a 0.5 factor.
# ------ #
loss, dL = softmax_loss(scores, y)
for p in self.params:
 if p[0] == 'W':
   loss += 0.5 * self.reg * np.sum(self.params[p]**2)
backward = affine_backward
dhi, dwi, dbi = dL, None, None
for i in range(L, 0, -1):
 dhi, dwi, dbi = backward(dhi, caches[i])
 grads[f'W{i}'] = dwi + self.reg * self.params[f'W{i}']
 grads[f'b{i}'] = dbi.T
 backward = affine_relu_backward
# ============ #
# END YOUR CODE HERE
# ----- #
return loss, grads
```

Fully connected networks

In the previous notebook, you implemented a simple two-layer neural network class. However, this class is not modular. If you wanted to change the number of layers, you would need to write a new loss and gradient function. If you wanted to optimize the network with different optimizers, you'd need to write new training functions. If you wanted to incorporate regularizations, you'd have to modify the loss and gradient function.

Instead of having to modify functions each time, for the rest of the class, we'll work in a more modular framework where we define forward and backward layers that calculate losses and gradients respectively. Since the forward and backward layers share intermediate values that are useful for calculating both the loss and the gradient, we'll also have these function return "caches" which store useful intermediate values.

The goal is that through this modular design, we can build different sized neural networks for various applications.

In this HW #3, we'll define the basic architecture, and in HW #4, we'll build on this framework to implement different optimizers and regularizations (like BatchNorm and Dropout).

Modular layers

This notebook will build modular layers in the following manner. First, there will be a forward pass for a given layer with inputs (x) and return the output of that layer (out) as well as cached variables (cache) that will be used to calculate the gradient in the backward pass.

```
def layer_forward(x, w):
    """ Receive inputs x and weights w
    # Do some computations ...
    z = # ... some intermediate value
    # Do some more computations ...
    out = # the output

cache = (x, w, z, out) # Values we need to compute gradients
    return out, cache
```

The backward pass will receive upstream derivatives and the cache object, and will return gradients with respect to the inputs and weights, like this:

```
def layer_backward(dout, cache):
```

```
.....
          # Unpack cache values
          x, w, z, out = cache
          # Use values in cache to compute derivatives
          dx = \# Derivative of loss with respect to x
          dw = # Derivative of loss with respect to w
          return dx, dw
In [1]: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc net import *
        from utils.data utils import get CIFAR10 data
        from utils.gradient_check import eval_numerical_gradient, eval_numerical_gra
        from utils.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ip
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
          """ returns relative error """
          return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
In [2]: # Load the (preprocessed) CIFAR10 data.
        data = get_CIFAR10_data()
        for k in data.keys():
          print('{}: {} '.format(k, data[k].shape))
        X train: (49000, 3, 32, 32)
        y_train: (49000,)
        X_val: (1000, 3, 32, 32)
        y val: (1000,)
        X_test: (1000, 3, 32, 32)
        y_test: (1000,)
```

Receive derivative of loss with respect to outputs and cache,

and compute derivative with respect to inputs.

Linear layers

In this section, we'll implement the forward and backward pass for the linear layers.

The linear layer forward pass is the function affine_forward in nndl/layers.py and the backward pass is affine_backward.

After you have implemented these, test your implementation by running the cell below.

Affine layer forward pass

Implement affine forward and then test your code by running the following cell.

Testing affine_forward function: difference: 9.7698500479884e-10

Affine layer backward pass

Implement affine_backward and then test your code by running the following cell.

```
In [4]: # Test the affine_backward function

x = np.random.randn(10, 2, 3)
w = np.random.randn(6, 5)
b = np.random.randn(5)
dout = np.random.randn(10, 5)

dx_num = eval_numerical_gradient_array(lambda x: affine_forward(x, w, b)[0],
dw_num = eval_numerical_gradient_array(lambda w: affine_forward(x, w, b)[0],
db_num = eval_numerical_gradient_array(lambda b: affine_forward(x, w, b)[0],
_, cache = affine_forward(x, w, b)
dx, dw, db = affine_backward(dout, cache)

# The error should be around le-10
print('Testing affine_backward function:')
```

```
print('dx error: {}'.format(rel_error(dx_num, dx)))
print('dw error: {}'.format(rel_error(dw_num, dw)))
print('db error: {}'.format(rel_error(db_num, db)))

Testing affine_backward function:
dx error: 7.31465044978936e-10
dw error: 9.088876066260483e-11
db error: 9.55575431106778e-12
```

Activation layers

In this section you'll implement the ReLU activation.

ReLU forward pass

Implement the relu_forward function in nndl/layers.py and then test your code by running the following cell.

Testing relu_forward function: difference: 4.999999798022158e-08

ReLU backward pass

Implement the relu_backward function in nndl/layers.py and then test your code by running the following cell.

