

Spatio temporal analysis of extreme wind velocities for infrastructure desing. Case  
study Colombia

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Master of Science in Geospatial Technologies

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I want to thank a few people.



# Preface

This is an example of a thesis setup to use the reed thesis document class (for LaTeX) and the R bookdown package, in general.





# Table of Contents

<b>Introduction</b>	<b>1</b>
<b>Chapter 1: Data</b>	<b>3</b>
1.1 IDEAM	4
1.2 ISD	8
1.3 ERA5	12
1.4 Data Download and Organization	13
1.5 Data Standarization	13
<b>Chapter 2: Theoretical Framework</b>	<b>15</b>
2.1 Probability Concepts	15
2.1.1 Probability Density Function - <i>pdf</i>	15
2.1.2 Cumulative Distribution Funtcion - <i>cdf</i>	17
2.1.3 Percent Point Function - <i>ppf</i>	18
2.1.4 Hazard Function - <i>hf</i>	19
2.2 Statistical Concepts For Extreme Analysis	20
2.2.1 Annual Excedance Probability - $P_e$	20
2.2.2 Return Period - Mean Recurrence Interval	21
2.2.3 Compound Excedance Probability - $P_n$	22
2.3 Extreme Value Analysis Overview	23
2.4 Peaks Over Threshold - Poisson Process	24
2.5 Wind Loads Requirements	27
<b>Chapter 3: Methodology</b>	<b>31</b>
3.1 Input Data Selection and Standarization	31
3.1.1 Data Selection	32
3.1.2 Data Standarization	32
3.1.3 Data Filterng	32
3.2 Fit data to a POT - Poisson Process	32
3.2.1 Data Requirements	32
3.2.2 Exploratory Data Analysis and Data Preparation	32
3.2.3 Parameters Estimation	32
3.2.4 Velocities at Return Periods	32
3.3 spatial Interpolation	32

Conclusion . . . . .	33
Appendix A: The First Appendix . . . . .	35
Appendix B: The Second Appendix, for Fun . . . . .	37
References . . . . .	39

# List of Tables

1.1	Datasets . . . . .	3
1.2	Variables . . . . .	3
1.3	Units and Time . . . . .	3
1.4	IDEAM Stations . . . . .	4
1.5	ISD Stations . . . . .	8



# List of Figures

1.1	IDEAM Stations . . . . .	5
1.2	IDEAM Station - Time Serie . . . . .	6
1.3	IDEAM Station ACF . . . . .	7
1.4	IDEAM Station PACF . . . . .	8
1.5	ISD Stations . . . . .	9
1.6	ISD Station - Time Serie . . . . .	10
1.7	ISD Station ACF . . . . .	11
1.8	IDEAM Station PACF . . . . .	12
1.9	ERA5 Stations (cells centers) . . . . .	13
2.1	Gumbel pdf . . . . .	16
2.2	Gumbel pdf - dgumbel function . . . . .	17
2.3	Gumbel cdf . . . . .	18
2.4	Gumbel cdf . . . . .	19
2.5	Gumbel cdf . . . . .	20
2.6	Sorted Winds by Magnitud - wind simulation database . . . . .	21
2.7	Compound Probability . . . . .	22
2.8	Domanin off the Poisson Process . . . . .	25
2.9	Volume under surfaces represents the mean of the Poisson process . . . . .	26
2.10	Maximun speeds averaged over t (sec), to hourly mean speed . . . . .	29



# Abstract

The preface pretty much says it all.

Second paragraph of abstract starts here.





# Dedication

You can have a dedication here if you wish.



# Introduction

This research aims to create non-hurricane non-tornadic maps of extreme wind speeds for *three specific recurrence intervals* (700, 1700, and 3000 years) covering the Colombian territory. These maps will be combined with existing hurricane wind speed studies, to be used as input loads due to wind for infrastructure desing.

For each station with wind speeds time histories in the input data, extreme wind speed corresponding to each recurrence interval are calculated using a *Peaks Over Threshold* onwards *POT* extreme value model, then wind velocities with the same recurrence interval are *spatially interpolated* to generate continuous maps for the whole study area.

A wind speed linked to a *mean recurrence interval - MRI* of *N-years* (N-years return value or return period) is interpreted as the highest probable wind speed along the period of N-years. The annual probability of equal or exceed that wind speed is  $1/N$ . The annual exceedance probability for all velocity values in 700-years output map will be  $1/700$ , for the 1700-years map will be  $1/1700$ , and  $1/3000$  for the 3000-years final map.

There are different methods to model extreme value data, among them are a) sample maxima using a *Generalized Extreme Value Distribution* onwards *GEVD* (traditional method), b) POT using a *Generalized Pareto Distribution* onwards *GPD*, c) POT using a two-dimensional Poisson Process, that can be homomegenos, non-homogeneous, stationary, and non-stationary (originally know as *Point Process* approach), and d) POT Poisson-GPD. Following Pintar, Simiu, Lombardo, & Levitan (2015) in this research a *POT using a non-homogeneous non-stationary two-dimensional poisson proces* was selected, despide there is no R package available to apply this approach.



# Chapter 1

## Data

Input data is made up of three different sources a) IDEAM - Institute of Hydrology, Meteorology and Environmental Studies of Colombia <http://www.ideam.gov.co>, b) ISD - Integrated Surface Database <https://www.ncdc.noaa.gov/isd>, and c) ERA5 climate reanalysis <https://www.ecmwf.int/en/forecasts/datasets/reanalysis-datasets/era5>.

Table 1.1: Datasets description

Institution	Dataset	Details
IDEAM	Historical records at weather stations	IDEAM is responsible for the instalation, maintenance and management of all kind of weather stations located everywhere along the country
NOAA	ISD	ISD (Integrated Surface Database. NOAA's National Centers for Environmental Information - NCEI) Lite: A subset from the full ISD dataset containing eight common surface parameters in a fixed-width format free of duplicate values, sub-hourly data, and complicated flags.
ECMWF	ERA5	ERA5 is a reanalysis dataset with hourly estimates of atmospheric variables with horizontal resolution of $0.25^{\circ}$ (33 kilómeters), this is equally spaced cells every 0.25 degrees

Table 1.2: Datasets variables

Dataset	Variables	Description
IDEAM	vvmx_aut_60	Hourly wind maximum velocity
ISD	wind speed rate	Maximum hourly wind velocity. The rate of horizontal travel of air past a fixed point.
ERA5	fg10	10 metre wind gust since previous post-processing
	fsr	Forecast Surface Roughness

Table 1.3: Variables units and time

Variable	Units	Time	Stations
----------	-------	------	----------

vvmx_aut_60	meters per second	Variable from 2001 until today. Irregular time series.	203
Wind speed	meters per second	Variable from 1941 until today. Note: There is too much variability in time (start, end, and time range) for each station. Irregutal time series.	101
fg10	meters per second	1979-Today	3381
fsr	meters per second	1979-Today	3381

Ideal data source to create extreme wind speeds maps should be field observed data from IDEAM, but there are not enough number of stations around the study area to represent all the local wind variability in a huge country with multiple variety of climates and and changing thermal floors, but there are other important motivations to include different sources trying to improve output results:

- As just mentioned, low quantity of IDEAM stations
- There are uncertainties related to the way IDEAM anemometers are registering data, then comparison with other datasources are needed to be able to do appropriate data standardization, needed as a prerequisite to the analysis.
- There is no time continuity in the registration of IDEAM data. Historical time series are different and variable in each station.

Importance of ISD database for this study is based on the fact that post-procesed ISD database has wind extreme values, and it was used to create extreme wind maps for United States. ISD allows comparison with IDEAM records to take better decitions in order to do needed data standarization.

Despite that ERA5 data are not observed data, but forecast, its main advantage is data availability to assess the local climatic variance every 33 square kilometers.

## 1.1 IDEAM

Historical observed wind speeds from 203 in Colombia are managed by the official environmental authority IDEAM. Table 1.4 shows a sample of five IDEAM stations. Figure 1.1 shows a map of IDEAM stations.

Table 1.4: IDEAM Stations sample

Name[Code]	Latitud	Longitud
EMAS - AUT [26155230]	5.09	-75.51
SAN BENITO - AUT [25025380]	9.16	-75.04
AEROPUERTO ALFONSO LOPEZ - [28025502]	10.44	-73.25
TIBAITATA - AUT [21206990]	4.69	-74.21
ELDORADO CATAM - AUT [21205791]	4.71	-74.15