```
In [6]: x = np.random.randn(10, 10)
dout = np.random.randn(*x.shape)

dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout
_, cache = relu_forward(x)
dx = relu_backward(dout, cache)

# The error should be around 1e-12
print('Testing relu_backward function:')
print('dx error: {}'.format(rel_error(dx_num, dx)))
```

Combining the affine and ReLU layers

Often times, an affine layer will be followed by a ReLU layer. So let's make one that puts them together. Layers that are combined are stored in nndl/layer_utils.py.

Affine-ReLU layers

We've implemented affine_relu_forward() and affine_relu_backward in nndl/layer_utils.py . Take a look at them to make sure you understand what's going on. Then run the following cell to ensure its implemented correctly.

```
In [7]: from nndl.layer_utils import affine_relu_forward, affine_relu_backward
        x = np.random.randn(2, 3, 4)
        w = np.random.randn(12, 10)
        b = np.random.randn(10)
        dout = np.random.randn(2, 10)
        out, cache = affine_relu_forward(x, w, b)
        dx, dw, db = affine_relu_backward(dout, cache)
        dx_num = eval_numerical_gradient_array(lambda x: affine_relu_forward(x, w, b
        dw_num = eval_numerical_gradient_array(lambda w: affine_relu_forward(x, w, t
        db_num = eval_numerical_gradient_array(lambda b: affine_relu_forward(x, w, t
        print('Testing affine relu forward and affine relu backward:')
        print('dx error: {}'.format(rel_error(dx_num, dx)))
        print('dw error: {}'.format(rel_error(dw_num, dw)))
        print('db error: {}'.format(rel_error(db_num, db)))
        Testing affine_relu_forward and affine_relu_backward:
        dx error: 1.4005251456258178e-10
        dw error: 4.764910208249058e-10
        db error: 7.826645559542029e-12
```

Softmax loss

You've already implemented it, so we have written it in layers.py. The following code will ensure they are working correctly.

```
In [8]: num_classes, num_inputs = 10, 50
x = 0.001 * np.random.randn(num_inputs, num_classes)
y = np.random.randint(num_classes, size=num_inputs)

dx_num = eval_numerical_gradient(lambda x: softmax_loss(x, y)[0], x, verbose loss, dx = softmax_loss(x, y)
```

```
# Test softmax_loss function. Loss should be 2.3 and dx error should be 1e-8
print('\nTesting softmax_loss:')
print('loss: {}'.format(loss))
print('dx error: {}'.format(rel_error(dx_num, dx)))
```

Testing softmax_loss: loss: 2.3025779226361585 dx error: 6.197432934655467e-09

Implementation of a two-layer NN

In nndl/fc_net.py, implement the class TwoLayerNet which uses the layers you made here. When you have finished, the following cell will test your implementation.

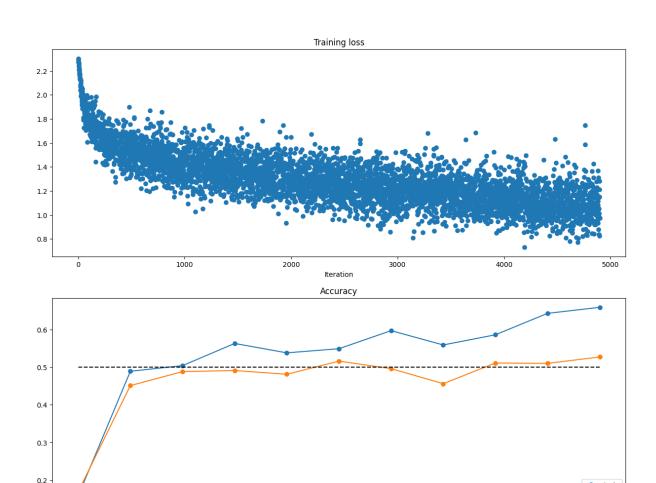
```
In [9]: N, D, H, C = 3, 5, 50, 7
        X = np.random.randn(N, D)
        y = np.random.randint(C, size=N)
        std = 1e-2
        model = TwoLayerNet(input_dim=D, hidden_dims=H, num_classes=C, weight_scale=
        print('Testing initialization ... ')
        W1_std = abs(model.params['W1'].std() - std)
        b1 = model.params['b1']
        W2_std = abs(model.params['W2'].std() - std)
        b2 = model.params['b2']
        assert W1_std < std / 10, 'First layer weights do not seem right'</pre>
        assert np.all(b1 == 0), 'First layer biases do not seem right'
        assert W2_std < std / 10, 'Second layer weights do not seem right'</pre>
        assert np.all(b2 == 0), 'Second layer biases do not seem right'
        print('Testing test-time forward pass ... ')
        model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
        model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
        model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
        model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
        X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).T
        scores = model.loss(X)
        correct_scores = np.asarray(
          [[11.53165108, 12.2917344, 13.05181771, 13.81190102, 14.57198434, 15.
           [12.05769098, 12.74614105, 13.43459113, 14.1230412, 14.81149128, 15.
           [12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.05099822, 15.
        scores_diff = np.abs(scores - correct_scores).sum()
        assert scores_diff < 1e-6, 'Problem with test-time forward pass'</pre>
        print('Testing training loss (no regularization)')
        y = np.asarray([0, 5, 1])
        loss, grads = model.loss(X, y)
        correct loss = 3.4702243556
        assert abs(loss - correct_loss) < 1e-10, 'Problem with training-time loss'</pre>
        model.reg = 1.0
        loss, grads = model.loss(X, y)
```

```
correct loss = 26.5948426952
assert abs(loss - correct_loss) < 1e-10, 'Problem with regularization loss'</pre>
for reg in [0.0, 0.7]:
  print('Running numeric gradient check with reg = {}'.format(reg))
  model.reg = reg
  loss, grads = model.loss(X, y)
  for name in sorted(grads):
    f = lambda _: model.loss(X, y)[0]
    grad_num = eval_numerical_gradient(f, model.params[name], verbose=False)
    print('{} relative error: {}'.format(name, rel_error(grad_num, grads[name))
Testing initialization ...
Testing test-time forward pass ...
Testing training loss (no regularization)
Running numeric gradient check with reg = 0.0
W1 relative error: 1.8265914102168292e-08
W2 relative error: 3.3458521609206087e-10
b1 relative error: 8.008665234879004e-09
b2 relative error: 1.9376073688240078e-10
Running numeric gradient check with reg = 0.7
W1 relative error: 2.5279152310200606e-07
W2 relative error: 1.3678364482660862e-07
b1 relative error: 1.564680139421095e-08
b2 relative error: 9.089616810648186e-10
```

Solver

We will now use the utils Solver class to train these networks. Familiarize yourself with the API in utils/solver.py. After you have done so, declare an instance of a TwoLayerNet with 200 units and then train it with the Solver. Choose parameters so that your validation accuracy is at least 50%.

```
batch size=100,
                         print_every=500)
         solver.train()
         # END YOUR CODE HERE
         # =============
         (Iteration 1 / 4900) loss: 2.301530
         (Epoch 0 / 10) train acc: 0.158000; val_acc: 0.169000
         (Epoch 1 / 10) train acc: 0.489000; val_acc: 0.451000
         (Iteration 501 / 4900) loss: 1.651384
         (Epoch 2 / 10) train acc: 0.504000; val_acc: 0.488000
         (Iteration 1001 / 4900) loss: 1.340158
         (Epoch 3 / 10) train acc: 0.563000; val acc: 0.491000
         (Iteration 1501 / 4900) loss: 1.617317
         (Epoch 4 / 10) train acc: 0.538000; val_acc: 0.481000
         (Iteration 2001 / 4900) loss: 1.159907
         (Epoch 5 / 10) train acc: 0.549000; val_acc: 0.516000
         (Iteration 2501 / 4900) loss: 1.099285
         (Epoch 6 / 10) train acc: 0.597000; val acc: 0.496000
         (Iteration 3001 / 4900) loss: 0.999669
         (Epoch 7 / 10) train acc: 0.559000; val_acc: 0.456000
         (Iteration 3501 / 4900) loss: 1.196356
         (Epoch 8 / 10) train acc: 0.586000; val_acc: 0.511000
         (Iteration 4001 / 4900) loss: 1.138254
         (Epoch 9 / 10) train acc: 0.643000; val acc: 0.510000
         (Iteration 4501 / 4900) loss: 0.855623
         (Epoch 10 / 10) train acc: 0.659000; val_acc: 0.527000
In [11]: # Run this cell to visualize training loss and train / val accuracy
         plt.subplot(2, 1, 1)
         plt.title('Training loss')
         plt.plot(solver.loss_history, 'o')
         plt.xlabel('Iteration')
         plt.subplot(2, 1, 2)
         plt.title('Accuracy')
         plt.plot(solver.train_acc_history, '-o', label='train')
         plt.plot(solver.val_acc_history, '-o', label='val')
         plt.plot([0.5] * len(solver.val_acc_history), 'k--')
         plt.xlabel('Epoch')
         plt.legend(loc='lower right')
         plt.gcf().set_size_inches(15, 12)
         plt.show()
```



Multilayer Neural Network

Now, we implement a multi-layer neural network.

Read through the FullyConnectedNet class in the file nndl/fc_net.py.

Implement the initialization, the forward pass, and the backward pass. There will be lines for batchnorm and dropout layers and caches; ignore these all for now. That'll be in HW #4.

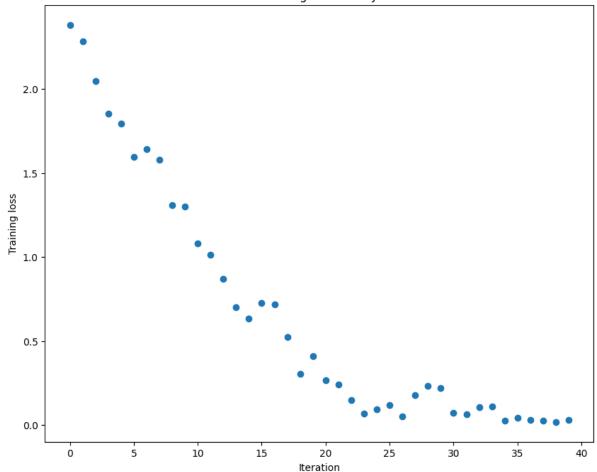
Epoch

10