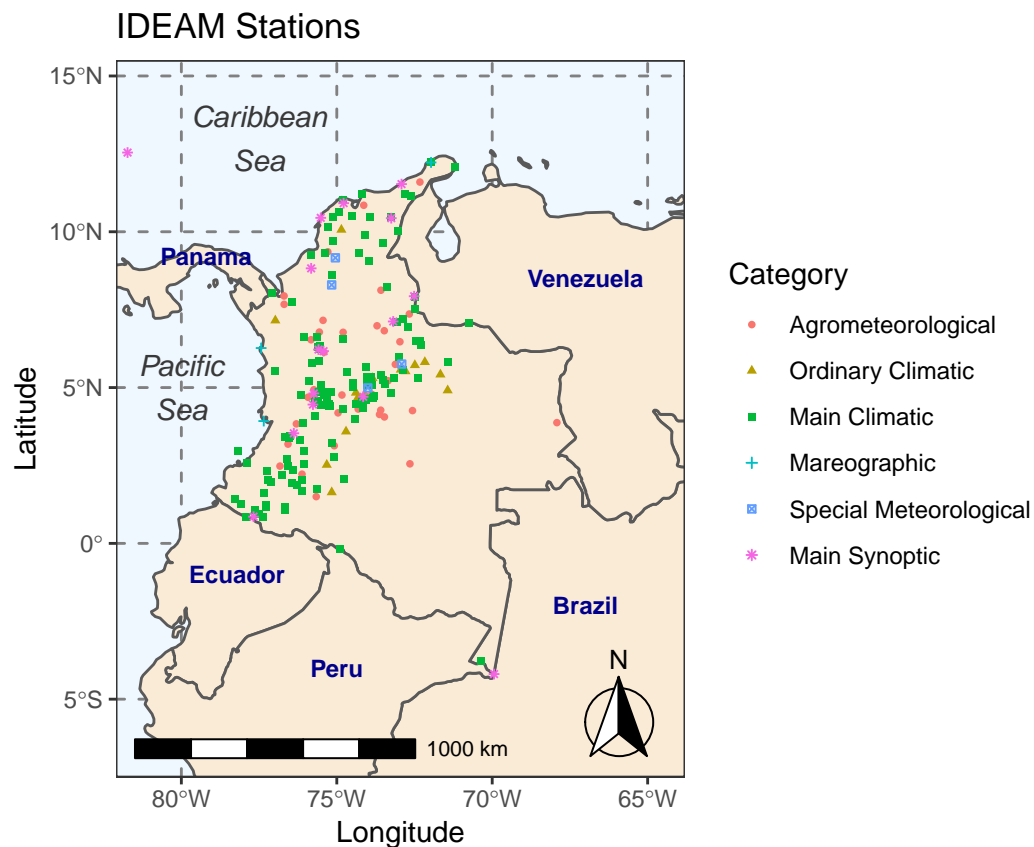


Figure 1.1: IDEAM Stations

Following, the time serie, autocorrelation function, and partial autocorrelation function, for IDEAM station “21205791” will be displayed.

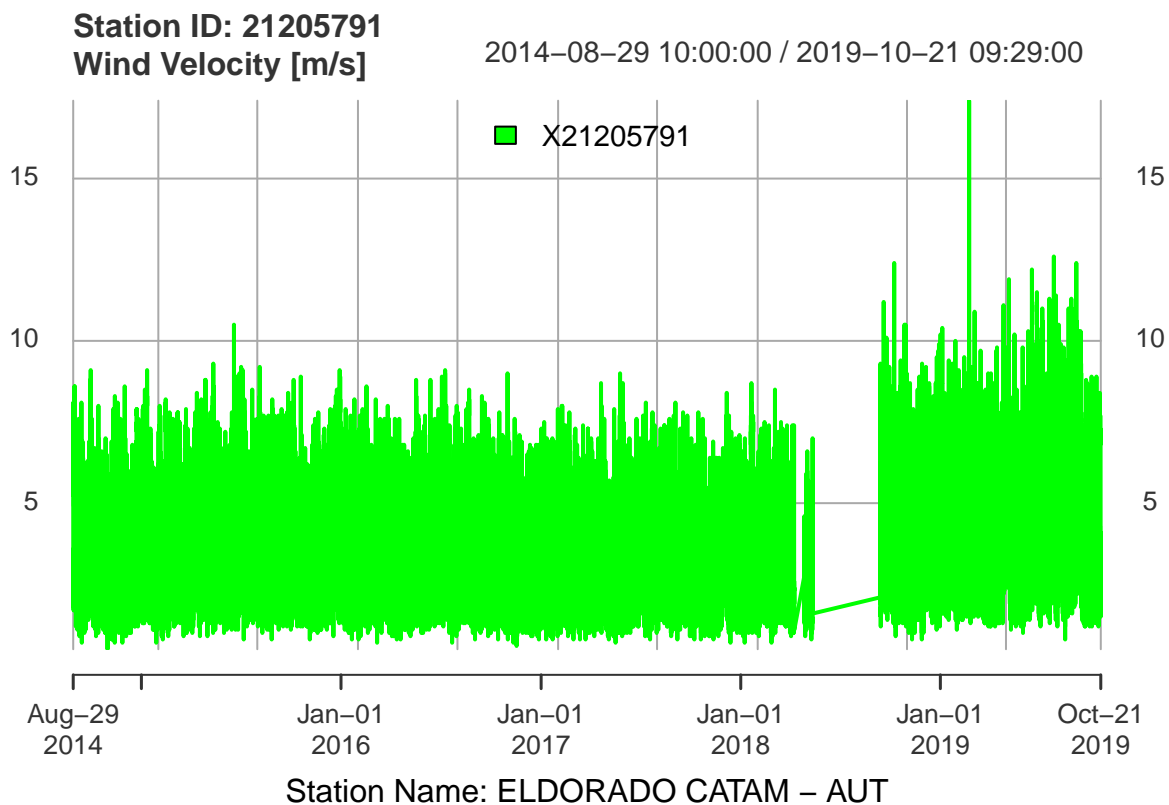


Figure 1.2: IDEAM Station - Time Serie



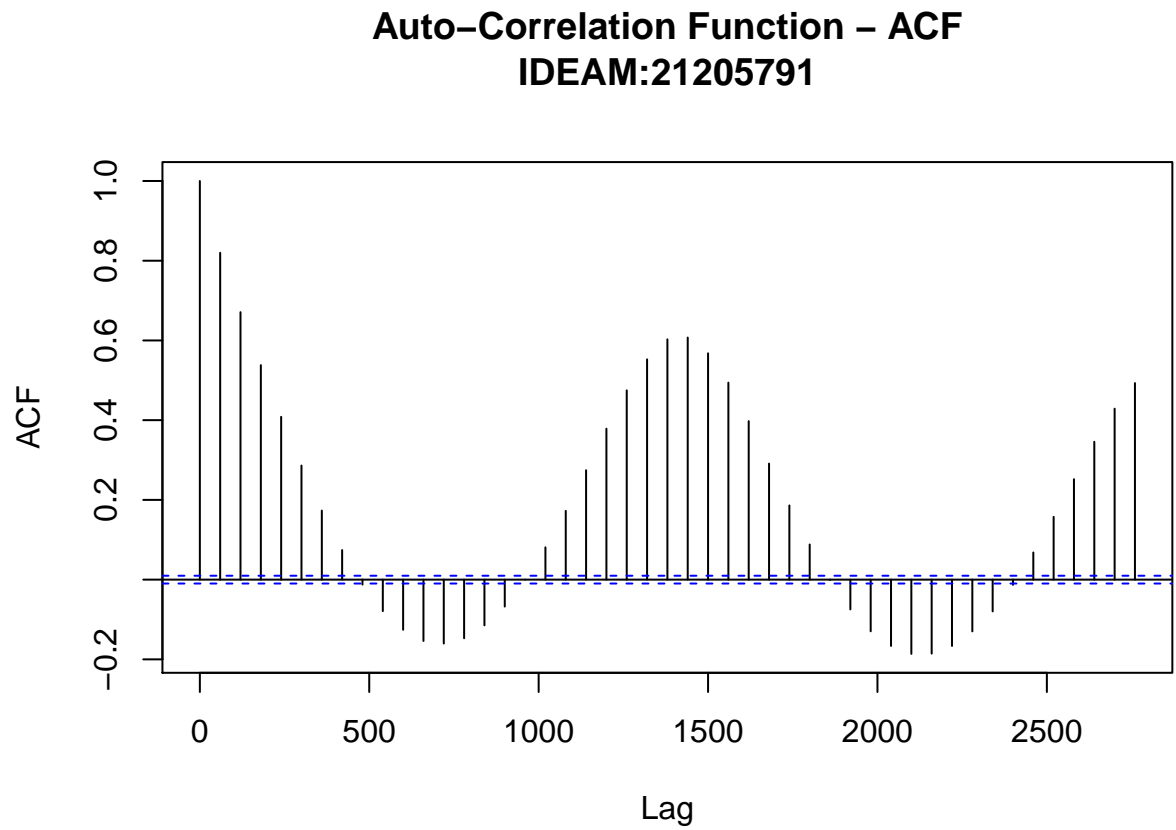


Figure 1.3: IDEAM Station ACF

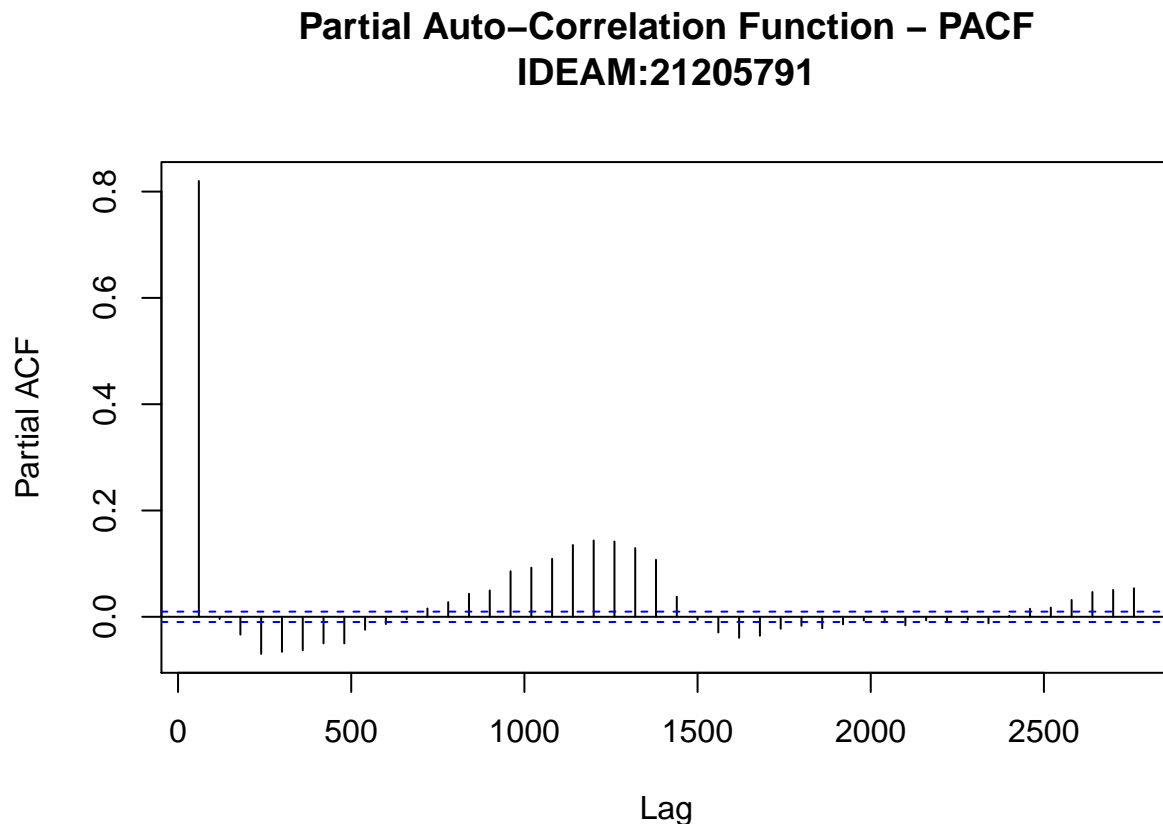


Figure 1.4: IDEAM Station PACF

## 1.2 ISD

ISD is a database with environmental variables among then extreme wind speeds. ISD has data for the whole planet, and is based on observed data at metereological stations in each country, which means that for Colombia is based on IDEAM data. Main advantage is data availability at neighbor countries and specialized postprocesing made by NOAA’s National Centers for Environmental Information - NCEI in United States, which facilitates its use. Table 1.5 shows a sample of five ISD stations. Figure 1.5 shows a map of ISD stations.

Table 1.5: ISD Stations sample

Code	Name	Latitud	Longitud
804400	BARINAS	8.62	-70.22
800810	ALTO CURICHE	7.05	-76.35
801000	BAHIA SOLANO / JOSE MUTIS	6.18	-77.40
802590	ALFONSO BONILLA ARAGON INTL	3.54	-76.38
803150	BENITO SALAS	2.95	-75.29

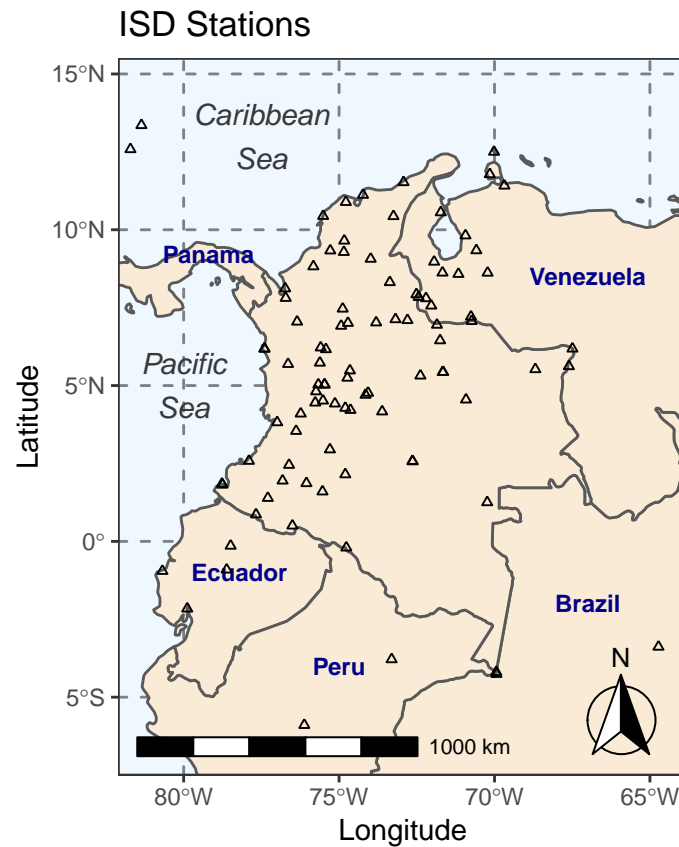


Figure 1.5: ISD Stations

Following, the time serie, autocorrelation function, and partial autocorrelation function, for ISD station “802590” will be displayed.

```
select "mydatetime", "802590" as "X802590" from isd_lite_unstack where "802590" IS NOT NULL
```

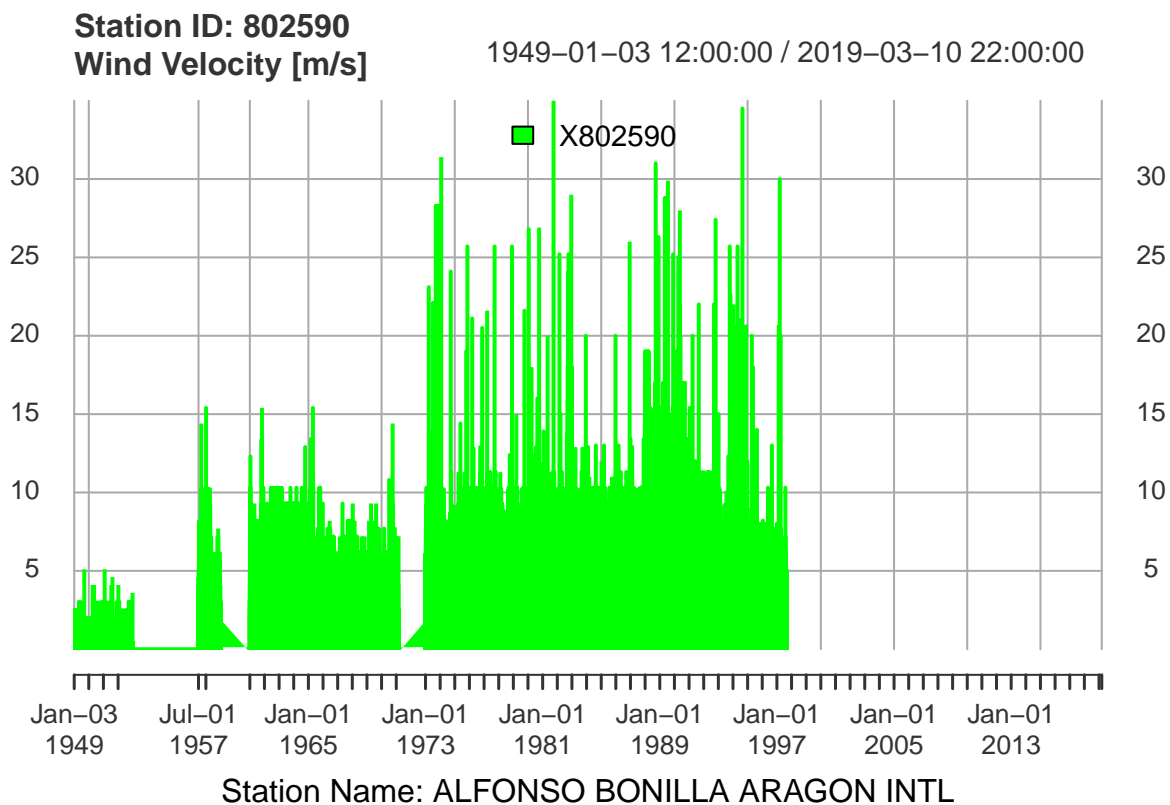


Figure 1.6: ISD Station - Time Serie

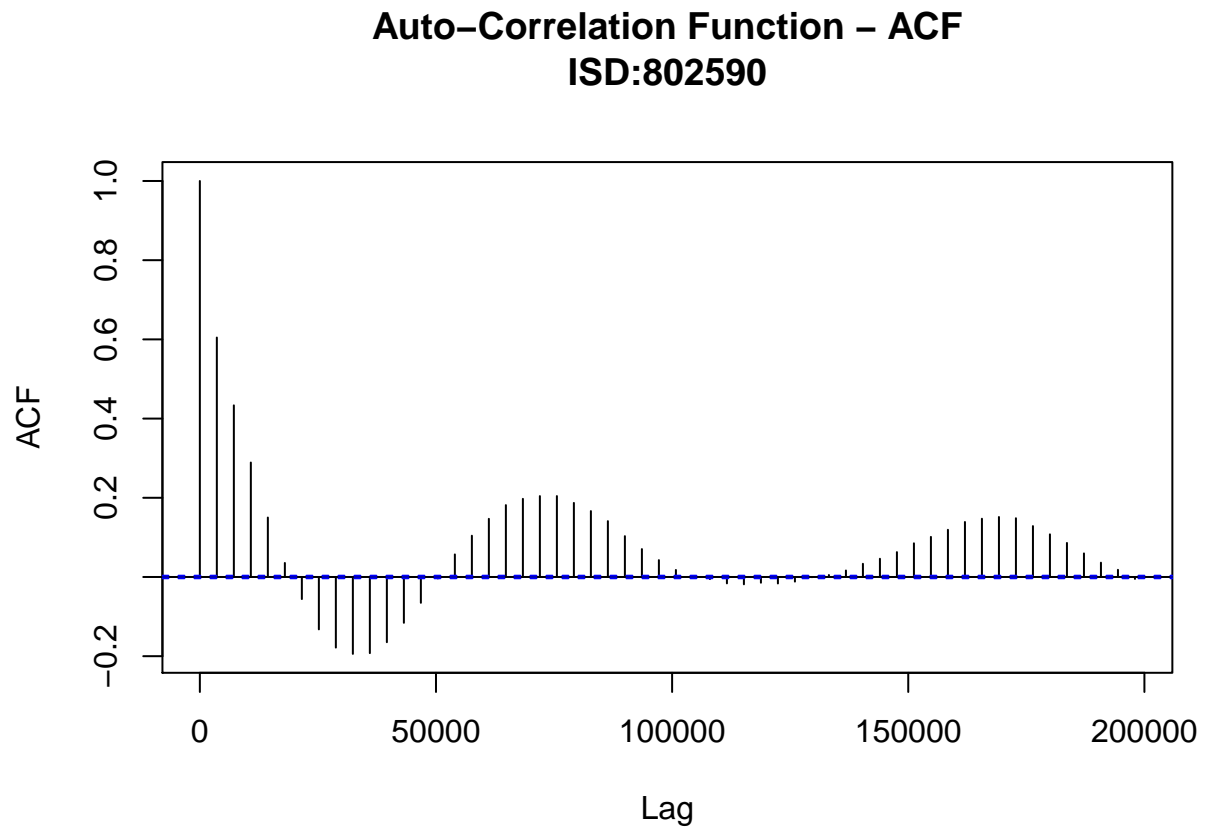


Figure 1.7: ISD Station ACF

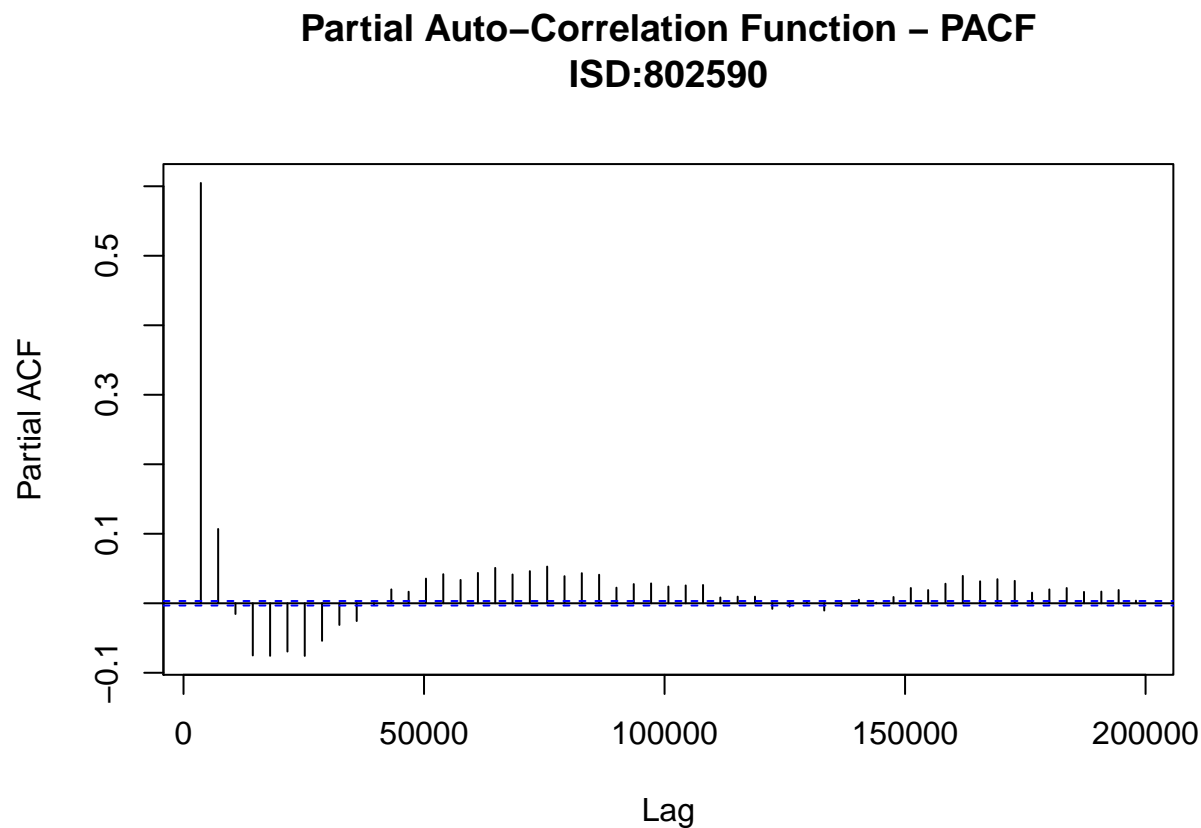


Figure 1.8: IDEAM Station PACF

### 1.3 ERA5

ERA5 is forecast reanalysis data processed by the *European Centre for Medium-Range Weather Forecasts* - ECMWF with wind speeds time series in square cells *matrix of pixels* of 0.25 degrees (33 km) covering the whole planet. For the study area was extracted a raster of 69 rows by 49 XXX columns in format NetCDF. Figure 1.9 shows a map of ERA5 stations (cells centers).

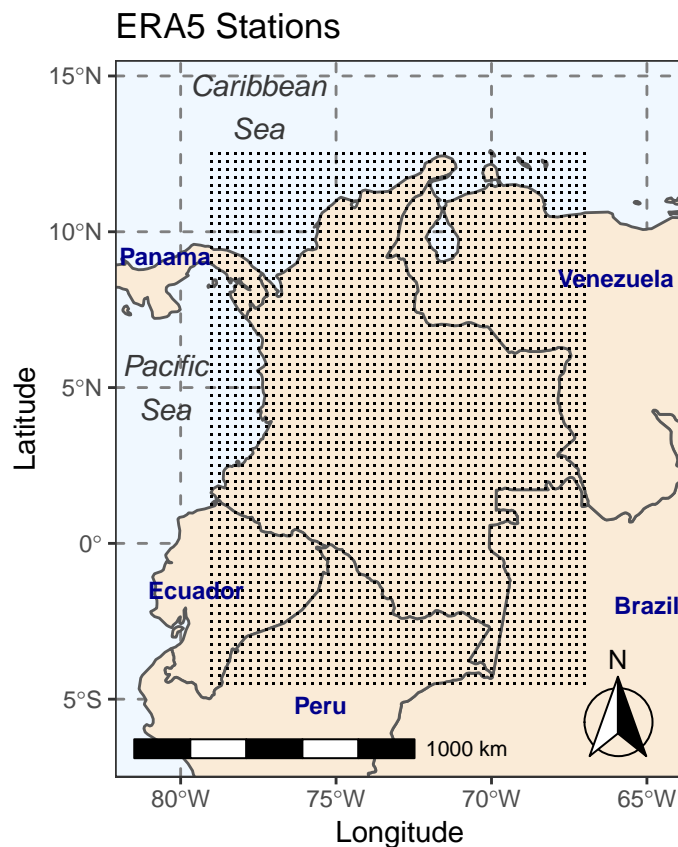


Figure 1.9: ERA5 Stations (cells centers)

## 1.4 Data Download and Organization

## 1.5 Data Standarization

Analysis of extreme wind speeds requires data standardization as an initial step. All input data must be standardized to represent three important conditions: a) anemometer height of 10 meters, b) open space roughness, and c) averaging time of 3-seconds wind gust. Data for analysis must represent 3-s peak wind speeds 10 meters high above the surface, in open terrain. \* 10 mts anemometer height \* Open space terrain roughness \* 3-s gust averaging time





# Chapter 2

## Theoretical Framework

### 2.1 Probability Concepts

Poisson process is an stochastic method that relies in the concepts of probability distributions. The main functions related to probability for extreme value analysis will be described below.

#### 2.1.1 Probability Density Function - *pdf*

Pdf defines the probability that a continuous variable falls between two points, this is, in *pdf* the probability is related to the area below the curve (integral) between two points, as for continuous probability distributions the probability at a single point is zero. The term density is directly related to the probability of a portion of the curve, if the density function has high values the probability will be greater in comparison with the same portion of curve for low values.

$$\int_a^b f(x)dx = Pr[a \leq X \leq b]$$

Equation (2.1) is the Gumbel *pdf*.

$$f(x) = \frac{1}{\beta} \exp \left\{ -\frac{x - \mu}{\beta} \right\} \exp \left\{ -\exp \left\{ -\left( \frac{x - \mu}{\beta} \right) \right\} \right\}, \quad -\infty < x < \infty \quad (2.1)$$

where  $\exp \{.\} \mapsto e^{\{.\}}$ ,  $\beta$  is the scale parameter, and  $\mu$  is the location parameter. Location ( $\mu$ ) has the effect to shift the *pdf* to left or right along 'x' axis, thus, if location value is changed the effect is a movement of *pdf* to the left (small value for location), or to the right (big value for location). Scale has the effect to stretch ( $\beta > 1$ ) or compress ( $0 < \beta < 1$ ) the *pdf*, if scale parameter is close to zero the pdf approaches a spike.

Figure 2.1 shows *pdf* with location ( $\mu$ ) = 100 and scale ( $\beta$ ) = 40, using equation (2.1).

```

location = 100
scale = 40
.x <- seq(0, 300, length.out=1000)
pdfG <- function(x) {
  1/location * exp(-(x-location)/scale) * exp(-exp(-(x-location)/scale))
}
.y = pdfG(.x)
plot(.x, .y, col="green", lty=4,
     xlab="Velocities Km/h", ylab="Density Function - Gumbel Distribution",
     main=paste("Gumbel - Density Function Gumbel Distribution\n", "Location=",
               round(location,2), " Scale=", round(scale,2)), type="l",
     cex.axis = 0.5, cex.lab= 0.6, cex.main=0.7, cex.sub=0.6)

```

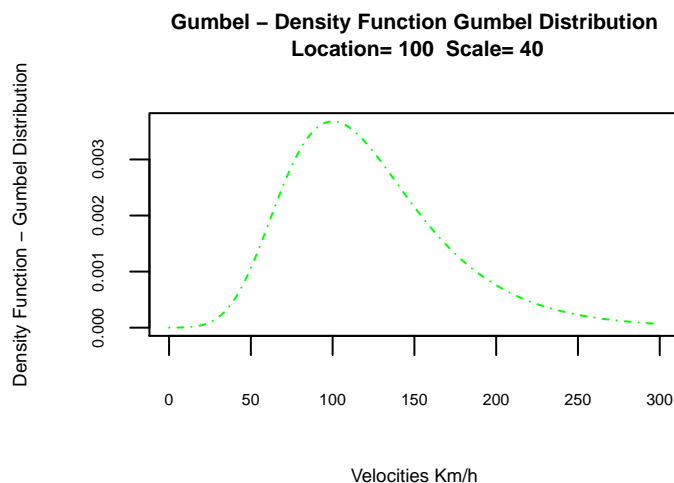


Figure 2.1: Gumbel pdf

Figure 2.2 shows  $pdf$  with location ( $\mu$ ) = 100 and scale ( $\beta$ ) = 40, using function `dgumbel` of the package `RcmdrMisc`

```

location = 100
scale = 40
.x <- seq(0, 300, length.out=1000)
dfG = dgumbel(.x, location=location, scale=scale)
plot(.x, dfG, col="red", lty=4,
     xlab="Velocities Km/h", ylab="Density Function - Gumbel Distribution",
     main=paste("Gumbel - Density Function Gumbel Distribution\n", "Location=",
               round(location,2), " Scale=", round(scale,2)), type="l",
     cex.axis = 0.5, cex.lab= 0.6, cex.main=0.7, cex.sub=0.6)

```

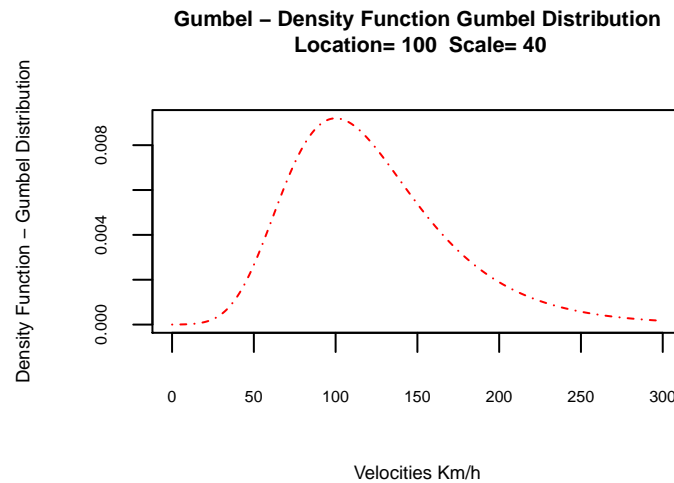


Figure 2.2: Gumbel pdf - dgumbel function

### 2.1.2 Cumulative Distribution Function - *cdf*

*Cdf* is the probability of taking a value less than or equal to  $x$ . That is

$$F(x) = Pr[X \leq x] = \alpha$$

For a continuous variable, *cdf* can be expressed as the integral of its *pdf*.

$$F(x) = \int_{-\infty}^x f(x)dx$$

Equation (2.2) is the Gumbel *cdf*.

$$F(x) = \exp \left\{ -\exp \left[ -\left( \frac{x - \mu}{\beta} \right) \right] \right\}, \quad -\infty < x < \infty \quad (2.2)$$

Figure 2.3 shows Gumbel *cdf* with location ( $\mu$ ) = 100 and scale ( $\beta$ ) = 40, using equation (2.2). As previously done with *pdf*, similar result can be achieved using function `pgumbel` of package `RcmdrMisc`.

```
location = 100
scale = 40
.x <- seq(0, 300, length.out=1000)
cdfG <- function(x) {
  exp(-exp(-(x-location)/scale))
}
.y = cdfG(.x)
plot(.x, .y, col="green", lty=4,
     xlab="Velocities Km/h", ylab="Probability",
     main=paste("Gumbel - Cumulative Distribution Function\n", "Location=",
               round(location,2), " Scale=", round(scale,2)), type="l",
     cex.axis = 0.5, cex.lab= 0.6, cex.main=0.7, cex.sub=0.6)
```

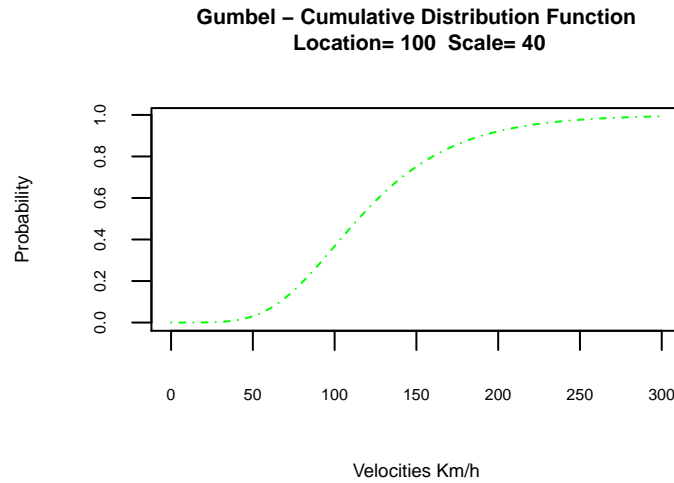


Figure 2.3: Gumbel cdf

### 2.1.3 Percent Point Function - *ppf*

*Ppf* is the inverse of *cdf*, also called the *quantile* function. This is, from a specific probability get the corresponding value  $x$  of the variable.

$$x = G(\alpha) = G(F(x))$$

Equation (2.3) is the Gumbel *ppf*.

$$G(\alpha) = \mu - \beta \ln(-\ln(\alpha)) \quad 0 < \alpha < 1 \quad (2.3)$$

Figure 2.4 shows Gumbel *ppf*, using equation (2.3). Similar result can be achieved using function `qgumbel` of package `RcmdrMisc`.

```
location = 100
scale = 40
.x <- seq(0, 1, length.out=1000)
ppfG <- function(x) {
  location - (scale*log(-log(x)))
}
.y = ppfG(.x)
plot(.x, .y, col="green", lty=4,
     ylab="Velocities Km/h", xlab="Probability",
     main=paste("Gumbel - Percent Point Function\n", "Location=",
               round(location,2), " Scale=", round(scale,2)), type="l",
     cex.axis = 0.5, cex.lab= 0.6, cex.main=0.7, cex.sub=0.6)
```

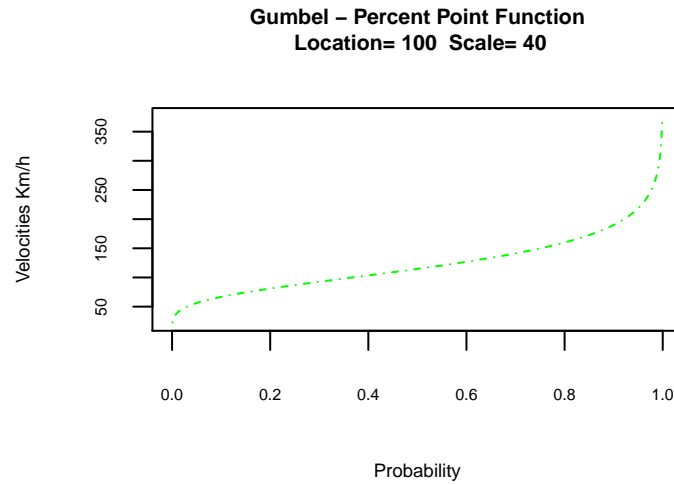


Figure 2.4: Gumbel cdf

### 2.1.4 Hazard Function - $hf$

Using  $S(x) = 1 - F(x)$  as survival function - $sf$ , the probability that a variable takes a value greater than  $x$   $S(x) = Pr[X > x] = 1 - F(x)$ , the  $hf$  is the ratio between  $pdf$  and  $sf$ .

$$h(x) = \frac{f(x)}{S(x)} = \frac{f(x)}{1 - F(x)}$$

Equation (2.4) is the Gumbel  $ppf$ .

$$h(x) = \frac{1}{\beta} \frac{\exp(-(x - \mu)/\beta)}{\exp(\exp(-(x - \mu)/\beta)) - 1} \quad (2.4)$$

Figure 2.5 shows Gumbel  $hf$ , using equation (2.4).

```
location = 100
scale = 40
.x <- seq(0, 3000, length.out=1000)
hfG <- function(x) {
  (1/scale)*(exp(-(x-location)/scale))/(exp(exp(-(x-location)/scale))-1)
}
.y = hfG(.x)
plot(.x, .y, col="green", lty=4,
     xlab="Velocities Km/h", ylab="Hazard",
     main=paste("Gumbel - Hazard Function\n", "Location=",
               round(location,2), " Scale=", round(scale,2)), type="l",
     cex.axis = 0.5, cex.lab= 0.6, cex.main=0.7, cex.sub=0.6)
```

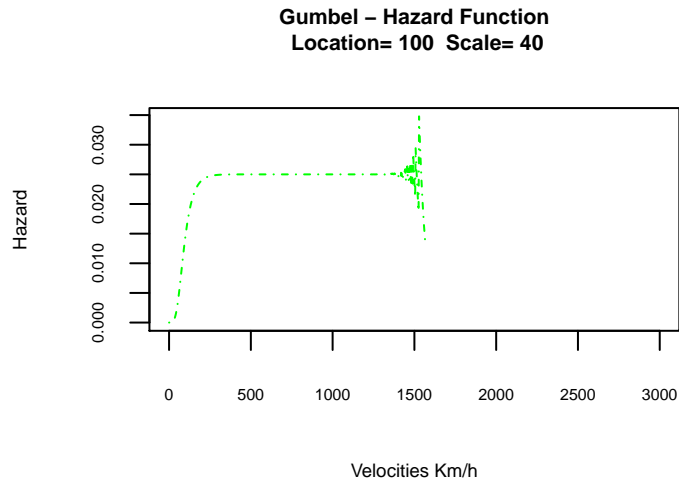


Figure 2.5: Gumbel cdf

```
#library(reliaR)
#plot(.x, hgumbel(.x, mu=location, sigma=scale))
#plot(.x, hra.gumbel(.x, mu=location, sigma=scale))
```

## 2.2 Statistical Concepts For Extreme Analysis

In order to approach the extreme value analysis, some statistical concepts are needed to understand the theoretical framework behind this knowledge area. In this section will be introduced the concepts annual exceedance probability, mean recurrence interval - MRI, exposure time, and compound probability for any given exposure time and MRI.

As an hypothetical example, a simulated database of extreme wind speed will be used. This database is supposed to have 10.000 years of simulated wind speeds.

### 2.2.1 Annual Exceedance Probability - $P_e$

Using the previously described database, a question arises to calculate the probability to exceed the highest probable loss due to the simulated winds. It is possible to conclude that there is only one event grather or equal (in this case equal) to the highest probable causing loss in 10.000 years, and it is the *highest wind*. If we sort the database by wind magnitude in descending order (small winds last), the question is solved calculating the annual exceedance probability  $P_e$  with next formula

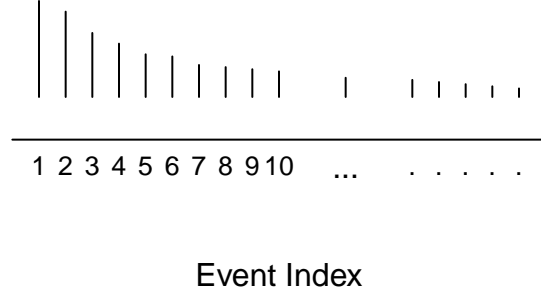


Figure 2.6: Sorted Winds by Magnitud - wind simulation database

$$P_e = \frac{\text{Event index after descending sorting}}{\text{Years of simulations}} = \frac{1}{10.000} = 0.001 = 0.01\%$$

because the highest wind will be the first in the sorted list. Same exercise can be done with all winds to construct the annual exceedance probability curve, that in this case will represent the probability to equal or exceed different probable losses due to wind.

### 2.2.2 Return Period - Mean Recurrence Interval

Continuing with the previous section, if the inverse of the exceedance probability is taken, the return period (in years) is obtained. The return period or Mean Recurrence Interval - MRI is associated with an specific return level (wind extreme velocity). MRI is the numbers of years (N) needed to obtain 63% of change that the corresponding return level will occur at least one time in that period. The return level is expected to be exceeded on average once every N-years. The annual exceedance probability of the return level corresponding to N-years of MRI, is  $P_e = \frac{1}{MRI} = \frac{1}{N}$ .

For an specific wind extreme event A, the probability that the event will occur in a period equal to MRI years is 63%. If we analyse for the same period a strongest wind extreme event B, its occurrence probability will be less than 67%. If the purpose of this research is to design infrastructure considering wind loads, the structure will be more resistant to wind if we design with stronger winds, this is high MRIs, and low annual exceedance probability. Common approach for infrastructure design, considering any type of load (earthquake, wind, etc) is to choose high MRI according to the importance/use/risk/type of the structure. For highly important structures like hospitals or coliseums, where the risk of collapse must be diminished, the MRI

used to design is higher in comparison to common structures (for instance a normal house), which implies less risks for its use and importance.

$$P_e = \begin{cases} 1 - \exp\left(-\frac{1}{MRI}\right), & \text{for } MRI < 10 \text{ years} \\ \frac{1}{MRI}, & \text{for } MRI \geq 10 \text{ years} \end{cases}$$

### 2.2.3 Compound Excedance Probability - $P_n$

If time of exposure is consider, understood as time the structure will be in use, it is possible to have a compound probability  $P_n$ , where  $n$  is the exposure period.  $P_n$  is the probability that the extreme wind speed will be equaled or exceeded at least one time in  $n$  years, and is related with the occurrence probability, but also is posible to calculate the non-occurrence compound probability (probability that the event will not occur).

$$P_n = \begin{cases} 1 - \left(1 - \frac{1}{MRI}\right)^n, & \text{occurrence probability} \\ \left(1 - \frac{1}{MRI}\right)^n, & \text{non - occurrence probability} \end{cases}$$

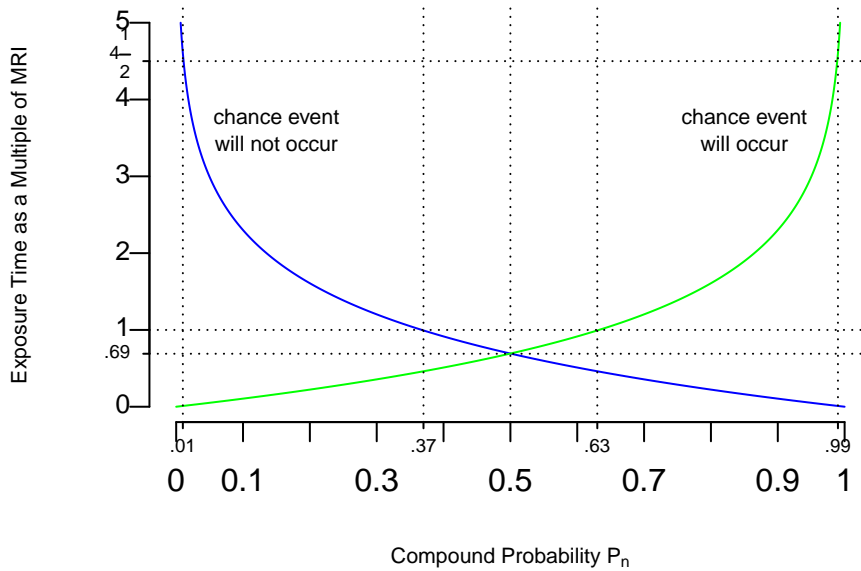


Figure 2.7: Compound Probability

If it is consider exposure time as a multiple of return period, the resulting figure 2.7, shows that:



- When exposure time is .69% of the return period, then probability (occurrence and non-occurrence) will be 50%
- As was stated previously, when exposure time is equal to return period, then the probability that the extreme wind speed (return level) occur is 63%, and 37% for the non occurrence probability.
- If exposure time is 4.5 times the return period, there is a 99% of chance that the return level will occur.

The example discussed here was presented as an instrument to introduce important concepts, nonetheless, there are specialized approaches to deal with extreme value analysis which will be discussed in Extreme Value Analysis Overview and more in detail in Peaks Over Threshold - Poisson Process. In summary, is necessary to fit the data over a specific threshold to an extreme value distribution, and  $P_e$  will be  $1 - F(y)$ , with  $F(y)$  as the *cdf*, and MRI as  $\frac{1}{1-F(y)}$ .

## 2.3 Extreme Value Analysis Overview

Analysis of extreme values is related with statistical inference to calculate probabilities of extreme events. Main methods to analyze extreme data are epochal, Peaks Over Threshold - POT, and extreme index. The epochal method, also known as block maxima, uses the most extreme value for a specific frame of time, typically, one year. POT is based in the selection of a single threshold value to do the analysis only with values above the threshold. But there are different POT approaches, the most common one is Generalized Pareto Distribution - POT-GPD, but also it is possible to use the Poisson process approach.

In both methods (Epochal and POT), the first step is to fit the data to an appropriate probability distribution model, among them the most used are, - Extreme Value Type I (Gumbel), Extreme Value Type II (Frechet), Weibull, Generalized Pareto - GPD, and Generalized Extreme Value - GEV.

Distribution models are fitted based in the estimation of its parameters, commonly called location, scale and shape, nonetheless each model has its own parameters names. There are different methods to estimate parameters, among them, - method of moments (modified moments - see Kubler (1994), and L moments - see Hosking & Wallis (1997)), - method of maximum likelihood MLE, see Harris & Stocker (1998), which is problematic for GPD and GEV, - probability plot correlation coefficient, and - elemental percentiles (for GPD and GEV)

Once candidate parameters are available, it is necessary to assess the goodness of fit of the selected model, using one of the next methods, - Kolmogorov-Smirnov (KS) goodness of fit test, and - Anderson-Darling goodness of fit test. Here a visual assessment is also useful using a probability plot or a kernel density plot with the fitted *pdf* overlaid.

The main use of the fitted model is the estimation of mean return intervals - MRI, and extreme wind speeds (return levels),

$$MRI = \frac{1}{1 - F(y)}$$

with  $F(y)$  as the *cdf*. If  $1 - F(y)$  is the annual exceedance probability, MRI is its inverse, see Simiu & Scanlan (1996) for more details about MRI. If  $y$  is solved from previous equation using a given MRI of  $N$ -years, its value represents the  $Y_N$  wind speed return level,

$$Y_N = G\left(1 - \frac{1}{\lambda N}\right)$$

where  $G$  is the *ppf* (quantile function) and  $\lambda$  is the number of wind spees over the threshold per year.

The CRAN Task View “Extreme Value Analysis” <https://cran.r-project.org/web/views/ExtremeValue.html> shows available **R** for block maxima, POT by GPD, and external indexes estimation approaches. Most important to consider are `evd`, `extremes`, `evir`, `POT`, `extremeStat`, `ismev`, and `Renext`.

## 2.4 Peaks Over Threshold - Poisson Process

According to Pintar et al. (2015) the stochastic poisson process is mainly defined by its intensity function. As the intensity function is not uniform over the domain, the poisson process considered here is non-homogeneous, and due to the intensity function dependance of magnitude and time, it is also bi-dimensional. Poisson Process was described for the first time in Pickands (1971), then extended in Smith (1989).

$$\lambda(y, t) \begin{cases} \lambda_t(y), & \text{for } t \text{ in thunderstorm period} \\ \lambda_{nt}(y), & \text{for } t \text{ in non - thunderstorm period} \end{cases} \quad (2.5)$$

Generic equation (2.5) shows the intensity function, which is defined in the domain  $D = D_t \cup D_{nt}$ , and allow to fit the poisson process at each station to the observed data  $\{t_i, y_i\}_{i=1}^I$  for all the times ( $t_i$ ) of threshold crossing observations and its corresponding wind speeds magnitudes ( $y_i$ ). Thus, only data above the threshold is used.

Intensity function of the Poisson Process is defined in Smith (2004),

$$\frac{1}{\psi_t} \left(1 + \zeta_t \frac{y - \omega_t}{\psi_t}\right)_+^{-\frac{1}{\zeta_t} - 1}$$

Where  $\zeta_t$  controls the tail length of the intensity function at a given time  $t$ , but to facilitate the estimation of the parameters then  $\zeta_t$  is taken to be zero, then doing the limit, the resulting intensity function is the same as the the GEV type I or Gumbel distribution,

$$\frac{1}{\psi_t} \exp \left\{ \frac{-(y - \omega_t)}{\psi_t} \right\}$$

In this study, the used intensity functions are shown in equation (2.6).

$$\lambda(y, t) \begin{cases} \frac{1}{\psi_s} \exp \left\{ \frac{-(y - \omega_s)}{\psi_s} \right\}, & \text{for } t \text{ in thunderstorm period} \\ \frac{1}{\psi_{nt}} \exp \left\{ \frac{-(y - \omega_{nt})}{\psi_{nt}} \right\}, & \text{for } t \text{ in non - thunderstorm period} \end{cases} \quad (2.6)$$

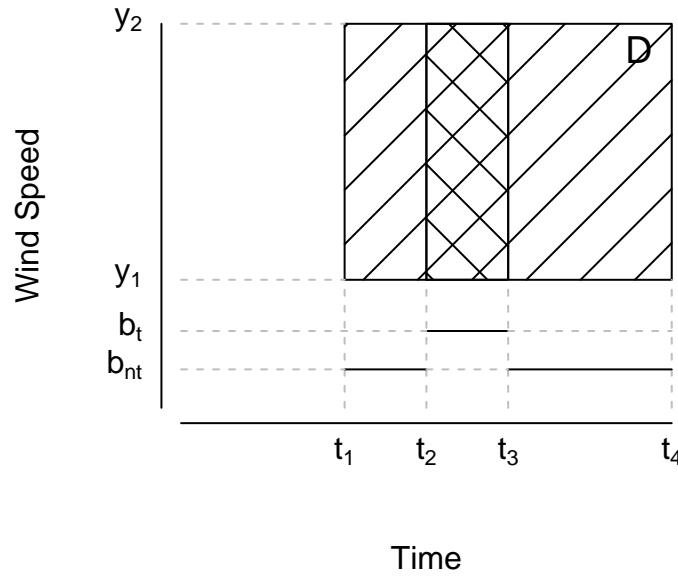


Figure 2.8: Domain of the Poisson Process

Figure 2.8 represents the domain  $D$  of the Poisson process. In time, the domain represents the station service period from first sample  $t_1$  to last sample  $t_4$ .  $D$  is the union of all thunderstorm periods  $D_t$  (from  $t_2$  to  $t_3$ ), and all non-thunderstorm periods  $D_{nt}$  (periods  $t_1$  to  $t_2$  and  $t_3$  to  $t_4$ ). In magnitude, only thunderstorm data above its threshold  $b_t$ , and only non-thunderstorm data above its threshold  $b_{nt}$  are used.

Thunderstorms and non-thunderstorms are modeled independently:

1. Observations in domain  $D$  follow a Poisson distribution with mean  $\int_D \lambda(t, y) dt dy$
2. For each disjoint subdomain  $D_1$  or  $D_2$  inside  $D$ , the observations in  $D_1$  or  $D_2$  are independent random variables.

Visual representation of the intensity function for the Poisson Process can be seen in figure 2.9. In vertical axis, two surfaces were drawn representing independent intensity functions for thunderstorm  $\lambda_t(y)$  and for non-thunderstorm  $\lambda_{nt}(y)$ . The volume under

each surface for its corresponding time periods and peak (over threshold) velocities, is the mean of the Poisson Process.

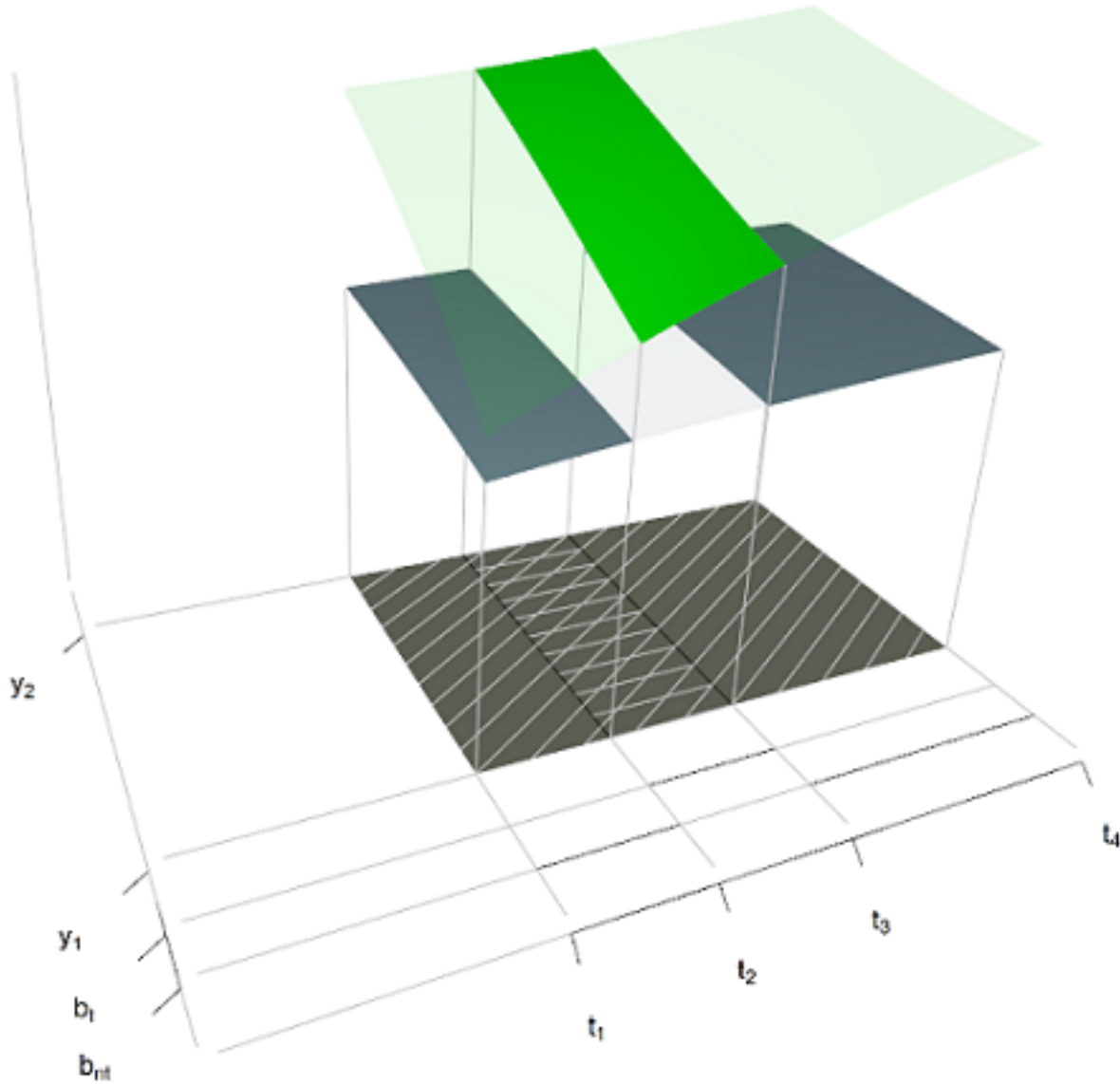


Figure 2.9: Volume under surfaces represents the mean of the Poisson process

The method of maximum likelihood is used to estimate the parameters of the Poisson process, the selected vector of parameters  $\eta$  are the  $\hat{\eta}$  values that maximize the function

$$L(\eta) = \left( \prod_{i=1}^I \lambda(y_i, t_i) \right) \exp \left\{ - \int_D \lambda(y, t) dy dt \right\} \quad (2.7)$$

$\hat{\eta}$  values need to be calculated using a numerical approach because there is not analytical solution available.

Once the Poisson process is fitted to the data, the model will provide extreme wind velocities (return levels), for different return periods (mean recurrence intervals).

A  $Y_N$  extreme wind velocity, called the return level (RL) belonging to the  $N$ -years return period, has a expected frequency to occur or to be exceeded (annual exceedance probability)  $P_e = \frac{1}{N}$ , and also has a probability that the event does not occur (annual non-exceedance probability)  $P_{ne} = 1 - \frac{1}{N}$ .  $Y_N$  will be the resulting value of the  $G$  (ppf or quantile) function using a probability equal to  $P_{ne}$ .  $Y_N = \text{quantile}(y, p = P_{ne}) = G(x, p = P_{ne}) = \text{ppf}(x, p = P_{ne})$ . As for this study  $\zeta = 0$ , the  $G$  function to use is the Gumbel quantile function.  $Y_N$  can be understood as the wind extreme value expected to be exceeded on average once every  $N$  years.

For different POT approaches, as POT-GPD described –, the value of the probability passed to the  $G$  function, has to be modified with the  $\lambda$  parameter, as is described in next equation.  $\lambda$  is the number of wind speed over the threshold per year.

$$Y_N = G\left(y, 1 - \frac{1}{\lambda N}\right)$$

For the Poisson process  $Y_N$  is also the solution to the next equation, which is defined in terms of the intensity function,

$$\int_{Y_N}^{\infty} \int_0^1 \lambda(y, t) dy dt = A_t \int_{Y_N}^{\infty} \lambda_t(y) dy + A_{nt} \int_{Y_N}^{\infty} \lambda_{nt}(y) dy = \frac{1}{N} \quad (2.8)$$

where  $A_t$ , is the multiplication of the average number of thunderstorm per year and the average length of a thunderstorm (taken to be 1 hour as defined in Pintar et al. (2015)), and  $A_{nt} = 1 - A_t$ . The average length of a non-thunderstorm event is variable, and it is adjusted in each station to guarantee that  $A_{nt} + A_t = 1$

The same thunderstorm event is considered to occur if the time lag distance between sucesive thunderstorm samples is small than six hours, and for non-thunderstorm this time is 4 days. For the Poisson process, all the measurements belonging to the same event (thunderstorm or non tunderstorm), need to be declustered to leave only one maximun value. In other words, the number of thunderstorm in the time serie is the number of time lag distances grather than 6 hours, and for non-thunderstorm grather than 4 days.

###Threshold Selection

$$U = F(Y)$$

$$W = -\log(1 - U)$$

## 2.5 Wind Loads Requirements

Colombian norm that defines wind loads today is the Earth

As the output maps of this research will be used as input loads for infrastructure design, the methodology used for its creation, need to be consistent with Colombian official wind loads requirements. Today (2020), the Colombian norm that defines wind

loads is the Seismic Resistant Standard 2010 - NSR-10 by its acronym of Spanish, see XXX. Chapter related to wind loads is B.6. NSR-10 was created and is maintained by the Colombian Association of Seismic Engineering - AIS.

NSR-10 is mainly based in the USA norm American Society of Civil Engineers 7-16, minimum design loads and associated criteria for buildings and other structures - ASCE7-16, see Engineers (2017). Under these circumstances, ASCE7-16 defines the minimum requirements of the research products. Especially the chapter C26 - “wind loads - general requirements”, C26.5 “wind hazard map”, and C26.7 “Exposure” - pages 733 to 747. Wind speeds requirements of ASCE7-16 are based in the combination of independent non-hurricane analysis, and hurricane wind speeds simulations models. The focus of this research will be the analysis of non-hurricane wind data, however, existing results of hurricane studies will be used to present final maps with both components. In ASCE7-16, for non-hurricane wind speed, the procedure is mainly based on Pintar et al. (2015).

ASCE7-16 (page 734), requires the calculation of wind extreme return levels for specific return periods according to the risk category of the structure to be designed: risk category I - 300 years, risk category II - 700 years, risk category III - 1700 years, risk category IV - 3000 years (NSR-10 only requires 700, 1700 and 3000 years). In addition, extreme wind speeds for those MRI need to correspond to: - 3 second gust speeds, - at 33 ft (10 meters) above the ground, and - exposure category C (open space).

To standarize wind speeds to gust speeds ASCE7-16 proposes the curve Durst (see C. S. Durst (1960), and figure 2.10). It is valid only for open terran conditions. Durst curve shows in axis  $y$  the gust factor  $\frac{V_t}{V_{3600}}$ , a ration between any wind gust averaged at  $t$  seconds,  $V_t$ , and the hourly averaged wind speed  $V_{3600}$ , and in the axis  $x$  the duration  $t$  of the gust.

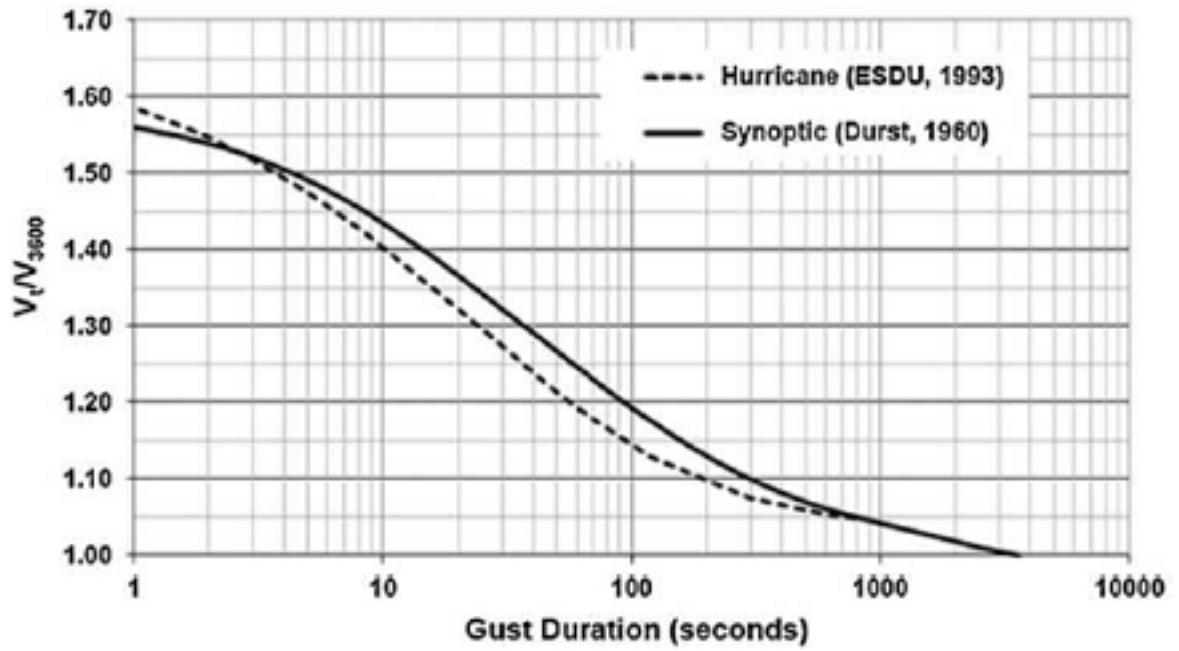


Figure 2.10: Maximum speeds averaged over  $t$  (sec), to hourly mean speed





# Chapter 3

## Methodology

### 3.1 Input Data Selection and Standarization

### **3.1.1 Data Selection**

### **3.1.2 Data Standarization**

Anemometer height - 10 m

Surface Roughness - 0.03 m

Averaging Time - 3-s gust

### **3.1.3 Data Filterng**

## **3.2 Fit data to a POT - Poisson Process**

### **3.2.1 Data Requirements**

### **3.2.2 Exploratory Data Analysis and Data Preparation**

Declustering of observations

Exclude no-data periods

Threshold selection

### **3.2.3 Parameters Estimation**

Intensity function

Density function

Distribution function

Maximun likelihood estimation

### **3.2.4 Velocities at Return Periods**

## **3.3 spatial Interpolation**

# Conclusion

If we don't want Conclusion to have a chapter number next to it, we can add the `{-}` attribute.

## **More info**

And here's some other random info: the first paragraph after a chapter title or section head *shouldn't be* indented, because indents are to tell the reader that you're starting a new paragraph. Since that's obvious after a chapter or section title, proper typesetting doesn't add an indent there.



# Appendix A

## The First Appendix

This first appendix includes all of the R chunks of code that were hidden throughout the document (using the `include = FALSE` chunk tag) to help with readability and/or setup.

In the main Rmd file

```
# This chunk ensures that the thesisdown package is  
# installed and loaded. This thesisdown package includes  
# the template files for the thesis.  
if(!require(devtools))  
  install.packages("devtools", repos = "http://cran.rstudio.com")  
if(!require(thesisdown))  
  devtools::install_github("ismayc/thesisdown")  
library(thesisdown)
```

In Chapter 3:

```
# This chunk ensures that the thesisdown package is  
# installed and loaded. This thesisdown package includes  
# the template files for the thesis and also two functions  
# used for labeling and referencing  
if(!require(devtools))  
  install.packages("devtools", repos = "http://cran.rstudio.com")  
if(!require(dplyr))  
  install.packages("dplyr", repos = "http://cran.rstudio.com")  
if(!require(ggplot2))  
  install.packages("ggplot2", repos = "http://cran.rstudio.com")  
if(!require(ggplot2))  
  install.packages("bookdown", repos = "http://cran.rstudio.com")  
if(!require(thesisdown)){  
  library(devtools)  
  devtools::install_github("ismayc/thesisdown")  
}
```

```
library(thesisdown)
flights <- read.csv("data/flights.csv")
```

## Appendix B

The Second Appendix, for Fun





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Retrieved from <https://www.amazon.com/Telecommunications-Environment-Monographs-Statistics-Probability/dp/1584884118?SubscriptionId=AKIAIOBINVZYXZQZ2U3A&tag=chimbori05-20&linkCode=xm2&camp=2025&creative=165953&creativeASIN=1584884118>