```
f = lambda _: model.loss(X, y)[0]
             grad_num = eval_numerical_gradient(f, model.params[name], verbose=False,
             print('{} relative error: {}'.format(name, rel error(grad num, grads[name)
         Running check with reg = 0
         Initial loss: 2.301039294372159
         W1 relative error: 1.7669291193587022e-06
         W2 relative error: 9.571653999079532e-06
         W3 relative error: 3.813095605592845e-07
         b1 relative error: 5.8842141120884016e-08
         b2 relative error: 4.8381987778526565e-09
         b3 relative error: 1.0354616622811734e-10
         Running check with reg = 3.14
         Initial loss: 6.890666355348374
         W1 relative error: 3.522896396863251e-08
         W2 relative error: 2.8962458969078816e-08
         W3 relative error: 1.5715536797469338e-08
         b1 relative error: 1.003128487146125e-07
         b2 relative error: 9.329412999788734e-09
         b3 relative error: 4.1517298487597025e-10
In [13]: # Use the three layer neural network to overfit a small dataset.
         num train = 50
         small data = {
           'X_train': data['X_train'][:num_train],
           'y_train': data['y_train'][:num_train],
           'X val': data['X val'],
           'y_val': data['y_val'],
         #### !!!!!!
         # Play around with the weight scale and learning rate so that you can overfi
         # Your training accuracy should be 1.0 to receive full credit on this part.
         weight scale = 1e-2
         learning rate = 1e-2
         model = FullyConnectedNet([100, 100],
                       weight scale=weight scale, dtype=np.float64)
         solver = Solver(model, small_data,
                          print_every=10, num_epochs=20, batch_size=25,
                          update_rule='sgd',
                          optim config={
                            'learning_rate': learning_rate,
         solver.train()
         plt.plot(solver.loss history, 'o')
         plt.title('Training loss history')
         plt.xlabel('Iteration')
         plt.ylabel('Training loss')
         plt.show()
```

```
(Iteration 1 / 40) loss: 2.380206
(Epoch 0 / 20) train acc: 0.240000; val acc: 0.095000
(Epoch 1 / 20) train acc: 0.220000; val acc: 0.138000
(Epoch 2 / 20) train acc: 0.320000; val_acc: 0.150000
(Epoch 3 / 20) train acc: 0.380000; val_acc: 0.134000
(Epoch 4 / 20) train acc: 0.620000; val_acc: 0.195000
(Epoch 5 / 20) train acc: 0.740000; val acc: 0.204000
(Iteration 11 / 40) loss: 1.081375
(Epoch 6 / 20) train acc: 0.800000; val acc: 0.160000
(Epoch 7 / 20) train acc: 0.740000; val_acc: 0.174000
(Epoch 8 / 20) train acc: 0.880000; val_acc: 0.192000
(Epoch 9 / 20) train acc: 0.960000; val acc: 0.196000
(Epoch 10 / 20) train acc: 0.960000; val_acc: 0.207000
(Iteration 21 / 40) loss: 0.266158
(Epoch 11 / 20) train acc: 0.980000; val acc: 0.201000
(Epoch 12 / 20) train acc: 0.960000; val acc: 0.194000
(Epoch 13 / 20) train acc: 0.960000; val_acc: 0.217000
(Epoch 14 / 20) train acc: 0.920000; val_acc: 0.170000
(Epoch 15 / 20) train acc: 0.980000; val acc: 0.197000
(Iteration 31 / 40) loss: 0.075206
(Epoch 16 / 20) train acc: 0.980000; val_acc: 0.190000
(Epoch 17 / 20) train acc: 1.000000; val acc: 0.197000
(Epoch 18 / 20) train acc: 1.000000; val_acc: 0.189000
(Epoch 19 / 20) train acc: 1.000000; val_acc: 0.187000
(Epoch 20 / 20) train acc: 1.000000; val acc: 0.188000
```

Training loss history



In []: